

CHAPTER

1.7

SINUSOIDAL STEADY STATE ANALYSIS

1. $i(t) = ?$

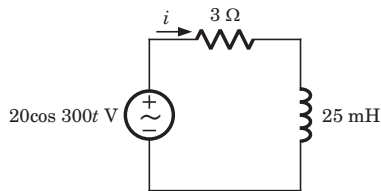


Fig. P1.7.1

- (A) $20 \cos(300t + 68.2^\circ) \text{ A}$
- (B) $20 \cos(300t - 68.2^\circ) \text{ A}$
- (C) $2.48 \cos(300t + 68.2^\circ) \text{ A}$
- (D) $2.48 \cos(300t - 68.2^\circ) \text{ A}$

2. $v_C(t) = ?$

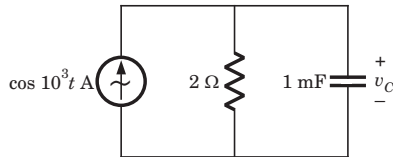


Fig. P1.7.2

- (A) $0.89 \cos(10^3 t - 63.43^\circ) \text{ V}$
- (B) $0.89 \cos(10^3 t + 63.43^\circ) \text{ V}$
- (C) $0.45 \cos(10^3 t + 26.57^\circ) \text{ V}$
- (D) $0.45 \cos(10^3 t - 26.57^\circ) \text{ V}$

3. $v_C(t) = ?$

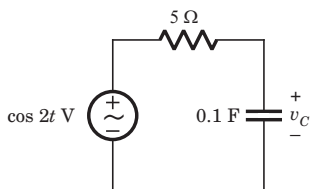


Fig. P1.7.3

- (A) $\frac{1}{\sqrt{2}} \cos(2t - 45^\circ) \text{ V}$
- (B) $\frac{1}{\sqrt{2}} \cos(2t + 45^\circ) \text{ V}$
- (C) $\frac{1}{\sqrt{2}} \sin(2t - 45^\circ) \text{ V}$
- (D) $\frac{1}{\sqrt{2}} \sin(2t + 45^\circ) \text{ V}$

4. $v_C(t) = ?$

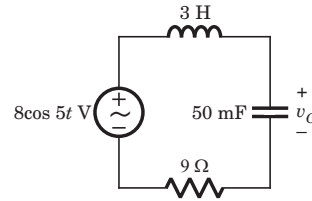


Fig. P1.7.4

- (A) $2.25 \cos(5t + 150^\circ) \text{ V}$
- (B) $2.25 \cos(5t - 150^\circ) \text{ V}$
- (C) $2.25 \cos(5t + 140.71^\circ) \text{ V}$
- (D) $2.25 \cos(5t - 140.71^\circ) \text{ V}$

5. $i(t) = ?$

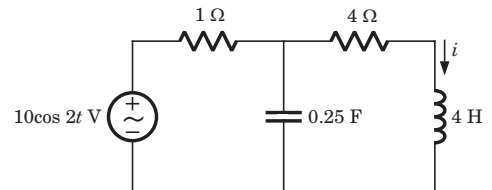


Fig. P1.7.5

- (A) $2 \sin(2t + 5.77^\circ) \text{ A}$
- (B) $\cos(2t - 84.23^\circ) \text{ A}$
- (C) $2 \sin(2t - 5.77^\circ) \text{ A}$
- (D) $\cos(2t + 84.23^\circ) \text{ A}$

13. In the bridge shown in fig. P1.7.13, $Z_1 = 300 \Omega$, $Z_2 = (300 - j 600) \Omega$, $Z_3 = (200 + j 100) \Omega$. The Z_4 at balance is

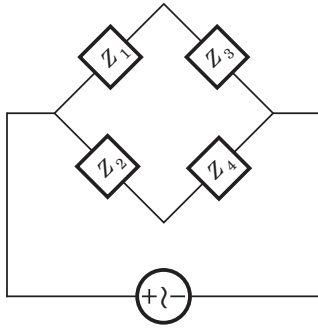


Fig. P1.7.13

- (A) $400 + j300 \Omega$ (B) $400 - j 300 \Omega$
(C) $j100 \Omega$ (D) $-j900 \Omega$

14. In a two element series circuit, the applied voltage and the resulting current are $v(t) = 60 + 66 \sin(10^3 t) \text{ V}$, $i(t) = 2.3 \sin(10^3 t + 68.3^\circ) \text{ A}$. The nature of the elements would be
(A) $R - C$ (B) $L - C$
(C) $R - L$ (D) $R - R$

15. $V_o = ?$

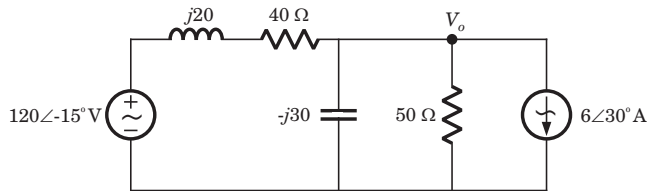


Fig. P1.7.15

- (A) $223 \angle -56^\circ \text{ V}$ (B) $223 \angle 56^\circ \text{ V}$
(C) $124 \angle -154^\circ \text{ V}$ (D) $124 \angle 154^\circ \text{ V}$

16. $v_o(t) = ?$

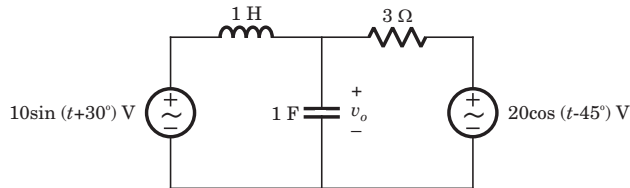


Fig. P1.7.16

- (A) $31.5 \cos(t + 112^\circ) \text{ V}$
(B) $43.2 \cos(t + 23^\circ) \text{ V}$
(C) $31.5 \cos(t - 112^\circ) \text{ V}$
(D) $43.2 \cos(t - 23^\circ) \text{ V}$

Statement for Q.17-18:

The circuit is as shown in fig. P1.7.17-18

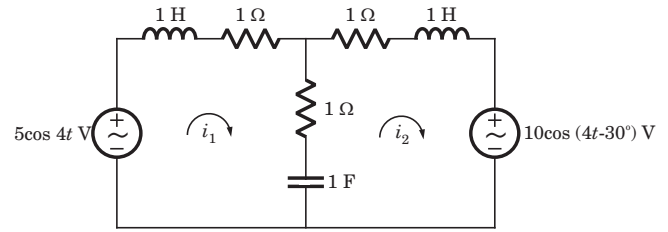


Fig. P1.7.17-18

17. $i_1(t) = ?$

- (A) $2.36 \cos(4t - 41.07^\circ) \text{ A}$
(B) $2.36 \cos(4t + 41.07^\circ) \text{ A}$
(C) $1.37 \cos(4t - 41.07^\circ) \text{ A}$
(D) $2.36 \cos(4t + 41.07^\circ) \text{ A}$

18. $i_2(t) = ?$

- (A) $2.04 \sin(4t + 92.13^\circ) \text{ A}$
(B) $-2.04 \sin(4t + 2.13^\circ) \text{ A}$
(C) $2.04 \cos(4t + 2.13^\circ) \text{ A}$
(D) $-2.04 \cos(4t + 92.13^\circ) \text{ A}$

19. $I_x = ?$

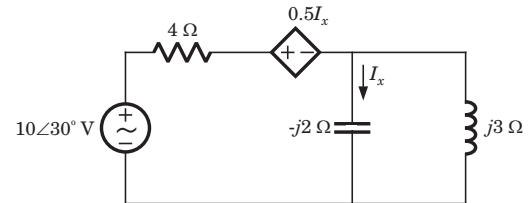


Fig. P1.7.19

- (A) $3.94 \angle 46.28^\circ \text{ A}$ (B) $4.62 \angle 97.38^\circ \text{ A}$
(C) $7.42 \angle 92.49^\circ \text{ A}$ (D) $6.78 \angle 49.27^\circ \text{ A}$

20. $V_x = ?$

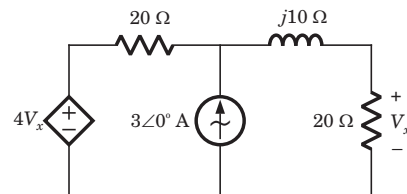


Fig. P1.7.20

- (A) $29.11 \angle 166^\circ \text{ V}$ (B) $29.11 \angle -166^\circ \text{ V}$
(C) $43.24 \angle 124^\circ \text{ V}$ (D) $43.24 \angle -124^\circ \text{ V}$

Statement for Q.27–32:

Determine the complex power for the given values in question.

27. $P = 269 \text{ W}$, $Q = 150 \text{ VAR}$ (capacitive)

- (A) $150 - j269 \text{ VA}$ (B) $150 + j269 \text{ VA}$
(C) $269 - j150 \text{ VA}$ (D) $269 + j150 \text{ VA}$

28. $Q = 2000 \text{ VAR}$, $pf = 0.9$ (leading)

- (A) $4129.8 + j2000 \text{ VA}$ (B) $2000 + j4129.8 \text{ VA}$
(C) $2000 - j4129.8 \text{ VA}$ (D) $4129.8 - j2000 \text{ VA}$

29. $S = 60 \text{ VA}$, $Q = 45 \text{ VAR}$ (inductive)

- (A) $39.69 + j45 \text{ VA}$ (B) $39.69 - j45 \text{ VA}$
(C) $45 + j39.69 \text{ VA}$ (D) $45 - j39.69 \text{ VA}$

30. $V_{rms} = 220 \text{ V}$, $P = 1 \text{ kW}$, $|Z| = 40 \Omega$ (inductive)

- (A) $1000 - j681.25 \text{ VA}$ (B) $1000 + j681.25 \text{ VA}$
(C) $681.25 + j1000 \text{ VA}$ (D) $681.25 - j1000 \text{ VA}$

31. $V_{rms} = 21 \angle 20^\circ \text{ V}$, $V_{rms} = 21 \angle 20^\circ \text{ V}$, $I_{rms} = 8.5 \angle -50^\circ \text{ A}$

- (A) $154.6 + j89.3 \text{ VA}$ (B) $154.6 - j89.3 \text{ VA}$
(C) $61 + j167.7 \text{ VA}$ (D) $61 - j167.7 \text{ VA}$

32. $V_{rms} = 120 \angle 30^\circ \text{ V}$, $Z = 40 + j80 \Omega$

- (A) $72 + j144 \text{ VA}$ (B) $72 - j144 \text{ VA}$
(C) $144 + j72 \text{ VA}$ (D) $144 - j72 \text{ VA}$

33. $V_o = ?$

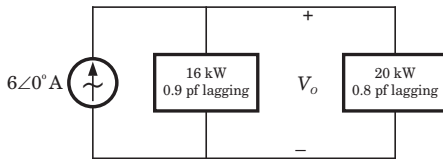


Fig. P1.7.33

- (A) $7.1 \angle 32.29^\circ \text{ kV}$ (B) $42.59 \angle 32.29^\circ \text{ kV}$
(C) $38.49 \angle 24.39^\circ \text{ kV}$ (D) $38.49 \angle 32.29^\circ \text{ kV}$

34. A relay coil is connected to a 210 V, 50 Hz supply. If it has resistance of 30Ω and an inductance of 0.5 H, the apparent power is

- (A) 30 VA (B) 275.6 VA
(C) 157 VA (D) 187 VA

35. In the circuit shown in Fig. P1.7.35 power factor is

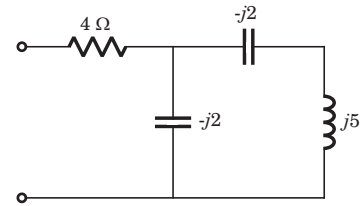


Fig. P1.7.35

- (A) 56.31 (leading) (B) 56.31 (lagging)
(C) 0.555 (lagging) (D) 0.555 (leading)

36. The power factor seen by the voltage source is

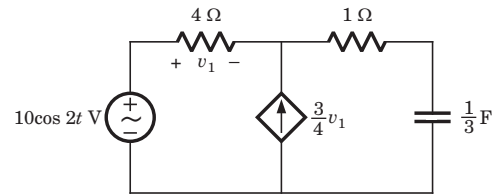


Fig. P1.7.36

- (A) 0.8 (leading) (B) 0.8 (lagging)
(C) 36.9 (leading) (D) 39.6 (lagging)

37. The average power supplied by the dependent source is

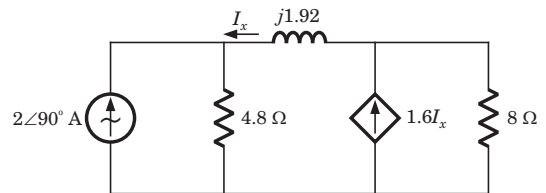


Fig. P1.7.37

- (A) 96 W (B) -96 W
(C) 92 W (D) -192 W

38. In the circuit of Fig. P1.7.38 the maximum power absorbed by Z_L is

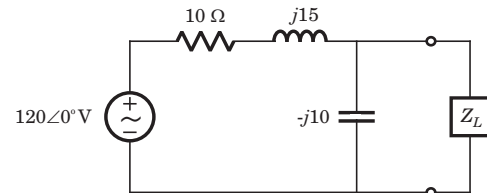


Fig. P1.7.38

- (A) 180 W (B) 90 W
(C) 140 W (D) 700 W

39. The value of the load impedance, that would absorb the maximum average power is

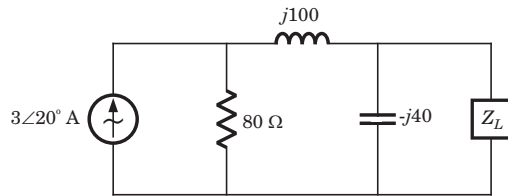


Fig. P1.7.39

- (A) $12.8 - j49.6 \Omega$ (B) $12.8 + j49.6 \Omega$
 (C) $33.9 - j86.3 \Omega$ (D) $33.9 + j86.3 \Omega$

Statement for Q.40–41:

In a balanced Y-connected three phase generator $V_{ab} = 400 V_{\text{rms}}$

40. If phase sequence is *abc* then phase voltage V_a , V_b , and V_c are respectively

- (A) $231\angle 0^\circ$, $231\angle 120^\circ$, $231\angle 240^\circ$
 (B) $231\angle -30^\circ$, $231\angle -150^\circ$, $231\angle 90^\circ$
 (C) $231\angle 30^\circ$, $231\angle 150^\circ$, $231\angle -90^\circ$
 (D) $231\angle 60^\circ$, $231\angle 180^\circ$, $231\angle -60^\circ$

41. If phase sequence is *acb* then phase voltage are

- (A) $231\angle 0^\circ$, $231\angle 120^\circ$, $231\angle 240^\circ$
 (B) $231\angle -30^\circ$, $231\angle -150^\circ$, $231\angle 90^\circ$
 (C) $231\angle 30^\circ$, $231\angle 150^\circ$, $231\angle -90^\circ$
 (D) $231\angle 60^\circ$, $231\angle 180^\circ$, $231\angle -60^\circ$

42. A balanced three-phase Y-connected load has one phase voltage $V_c = 277\angle 45^\circ V$. The phase sequence is *abc*. The line to line voltage V_{AB} is

- (A) $480\angle 45^\circ V$ (B) $480\angle -45^\circ V$
 (C) $339\angle 45^\circ V$ (D) $339\angle -45^\circ V$

43. A three-phase circuit has two parallel balanced Δ loads, one of the 6Ω resistor and one of 12Ω resistors. The magnitude of the total line current, when the line-to-line voltage is $480 V_{\text{rms}}$, is

- (A) $120 A_{\text{rms}}$ (B) $360 A_{\text{rms}}$
 (C) $208 A_{\text{rms}}$ (D) $470 A_{\text{rms}}$

44. In a balanced three-phase system, the source has an *abc* phase sequence and is connected in delta. There are two parallel Y-connected load. The phase impedance of load 1 and load 2 is $4 + j4 \Omega$ and $10 + j4 \Omega$ respectively.

The line impedance connecting the source to load is $0.3 + j0.2 \Omega$. If the current in a phase of load 1 is $I = 10\angle 20^\circ A_{\text{rms}}$, the current in source in *ab* branch is

- (A) $15\angle -122^\circ A_{\text{rms}}$ (B) $8.67\angle -122^\circ A_{\text{rms}}$
 (C) $15\angle 27.9^\circ A_{\text{rms}}$ (D) $8.67\angle -57.9^\circ A_{\text{rms}}$

45. An *abc* phase sequence 3-phase balanced Y-connected source supplies power to a balanced Δ -connected load. The impedance per phase in the load is $10 + j8 \Omega$. If the line current in a phase is $I_{aA} = 28.10\angle -28.66^\circ A_{\text{rms}}$ and the line impedance is zero, the load voltage V_{AB} is

- (A) $207.8\angle -140^\circ V_{\text{rms}}$ (B) $148.3\angle 40^\circ V_{\text{rms}}$
 (C) $148.3\angle -40^\circ V_{\text{rms}}$ (D) $207.8\angle 40^\circ V_{\text{rms}}$

46. The magnitude of the complex power supplied by a 3-phase balanced Y-Y system is 3600 VA. The line voltage is $208 V_{\text{rms}}$. If the line impedance is negligible and the power factor angle of the load is 25° , the load impedance is

- (A) $5.07 + j10.88 \Omega$ (B) $10.88 + j5.07 \Omega$
 (C) $43.2 + j14.6 \Omega$ (D) $14.6 + j43.2 \Omega$

SOLUTIONS

1. (D) $Z = 3 + j(25\text{m})(300) = 3 + j7.5 \Omega = 8.08 \angle 68.2^\circ$

$$I = \frac{20 \angle 0}{8.08 \angle 68.2^\circ} = 2.48 \angle -68.2^\circ \text{ A}$$

$$i(t) = 2.48 \cos(300t - 68.2^\circ) \text{ A}$$

2. (A) $Y = \frac{1}{2} + j(1\text{m})(10^3) = 0.5 + j = 1.12 \angle 63.43^\circ$

$$V_C = \frac{(1 \angle 0)}{1.12 \angle 63.43^\circ} = 0.89 \angle -63.43^\circ \text{ V}$$

$$v_C(t) = 0.89 \cos(10^3 t - 63.43^\circ) \text{ V}$$

3. (A) $Z = 5 + \frac{-j}{(0.1)(2)} = 5 - j5 = 5\sqrt{2} \angle -45^\circ$

$$V_C = \frac{(1 \angle 0)(5 \angle -90^\circ)}{5\sqrt{2} \angle -45^\circ} = \frac{1}{\sqrt{2}} \angle -45^\circ \text{ V}$$

$$v_C(t) = \frac{1}{\sqrt{2}} \cos(2t - 45^\circ) \text{ V}$$

4. (D) $Z = 9 + j(3)(5) + \frac{-j}{(50\text{m})(5)} = 9 + j11$

$$\Rightarrow Z = 14.21 \angle 50.71^\circ \Omega$$

$$V_C = \frac{(8 \angle 0)(4 \angle -90^\circ)}{14.21 \angle 50.71^\circ} = 2.25 \angle 140.71^\circ \text{ V}$$

$$v_C(t) = 2.25 \cos(5t - 140.71^\circ) \text{ V}$$

5. (B) $V_a = \frac{\frac{10 \angle 0}{1}}{\frac{1}{1} + \frac{1}{-j2} + \frac{1}{4 + j8}} = \frac{10 \angle 0}{105 + j0.4} \text{ V}$

$$I = \frac{V_a}{4 + j8} = \frac{10 \angle 0}{1 + j10} = 1 \angle -84.23^\circ \text{ A}$$

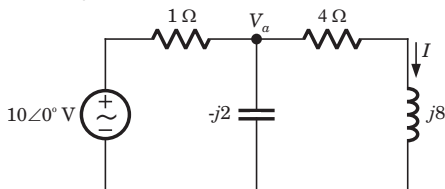


Fig. S1.7.5

$$i(t) = \cos(2t - 84.23^\circ) \text{ A}$$

6. (D) $\omega = 2\pi \times 10 \times 10^3 = 2\pi \times 10^4$

$$Y = j(1\mu)(2\pi \times 10^4) + \frac{-j}{(160\mu)(2\pi \times 10^4)} + \frac{1}{36}$$

$$= 0.0278 - j0.0366 \text{ S}$$

$$Z = \frac{1}{Y} = 13.16 + j17.33 \Omega$$

7. (C) $Z = \left(\frac{-j}{\omega(22\mu)} \right) \parallel (6 + j(27\text{m})\omega)$

$$= \frac{\frac{-j10^6}{22\omega} (6 + j27 \times 10^{-3} \omega)}{6 + j(27\text{m})\omega - \frac{10^6}{22\omega}} = \frac{\frac{27 \times 10^3}{22} - \frac{j6 \times 10^6}{22\omega}}{6 + j\omega \left(27\text{m} - \frac{10^6}{22\omega^2} \right)}$$

$$\frac{-j36 \times 10^6}{\omega 22} - \frac{j27 \times 10^3}{22} \omega \left(27\text{m} - \frac{10^6}{22\omega^2} \right) = 0$$

$$\Rightarrow \omega = 1278$$

$$f = \frac{\omega}{2\pi} \text{ Hz} = \frac{1278}{2\pi} = 203 \text{ Hz}$$

8. (C) $V_s = 7.68 \angle 47^\circ \text{ V}$, $V_2 = 7.51 \angle 35^\circ$

$$V_1 = V_s - V_2 = 7.68 \angle 47^\circ - 7.51 \angle 35^\circ = 1.59 \angle 125^\circ$$

9. (B) $v_{in} = \sqrt{3^2 + (14 - 10)^2} = 5$

10. (C) $I_1 = 744 \angle -118^\circ \text{ mA}$,

$$I_2 = 540 \angle 100^\circ \text{ mA}$$

$$I = I_1 + I_2 = 744 \angle -118^\circ + 540.5 \angle 100^\circ$$

$$= 460 \angle -164^\circ$$

$$i(t) = 460 \cos(3t - 164^\circ) \text{ mA}$$

11. (A) $\sqrt{2} \angle 45^\circ = \frac{V_C}{-j4} + \frac{V_C - 20 \angle 0}{j5 + 10}$

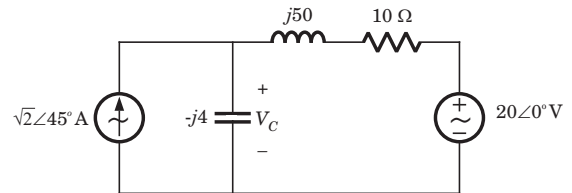


Fig. S1.7.11

$$(1 + j)(-j4)(10 + j5) = V_C(10 + j5 - j4) + j8$$

$$\Rightarrow 60 - j100 = V_C(10 + j)$$

$$\Rightarrow V_C = 11.6 \angle -64.7^\circ$$

12. (D) $X = X_L + X_C = 0$

So reactive power drawn from the source is zero.

13. (B) $Z_1 Z_4 = Z_3 Z_2$

$$300 Z_4 = (300 - j600)(200 + j100)$$

$$\Rightarrow Z_4 = 400 - j300$$

14. (A) $R - C$ causes a positive phase shift in voltage

$$Z = |Z| \angle \theta, -90^\circ < \theta < 0,$$

$$I = \frac{V}{Z} = \frac{V}{|Z|} \angle -\theta$$

$$15. (C) V_o = \frac{\frac{120\angle 15^\circ}{40 + j20} - 6\angle 30^\circ}{\frac{1}{40 + j20} + \frac{1}{-j30} + \frac{1}{50}} = 124\angle -154^\circ$$

$$16. (C) 10 \sin(t + 30^\circ) = 10 \cos(t - 60^\circ)$$

$$V_o = \frac{\frac{10\angle -60^\circ}{j} + \frac{20\angle -45^\circ}{3}}{\frac{1}{j} + \frac{1}{-j} + \frac{1}{3}}$$

$$= 30\angle -150^\circ + 20\angle -45^\circ$$

$$V_o = 31.5\angle -112^\circ \text{ V}$$

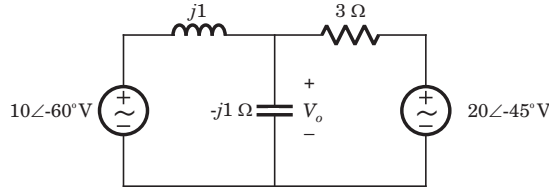


Fig. S.1.7.16

$$17. (C) 5\angle 0^\circ = I_1 \left(j4 + 1 + 1 - \frac{j}{4} \right) - I_2 \left(1 - \frac{j}{4} \right)$$

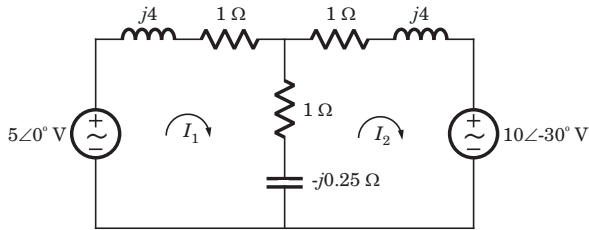


Fig. S.1.7.17

$$\Rightarrow (8 + j15)I_1 - (4 - j)I_2 = 20\angle 0 \quad \dots(i)$$

$$-10\angle -30^\circ = I_2(1 + j4 + 1 - \frac{j}{4}) - I_1(1 - \frac{j}{4})$$

$$\Rightarrow (4 - j)I_1 - (8 + j15)I_2 = 40\angle -30^\circ \quad \dots(ii)$$

$$I_1[(8 + j15)^2 - (4 - j)^2]$$

$$= (20\angle 0)(8 + j15) - (40\angle -30^\circ)(4 - j)$$

$$I_1(-176 + j248) = 41.43 + j414.64$$

$$\Rightarrow I_1 = 103 - j0.9 = 1.37\angle -41.07^\circ$$

$$18. (B) I_2 = \frac{(8 + j15)(103 - j0.9) - 20\angle 0^\circ}{4 - j}$$

$$= -0.076 + j2.04 \Rightarrow I_2 = 2.04\angle 92.13^\circ$$

$$19. (B) 10\angle 30^\circ = 4I_1 - 0.5I_x + (-j2)I_x$$

$$(-j2)I_x = (I_1 - I_x)j3, I_1 = \frac{I_x}{3}$$

$$10\angle 30^\circ = \left(\frac{4}{3} - 0.5 - j2 \right) I_x \Rightarrow I_x = \frac{10\angle 30^\circ}{2.17\angle -67.38^\circ}$$

20. (B) Let V_o be the voltage across current source

$$\frac{V_o - 4V_x}{20} + \frac{V_o - V_x}{j10} = 3$$

$$V_o(20 + j10) - (20 + j40)V_x = j600$$

$$V_x = \frac{V_o(20)}{20 + j10} \Rightarrow V_o = \frac{V_x}{2}(2 + j)$$

$$V_x = \left(\frac{(2 + j)(20 + j10)}{2} - 20(1 + j2) \right) = j600$$

$$V_x = \frac{j600}{-5 - j20} = 29.22\angle -166^\circ$$

$$21. (A) I_1 = V_3 \left(\frac{j}{2} \right) + \frac{V_3 - V_2}{j10} = j0.1V_2 + j0.4V_3$$

$$= (0.1\angle 90^\circ)(0.757\angle 66.7^\circ) + (0.4\angle 90^\circ)(0.606\angle -69.8^\circ)$$

$$\Rightarrow I_1 = 0.196\angle 35.6^\circ$$

$$22. (A) \frac{V_o}{2} + \frac{V_o - 3V_o}{j4} = 4\angle -30^\circ$$

$$V_o(0.5 + j0.5) = 3.46 - j2 \Rightarrow V_o = 5.65\angle -75^\circ$$

$$23. (D) I_2 = 4\angle 90^\circ, I_3 = 2\angle 0^\circ$$

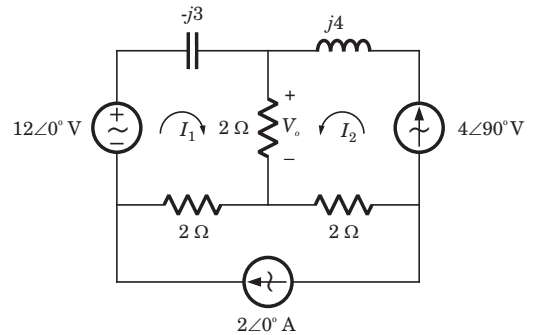


Fig. P1.7.23

$$12\angle 0^\circ = I_1(-j3 + 2 + 2) + 8\angle 90^\circ - 4\angle 0^\circ$$

$$\Rightarrow I_1 = 3.52 + j0.64$$

$$V_o = 2(3.52 + j0.64 + j4) = 11.65\angle 52.82^\circ \text{ V}$$

$$24. (D) I_2 = 3\angle 0^\circ \text{ A}, I_4 - I_3 = 6\angle 0^\circ \text{ A}$$

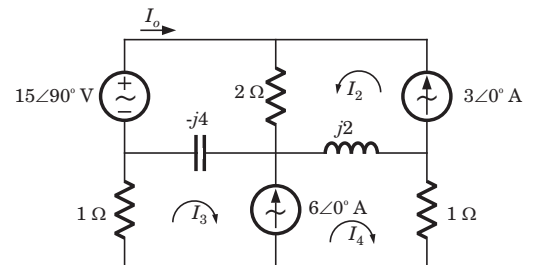


Fig. S.1.7.24

$$I_3(1) + (I_3 - I_o)(-j4) + (I_4 + I_2)(j2) + I_4 = 0$$

$$I_3 + (I_3 - I_o)(-j4) + (I_3 + 6\angle 0^\circ + 3\angle 0^\circ)(j2) + I_3 + 60^\circ = 0$$

$$I_3(2 - j2) + I_o(j4) = -18j - 6$$

$$I_3 = \frac{-I_o(j2) - 3 - 9j}{(1 - j)}$$

$$\Rightarrow I_3 = I_o + 3 - j6$$

$$15\angle 90^\circ = (I_o + 3\angle 0^\circ)(2) + (I_o - I_3)(-j4)$$

$$\Rightarrow j15 = 2I_o + 6 + (j4)(3 - j6)$$

$$25. (A) Z_{TH} = \frac{(j10)(8 - j5)}{8 + j10 - j5} = 9 + j4.4$$

$$V_{TH} = \frac{(32\angle 0^\circ)(j10)}{8 + j10 - j5} = 33.9\angle 58^\circ \text{ V}$$

$$26 (D) (600 - j300)I_1 + j300I_2 = 9 \quad \dots(i)$$

$$300I_2 = 3V_1, \quad V_1 = (-j300)(I_1 - I_2)$$

$$\Rightarrow I_2 = -j3(I_1 - I_2) \Rightarrow 3I_1 = (3 + j)I_2 \quad \dots(ii)$$

$$\text{Solving (i) and (ii) } I_2 = 12.36\angle -16^\circ \text{ mA}$$

$$V_{oc} = 300I_2 = 3.71\angle -16^\circ$$

$$-2V_1 - V_1 = 0 \Rightarrow V_1 = 0$$

$$\Rightarrow I_{sc} = \frac{9\angle 0^\circ}{600} = 15\angle 0^\circ \text{ mA}$$

$$Z_{TH} = \frac{V_{oc}}{I_{sc}} = \frac{3.11\angle -16^\circ}{15\angle 0^\circ \times 10^{-3}} = 247\angle -16^\circ \Omega$$

$$27. (C) S = P - jQ = 269 - j150 \text{ VA}$$

$$28. (D) pf = \cos \theta = 0.9 \Rightarrow \theta = 25.84^\circ$$

$$Q = S \sin \theta \Rightarrow S = \frac{Q}{\sin \theta} = \frac{2000}{\sin 25.84^\circ} = 4588.6 \text{ VA}$$

$$P = S \cos \theta = 4129.8,$$

$$S = 4129.8 - j2000$$

$$29. (A) Q = S \sin \theta \Rightarrow \sin \theta = \frac{Q}{S} = \frac{45}{60} \text{ or}$$

$$\Rightarrow \theta = 48.59^\circ,$$

$$P = S \cos \theta = 39.69,$$

$$S = 39.69 + j45 \text{ VA}$$

$$30. (B) S = \frac{|V_{rms}|^2}{|Z|} = \frac{(220^2)}{40} = 1210$$

$$\cos \theta = \frac{P}{S} = \frac{1000}{1210} = 0.8264 \text{ or } \theta = 34.26^\circ,$$

$$Q = S \sin \theta = 681.25,$$

$$S = 1000 + j681.25 \text{ VA}$$

$$31. (C) S = V_{rms} I_{rms}^* = (21\angle 20^\circ)(8.5\angle 50^\circ)$$

$$= 61 + j167.7 \text{ VA}$$

$$32. (A) S = \frac{|V|^2}{Z^*} = \frac{(120)^2}{40 - j80} = 72 + j144 \text{ VA}$$

$$33. (A) S_1 = 16 + j \frac{16}{0.9} \sin(\cos^{-1}(0.9)) = 16 + j7.75$$

$$S_2 = 20 + j \frac{20}{0.8} \sin(\cos^{-1}(0.8)) = 20 + j15$$

$$S = S_1 + S_2 = 36 + j27.5 = 42.59\angle 32.29^\circ$$

$$S = V_o I^* = 6V_o \Rightarrow V_o = 7.1\angle 32.29^\circ$$

$$34. (B) Z = 30 + j(0.5)(2\pi)(50) = 30 + j157,$$

$$S = \frac{|V|^2}{Z^*} = \frac{(210)^2}{30 - j157}$$

$$\text{Apparent power} = |S| = \frac{(210)^2}{\sqrt{30^2 + 157^2}} = 275.6 \text{ VA}$$

$$35. (D) Z = 4 + \frac{(-j2)(j5 - j2)}{-j2 + j5 - j2}$$

$$= 4 - j6 = 7.21\angle -56.31^\circ,$$

$$pf = \cos 56.31^\circ = 0.555 \text{ leading}$$

$$36. (A) \frac{V_1}{4} + \frac{3}{4}V_1 = \frac{10 - V_1}{1 - j15} \Rightarrow V_1 = 4\angle 36.9^\circ,$$

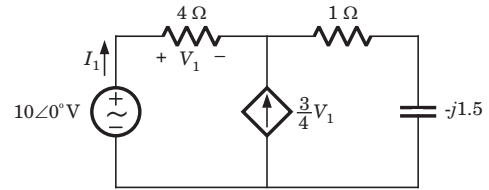


Fig. S.1.7.36

$$I_1 = 1\angle 36.9^\circ$$

$$S = \frac{(1\angle 36.9^\circ)(10\angle 0^\circ)}{2} = 5\angle -36.9^\circ$$

$$pf = \cos 36.9^\circ = 0.8 \text{ leading}$$

$$37. (A) (2\angle -90^\circ)4.8 = -I_x(4.8 + j1.92) + 0.6I_x(8)$$

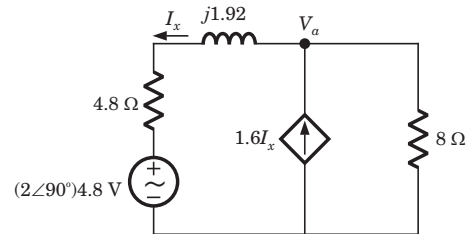


Fig. S.1.7.37

$$I_x = 5\angle 0^\circ, \quad V_a = 0.6 \times 5 \times 8 = 24\angle 0^\circ,$$

$$P_{ave} = \frac{1}{2} \times 24 \times 1.6 \times 5 = 96$$

$$38. (A) Z_{TH} = \frac{(-j10)(10 + j15)}{10 + j15 - j10} = 8 - j14 \Omega$$

$$V_{TH} = \frac{120(-j10)}{10 + j5} = 107.3 \angle -116.6^\circ \text{ V}$$

$$I_L = \frac{107.3 \angle -116.6^\circ}{16} = 6.7 \angle -116.6^\circ$$

$$P_{Lmax} = \frac{1}{2} (6.7)^2 \times 8 = 180 \text{ W}$$

$$39. (B) Z_{TH} = \frac{(-j40)(80 + j100)}{80 + j60} = 12.8 - j49.6 \Omega$$

$$40. (B) V_a = \frac{400}{\sqrt{3}} \angle -30^\circ = 231 \angle -30^\circ \text{ V}$$

$$V_b = 231 \angle -150^\circ \text{ V}, V_c = 231 \angle -270^\circ \text{ V}$$

41. (C) For the acb sequence

$$V_{ab} = V_a - V_b = V_p \angle 0^\circ - V_p \angle 120^\circ$$

$$400 = V_p \left(1 + \frac{1}{2} - j \frac{\sqrt{3}}{2} \right) = V_p \sqrt{3} \angle -30^\circ$$

$$\Rightarrow V_p = \frac{400}{\sqrt{3}} \angle 30^\circ$$

$$V_a = V_p \angle 0^\circ = 231 \angle 30^\circ \text{ V},$$

$$V_b = V_p \angle 120^\circ = 231 \angle 150^\circ \text{ V}$$

$$V_c = V_p \angle 240^\circ = 231 \angle -90^\circ \text{ V}$$

$$42. (B) V_A = 277 \angle (45^\circ - 120^\circ) = 277 \angle -75^\circ \text{ V}$$

$$V_B = 277 \angle (45^\circ + 120^\circ) = 277 \angle 165^\circ \text{ V}$$

$$V_{AB} = V_A - V_B = 480 \angle -45^\circ \text{ V}$$

$$43. (C) Z_A = 6 \parallel 12 = 4,$$

$$I_P = \frac{480}{4} = 120 \text{ A}_{\text{rms}}$$

$$I_L = \sqrt{3} I_P = 208 \text{ A}_{\text{rms}}$$

$$44 (B) I = \frac{I_{aA}(10 + j4)}{(10 + j4) + (4 + j4)} = 10 \angle 20^\circ$$

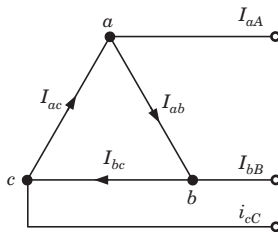


Fig. S.1.7.44

$$I_{aA} = 15 \angle -27.9^\circ \text{ A}_{\text{rms}}$$

$$I_{ab} = -\frac{|I_{aA}|}{\sqrt{3}} \angle (\theta + 30^\circ) = 8.67 \angle -122.1^\circ \text{ A}_{\text{rms}}$$

$$45. (D) I_{AB} = \frac{I_{aA}}{\sqrt{3}} \angle (\theta + 30^\circ) = 16.22 \angle 1.34^\circ \text{ A}_{\text{rms}}$$

$$V_{AB} = I_{AB} \cdot Z_{\Delta} = (16.22 \angle 1.34^\circ)(10 + j8) \\ = 207.8 \angle 40^\circ \text{ V}_{\text{rms}}$$

$$46. (B) |S| = \sqrt{3} V_L I_L \Rightarrow I_L = \frac{3600}{208\sqrt{3}} = 10 \text{ A}_{\text{rms}}$$

$$Z_Y = \frac{208}{10\sqrt{3}} \angle 25^\circ = 12 \angle 25^\circ = 10.88 + j5.07 \Omega$$
