

Chapter 3. Solving Linear Equations

Exercise 3.3

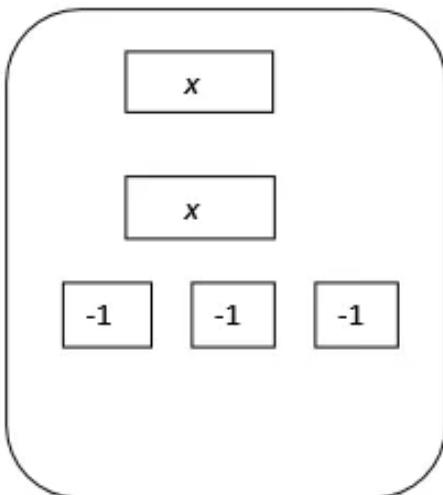
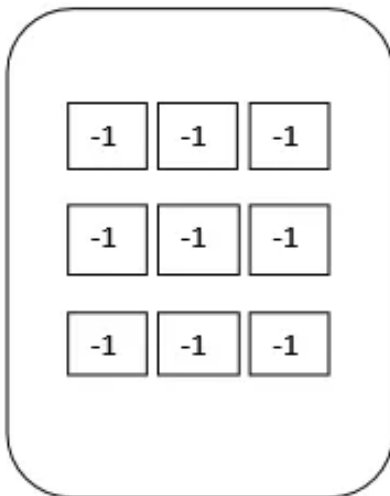
Answer 1AA.

Solving an equation involves operations like addition, subtraction, multiplication and division.
Consider the expression,

$$2x - 3 = -9 \dots\dots(1)$$

Equation(1) is solved in the following ways.

Step 1: Model the equation.

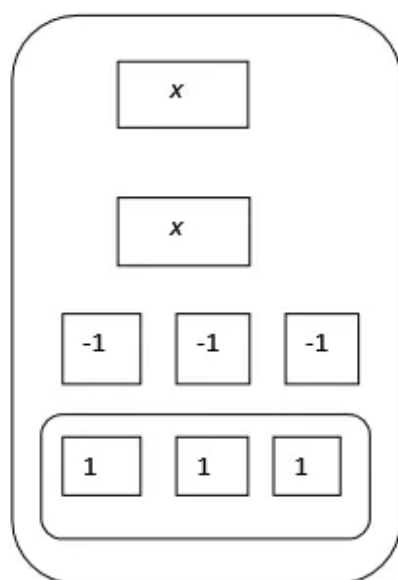
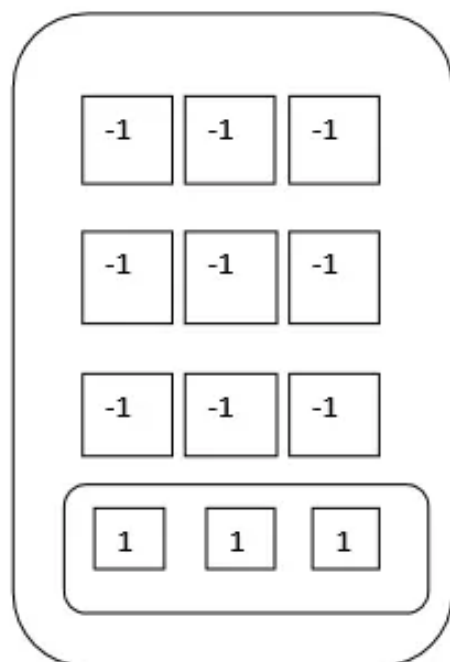


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$$2x - 3 = -9$$

Place 2 x tiles and 3 negative 1 tiles on side of the mat. Place 9 negative 1 tiles on the other side of the mat.

Step 2 : Isolate the x term.



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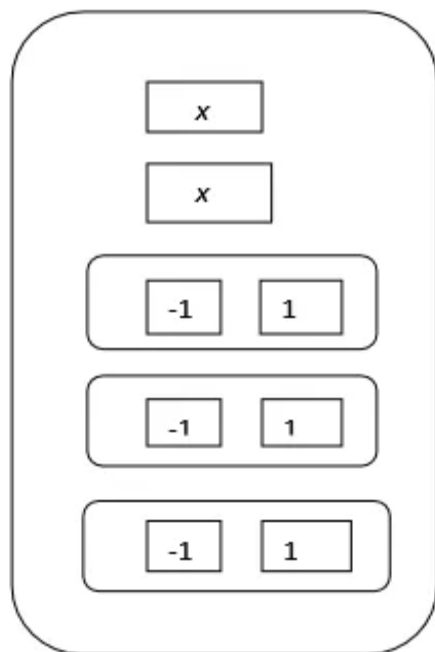
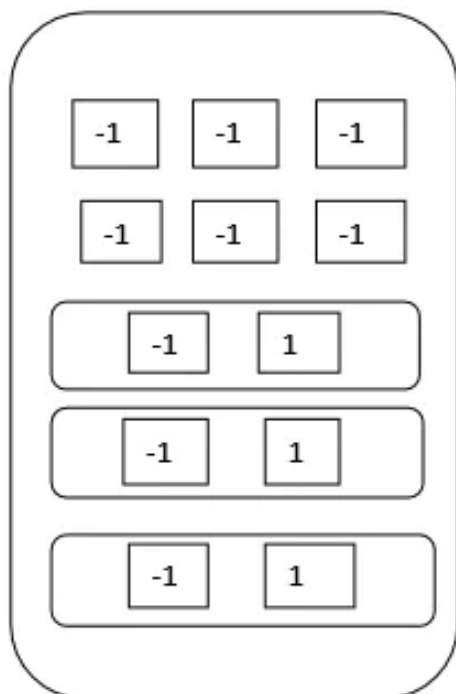


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$$2x - 3 + 3 = -9 + 3$$

Since there are 3 negative 1 tiles with the x tiles, add 3 positive 1 tiles to each side to form zero pairs.

Step 3 : Remove zero pairs.

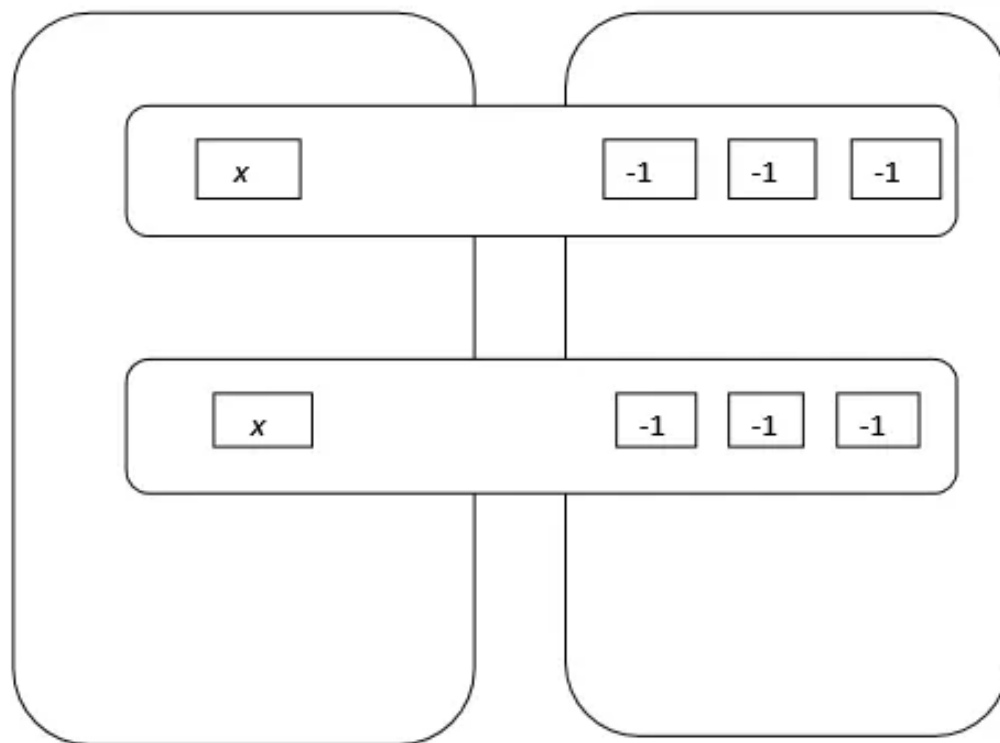


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$$2x = -6$$

Group the tiles to form zero pairs and remove the zero pairs.

Step 4: Group the tiles.



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$$\frac{2x}{2} = \frac{-6}{2}$$

Separate the tiles into 2 equal groups to match the 2 x tiles. Each x tile is paired with 3 negative 1 tiles. Thus, $x = -3$

Answer 1CU.

For any numbers a , b and c if $a = b$, then $ac = bc$.

Consider the equation,

$$2x = -6 \dots\dots(1)$$

Equation(1) can be solved as,

$$2x = -6 \quad \text{original equation}$$

$$\frac{2x}{2} = \frac{-6}{2} \quad \text{divide by 2 on each side}$$

$$x = -3 \quad \text{check this result}$$

Thus, we get the solution of equation(1) is $x = -3$.

CHECK

$$2x = -6 \quad \text{original equation}$$

$$2(-3) = -6 \quad \text{substitute } -3 \text{ for } x$$

$$-6 = -6 \quad \text{The solution is } -3$$

Therefore, $2x = -6$ is the required equation which has a solution $x = -3$

Answer 1PQ.

Consider the statement,

The surface area S of a sphere equals four times π times the square of the radius r .

This statement can be expressed in symbol as:

The surface area S of a sphere equals $\underbrace{\text{four}}_4 \underbrace{\text{times}}_{\times} \underbrace{\pi}_{\pi} \underbrace{\text{times}}_{\times} \underbrace{\text{the square of the radius } r}_{r^2}$

$$S = 4\pi r^2$$

Therefore, the required formula is, Surface area $S = 4\pi r^2$

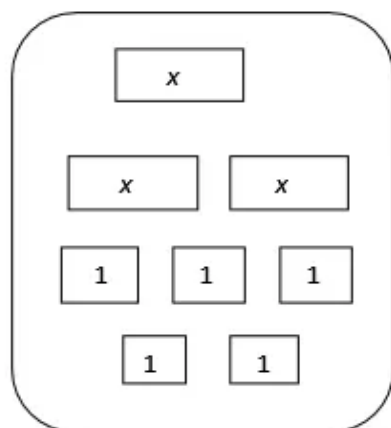
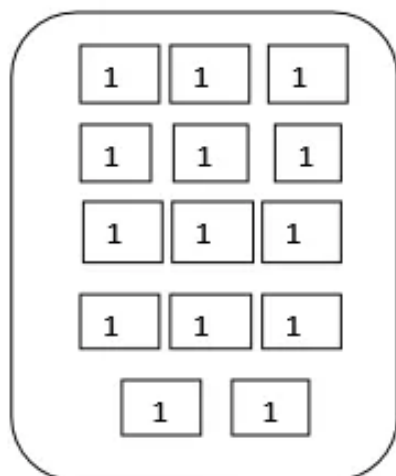
Answer 2AA.

Solving an equation involves operations like addition, subtraction, multiplication and division. Consider the expression,

$$3x + 5 = 14 \dots\dots(1)$$

Equation(1) is solved in the following ways.

Step 1: Model the equation.

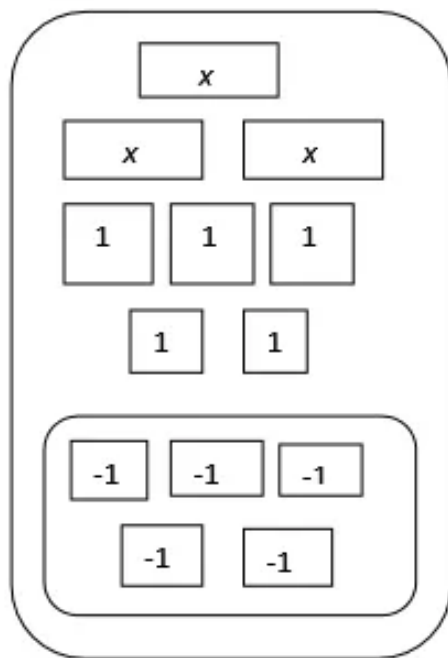
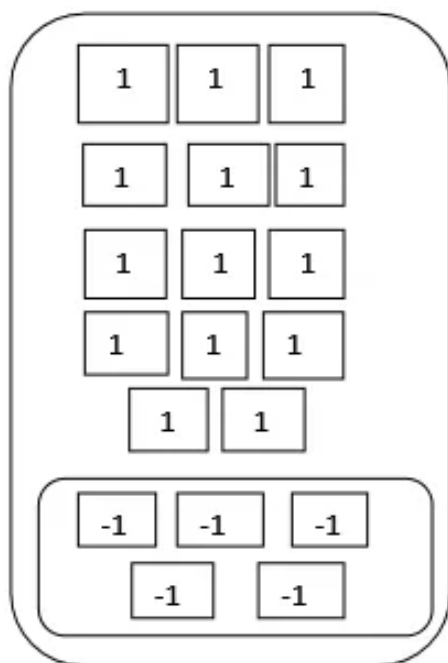


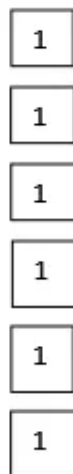
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$$3x + 5 = 14$$

Place 3 x tiles and 5 positive 1 tiles on side of the mat. Place 14 positive 1 tiles on the other side of the mat.

Step 2 : Isolate the x term.





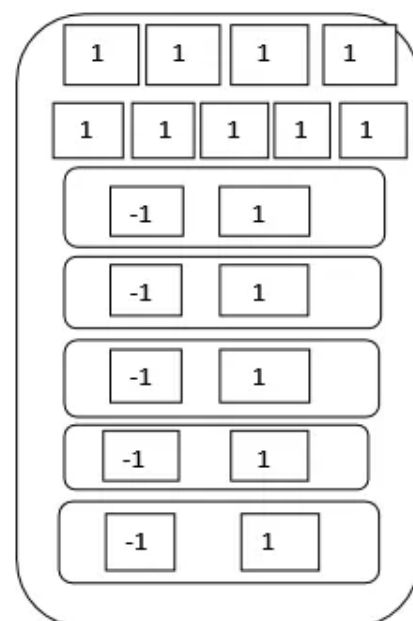
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$$3x + 5 - 5 = 14 - 5$$

Since there are 5 positive 1 tiles with the x tiles, add 5 negative 1 tiles to each side to form zero pairs.

Step 3 : Remove zero pairs.



x	x	x
-1	1	
-1	1	
-1	1	
-1	1	
-1	1	

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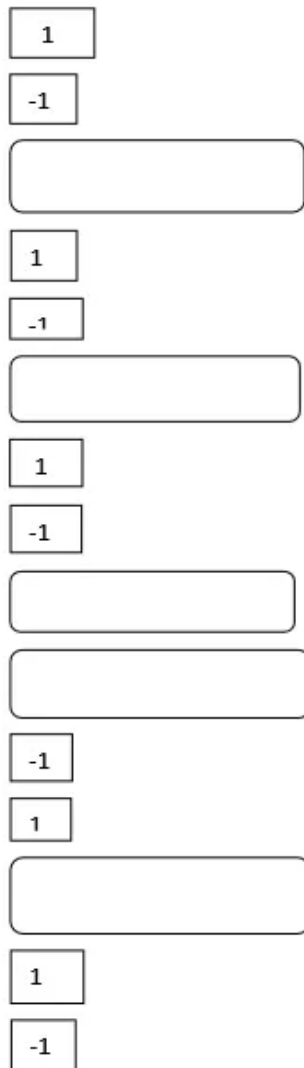
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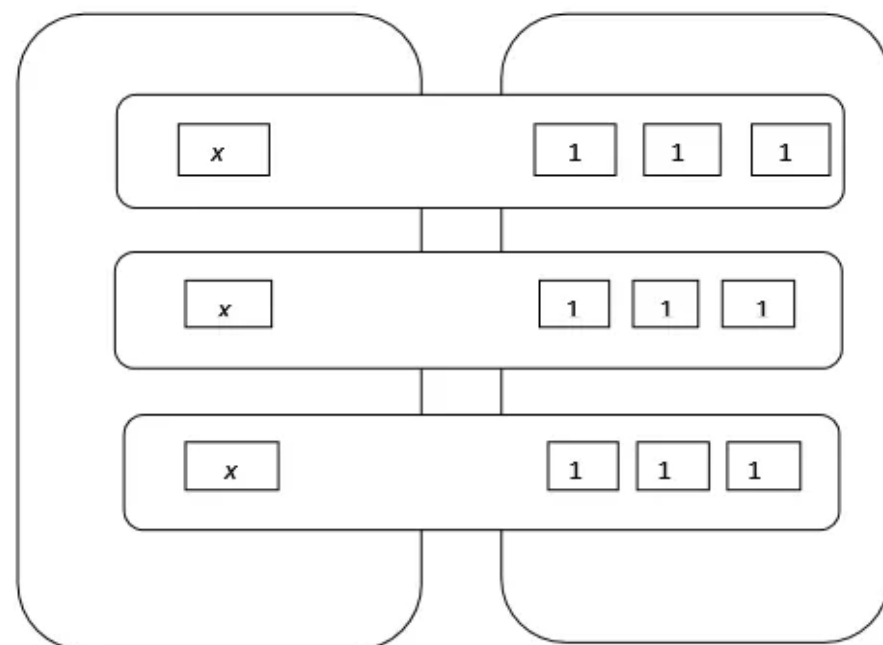
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$$3x = 9$$

Group the tiles to form zero pairs and remove the zero pairs.

Step 4: Group the tiles.



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$$\frac{3x}{3} = \frac{9}{3}$$

Separate the tiles into 3 equal groups to match the 3 x tiles. Each x tile is paired with 3 positive 1 tiles. Thus, $x = 3$

Answer 2CU.

Recollect that the multiplication property of equality

For any numbers a , b and c , if $a = b$, then $ac = bc$ (1)

Division Property of equality

In particular, for $c \neq 0$, we have $\frac{a}{c} = \frac{b}{c}$ (2)

For any non-zero number n , consider the reciprocal of the number $\frac{1}{n}$. Let us assume that

$a = b$ is true for any two numbers a and b .

Then, by multiplication property of equality we have,

$$\frac{a}{n} = \frac{b}{n} \text{ (3)}$$

Equation (3) can be compared with equation (2), which is division property of equality.

Hence, for every non-zero number Multiplication property of equality and Division property of equality can be considered as the same.

Answer 2PQ.

The surface area S of a sphere is, $S = 4\pi r^2$ where r is the radius of the sphere(1)

Substitute $r = 7$ cm in equation(1).Therefore, equation(1) becomes

$$S = 4\pi r^2 \quad \text{original equation}$$

$$S = 4 \cdot \frac{22}{7} \cdot (7)^2 \quad \text{substitute } \frac{22}{7} \text{ for } \pi \text{ and } 7 \text{ for } r$$

$$S = \frac{4312}{7} \quad \text{simplify}$$

$$S = 616 \text{ cm}^2$$

Therefore, the surface area S of the sphere whose radius $r = 7$ cm is,

$$S = 616 \text{ centimeter square .}$$

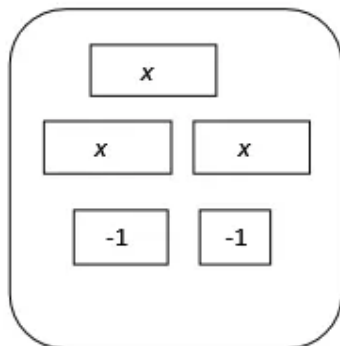
Answer 3AA.

Solving an equation involves operations like addition, subtraction, multiplication and division.
Consider the expression,

$$3x - 2 = 10 \dots\dots(1)$$

Equation(1) is solved in the following ways.

Step 1: Model the equation.

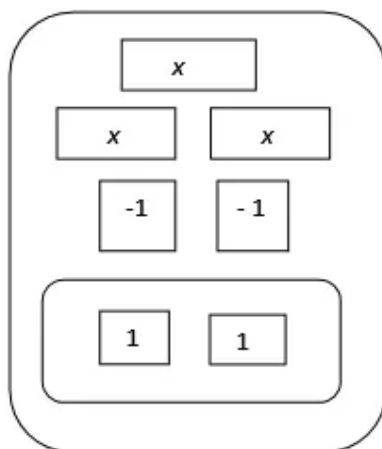
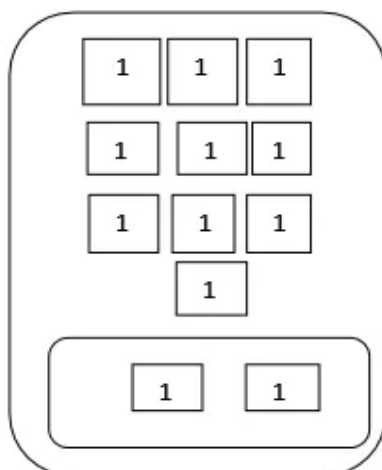


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$$3x - 2 = 10$$

Place 3 x tiles and 2 negative 1 tiles on side of the mat. Place 10 positive 1 tiles on the other side of the mat.

Step 2 : Isolate the x term.

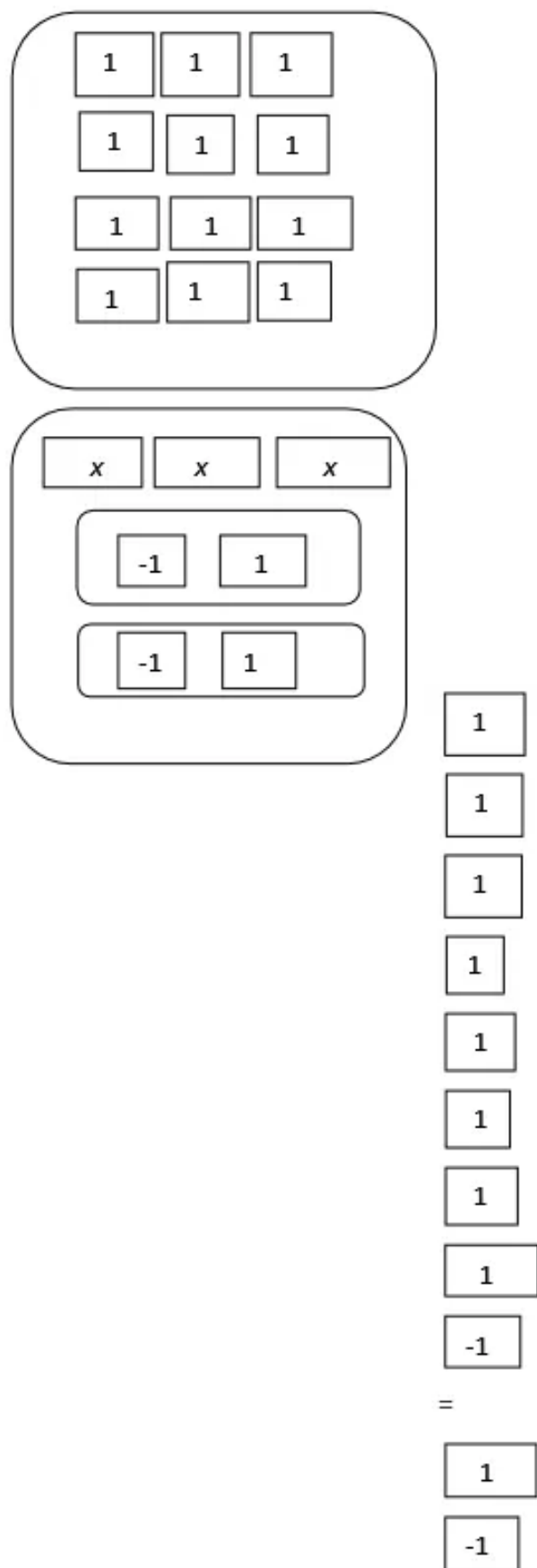


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$$3x - 2 + 2 = 10 + 2$$

Since there are 2 negative 1 tiles with the x tiles, add 2 positive 1 tiles to each side to form zero pairs.

Step 3 : Remove zero pairs.

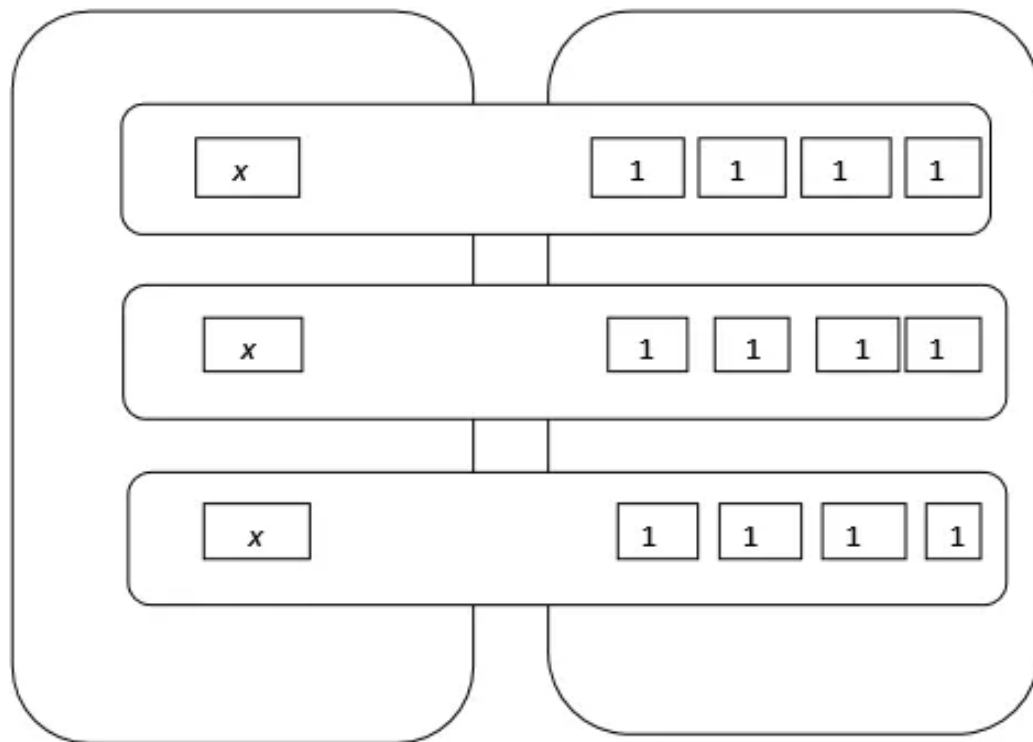


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$$3x = 12$$

Group the tiles to form zero pairs and remove the zero pairs.

Step 4: Group the tiles.



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$$\frac{3x}{3} = \frac{12}{3}$$

Separate the tiles into 3 equal groups to match the 3 x tiles. Each x tile is paired with 4 positive 1 tiles. Thus, $x = 4$

Consider the equation $8n = -72$

Method 1:

$$8n = -72 \quad \text{original equation}$$

$$8n(8) = -72(8) \quad \text{multiply by 8 on each side}$$

$$n = -576 \quad \text{simplify}$$

Method 2:

$$8n = -72 \quad \text{original equation}$$

$$\frac{8n}{8} = \frac{-72}{8} \quad \text{divide by 8 on each side}$$

$$n = -9 \quad \text{simplify}$$

Answer 3PQ.

Since in method 1, while calculating, $64n$ is interpreted as, n and the value of n is -576.

Therefore, the second method is correct.

Solving an equation involves various operations like addition, subtraction, multiplication and division. Consider the equation,

$$d + 18 = -27 \quad \text{.....(1)}$$

Equation(1) is solved in following steps:

$$d + 18 = -27 \quad \text{original equation}$$

$$d + 18 - 18 = -27 - 18 \quad \text{subtract 18 from each side}$$

$$d = -45 \quad \text{simplify}$$

Check the result $d = -45$.

$$d + 18 = -27 \text{ original equation}$$

$$-45 + 18 = -27 \text{ substitute } -45 \text{ for } d$$

$$-27 = -14 \text{ the solution is } -45$$

Therefore, the final answer is $d = -45$

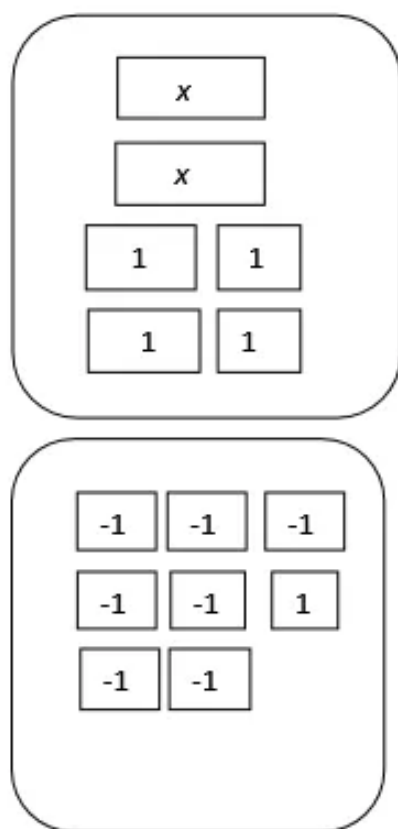
Answer 4AA.

Solving an equation involves operations like addition, subtraction, multiplication and division.
Consider the expression,

$$2x + 4 = -8 \text{(1)}$$

Equation(1) is solved in the following ways.

Step 1: Model the equation.

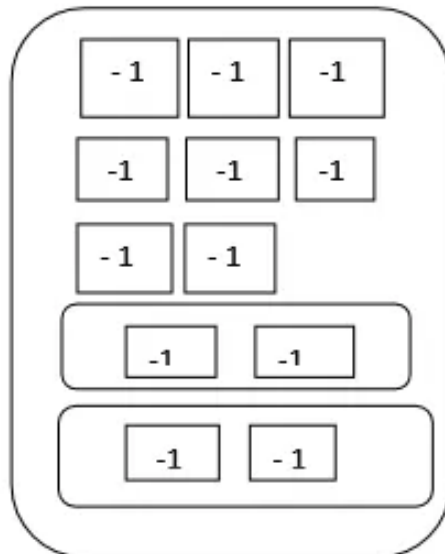
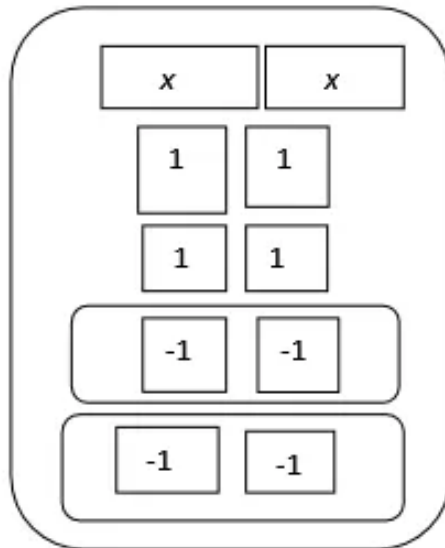


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$$2x + 4 = -8$$

Place 2 x tiles and 4 positive 1 tiles on side of the mat. Place 8 negative 1 tiles on the other side of the mat.

Step 2 : Isolate the x term.



Answer 4CU.

For any numbers a , b and c if $a = b$, then $ac = bc$.

Consider the equation,

$$-2g = -84 \dots\dots(1)$$

Multiply equation(1) by $\left(-\frac{1}{2}\right)$ on both sides. Therefore, equation(1) becomes

$$(-2g) \cdot \left(-\frac{1}{2}\right) = (-84) \cdot \left(-\frac{1}{2}\right)$$

$$g = 42$$

CHECK

$$-2g = -84 \quad \text{original equation}$$

$$-2(42) = -84 \quad \text{substitute 42 for } g$$

$$-84 = -84 \quad \text{the solution is 42}$$

Hence the final answer is $g = 42$.

Answer 4PQ.

Solving an equation involves various operations like addition, subtraction, multiplication and division. Consider the equation,

$$m - 77 = -61 \quad \dots\dots(1)$$

Equation(1) is solved in following steps:

$$m - 77 = -61 \quad \text{original equation}$$

$$m - 77 + 77 = -61 + 77 \quad \text{add 77 to each side}$$

$$m = 16 \quad \text{simplify}$$

Check the result $m = 16$.

$$m - 77 = -61 \quad \text{original equation}$$

$$16 - 77 = -61 \quad \text{substitute 16 for } m$$

$$-61 = -61 \quad \text{the solution is 16}$$

Therefore, the final answer is $m = 16$

Answer 5AA.

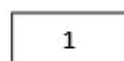
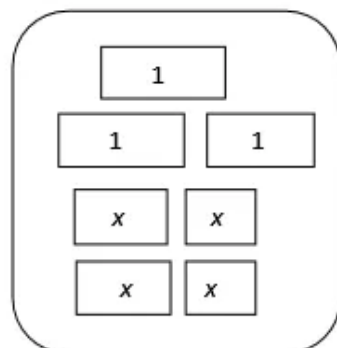
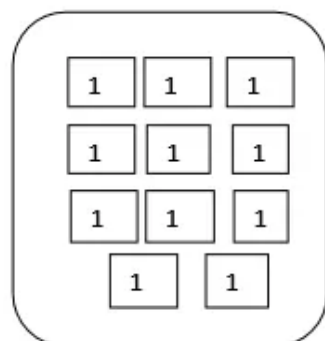
Solving an equation involves operations like addition, subtraction, multiplication and division.

Consider the expression,

$$4x + 3 = 11 \quad \dots\dots(1)$$

Equation(1) is solved in the following ways.

Step 1: Model the equation.

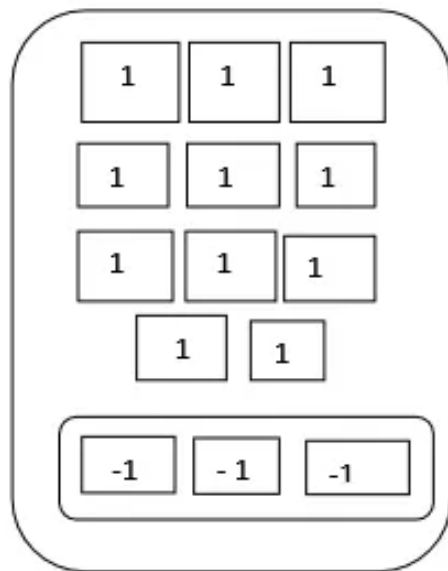
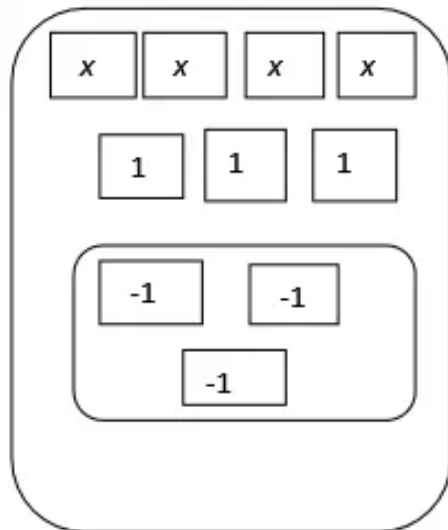


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$$3+4x=11$$

Place 4 x tiles and 3 positive 1 tiles on side of the mat. Place 11 positive 1 tiles on the other side of the mat.

Step 2 : Isolate the x term.



Answer 5PQ.

Solving an equation involves various operations like addition, subtraction, multiplication and division. Consider the equation,

$$-12 + a = -36 \dots\dots(1)$$

Equation(1) is solved in following steps:

$-12 + a = -36$	original equation
$-12 + a + 12 = -36 + 12$	add 12 to each side
$a = -24$	simplify

Check the result $a = -24$.

$-12 + a = -36$	original equation
$-12 - 24 = -36$	substitute -24 for a
$-36 = -36$	the solution is -24

Therefore, the final answer is $a = -24$

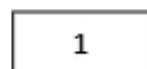
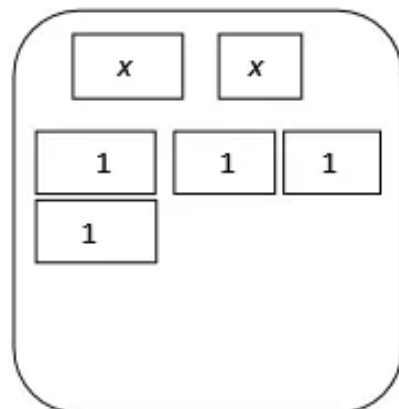
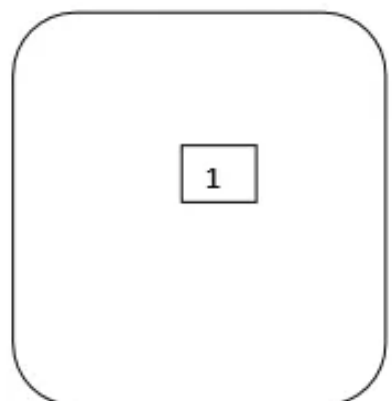
Answer 6AA.

Solving an equation involves operations like addition, subtraction, multiplication and division. Consider the expression,

$$2x + 7 = 1 \dots\dots(1)$$

Equation(1) is solved in the following ways.

Step 1: Model the equation.



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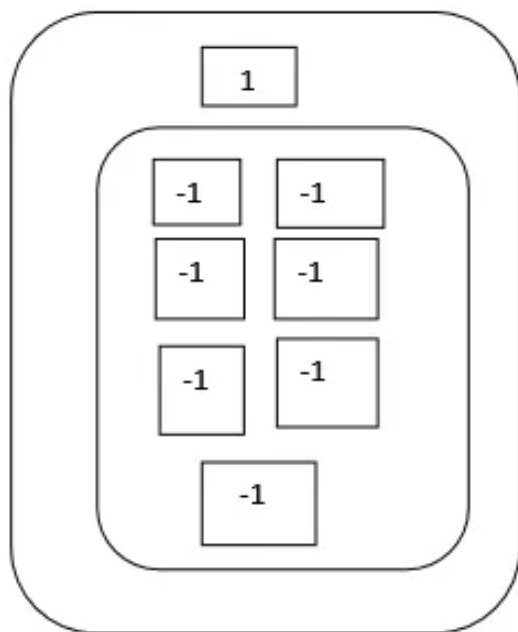
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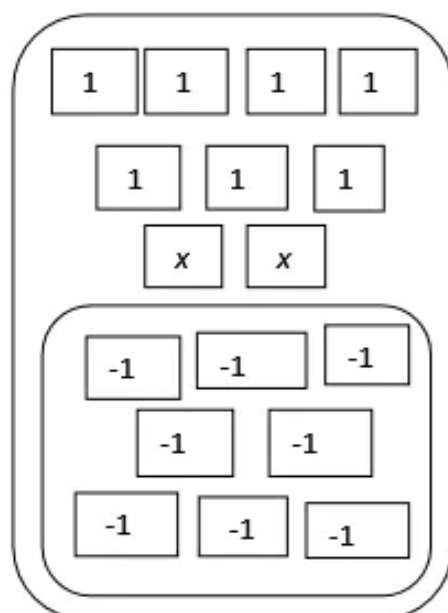
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$$2x + 7 = 1$$

Place 2 x tiles and 7 positive 1 tiles on side of the mat. Place 1 positive 1 tiles on the other side of the mat.

Step 2 : Isolate the x term.





x

x

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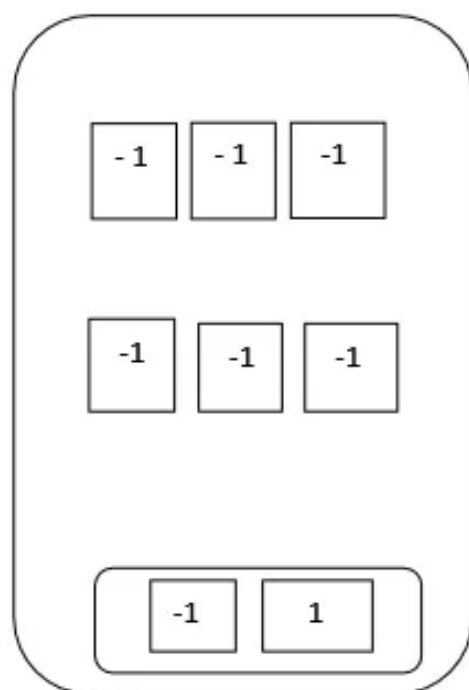
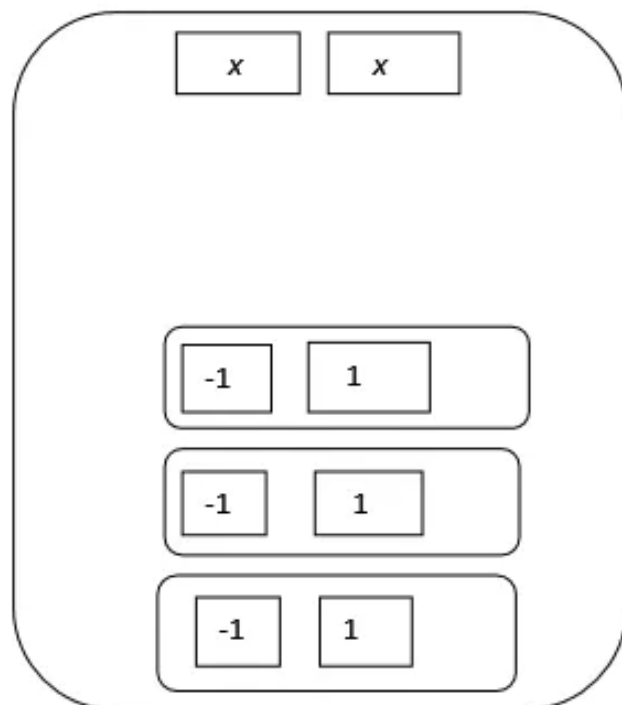
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$$2x + 7 - 7 = 1 - 7$$

Since there are 7 positive 1 tiles with the x tiles, add 7s negative 1 tiles to each side to form zero pairs.

Step 3 : Remove zero pairs.



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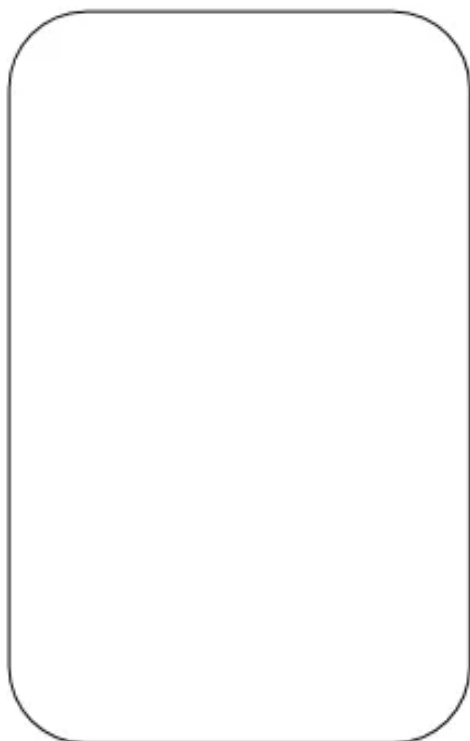
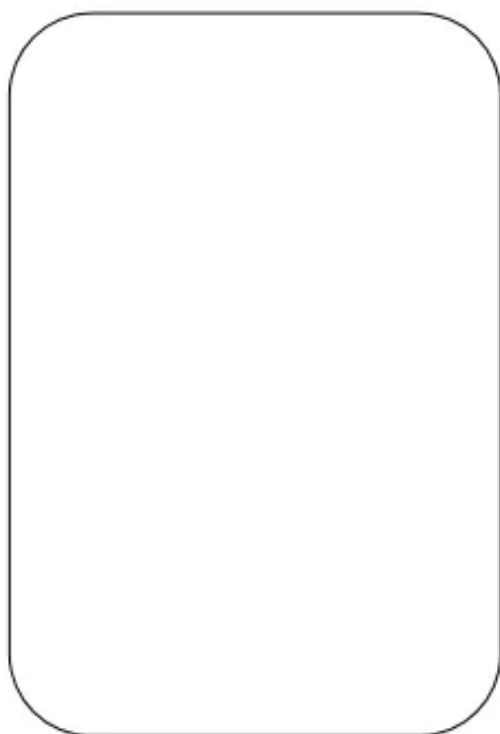
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$$2x = -6$$

Group the tiles to form zero pairs and remove the zero pairs.

Step 4: Group the tiles.



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$$\frac{2x}{2} = \frac{-6}{2}$$

Separate the tiles into 2 equal groups to match the 4 x tiles. Each x tile is paired with 3 negative 1 tiles. Thus, $x = -3$

Answer 6CU.

For any numbers a , b and c , if $a = b$, then $ac = bc$.

Consider the equation

$$\frac{a}{36} = \frac{4}{9} \dots\dots(1)$$

Multiply equation(1) by 36 on both sides. Then equation(1) becomes

$$\frac{a}{36} \cdot 36 = \frac{4}{9} \cdot 36$$

$$a = \frac{144}{9}$$

$$a = 16$$

CHECK

$$\frac{a}{36} = \frac{4}{9}$$

original equation

$$\frac{16}{36} = \frac{4}{9}$$

substitute 16 for a

$$\frac{4}{9} = \frac{4}{9}$$

on simplification

Hence the final answer is $a = 16$.

Answer 6PQ.

Solving an equation involves various operations like addition, subtraction, multiplication and division. Consider the equation,

$$t - (-16) = 9 \dots\dots(1)$$

Equation(1) is solved in following steps:

$$t - (-16) = 9 \quad \text{original equation}$$

$$t + 16 = 9 \quad \text{simplify}$$

$$t + 16 - 16 = 9 - 16 \quad \text{subtract 16 from each side}$$

$$t = -7 \quad \text{simplify}$$

Check the result $t = -7$.

$$t - (-16) = 9 \quad \text{original equation}$$

$$t + 16 = 9 \quad \text{simplify}$$

$$-7 + 16 = 9 \quad \text{substitute } -7 \text{ for } t$$

$$9 = 9 \quad \text{the solution is } -7$$

Therefore, the final answer is $t = -7$

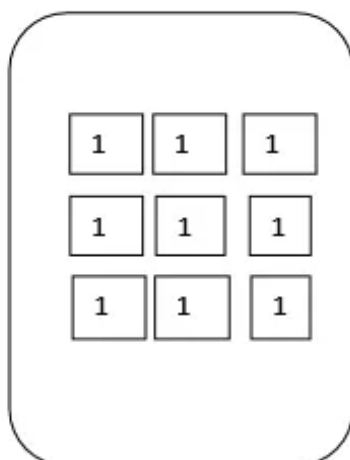
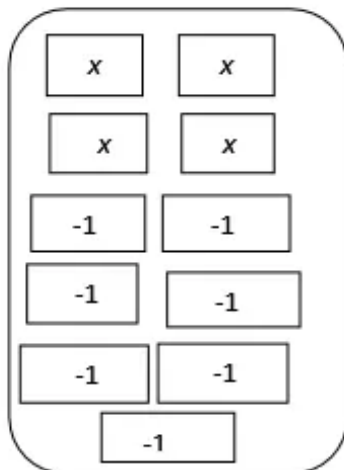
Answer 7AA.

Solving an equation involves operations like addition, subtraction, multiplication and division. Consider the expression,

$$4x - 7 = 9 \dots\dots(1)$$

Equation(1) is solved in the following ways.

Step 1: Model the equation.



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$$-1$$

$$-1$$

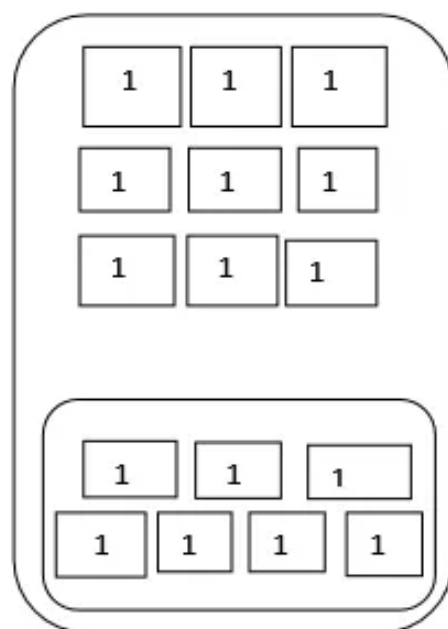
$$-1$$

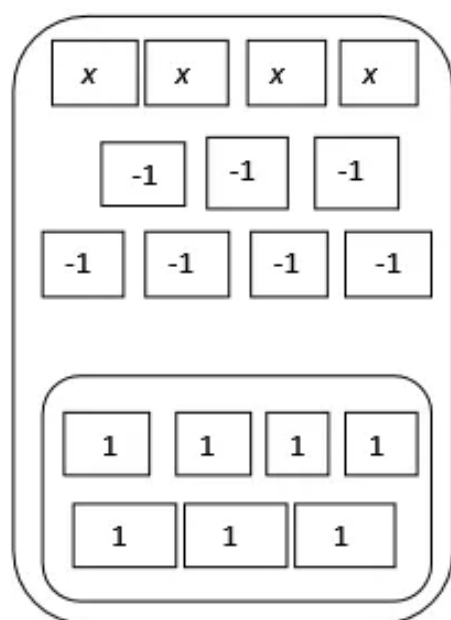
$$-1$$

$$4x - 7 = 9$$

Place 4 x tiles and 7 negative 1 tiles on side of the mat. Place 9 positive 1 tiles on the other side of the mat.

Step 2 : Isolate the x term.





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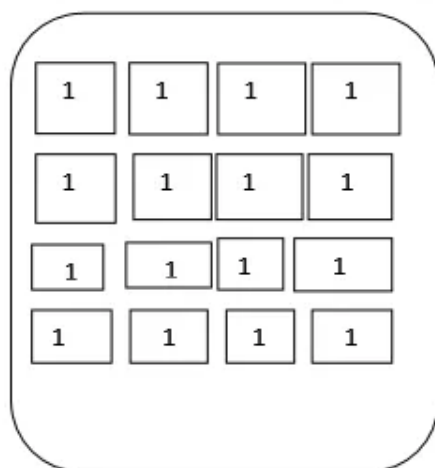
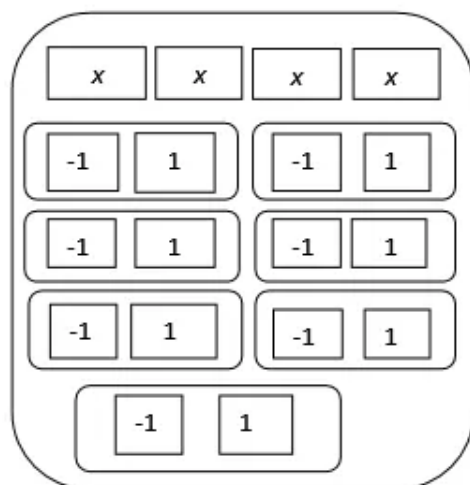
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$$4x - 7 + 7 = 9 + 7$$

Since there are 7 negative 1 tiles with the x tiles, add 7 positive 1 tiles to each side to form zero pairs.

Step 3 : Remove zero pairs.



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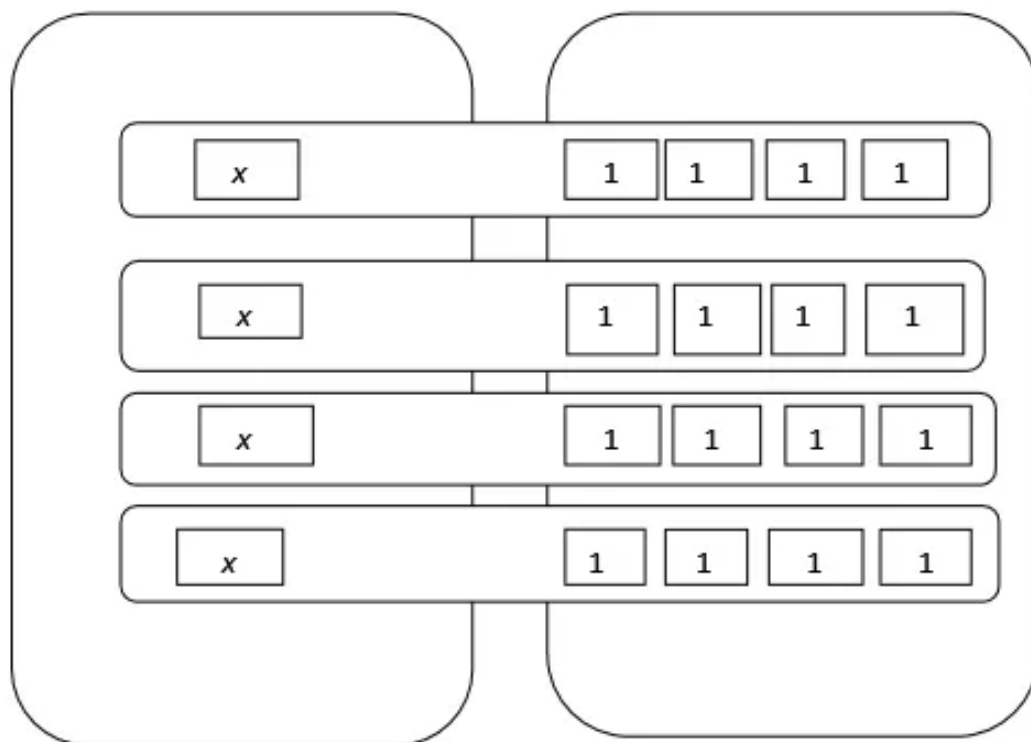
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$$4x = 16$$

Group the tiles to form zero pairs and remove the zero pairs.

Step 4: Group the tiles.



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$$\boxed{1}$$

$$\frac{4x}{4} = \frac{16}{4}$$

Separate the tiles into 4 equal groups to match the 4 x tiles. Each x tile is paired with 4 positive 1 tiles. Thus, $x = 4$

Answer 7CU.

For any numbers a , b and c , if $a = b$, then $ac = bc$.

Consider the equation

$$\frac{4}{5}k = \frac{8}{9} \dots\dots(1)$$

Multiply equation(1) by $\frac{5}{4}$ on both sides. Then equation(1) becomes

$$\frac{5}{4} \cdot \frac{4}{5}k = \frac{5}{4} \cdot \frac{8}{9}$$

$$k = \frac{10}{9}$$

CHECK

$$\frac{4}{5}k = \frac{8}{9}$$

original equation

$$\frac{4}{5} \cdot \frac{10}{9} = \frac{8}{9}$$

substitute $\frac{10}{9}$ for k

$$\frac{8}{9} = \frac{8}{9}$$

on simplification

Hence the final answer is $k = \frac{10}{9}$.

Answer 7PQ.

For any numbers a , b and c with if $a = b$ then

$$ac = bc \dots\dots(1)$$

Consider the equation,

$$\frac{2}{3}p = 18 \dots\dots(2)$$

Apply equation(1) to equation(2). That is, multiply equation(2) by 3.

Therefore, equation(2) becomes

$$\frac{2}{3}p \cdot 3 = 18 \cdot 3 \quad \text{multiply by 3 on both sides}$$

$$2p = 54 \quad \text{simplify}$$

$$\frac{2p}{2} = \frac{54}{2} \quad \text{divide by 2 on each side}$$

$$p = 27 \quad \text{simplify}$$

Hence the value of $p = 27$. Check this result.

CHECK

$$\frac{2}{3}p = 18 \quad \text{original equation}$$

$$\frac{2}{3} \cdot 27 = 18 \quad \text{substitute 27 for } p$$

$$\frac{54}{3} = 18 \quad \text{simplify}$$

$$18 = 18 \quad \text{the solution is 27}$$

Therefore the final answer is $p = 27$

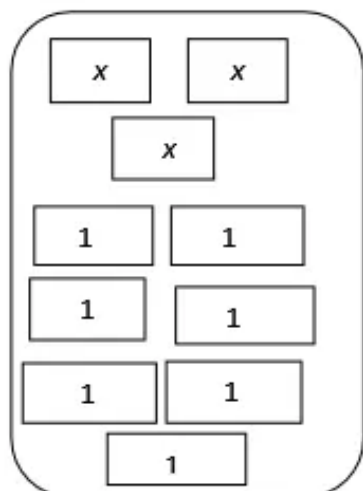
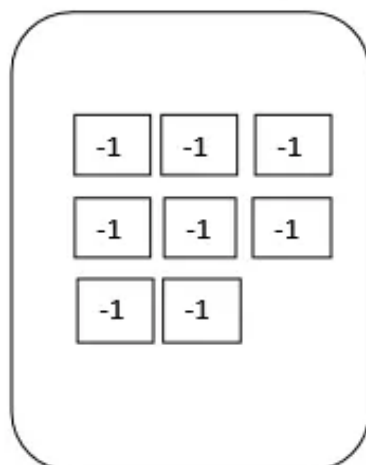
Answer 8AA.

Solving an equation involves operations like addition, subtraction, multiplication and division.
Consider the expression,

$$3x + 7 = -8 \dots\dots(1)$$

Equation(1) is solved in the following ways.

Step 1: Model the equation.



$$1$$

=

$$-1$$

$$-1$$

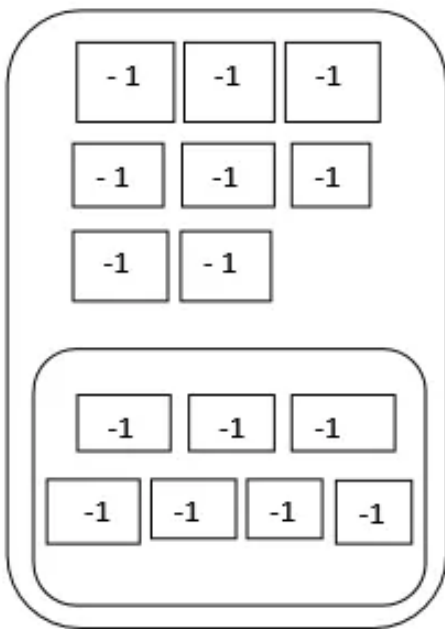
$$-1$$

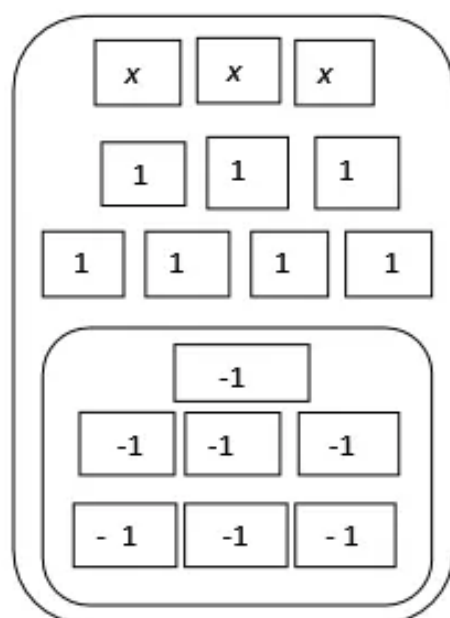
$$-1$$

$$3x + 7 = -8$$

Place 3 x tiles and 7 positive 1 tiles on side of the mat. Place 8 negative 1 tiles on the other side of the mat.

Step 2 : Isolate the x term.





x

x

1

=

1

1

1

-1

-1

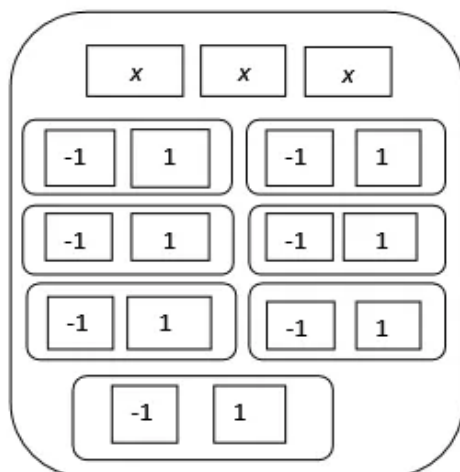
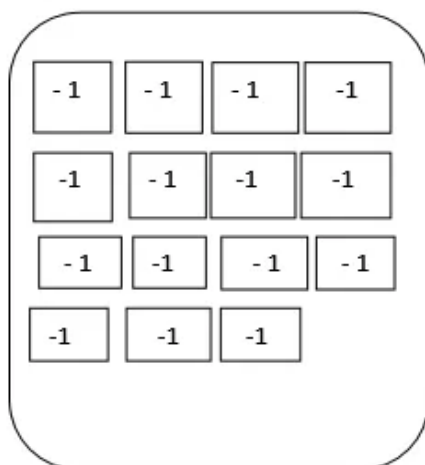
-1

-1

$$3x + 7 - 7 = -8 - 7$$

Since there are 7 positive 1 tiles with the x tiles, add 7 negative 1 tiles to each side to form zero pairs.

Step 3 : Remove zero pairs.



1

1

1

1

1

1

1

1

-1

=

-1

1

-1

$$3x = -15$$

Group the tiles to form zero pairs and remove the zero pairs.

Step 4: Group the tiles.

<div style="border: 1px solid black; display: inline-block; padding: 2px 10px;">x</div>	<div style="display: flex; justify-content: space-around;"> <div style="border: 1px solid black; padding: 2px 10px;">-1</div> <div style="border: 1px solid black; padding: 2px 10px;">-1</div> <div style="border: 1px solid black; padding: 2px 10px;">-1</div> <div style="border: 1px solid black; padding: 2px 10px;">-1</div> <div style="border: 1px solid black; padding: 2px 10px;">-1</div> </div>
<div style="border: 1px solid black; display: inline-block; padding: 2px 10px;">x</div>	<div style="display: flex; justify-content: space-around;"> <div style="border: 1px solid black; padding: 2px 10px;">-1</div> <div style="border: 1px solid black; padding: 2px 10px;">-1</div> <div style="border: 1px solid black; padding: 2px 10px;">-1</div> <div style="border: 1px solid black; padding: 2px 10px;">-1</div> <div style="border: 1px solid black; padding: 2px 10px;">-1</div> </div>
<div style="border: 1px solid black; display: inline-block; padding: 2px 10px;">x</div>	<div style="display: flex; justify-content: space-around;"> <div style="border: 1px solid black; padding: 2px 10px;">-1</div> <div style="border: 1px solid black; padding: 2px 10px;">-1</div> <div style="border: 1px solid black; padding: 2px 10px;">-1</div> <div style="border: 1px solid black; padding: 2px 10px;">-1</div> <div style="border: 1px solid black; padding: 2px 10px;">-1</div> </div>

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1

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1

Answer 8CU.

For any numbers a , b and c , if $a = b$, then $ac = bc$.

Consider the equation

$$3.15 = 1.5y \dots\dots(1)$$

Multiply equation(1) by $\frac{1}{1.5}$ on both sides. Then equation(1) becomes

$$\frac{1}{1.5} \cdot (3.15) = \frac{1}{1.5} \cdot (1.5y)$$

$$\left(\frac{3.15}{1.5} \right) = y$$

$$2.1 = y$$

CHECK

$$3.15 = 1.5y \quad \text{original equation}$$

$$3.15 = 1.5(2.1) \quad \text{substitute 2.1 for } y$$

$$3.15 = 3.15 \quad \text{on multiplication}$$

Hence the final answer is $y = 2.1$.

Answer 8PQ.

For any numbers a , b and c with $c \neq 0$ if $a = b$ then

$$\frac{a}{c} = \frac{b}{c} \dots\dots(1)$$

Consider the equation,

$$-17y = 391 \dots\dots(2)$$

Since $-17 \neq 0$, apply equation(1) to equation(2). Therefore, equation(2) becomes

$$\begin{aligned} \frac{-17y}{-17} &= \frac{391}{-17} && \text{divide by } -17 \text{ on both sides} \\ y &= -23 && \text{simplify} \end{aligned}$$

Hence the value of $y = -23$. Check this result

CHECK

$$-17y = 391 \quad \text{original equation}$$

$$-17(-23) = 391 \quad \text{substitute } -23 \text{ for } y$$

$$391 = 391 \quad \text{the solution is } -23$$

Therefore the final answer is $y = -23$

Answer 9AA.

Solving an equation involves operations like addition, subtraction, multiplication and division.

Consider the equation,

$$7x - 12 = -61 \dots\dots(1)$$

Equation(1) can be solved as,

$$7x - 12 + 12 = -61 + 12 \quad \text{add 12 to each side}$$

$$7x = -49$$

$$\frac{7x}{7} = \frac{-49}{7} \quad \text{divide by 7 on each side}$$

$$x = -7$$

Thus, we get $x = -7$.

CHECK

$$7x - 12 = -61 \quad \text{original equation}$$

$$7(-7) - 12 = -61 \quad \text{substitute } -7 \text{ for } x$$

$$-49 - 12 = -61$$

$$-61 = -61 \quad \text{the solution is } -7$$

Therefore, the required answer is $x = -7$.

Answer 9CU.

For any numbers a , b and c with $c \neq 0$ if $a = b$ then

$$\frac{a}{c} = \frac{b}{c} \dots\dots(1)$$

For any numbers a , b and c if $a = b$, then

$$ac = bc \dots\dots(2)$$

Consider the equation,

$$\left(3\frac{1}{4}\right)p = 2\frac{1}{2} \dots\dots(3)$$

Equation(3) can be expressed as,

$$\frac{13}{4}p = \frac{5}{2} \quad \text{Rewrite each mixed number as an improper fraction} \dots\dots(4)$$

Apply equation(2) to equation(4). That is, multiply equation (4) by 4 on both sides .

Therefore, equation(4) becomes,

$$\begin{aligned} 4 \cdot \frac{13}{4}p &= 4 \cdot \frac{5}{2} \\ 13p &= \frac{20}{2} \quad \text{simplify} \\ 13p &= 10 \quad \text{simplify} \end{aligned}$$

Consider the equation,

$$13p = 10 \dots\dots(5)$$

Since $13 \neq 0$, apply equation(1) to equation(5). That is,

$$\begin{aligned} \text{divide equation(5) by 13 on both sides .Hence equation(5) becomes,} \quad \frac{13}{13}p &= \frac{10}{13} \\ p &= \frac{10}{13} \quad \text{simplify} \end{aligned}$$

Thus, we get $p = \frac{10}{13}$. Check the value of p is correct or not.

CHECK

$$\begin{aligned} \left(3\frac{1}{4}\right)p &= 2\frac{1}{2} \quad \text{originaequation} \\ \frac{13}{4}p &= \frac{5}{2} \quad \text{rewrite each mixed number as an improper fraction} \\ \frac{13}{4} \cdot \frac{10}{13} &= \frac{5}{2} \quad \text{substitute } \frac{10}{13} \text{ for } p \\ \frac{130}{52} &= \frac{5}{2} \\ \frac{5}{2} &= \frac{5}{2} \quad \text{simplify} \end{aligned}$$

Therefore, the value of $p = \frac{10}{13}$.

Answer 9PQ.

For any numbers a , b and c with $c \neq 0$ if $a = b$ then

$$\frac{a}{c} = \frac{b}{c} \dots\dots(1)$$

Consider the equation,

$$5x = -45 \dots\dots(2)$$

Since $5 \neq 0$, apply equation(1) to equation(2). Therefore, equation(2) becomes

$$\begin{aligned} \frac{5x}{5} &= \frac{-45}{5} && \text{divide by 5 on both sides} \\ x &= -9 && \text{simplify} \end{aligned}$$

Hence the value of $x = -9$. Check this result

CHECK

$$5x = -45 \quad \text{original equation}$$

$$5(-9) = -45 \quad \text{substitute } -9 \text{ for } x$$

$$-45 = -45 \quad \text{the solution is } -9$$

Therefore the final answer is $x = -9$

Answer 10CU.

For any numbers a , b and c with $c \neq 0$, if $a = b$, then

$$\frac{a}{c} = \frac{b}{c} \dots\dots(1)$$

Consider the statement, five times a number is 120. This statement can be expressed as,

$$\underbrace{\text{Five}}_5 \underbrace{\text{times a number}}_n \underbrace{\text{is}}_{= 120} \underbrace{120}_{120}$$

$$5n = 120 \quad \text{original equation}$$

$$\frac{5n}{5} = \frac{120}{5} \quad \text{apply equation(1) and divide each side by 5}$$

$$n = 24 \quad \text{simplify}$$

Thus, we get $n = 24$. Check this result.

CHECK

$$5n = 120 \quad \text{original equation}$$

$$5.24 = 120 \quad \text{substitute 24 for } n$$

$$120 = 120$$

Therefore, the value of $n = 24$.

Answer 10PQ.

For any numbers a , b and c with if $a = b$ then

$$ac = bc \dots\dots(1)$$

Consider the equation,

$$-\frac{2}{5}d = -10 \dots\dots(2)$$

Apply equation(1) to equation(2). That is, multiply equation(2) by 3.

Therefore, equation(2) becomes

$$-\frac{2}{5}d \cdot 5 = -10 \cdot 5 \quad \text{multiply by 5 on both sides}$$

$$-2d = -50 \quad \text{simplify}$$

$$\frac{-2d}{-2} = \frac{-50}{-2} \quad \text{divide by } -2 \text{ on each side}$$

$$d = 25 \quad \text{simplify}$$

Hence the value of $d = 25$. Check this result.

CHECK

$$-\frac{2}{5}d = -10 \quad \text{original equation}$$

$$-\frac{2}{5} \cdot 25 = -10 \quad \text{substitute 25 for } d$$

$$-\frac{50}{5} = -10 \quad \text{simplify}$$

$$-10 = -10 \quad \text{the solution is 25}$$

Therefore the final answer is $d = 25$

Answer 11CU.

For any numbers a , b and c with $c \neq 0$, if $a = b$, then

$$\frac{a}{c} = \frac{b}{c} \dots\dots(1)$$

Consider the statement, two fifths of a number equals -24 . This statement can be expressed as,

$$\underbrace{\underbrace{2}_{\frac{2}{5}} \underbrace{\text{fifths of a number}}_n}_{\text{is}} \underbrace{-24}_{= -24}$$

$$\frac{2}{5}n = -24 \quad \text{original equation}$$

$$5 \cdot \frac{2}{5}n = 5 \cdot (-24) \quad \text{multiply each side by 5}$$

$$2n = -120 \quad \text{simplify}$$

$$\frac{2n}{2} = \frac{-120}{2} \quad \text{apply equation(1) and divide each side by 2}$$

$$n = -60 \quad \text{simplify}$$

Thus, we get $n = -60$. Check this result.

CHECK

$$\frac{2}{5}n = -24 \quad \text{original equation}$$

$$\frac{2}{5}(-60) = -24 \quad \text{substitute } -60 \text{ for } n$$

$$-\frac{120}{5} = -24$$

$$-24 = -24$$

Therefore, the value of $n = -60$.

12CU.

For any numbers a , b and c with $c \neq 0$ if $a = b$ then

$$\frac{a}{c} = \frac{b}{c} \quad \dots\dots(1)$$

Let discharge of a river be D , width of the river be w , depth of the river be d and speed of the river be S . These notations are related as,

$$\underbrace{\text{Discharge of a river}}_D = \underbrace{\text{width}}_w \times \underbrace{\text{depth}}_d \times \underbrace{\text{speed of river}}_S$$

$$D = wdS \quad \text{original equation}$$

Thus, we get $D = wdS \quad \dots\dots(2)$

Substitute $w = 533 \text{ m}$, $S = 0.6 \text{ m/s}$, $D = 3198 \text{ m}^3/\text{s}$ in equation(2). Therefore, equation(2) becomes

$$D = wdS \quad \text{original equation}$$

$$3198 = (533)d(0.6) \quad \text{substitute the values}$$

$$3198 = 319.8d \quad \text{simplify}$$

$$\frac{3198}{319.8} = \frac{319.8}{319.8}d \quad \text{divide by 319.8 one each side}$$

$$10 \text{ m} = d \quad \text{simplify}$$

Thus, we get $d = 10 \text{ m}$.

Hence, average depth of the river is 10 meters

Answer 13PA.

For any numbers a , b and c with $c \neq 0$ if $a = b$ then

$$\frac{a}{c} = \frac{b}{c} \quad \dots\dots(1)$$

Consider the equation,

$$-5r = 55 \quad \dots\dots(2)$$

Since $-5 \neq 0$, apply equation(1) to equation(2).Therefore, equation(2) becomes

$$\frac{-5r}{-5} = \frac{55}{-5} \quad \text{divide by } -5 \text{ on both sides}$$
$$r = -11 \quad \text{simplify}$$

Hence the value of $r = -11$. Check this result.

CHECK

$$-5r = 55 \quad \text{original equation}$$

$$-5(-11) = 55 \quad \text{substitute } -11 \text{ for } r$$

$$55 = 55 \quad \text{the solution is } -11$$

Therefore the final answer is $r = -11$

Answer 14PA.

For any numbers a , b and c with $c \neq 0$ if $a = b$ then

$$\frac{a}{c} = \frac{b}{c} \quad \text{.....(1)}$$

Consider the equation,

$$8d = 48 \quad \text{.....(2)}$$

Since $8 \neq 0$, apply equation(1) to equation(2).Therefore, equation(2) becomes

$$\frac{8d}{8} = \frac{48}{8} \quad \text{divide by 8 on both sides}$$
$$d = 6 \quad \text{simplify}$$

Hence the value of $d = 6$.

CHECK

$$8d = 48 \quad \text{original equation}$$

$$8(6) = 48 \quad \text{substitute 6 for } d$$

$$48 = 48 \quad \text{the solution is 6}$$

Therefore the final answer is $d = 6$

Answer 15PA.

For any numbers a , b and c with $c \neq 0$ if $a = b$ then

$$\frac{a}{c} = \frac{b}{c} \quad \text{.....(1)}$$

Consider the equation,

$$-910 = -26a \quad \text{.....(2)}$$

Since $-26 \neq 0$, apply equation(1) to equation(2). Therefore, equation(2) becomes

$$\frac{-910}{-26} = \frac{-26a}{-26} \quad \text{divide by } -26 \text{ on both sides}$$
$$35 = a \quad \text{simplify}$$

Hence the value of $a = 35$.

CHECK

$$\begin{aligned} -910 &= -26a && \text{original equation} \\ -910 &= -26(35) && \text{substitute 35 for } a \\ -910 &= -910 && \text{the solution is 35} \end{aligned}$$

Therefore the final answer is $a = 35$

Answer 16PA.

For any numbers a , b and c with $c \neq 0$ if $a = b$ then

$$\frac{a}{c} = \frac{b}{c} \quad \dots\dots(1)$$

Consider the equation,

$$-1634 = 86s \quad \dots\dots(2)$$

Since $86 \neq 0$, apply equation(1) to equation(2). Therefore, equation(2) becomes

$$\frac{-1634}{86} = \frac{86s}{86} \quad \text{divide by 86 on both sides}$$
$$-19 = s \quad \text{simplify}$$

Hence the value of $s = -19$.

CHECK

$$\begin{aligned} -1634 &= 86s && \text{original equation} \\ -1634 &= 86(-19) && \text{substitute } -19 \text{ for } s \\ -1634 &= -1634 && \text{the solution is } -19 \end{aligned}$$

Therefore the final answer is $s = -19$

Answer 17PA.

For any numbers a , b and c with if $a = b$ then

$$ac = bc \quad \dots\dots(1)$$

Consider the equation,

$$\frac{b}{7} = -11 \quad \dots\dots(2)$$

Apply equation(1) to equation(2). That is, multiply equation(2) by 7.

Therefore, equation(2) becomes

$$\frac{b}{7} \cdot 7 = -11 \cdot 7 \quad \text{multiply by 7 on both sides}$$
$$b = -77 \quad \text{simplify}$$

Hence the value of $b = -77$.

CHECK

$$\frac{b}{7} = -11 \quad \text{original equation}$$
$$\frac{-77}{7} = -11 \quad \text{substitute } -77 \text{ for } b$$
$$-11 = -11 \quad \text{the solution is } -77$$

Therefore the final answer is $b = -77$

Answer 18PA.

For any numbers a , b and c if $a = b$, then

$$ac = bc \quad \dots\dots(1)$$

Consider the equation

$$-\frac{v}{5} = -45 \quad \dots\dots(2)$$

Apply equation(1) to equation(2).

That is, multiply equation(2) by 5 on both sides. Therefore, equation(2) becomes

$$-\frac{v}{5} \cdot 5 = -45 \cdot 5$$
$$-v = -225 \quad \text{simplify}$$
$$v = 225$$

Hence we get $v = 225$

CHECK

$$-\frac{v}{5} = -45 \quad \text{original equation}$$
$$-\frac{225}{5} = -45 \quad \text{substitute 225 for } v$$
$$-45 = -45$$

Therefore, the final answer is $v = 225$

Answer 19PA.

For any numbers a , b and c if $a = b$, then

$$ac = bc \dots\dots(1)$$

Consider the equation

$$\frac{2}{3}n = 14 \dots\dots(2)$$

Apply equation(1) to equation(2).

That is, multiply equation(2) by 3 on both sides. Therefore, equation(2) becomes

$$\frac{2}{3}n \cdot 3 = 14 \cdot 3$$

$$2n = 42 \quad \text{simplify}$$

$$n = 21 \quad \text{simplify}$$

Hence we get $n = 21$

CHECK

$$\frac{2}{3}n = 14 \quad \text{original equation}$$

$$\frac{2}{3} \cdot 21 = 14 \quad \text{substitute 21 for n}$$

$$\frac{42}{3} = 14 \quad \text{simplify}$$

$$14 = 14$$

Therefore, the final answer is $n = 21$

Answer 20PA.

For any numbers a , b and c if $a = b$, then

$$ac = bc \dots\dots(1)$$

Consider the equation

$$\frac{2}{5}g = -14 \dots\dots(2)$$

Apply equation(1) to equation(2).

That is, multiply equation(2) by 5 on both sides. Therefore, equation(2) becomes

$$\frac{2}{5}g \cdot 5 = -14 \cdot 5$$

$$2g = -70 \quad \text{simplify}$$

$$g = -35 \quad \text{simplify}$$

Hence we get $g = -35$

CHECK

$$\frac{2}{5}g = -14 \quad \text{original equation}$$

$$\frac{2}{5}(-35) = -14 \quad \text{substitute } -35 \text{ for } g$$

$$\frac{-70}{5} = -14 \quad \text{simplify}$$

$$-14 = -14$$

Therefore, the final answer is $g = -35$

Answer 21PA.

For any numbers a , b and c if $a = b$, then

$$ac = bc \quad \dots\dots(1)$$

Consider the equation

$$\frac{g}{24} = \frac{5}{12} \quad \dots\dots(2)$$

Apply equation(1) to equation(2).

That is, multiply equation(2) by 24 on both sides. Therefore, equation(2) becomes

$$\frac{g}{24} \cdot 24 = \frac{5}{12} \cdot 24$$

$$g = \frac{120}{12} \quad \text{simplify}$$

$$g = 10 \quad \text{simplify}$$

Hence we get $g = 10$

CHECK

$$\frac{g}{24} = \frac{5}{12} \quad \text{original equation}$$

$$\frac{10}{24} = \frac{5}{12} \quad \text{substitute } 10 \text{ for } g$$

$$\frac{5}{12} = \frac{5}{12} \quad \text{simplify}$$

Therefore, the final answer is $g = 10$

Answer 22PA.

For any numbers a , b and c if $a = b$, then

$$ac = bc \quad \dots\dots(1)$$

Consider the equation

$$\frac{z}{45} = \frac{2}{5} \quad \dots\dots(2)$$

Apply equation(1) to equation(2).

That is, multiply equation(2) by 45 on both sides. Therefore, equation(2) becomes

$$\frac{z}{45} \cdot 45 = \frac{2}{5} \cdot 45$$

$$z = \frac{90}{5} \quad \text{simplify}$$

$$z = 18 \quad \text{simplify}$$

Hence we get $z = 18$

CHECK

$$\frac{z}{45} = \frac{2}{5} \quad \text{original equation}$$

$$\frac{18}{45} = \frac{2}{5} \quad \text{substitute 18 for } z$$

$$\frac{2}{5} = \frac{2}{5} \quad \text{simplify}$$

Therefore, the final answer is $z = 18$

Answer 23PA.

For any numbers a , b and c with $c \neq 0$ if $a = b$ then

$$\frac{a}{c} = \frac{b}{c} \quad \text{.....(1)}$$

Consider the equation,

$$1.9f = -11.78 \quad \text{.....(2)}$$

Since $1.9 \neq 0$, apply equation(1) to equation(2). Therefore, equation(2) becomes

$$\frac{1.9}{1.9}f = -\frac{11.78}{1.9} \quad \text{divide by 1.9 on both sides}$$

$$f = -6.2 \quad \text{simplify}$$

Hence the value of $f = -6.2$.

CHECK

$$1.9f = -11.78 \quad \text{original equation}$$

$$1.9(-6.2) = -11.78 \quad \text{substitute } -6.2 \text{ for } f$$

$$-11.78 = -11.78 \quad \text{the solution is } -6.2$$

Therefore the final answer is $f = -6.2$

Answer 24PA.

For any numbers a , b and c with $c \neq 0$ if $a = b$ then

$$\frac{a}{c} = \frac{b}{c} \dots\dots(1)$$

Consider the equation,

$$0.49k = 6.272 \dots\dots(2)$$

Since $0.49 \neq 0$, apply equation(1) to equation(2). Therefore, equation(2) becomes

$$\begin{aligned} \frac{0.49}{0.49}k &= \frac{6.272}{0.49} && \text{divide by 0.49 on both sides} \\ k &= 12.8 && \text{simplify} \end{aligned}$$

Hence the value of $k = 12.8$.

CHECK

$$0.49k = 6.272 \quad \text{original equation}$$

$$0.49(12.8) = 6.272 \quad \text{substitute 12.8 for } k$$

$$6.272 = 6.272 \quad \text{the solution is 12.8}$$

Therefore the final answer is $k = 12.8$

Answer 25PA.

For any numbers a , b and c with $c \neq 0$ if $a = b$ then

$$\frac{a}{c} = \frac{b}{c} \dots\dots(1)$$

Consider the equation,

$$-2.8m = 9.8 \dots\dots(2)$$

Since $-2.8 \neq 0$, apply equation(1) to equation(2). Therefore, equation(2) becomes

$$\begin{aligned} \frac{-2.8}{-2.8}m &= \frac{9.8}{-2.8} && \text{divide by } -2.8 \text{ on both sides} \\ m &= -3.5 && \text{simplify} \end{aligned}$$

Hence the value of $m = -3.5$.

CHECK

$$-2.8m = 9.8 \quad \text{original equation}$$

$$-2.8(-3.5) = 9.8 \quad \text{substitute } -3.5 \text{ for } m$$

$$9.8 = 9.8 \quad \text{the solution is } -3.5$$

Therefore the final answer is $m = -3.5$

Answer 26PA.

For any numbers a , b and c with $c \neq 0$ if $a = b$ then

$$\frac{a}{c} = \frac{b}{c} \dots\dots(1)$$

Consider the equation,

$$-5.73q = 97.41 \dots\dots(2)$$

Since $-5.73 \neq 0$, apply equation(1) to equation(2). Therefore, equation(2) becomes

$$\begin{aligned} \frac{-5.73}{-5.73}q &= \frac{97.41}{-5.73} && \text{divide by } -5.73 \text{ on both sides} \\ q &= -17 && \text{simplify} \end{aligned}$$

Hence the value of $q = -17$.

CHECK

$$-5.73q = 97.41 \quad \text{original equation}$$

$$-5.73(-17) = 97.41 \quad \text{substitute } -17 \text{ for } q$$

$$97.41 = 97.41 \quad \text{the solution is } -17$$

Therefore the final answer is $q = -17$

Answer 27PA.

For any numbers a , b and c with $c \neq 0$ if $a = b$ then

$$\frac{a}{c} = \frac{b}{c} \dots\dots(1)$$

For any numbers a , b and c if $a = b$, then

$$ac = bc \dots\dots(2)$$

Consider the equation,

$$\left(-2\frac{3}{5}\right)t = -22 \dots\dots(3)$$

Equation(3) can be rewritten as,

$$-\frac{13}{5}t = -22 \quad \text{rewrite mixed number as an improper fraction} \dots\dots(4)$$

Apply equation(2) to equation(4). That is,

$$\begin{aligned} \left(-\frac{13}{5}t\right)5 &= -22 \cdot 5 && \text{multiply equation(4) by 5 on both sides} \\ -\frac{65}{5}t &= -110 \\ 13t &= 110 && \text{simplify} \end{aligned}$$

Hence equation(4) is reduced to the form

$$13t = 110 \dots\dots(5)$$

Since $13 \neq 0$, apply equation(1) to equation(5). Therefore, equation(5) becomes

$$13t = 110 \quad \text{original equation}$$

$$\frac{13}{13}t = \frac{110}{13} \quad \text{divide by 13 on both sides}$$

$$t = \frac{110}{13} \quad \text{simplify}$$

CHECK

$$-\frac{13}{5}t = -22 \quad \text{original equation}$$

$$-\frac{13}{5}\left(\frac{110}{13}\right) = -22 \quad \text{substitute } \frac{110}{13} \text{ for } t$$

$$-22 = -22 \quad \text{simplify}$$

Therefore, the final answer is, $t = \frac{110}{13}$

Answer 28PA.

For any numbers a , b and c with $c \neq 0$ if $a = b$ then

$$\frac{a}{c} = \frac{b}{c} \dots\dots(1)$$

For any numbers a , b and c if $a = b$, then

$$ac = bc \dots\dots(2)$$

Consider the equation,

$$\left(3\frac{2}{3}\right)x = -5\frac{1}{2} \dots\dots(3)$$

Equation(3) can be expressed as,

$$\frac{11}{3}x = -\frac{11}{2} \quad \text{Rewrite each mixed number as an improper fraction} \dots\dots(4)$$

Consider the equation,

$$\frac{11}{3}x = -\frac{11}{2} \dots\dots(5)$$

Since $11 \neq 0$, apply equation(1) to equation(5). That is,

divide equation(5) by 11 on both sides .Hence equation(5) becomes,

$$\frac{1}{11} \cdot \frac{11}{3}x = -\frac{1}{11} \cdot \frac{11}{2}$$

$$\frac{x}{3} = -\frac{1}{2} \quad \text{simplify}$$

Consider the equation,

$$\frac{x}{3} = -\frac{1}{2} \dots\dots(6)$$

Apply equation(2) to equation(6). That is, multiply equation(6) by 3 on both sides . Hence equation(6) becomes

$$\begin{aligned}\frac{x}{3} \cdot 3 &= -\frac{1}{2} \cdot 3 \\ x &= -\frac{3}{2} \text{ simplify}\end{aligned}$$

Thus, we get $x = -\frac{3}{2}$

CHECK

$$\begin{aligned}\left(3\frac{2}{3}\right)x &= -5\frac{1}{2} && \text{original equation} \\ \frac{11}{3}x &= -\frac{11}{2} && \text{rewrite each mixed number as an improper fraction} \\ \frac{11}{3} \cdot \left(-\frac{3}{2}\right) &= -\frac{11}{2} && \text{substitute } -\frac{3}{2} \text{ for } x \\ -\frac{33}{6} &= -\frac{11}{2} \\ -\frac{11}{2} &= -\frac{11}{2} && \text{simplify}\end{aligned}$$

Therefore, the value of $x = -\frac{3}{2}$.

Answer 29PA.

For any numbers a , b and c with $c \neq 0$ if $a = b$ then

$$\frac{a}{c} = \frac{b}{c} \dots\dots(1)$$

Consider the equation,

$$-5h = -3\frac{2}{3} \dots\dots(2)$$

Equation(2) can be expressed as,

$$-5h = -\frac{11}{3} \text{ rewrite mixed number as an improper fraction } \dots\dots(3)$$

Since $-5 \neq 0$ apply equation(1) to equation(3).That is,

$$\frac{-5}{-5}h = -\frac{11}{3 \cdot (-5)} \quad \text{divide by } -5 \text{ on both sides}$$

$$h = \frac{11}{15} \quad \text{simplify}$$

CHECK

$$-5h = -\frac{11}{3} \quad \text{original equation}$$

$$-5\left(\frac{11}{15}\right) = -\frac{11}{3} \quad \text{substitute } \frac{11}{15} \text{ for } h$$

$$-\frac{55}{15} = -\frac{11}{3}$$

$$-\frac{11}{3} = -\frac{11}{3} \quad \text{simplify}$$

Therefore the final answer is $h = \frac{11}{15}$

Answer 30PA.

For any numbers a , b and c with $c \neq 0$ if $a = b$ then

$$\frac{a}{c} = \frac{b}{c} \quad \text{.....(1)}$$

Consider the equation,

$$3p = 4\frac{1}{5} \quad \text{.....(2)}$$

Equation(2) can be expressed as, $3p = \frac{21}{5}$ rewrite mixed number as an improper fraction
.....(3)

Since $3 \neq 0$ apply equation(1) to equation(3). That is,

$$\frac{3}{3}p = \frac{21}{5 \cdot (3)} \quad \text{divide by 3 on both sides}$$

$$p = \frac{21}{15} \quad \text{simplify}$$

$$p = \frac{7}{5} \quad \text{simplify}$$

Check the result $p = \frac{7}{5}$

CHECK

$$3p = \frac{21}{5} \quad \text{original equation}$$

$$3\left(\frac{7}{5}\right) = \frac{21}{5} \quad \text{substitute } \frac{7}{5} \text{ for } p$$

$$\frac{21}{5} = \frac{21}{5} \quad \text{simplify}$$

Therefore the final answer is $p = \frac{7}{5}$

Answer 31PA.

For any numbers a , b and c with $c \neq 0$ and if, $a = b$, then

$$\frac{a}{c} = \frac{b}{c} \dots\dots(1)$$

Consider the equation,

$$4m = 10 \dots\dots(2)$$

Since $4 \neq 0$, apply equation(1) to equation(2). That is, divide equation(2) by 4 on each side. Therefore, equation(2) becomes

$$\begin{aligned} \frac{4m}{4} &= \frac{10}{4} \quad \text{divide by 4 on each side} \\ m &= \frac{5}{2} \quad \text{simplify} \end{aligned}$$

Thus, we get $m = \frac{5}{2}$.

Use the value of m and calculate the value of $12m$. Therefore, we have

$$\begin{aligned} 12m &= 12 \cdot \frac{5}{2} \quad \text{substitute } \frac{5}{2} \text{ for } m \\ 12m &= \frac{60}{2} \\ 12m &= 30 \end{aligned}$$

Thus, we get $12m = 30$. Check this result.

CHECK

$$\begin{aligned} 4m &= 10 \quad \text{original equation} \\ 4m \cdot 3 &= 10 \cdot 3 \quad \text{multiply by 3 on each side} \\ 12m &= 30 \quad \text{simplify} \end{aligned}$$

Therefore, the value of $12m = 30$.

Answer 32PA.

For any numbers a , b and c with $c \neq 0$ and if, $a = b$, then

$$\frac{a}{c} = \frac{b}{c} \dots\dots(1)$$

Consider the equation,

$$15b = 55 \dots\dots(2)$$

Since $15 \neq 0$, apply equation(1) to equation(2). That is, divide equation(2) by 15 on each side. Therefore, equation(2) becomes

$$\frac{15b}{15} = \frac{55}{15} \quad \text{divide by 15 on each side}$$

$$b = \frac{11}{3} \quad \text{simplify}$$

Thus, we get $b = \frac{11}{3}$.

Use the value of b and calculate the value of $3b$. Therefore, we have

$$3b = 3 \cdot \frac{11}{3} \quad \text{substitute } \frac{11}{3} \text{ for } b$$

$$3b = \frac{33}{3}$$

$$3b = 11$$

Thus, we get $3b = 11$. Check this result.

CHECK

$$15b = 55 \quad \text{original equation}$$

$$\frac{15b}{5} = \frac{55}{5} \quad \text{divide by 5 on each side}$$

$$3b = 11 \quad \text{simplify}$$

Therefore, the value of $3b = 11$.

Answer 33PA.

For any numbers a , b and c with $c \neq 0$, if $a = b$, then

$$\frac{a}{c} = \frac{b}{c} \quad \dots\dots(1)$$

Consider the statement, seven times a number equals -84 . This statement can be expressed as,

$$\underbrace{\text{Seven}}_7 \underbrace{\text{times}}_{\times} \underbrace{\text{a number}}_n \underbrace{\text{equals}}_{=} \underbrace{-84}_{-84}$$

$$7n = -84 \quad \text{original equation}$$

$$\frac{7n}{7} = \frac{-84}{7} \quad \text{apply equation(1) and divide each side by 7}$$

$$n = -12 \quad \text{simplify}$$

Thus, we get $n = -12$.Check this result.

CHECK

$$7n = -84 \quad \text{original equation}$$

$$7(-12) = -84 \quad \text{substitute } -12 \text{ for } n$$

$$-84 = -84$$

Therefore, the value of $n = -12$.

Answer 34PA.

For any numbers a , b and c with $c \neq 0$,if $a = b$, then

$$\frac{a}{c} = \frac{b}{c} \dots\dots(1)$$

Consider the statement, **negative nine times a number is -117** .This statement can be expressed as,

$$\underbrace{\text{Negative nine}}_{-9} \underbrace{\text{times}}_{\times} \underbrace{\text{a number}}_n \underbrace{\text{is}}_{=} \underbrace{-117}_{-117}$$

$$-9n = -117 \quad \text{original equation}$$

Thus, we get the equation as,

$$-9n = -117 \dots\dots(2)$$

Since $-9 \neq 0$, apply equation(1) to equation(2).Therefore, equation(2) becomes

$$\frac{-9n}{-9} = \frac{-117}{-9} \quad \text{divide each side by } -9 \text{ on both sides}$$

$$n = 13 \quad \text{simplify}$$

Hence the required number is $n = 13$.

Answer 35PA.

For any numbers a , b and c if $a = b$, then

$$ac = bc \dots\dots(1)$$

Consider the statement, **one fifth of a number is 12** .This statement can be expressed as,

$$\underbrace{\text{One fifth of a number}}_{\frac{1}{5}n} \underbrace{\text{is}}_{=} \underbrace{12}_{12}$$

$$\frac{1}{5}n = 12 \quad \text{original equation}$$

Thus, we get the equation as,

$$\frac{1}{5}n = 12 \dots\dots(2)$$

Apply equation(1) to equation(2).That is, multiply each side of the equation by 5. Therefore, equation(2) becomes

$$\begin{aligned}\frac{n}{5} \cdot 5 &= 12 \cdot 5 \quad \text{multiply each side by 5 on both sides} \\ n &= 60 \quad \text{simplify}\end{aligned}$$

Hence the required number is $n = 60$.

Answer 36PA.

For any numbers a , b and c if $a = b$, then

$$ac = bc \dots\dots(1)$$

Consider the statement, **Negative three eighths times a number equals 12** .This statement can be expressed as,

$$\underbrace{\text{Negative three eighths}}_{\frac{3}{8}} \underbrace{\text{times}}_{\times} \underbrace{\text{a number}}_n \underbrace{\text{equals}}_{=} \underbrace{12}_{12} \quad \text{S}$$
$$-\frac{3}{8}n = 12 \quad \text{original equation}$$

Thus, we get the equation as,

$$-\frac{3}{8}n = 12 \dots\dots(2)$$

Apply equation(1) to equation(2).That is, multiply each side of the equation by 8. Therefore, equation(2) becomes

$$\begin{aligned}-\frac{3n}{8} \cdot 8 &= 12 \cdot 8 \quad \text{multiply each side by 8 on both sides} \\ -3n &= 96 \quad \text{simplify} \\ \frac{-3n}{-3} &= \frac{96}{-3} \quad \text{divide each side by } -3 \text{ on both sides} \\ n &= -32 \quad \text{simplify}\end{aligned}$$

Hence the required number is $n = -32$.

Answer 37PA.

For any numbers a , b and c if $a = b$, then

$$ac = bc \dots\dots(1)$$

Consider the statement, two and half times a number equals one and one fifth. This statement can be expressed as,

$$\underbrace{\text{Two and half}}_{2\frac{1}{2}} \underbrace{\text{times}}_{\times} \underbrace{\text{a number}}_n \underbrace{\text{equals}}_{=} \underbrace{\text{one and one fifth}}_{1\frac{1}{5}}$$

$$2\frac{1}{2}n = 1\frac{1}{5} \quad \text{original equation}$$

$$\frac{5}{2}n = \frac{6}{5} \quad \text{rewrite each mixed number as an improper fraction}$$

Thus, we get the equation as,

$$\frac{5}{2}n = \frac{6}{5} \dots\dots(2)$$

Apply equation(1) to equation(2). That is, multiply each side of the equation by 2. Therefore, equation(2) becomes

$$\frac{5n}{2} \cdot 2 = \frac{6}{5} \cdot 2 \quad \text{multiply each side by 2 on both sides}$$

$$5n = \frac{12}{5} \quad \text{simplify}$$

$$\frac{5n}{5} = \frac{12}{5(5)} \quad \text{divide each side by 5 on both sides}$$

$$n = \frac{12}{25} \quad \text{simplify}$$

Hence the required number is $n = \frac{12}{25}$.

Answer 38PA.

For any numbers a , b and c if $a = b$, then

$$ac = bc \dots\dots(1)$$

Consider the statement, One and one third times a number is -4.82 . This statement can be expressed as,

$$\underbrace{\text{one and one third}}_{1\frac{1}{3}} \underbrace{\text{times}}_{\times} \underbrace{\text{a number}}_n \underbrace{\text{is}}_{=} \underbrace{-4.82}_{-4.82}$$

$$1\frac{1}{3}n = -4.82 \quad \text{original equation}$$

$$\frac{4}{3}n = -4.82 \quad \text{rewrite mixed number as an improper fraction}$$

Thus, we get the equation as,

$$\frac{4}{3}n = -4.82 \dots\dots(2)$$

Apply equation(1) to equation(2). That is, multiply each side of the equation by 3. Therefore, equation(2) becomes

$$\frac{4n}{3} \cdot 3 = (-4.82) \cdot 3 \quad \text{multiply each side by 3 on both sides}$$

$$4n = -14.46 \quad \text{simplify}$$

$$\frac{4n}{4} = -\frac{14.46}{4} \quad \text{divide each side by 4 on both sides}$$

$$n = -3.615 \quad \text{simplify}$$

Hence the required number is $n = -3.615$.

Answer 39PA.

Let the total number of people = p

The number of left-handed people = l

One-seventh of the people are left-handed. This statement can be represented in equation form as,

$$\underbrace{\text{One-seventh of people}}_{\frac{1}{7}p} \underbrace{\text{are}}_{=} \underbrace{\text{left-handed}}_l$$

$$\frac{1}{7}p = l \quad \text{original equation}$$

Therefore, multiplication equation relating the number of left-handed people l and the total number of people p is $\boxed{l = \frac{1}{7}p}$

Answer 40PA.

Let the total number of people = p and the number of left-handed people = l

Consider one-seventh of the people are left-handed.

This statement can be represented in equation form as,

$$\underbrace{\text{One-seventh of people}}_{\frac{1}{7}p} \underbrace{\text{are}}_{=} \underbrace{\text{left-handed}}_l$$

$$\frac{1}{7}p = l \quad \text{original equation}$$

Find the number of left-handed people in a group of 350 people:

$$\frac{1}{7}p = l \quad \text{original equation}$$

$$\frac{1}{7}(350) = l \quad \text{substitute 350 for } p$$

$$50 = l \quad \text{simplify}$$

Therefore, the number of left-handed people in a group of 350 people is 50

Answer 41PA.

Consider the number of left-handed people in the group 65.

Find the number of people in the group:

Let the total number of people $= p$

The number of left-handed people $= l$

One-seventh of the people are left-handed. This statement can be represented in equation form as,

$$\underbrace{\text{One-seventh of people}}_{\frac{1}{7}p} \underbrace{\text{are}}_{=} \underbrace{\text{left-handed}}_l$$

$$\frac{1}{7}p = l \quad \text{original equation}$$

Therefore, multiplication equation relating the number of left-handed people l and the total number of people p is $l = \frac{1}{7}p$

Here $l = 65$

Now calculate the value of p :

$$\frac{1}{7}p = l \quad \text{original equation}$$

$$\frac{1}{7}p = 65 \quad \text{substitute 65 for } l$$

$$\frac{p}{7} \cdot 7 = 65 \cdot 7 \quad \text{multiply by 7 on each side}$$

$$p = 455$$

Hence, the number of people in that group is $p =$ 455

Answer 42PA.

Consider the doughnut weighed 1.5 tons and circumference 50 feet.

Find the diameter of the doughnut:

For a doughnut of diameter d , it's circumference C is given by, $C = \pi d$.

$$C = \pi d \quad \text{Original equation}$$

$$50 = \frac{22}{7} d \quad \text{Substitute 50 for } C \text{ and } \frac{22}{7} \text{ for } \pi$$

$$50 \cdot 7 = \left(\frac{22d}{7} \right) \cdot 7 \quad \text{Multiply by 7 on each side.}$$

$$350 = 22d$$

$$\frac{350}{22} = \frac{22d}{22} \quad \text{Divide by 22 on each side}$$

$$15.90 \approx d \quad \text{Simplify}$$

Therefore, the diameter of the doughnut is $d = \boxed{15.9 \text{ feet}}$ approximately.

Answer 43PA.

For any numbers a , b and c with $c \neq 0$ if $a = b$ then

$$\frac{a}{c} = \frac{b}{c} \dots\dots(1)$$

For a two-seam fastball , let d be the distance from the pitcher's mound to home plate. Let t be the time taken and r be the speed of the ball . Then these are related by the relation,

$$rt = d \dots\dots(2)$$

Now, $d = 60.5$ and $r = 126$

How long does it take a ball to go from mound to home plate
 t

Equation(2) becomes,

$$rt = d \quad \text{original equation}$$

$$126 \cdot t = 60.5 \quad \text{substitute 126 for } r \text{ and 60.5 for } d$$

$$\frac{126t}{126} = \frac{60.5}{126} \quad \text{divide by 126 on each side}$$

$$t = 0.48015873$$

Therefore, the time taken by two-seam fastball to go the home plate is

$$0.48015873 = 48.015873 \times 10^{-2} .$$

Answer 44PA.

For any numbers a , b and c with $c \neq 0$ if $a = b$ then

$$\frac{a}{c} = \frac{b}{c} \dots\dots(1)$$

For a four-seam fastball, let d be the distance from the pitcher's mound to home plate. Let t be the time taken and r be the speed of the ball. Then these are related by the relation,

$$rt = d \dots\dots(2)$$

Now, $d = 60.5$ and $r = 132$

How long does it take a ball to go from mound to home plate
 t

Equation(2) becomes,

$$rt = d \quad \text{original equation}$$

$$132t = 60.5 \quad \text{substitute 132 for } r \text{ and 60.5 for } d$$

$$\frac{132t}{132} = \frac{60.5}{132} \quad \text{divide by 132 on each side}$$

$$t = 0.458\bar{3}$$

Therefore, the time taken by four-seam fastball to go the home plate is $0.458\bar{3} = 458.\bar{3} \times 10^{-3}$.

Answer 45PA.

For any numbers a , b and c with $c \neq 0$ if $a = b$ then

$$\frac{a}{c} = \frac{b}{c} \dots\dots(1)$$

For a four-seam fastball, let d be the distance from the pitcher's mound to home plate. Let t be the time taken and r be the speed of the ball. Then these are related by the relation,

$$rt = d \dots\dots(2)$$

Now, $d = 60.5$ and $r = 132$

How long does it take a ball to go from mound to home plate
 t

Equation(2) becomes,

$$rt = d \quad \text{original equation}$$

$$132t = 60.5 \quad \text{substitute 132 for } r \text{ and 60.5 for } d$$

$$\frac{132t}{132} = \frac{60.5}{132} \quad \text{divide by 132 on each side}$$

$$t = 0.458\bar{3}$$

Therefore, the time taken by four-seam fastball to go the home plate is $0.458\bar{3} = 458.\bar{3} \times 10^{-3}$

For a two-seam fastball, let d' be the distance from the pitcher's mound to home plate. Let t' be the time taken and r' be the speed of the ball. Then these are related by the relation,

$$r't' = d' \dots\dots(2)$$

Now, $d = 60.5$ and $r = 126$

How long does it take a ball to go from mound to home plate
 t'

Equation(2) becomes,

$$r' t' = d' \quad \text{original equation}$$

$$126 \cdot t' = 60.5 \quad \text{substitute 126 for } r' \text{ and 60.5 for } d'$$

$$\frac{126 t'}{126} = \frac{60.5}{126} \quad \text{divide by 126 on each side}$$

$$t' = 0.48015873$$

Therefore, the time taken by two-seam fastball to go the home plate is

$$0.48015873 = 48.015873 \times 10^{-2} .$$

How much does it take for a two-seamfastball to reach than a fourseam fastball
 $t' - t$

$$t' - t \quad \text{original equation}$$

$$t' - t = 0.48015873 - 0.4583 \quad \text{substitute 0.48015873 for } t' \text{ and 0.4583 for } t$$

$$= 0.021825396$$

Therefore, the final answer is 0.021825396 .

Answer 46PA.

Each gram of water is a combination of hydrogen and oxygen.

In 477 grams of water, for every 8 grams of oxygen there is 1 gram of hydrogen.

The number of grams of hydrogen in water is denoted by x .

Let the number of grams of oxygen in water $= y$

$$\text{Number of 8 grams of oxygen} = \frac{y}{8}$$

The relation between x and y is:

$$\underbrace{\text{number of grams of hydrogen}}_x \text{ is } \underbrace{\text{number of 8 grams of oxygen}}_{\frac{y}{8}}$$

$$x = \frac{y}{8} \quad \text{Original equation}$$

$$x \cdot 8 = \frac{y}{8} \cdot 8 \quad \text{Multiply by 8 on each side}$$

$$8x = y$$

Therefore, the required expression to represent the number of grams of oxygen is $y = 8x$

Answer 47PA.

Each gram of water is a combination of hydrogen and oxygen.

In 477 grams of water, for every 8 grams of oxygen there is 1 gram of hydrogen.

The number of grams of hydrogen in water is denoted by x .

Let the number of grams of oxygen in water $= y$

Thus, $x + y = 477$

Number of 8 grams of oxygen $= \frac{y}{8}$

The relation between x and y is:

$$\underbrace{\text{number of grams of hydrogen}}_x \text{ is } \underbrace{\text{number of 8 grams of oxygen}}_{\frac{y}{8}}$$

$$x = \frac{y}{8} \quad \text{Original equation}$$

$$x \cdot 8 = \frac{y}{8} \cdot 8 \quad \text{Multiply by 8 on each side}$$

$$8x = y$$

Substitute $y = 8x$ in $x + y = 477$, it becomes $x + 8x = 477$

Therefore, the required expression to represent 477 grams of water is $\boxed{477 = x + 8x}$

Answer 48PA.

Each gram of water is a combination of hydrogen and oxygen.

In 477 grams of water, for every 8 grams of oxygen there is 1 gram of hydrogen.

The number of grams of hydrogen in water is denoted by x .

Let the number of grams of oxygen in water $= y$

Thus, $x + y = 477$

Number of 8 grams of oxygen $= \frac{y}{8}$

The relation between x and y is:

$$\underbrace{\text{number of grams of hydrogen}}_x \text{ is } \underbrace{\text{number of 8 grams of oxygen}}_{\frac{y}{8}}$$

$$x = \frac{y}{8} \quad \text{Original equation}$$

$$x \cdot 8 = \frac{y}{8} \cdot 8 \quad \text{Multiply by 8 on each side}$$

$$8x = y$$

Substitute $y = 8x$ in $x + y = 477$, it becomes $x + 8x = 477$

$$477 = x + 8x \quad \text{original equation}$$

$$477 = 9x$$

$$\frac{477}{9} = \frac{9x}{9} \quad \text{divide by 9 on each side}$$

$$53 = x \quad \text{simplify}$$

Therefore, the number of grams of hydrogen in water is $\boxed{53}$

Answer 49PA.

Each gram of water is a combination of hydrogen and oxygen.

In 477 grams of water, for every 8 grams of oxygen there is 1 gram of hydrogen.

The number of grams of hydrogen in water is denoted by x .

Let the number of grams of oxygen in water $= y$

Thus, $x + y = 477$

Number of 8 grams of oxygen $= \frac{y}{8}$

The relation between x and y is:

$$\underbrace{\text{number of grams of hydrogen}}_x \text{ is } \underbrace{\text{number of 8 grams of oxygen}}_{\frac{y}{8}}$$

$$x = \frac{y}{8} \quad \text{Original equation}$$

$$x \cdot 8 = \frac{y}{8} \cdot 8 \quad \text{Multiply by 8 on each side}$$

$$8x = y$$

Substitute $y = 8x$ in $x + y = 477$, it becomes $x + 8x = 477$

$$477 = x + 8x \quad \text{original equation}$$

$$477 = 9x$$

$$\frac{477}{9} = \frac{9x}{9} \quad \text{divide by 9 on each side}$$

$$53 = x \quad \text{simplify}$$

Substitute $x = 53$ in $y = 8x$ to find the number of grams of hydrogen in water.

$$y = 8x \quad \text{original equation}$$

$$y = 8 \cdot 53 \quad \text{substitute 53 for } x$$

$$y = 424$$

Therefore, the number of grams of hydrogen in water is 424

Answer 50PA.

For any numbers a , b and c if $a = b$ then $ac = bc$. In particular for $c \neq 0$, we also have,

$$\frac{a}{c} = \frac{b}{c} \quad \text{Consider the equation,}$$

$$6y - 7 = 4 \quad \dots\dots(1)$$

Simplify left-hand side of equation(1) to the form,

$$18y - 21 \quad \dots\dots(2)$$

Therefore, equation(1) becomes

$$\begin{array}{ll}
 6y - 7 = 4 & \text{original equation} \\
 6y - 7 + 7 = 4 + 7 & \text{add 7 to each side} \\
 6y = 11 & \text{simplify} \\
 6y \cdot 3 = 11 \cdot 3 & \text{multiply by 3 on each side} \\
 18y = 33 & \text{simplify} \\
 18y - 21 = 33 - 21 & \text{subtract 21 from each side} \\
 18y - 21 = 12 & \text{simplify}
 \end{array}$$

Therefore, the value of $18y - 21 = 12$.

Answer 52PA.

For a rectangle of length l and breadth b ,the perimeter P , is $P = 2(l + b)$.Area of a square of side a is a^2 .The rectangle is divided into 5 identical squares. Let the measure of each side of square be n . The graphical representation is:



$$\underbrace{\text{Perimeter of the rectangle}}_{2(l+b)} \underbrace{\text{is}}_{=} \underbrace{48 \text{ inches}}_{48}$$

$$2(l + b) = 48 \quad \text{original equation}$$

Thus, we get $2(l + b) = 48$ (1)

Each square is of measure n . Consider the first square. We observe that $n = b$.From the figure, we observe that length of the rectangle is sum of the sides of 5 squares. That is

$$l = n + n + n + n + n$$

$$l = 5n \quad \text{simplify}$$

Therefore, equation(1)becomes

$$\begin{array}{ll}
 2(l + b) = 48 & \text{original equation} \\
 2l + 2b = 48 & \\
 2(5n) + 2n = 48 & \text{substitute } n \text{ for } b \text{ and } 5n \text{ for } l \\
 10n + 2n = 48 & \\
 12n = 48 & \\
 \frac{12n}{12} = \frac{48}{12} & \text{divide by 12 on each side} \\
 n = 4 &
 \end{array}$$

Therefore, each square is of size 4 inches. Hence,

$$\begin{aligned}\text{Area of the square} &= 4 \cdot 4 \\ &= 16\end{aligned}$$

Therefore, required area is 16 inches

Answer 53PA.

For any numbers a , b and c if $a = b$, and $c \neq 0$ then

$$\frac{a}{c} = \frac{b}{c} \dots\dots(1)$$

Consider the equation, $4t = 20 \dots\dots(2)$

Simplify equation(2).

Therefore, equation(2) becomes

$$4t = 20 \quad \text{original equation}$$

$$\frac{4t}{4} = \frac{20}{4} \quad \text{divide by 4 on each side}$$

$$t = 5$$

Hence, the value of $t = 5$. Therefore, the values of

$$\begin{aligned}-2t &= -2(5) \quad \text{substitute 5 for } t \\ &= -10\end{aligned}$$

$$\begin{aligned}2t &= 2(5) \quad \text{substitute 5 for } t \\ &= 10\end{aligned}$$

$$\begin{aligned}-8t &= -8(5) \quad \text{substitute 5 for } t \\ &= -40\end{aligned}$$

Hence, $-2t = -10$, $2t = 10$, $-8t = -40$. Therefore, $4t = 20$ is equivalent to
option A $-2t = -10$.

Answer 54MYS.

Solving an equation involves various operations like addition, subtraction, multiplication and division. Consider the equation,

$$m + 14 = 81 \dots\dots(1)$$

Equation(1) is solved in following steps:

$$m + 14 = 81 \quad \text{original equation}$$

$$m + 14 - 14 = 81 - 14 \quad \text{subtract 14 from each side}$$

$$m = 67 \quad \text{simplify}$$

Thus, we get $m = 67$.

Check the result $m = 67$.

CHECK

$$m + 14 = 81 \quad \text{original equation}$$

$$67 + 14 = 81 \quad \text{substitute 67 for } m$$

$$81 = 81 \quad \text{the solution is 67}$$

Therefore, the final answer is $m = 67$

Answer 55MYS.

Solving an equation involves various operations like addition, subtraction, multiplication and division. Consider the equation,

$$d - 27 = -14 \quad \dots\dots(1)$$

Equation(1) is solved in following steps:

$$d - 27 = -14 \quad \text{original equation}$$

$$d - 27 + 27 = -14 + 27 \quad \text{add 27 to each side}$$

$$d = 13 \quad \text{simplify}$$

Thus, we get $d = 13$.

Check the result $d = 13$.

CHECK

$$d - 27 = -14 \quad \text{original equation}$$

$$13 - 27 = -14 \quad \text{substitute 13 for } d$$

$$-14 = -14 \quad \text{the solution is 13}$$

Therefore, the final answer is $d = 13$

Answer 56MYS.

Solving an equation involves various operations like addition, subtraction, multiplication and division. Consider the equation,

$$17 - (-w) = -55 \quad \dots\dots(1)$$

Equation(1) is solved in following steps:

$$17 - (-w) = -55 \quad \text{original equation}$$

$$17 + w = -55 \quad \text{simplify}$$

$$17 + w - 17 = -55 - 17 \quad \text{subtract 17 from each side}$$

$$w = -72 \quad \text{simplify}$$

Thus, we get $w = -72$

Check the result $w = -72$.

CHECK

$$17 - (-w) = -55 \quad \text{original equation}$$

$$17 + w = -55 \quad \text{simplify}$$

$$17 - 72 = -55 \quad \text{substitute } -72 \text{ for } w$$

$$-55 = -55 \quad \text{the solution is } -72$$

Therefore, the final answer is $w = -72$

Answer 57MYS.

Consider the statement,

Ten times a number a is equal to 5 times the sum of b and c (1)

This statement can be expressed in equation form as follows:

$$\underbrace{\text{Ten}}_{10} \underbrace{\text{times}}_{\times} \underbrace{\text{a number } a}_a \underbrace{\text{is equal to}}_{=} \underbrace{5}_5 \underbrace{\text{times}}_{\times} \underbrace{\text{the sum of } b \text{ and } c}_{b+c}$$

$$10 \cdot a = 5(b + c) \quad \text{equation form}$$

Therefore, the required equation is, $10 \cdot a = 5(b + c)$.

Answer 58MYS.

The objective is to find the product of -5 and 12 .

As the signs of two numbers are different, so their product is negative.

That is,

$$(-5)(12) = -60$$

Therefore, the product of (-5) and 12 is $\boxed{-60}$.

Answer 59MYS.

The objective is to find the product of -2.93 and -0.003 .

As the signs of two numbers are same, so their product is positive.

That is,

$$\begin{aligned} (-2.93)(-0.003) &= (2.93)(0.003) \\ &= 0.00879 \end{aligned}$$

Therefore, the product of -2.93 and -0.003 is $\boxed{0.00879}$.

Answer 60MYS.

The objective is to find the product of $(-4)(0)(-2)(-3)$.

Any number multiplied with zero is zero.

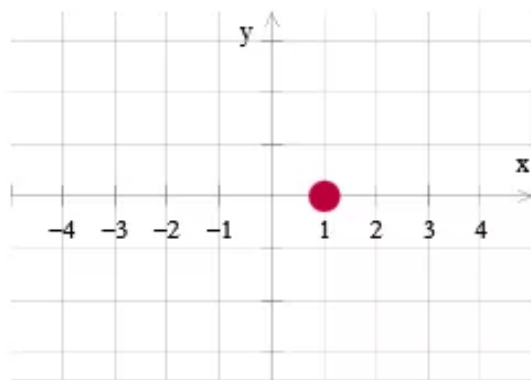
That is,

$$(-4)(0)(-2)(-3) = 0$$

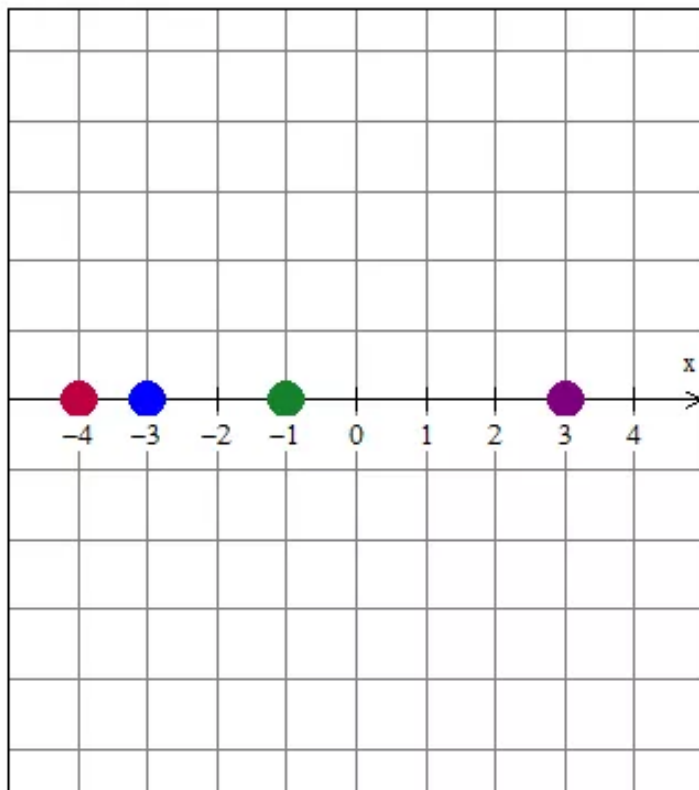
Therefore, the product of $(-4)(0)(-2)(-3)$ is $\boxed{0}$.

Answer 61MYS.

The graph of $x = 1$ is



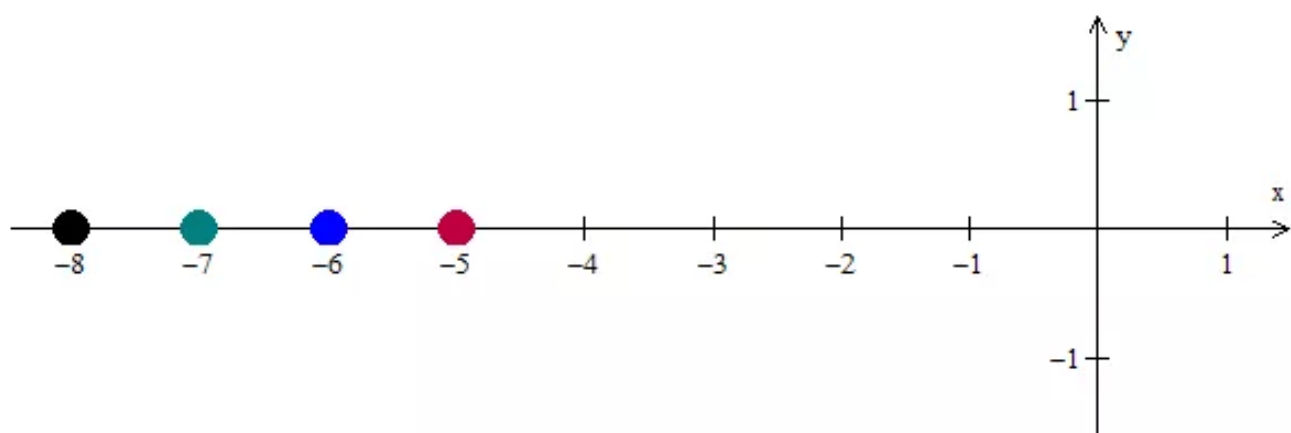
Consider the set of numbers $\{-4, -3, -1, 3\}$. The graphical representation of these numbers is:



Answer 63MYS.

The integers are $\{\dots -3, -2, -1, 0, 1, 2, 3, \dots\}$. The

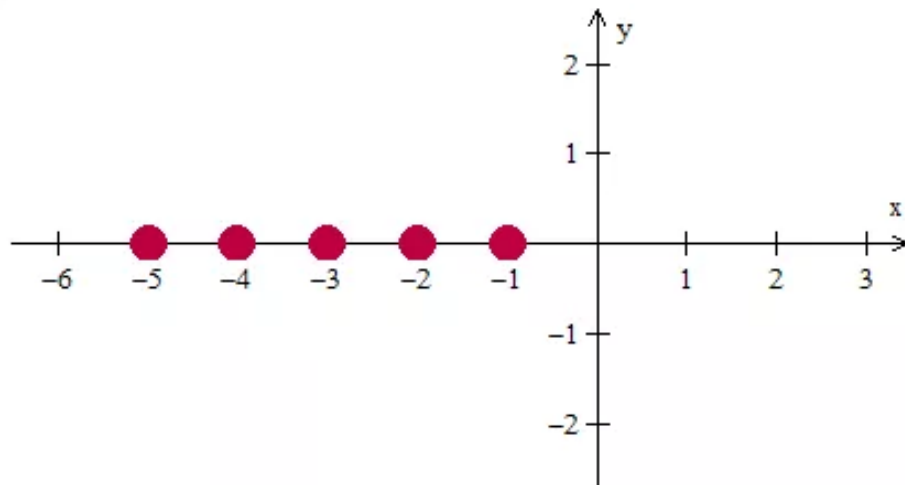
integers less than -4 are $\{-5, -6, -7, -8, -9, \dots\}$. The graphical representation of these numbers is:



Answer 64MYS.

The integers are $\{\dots -3, -2, -1, 0, 1, 2, 3, \dots\}$. The

integers less than 0 and greater than -6 are $\{-1, -2, -3, -4, -5\}$. The graphical representation of these numbers is:

**Answer 65MYS.**

Let u , v and w be real numbers, variables or algebraic expressions.

PROPERTY	ALGEBRAIC EXPRESSION
Commutative	$u + v = v + u$
Associative	$(u + v)w = u(v + w)$
Identity	$u + 0 = u$
Inverse	$u + (-u) = 0$
Distributive property under addition	$u(v + w) = uv + uw$ $(u + v)w = uw + vw$

Consider the expression,

$$67 + 3 = 3 + 67 \dots\dots(1)$$

Compare equation(1) with the above table. Therefore, it is of the form

$$u + v = v + u$$

Hence, we conclude that equation(1) represent commutative property under addition

Answer 66MYS.

Let u , v and w be real numbers, variables or algebraic expressions.

PROPERTY	ALGEBRAIC EXPRESSION
Commutative	$uv = vu$
Associative	$(uv)w = u(vw)$
Identity	$u \cdot 1 = u$
Inverse	$u \cdot \frac{1}{u} = 1, u \neq 0$
Distributive property under addition	$u(v + w) = uv + uw$ $(u + v)w = uw + vw$

Consider the expression,

$$(5 \cdot m) \cdot n = 5 \cdot (m \cdot n) \dots\dots(1)$$

Compare equation(1) with the above table. Therefore, we conclude that equation(1) represent the **associative property under multiplication** of variables $5, m$ and n .

Answer 67MYS.

The objective is to find the value of $2 \times 8 + 9$.

Use the order of operations to find the value.

First find the product of 2×8 and then add the resultant to 9.

$$\begin{aligned} 2 \times 8 + 9 &= 16 + 9 \\ &= 25 \end{aligned}$$

Therefore, the value of $2 \times 8 + 9$ is 25.

Answer 68MYS.

The objective is to find the value of $24 \div 3 - 8$.

Use the order of operations to find the value.

First do the division $24 \div 3$ and then subtract 8 from the resultant.

$$\begin{aligned} 24 \div 3 - 8 &= 8 - 8 \\ &= 0 \end{aligned}$$

Therefore, the value of $24 \div 3 - 8$ is 0.

Answer 69MYS.

The objective is to find the value of $\frac{3}{8}(17+7)$.

Use the order of operations to find the value.

Simplify the expression inside the parenthesis.

$$\begin{aligned}\frac{3}{8}(17+7) &= \frac{3}{8}(24) && \text{Add 17 and 7} \\ &= \frac{72}{8} && \text{Multiply 24 by } \frac{3}{8} \\ &= 9 && \text{Divide 72 by 8}\end{aligned}$$

Therefore, the value of $\frac{3}{8}(17+7)$ is $\boxed{9}$.

Answer 70MYS.

The objective is to find the value of $\frac{15-9}{26+12}$.

Use the order of operations to find the value.

Simplify the expressions in the numerator and denominator.

$$\begin{aligned}\frac{15-9}{26+12} &= \frac{6}{38} \\ &= 0.158 \quad \text{simplify}\end{aligned}$$

Therefore, the value of $\frac{15-9}{26+12}$ is $\boxed{0.158}$.