

Class VIII Session 2024-25
Subject - Mathematics
Sample Question Paper - 7

Time Allowed: 3 hours

Maximum Marks: 80

General Instructions:

1. This Question Paper has 4 Sections A-D.
2. Section A has 20 MCQs carrying 1 mark each.
3. Section B has 6 questions carrying 02 marks each.
4. Section C has 8 questions carrying 03 marks each.
5. Section D has 6 questions carrying 04 marks each.
6. All Questions are compulsory.
7. Draw neat figures wherever required. Take $\pi = 22/7$ wherever required if not stated

Section A

1. Which of the following statements is correct? [1]
 - i. 0 is called the additive identity for rational numbers.
 - ii. 1 is called the multiplicative identity for rational numbers
 - iii. The additive inverse of 0 is zero itself.
 - iv. All of these

a) Option (iv)

c) Option (iii)

b) Option (i)

d) Option (ii)
2. Simplify: $\frac{\left(-18\frac{1}{3} \times 2\frac{8}{11}\right) - \left(4\frac{5}{7} \times 2\frac{1}{3}\right)}{\left|\frac{3}{5} + \left(\frac{-9}{10}\right)\right| + \left|-\left(\frac{-3}{5}\right)\right|}$ [1]

a) $63\frac{4}{81}$

c) $-67\frac{7}{9}$

b) $-23\frac{7}{9}$

d) $12\frac{6}{17}$
3. The value of x for which the expressions $3x - 4$ and $2x + 1$ become equal is [1]

a) 5

c) 0

b) -3

d) 1
4. Given that $\frac{-6p-9}{3} = \frac{2p+9}{5}$, the value of p is [1]

a) -2


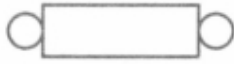


c) -4

b) 3

d) 5
5. A parallelogram each of whose angles measures 90° is _____. [1]

a) rectangle

b) trapezium

- c) kite d) rhombus
6. Find the number of sides of a regular polygon whose each exterior angle has a measure of 30° . [1]
- a) 15 b) 13
c) 12 d) 14
7. Which one of the following is not perfect square? [1]
- a) $4^5 \times 5^5 \times 20$ b) $4^6 \times 5^6 \times 6^6$
c) $4^4 \times 5^4 \times 6^4$ d) $4^4 \times 5^5 \times 6^6$
8. The number of digits in the square root of 298116 is [1]
- a) 6 b) 5
c) 3 d) 4
9. If cube root of 175616 is 56, then the value of $\sqrt[3]{175.616} + \sqrt[3]{0.175616} + \sqrt[3]{0.000175616}$ is [1]
- a) 6.116 b) 6.216
c) 0.168 d) 62.16
10. Find the compound interest on ₹ 2,000 for 2 years at 10% per annum compounded annually. [1]
- a) ₹ 420 b) ₹ 350
c) ₹ 2350 d) ₹ 2450
11. If x% of y is 100 and y% of z is 200, then [1]
- a) $z = 2x$ b) $z = \frac{x}{4}$
c) $z = 3x$ d) $z = \frac{x}{3}$
12. Subtract $5x^2 - 4y^2 + 6y - 3$ from $7x^2 - 4xy + 8y^2 + 5x - 3y$. [1]
- a) $2x^2 - 4xy + 12y^2 + 5x - 9y + 3$ b) $2x^2 - 4xy + 12y^2 + 5x$
c) $2x^2 - 4xy + 12y^2 + 5x - 9y$ d) $5x - 9y + 3$
13. The sum of $-7pq$ and $2pq$ is: [1]
- a) $5pq$ b) $-9pq$
c) $9pq$ d) $-5pq$
14. Which of the following is the net of a cylinder? [1]
- a)  b) 
c)  d) 
15. The capacity of a closed cylindrical water tank is 46.2 kilolitres. If the height of the cylinder is 1.2 m, then what is its radius? [1]
- a) 30 m b) 3.5 m
c) 20 m d) 2.8 m

16. Simplify: $\frac{\sqrt{216} + \sqrt{96}}{\sqrt{50^2 - 10^2}}$ [1]
 a) $\frac{1}{2}$ b) 2
 c) $\frac{1}{4}$ d) 1
17. Evaluate the exponential expression $(-n)^4 \times (-n)^2$, for $n = 5$. [1]
 a) 25 b) 625
 c) 3125 d) 15625
18. If 6 men and 8 boys can do a piece of work in 10 days and 26 men and 48 boys can do the same work in 2 days, the time taken by 15 men and 20 boys to do the same type of work will be [1]
 a) 4 days b) 7 days
 c) 6 days d) 8 days
19. Simplify $\frac{49a^4b^6c^8}{7a^2b^2c^2}$ [1]
 a) $7a^4b^4c^6$ b) $7a^2b^2c^2$
 c) $7a^4b^2c^6$ d) $7a^2b^4c^6$
20. Simplified form of $\frac{(-6a^3b^5)(2a^2b^3)}{-18a^4b^8c^3}$ [1]
 a) $\frac{2a}{3c^3}$ b) $\frac{-2a^2b}{3c^3}$
 c) $\frac{2a^2b}{3bc^3}$ d) $\frac{-2ab}{3c^3}$

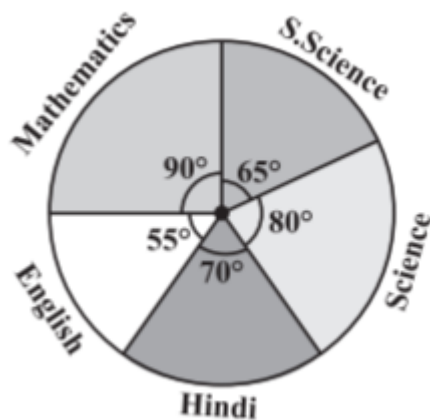
Section B

21. Solve the linear equation: $m - \frac{m-1}{2} = 1 - \frac{m-2}{3}$ [2]
22. The measure of two adjacent angles of a parallelogram are in the ratio 3 : 2. Find the measure of each of the angles of the parallelogram. [2]

OR

Both the pairs of opposite angles of a quadrilateral are equal and supplementary. Find the measure of each angle.

23. The adjoining pie chart gives the marks scored in an examination by a student in Hindi, English, Mathematics, Social Science and Science. If the total marks obtained by the students were 540, answer the question. [2]



Examine whether the sum of the marks obtained in Social Science and Mathematics is more than that in Science and Hindi. (Hint: Just study the central angles).

24. Using prime factorisation, find the cube root of 5832. [2]

[2]

25. Add: $4y(3y^2 + 5y - 7)$ and $2(y^3 - 4y^2 + 5)$

OR

The cost of a chocolate is ₹ $(x + 4)$ and Rohit bought $(x + 4)$ chocolates. Find the total amount paid by him in terms of x . If $x = 10$.

26. Draw a prism with its base as regular hexagon with one of its face facing you. Now draw the top view, front view and side view of this solid. [2]

27. Verify commutative property of multiplication if $x = 2$ and $y = \frac{-7}{8}$. [3]

28. Solve the linear equation $\frac{3t-2}{4} - \frac{2t+3}{3} = \frac{2}{3} - t$. [3]

29. Find the value of $\sqrt{\sqrt{144} + \sqrt{25}}$ [3]

OR

Find the number of plants in each row, if 1024 plants are arranged, so that number of plants in a row is the same as the number of rows.

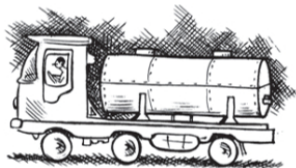
30. Three bags contain 64.2 kg of sugar. The second bag contains $\frac{4}{5}$ of the contents of the first and the third contains $45\frac{1}{2}\%$ of what there is in the second bag. How much sugar is there in each bag? [3]

31. The product of two expressions is $x^5 + x^3 + x$. If one of them is $x^2 + x + 1$, find the other. [3]

32. Four times the area of the curved surface of a cylinder is equal to 6 times the sum of the areas of its bases. If its height is 12 cm, find its curved surface area. [3]

OR

A milk tank is in the form of cylinder whose radius is 1.5 m and length is 7 m. Find the quantity of milk in litres that can be stored in the tank?



33. Find the value of : $\left\{ \left(\frac{-2}{3} \right)^{-2} \right\}^2$ [3]

34. Divide: $24(x^2yz + xy^2z + xyz^2)$ by $8xyz$. [3]

35. PQRS is a rectangle. The perpendicular ST from S on PR divides $\angle S$ in the ratio 2 : 3. Find $\angle TPQ$. [4]

OR

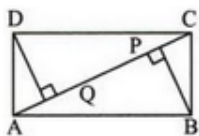
In the given rectangle ABCD, BP and DQ are perpendiculars to AC from B and D respectively/ Answer the following and give reasons for your answers.

i. Is $AD = BC$?

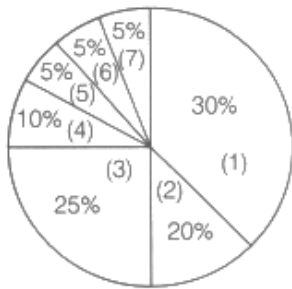
ii. Is $\angle BAP = \angle DCQ$?

iii. Is $\triangle DAQ \cong \triangle BCP$?

iv. Is $BP = DQ$?



36. A financial counselor gave a client this pie chart describing how to budget his income. If the client brings home 50000 each month, how much should he spend in each category? [4]



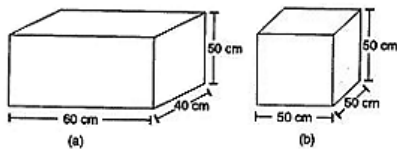
1. Housing
2. Food (including eating out)
3. Car loan and maintenance
4. Utilities
5. Phone
6. Clothing
7. Entertainment

OR

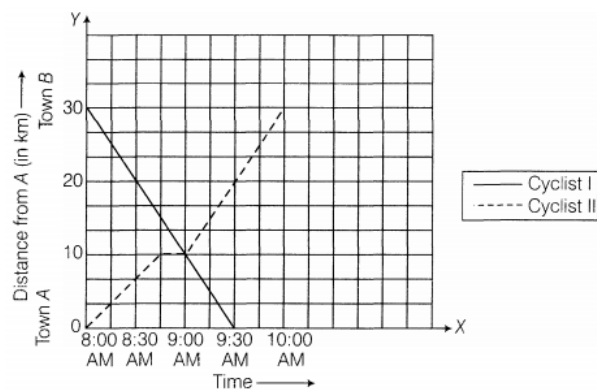
The following data represents the approximate percentage of water in various oceans. Prepare a pie chart of the given data.

Ocean	Percentage of water
pacific	40%
Atlantic	30%
Indian	20%
Others	10%

37. Given, principal = ₹40000, rate of interest = 8% per annum compounded annually. Find [4]
- i. Interest if period is one year.
 - ii. Principal for 11th year.
 - iii. Interest for 11th year.
 - iv. Amount if period is two year.
38. There are two cuboidal boxes as shown in the adjoining figure. Which box requires the least amount of material to make? [4]



39. The cost of 5 metres of a particular quality of cloth is ₹210. Tabulate the cost of 2, 4, 10 and 13 metres of cloth of the same type. [4]
40. The following graph shows the journey made by two cyclists, one from town A to B and the other from town B to A. [4]



- At what time did cyclist II rest? How long did the cyclist rest?
- Was cyclist II cycling faster or slower after the rest?
- At what time did the two cyclists meet?
- How far had cyclist II travelled when he met cyclist I?
- When cyclist II reached town A, how far was cyclist I from town S?

Solution

Section A

1. (a) Option (iv)

Explanation: All the given statements are correct.

2.

(c) $-67\frac{7}{9}$

Explanation: We have,
$$\frac{\left(-18\frac{1}{3} \times 2\frac{8}{11}\right) - \left(4\frac{5}{7} \times 2\frac{1}{3}\right)}{\left|\frac{3}{5} + \left(-\frac{9}{10}\right)\right| + \left|-\left(-\frac{3}{5}\right)\right|}$$
$$= \frac{\left(\frac{-55}{3} \times \frac{30}{11}\right) - \left(\frac{33}{7} \times \frac{7}{3}\right)}{\left|\frac{3}{5} - \frac{9}{10}\right| + \left|\frac{3}{5}\right|} = \frac{-50 - 11}{\left|\frac{6-9}{10}\right| + \frac{3}{5}}$$
$$= \frac{-61}{\frac{3}{10} + \frac{3}{5}} = \frac{-61}{\frac{3+6}{10}} = \frac{-61 \times 10}{9} = \frac{-610}{9} = -67\frac{7}{9}$$

3. (a) 5

Explanation: When the value of x is 5 then both the expressions will be equal.

Proof

$$3x - 4 = 2x + 1$$

$$x = 5$$

4. (a) -2

Explanation: $\frac{-6p-9}{3} = \frac{2p+9}{5}$

$$\Rightarrow 5(-6p - 9) = 3(2p + 9)$$

$$\Rightarrow -30p - 45 = 6p + 27$$

$$\Rightarrow -30p - 6p = 45 + 27$$

$$\Rightarrow -36p = 72$$

$$\Rightarrow p = -2$$

5. (a) rectangle

Explanation: A rectangle is a type of parallelogram in which all the four angles are of 90^0 but the opposite sides are equal.

6.

(c) 12

Explanation: Number of sides

$$n = \frac{360^0}{30^0}$$

$$= 12$$

7.

(d) $4^4 \times 5^5 \times 6^6$

Explanation: $4^4 \times 5^5 \times 6^6$

$$= = \underline{4 \times 4 \times 4 \times 4} \times \underline{5 \times 5 \times 5 \times 5 \times 5} \times \underline{6 \times 6} \times \underline{6 \times 6} \times \underline{6 \times 6}$$

Since each factor cannot be paired. So, is not a perfect square.

8.

(c) 3

	2	298116
	2	149058
	3	74529
	3	24843
Explanation:	7	8281
	7	1183
	13	169
	13	13
		1

$$\Rightarrow \sqrt{298116} = 2 \times 3 \times 7 \times 13$$

$$= 546$$

\therefore Number of digits = 3

9.

(b) 6.216

Explanation: $\sqrt[3]{175.616} + \sqrt[3]{0.175616} + \sqrt[3]{0.000175616}$
 $= 5.6 + 0.56 + 0.056 = 6.216$

10. (a) ₹ 420

Explanation: C.I. = $2000 \left(1 + \frac{10}{100}\right)^2 - 2000 = 2000 \times \frac{11}{10} \times \frac{11}{10} - 2000$
 $= ₹ (2420 - 2000) = ₹ 420$

11. (a) $z = 2x$

Explanation: It is given that $x\%$ of $y = 100$

$$\Rightarrow \frac{xy}{100} = 100 \Rightarrow xy = 10000 \Rightarrow y = \frac{10000}{x}$$

Also, $y\%$ of $z = 200$

$$\Rightarrow \frac{yz}{100} = 200 \Rightarrow yz = 20000$$

$$\Rightarrow \left(\frac{10000}{x}\right)z = 20000$$

$$\Rightarrow \frac{z}{x} = 2 \text{ or } z = 2x$$

12. (a) $2x^2 - 4xy + 12y^2 + 5x - 9y + 3$

Explanation: $(7x^2 - 4xy + 8y^2 + 5x - 3y) - (5x^2 - 4y^2 + 6y - 3)$

opening brackets we get,

$$7x^2 - 4xy + 8y^2 + 5x - 3y - 5x^2 + 4y^2 - 6y + 3$$

solving like terms we get,

$$7x^2 - 4xy + 8y^2 + 5x - 3y - 5x^2 + 4y^2 - 6y + 3$$

$$7x^2 - 5x^2 + 8y + 4y^2 + 5x - 3y - 6y - 4xy + 3$$

$$2x^2 + 12y^2 + 5x - 9y - 4xy + 3$$

$$2x^2 - 4xy + 12y^2 + 5x - 9y + 3$$

13.

(d) $-5pq$

Explanation: Given, monomials are $-7pq$ and $2pq$.

\therefore Their sum = $-7pq + 2pq = (-7 + 2)pq$ [both monomials consist of like terms, so adding their numerical coefficient]

$$= -5pq$$

14.

(b) 

Explanation: 

15.

(b) 3.5 m

Explanation: Volume of cylindrical tank = 46.2 kL

$$= 46200 \text{ L} = \left(\frac{46200}{1000} \right) \text{m}^3 = 46.2 \text{ m}^3$$

Height of tank (h) = 1.2 m

Let r be the radius. Then, $\pi r^2 h = 46.2$

$$\Rightarrow \frac{22}{7} \times r^2 \times 1.2 = 46.2$$

$$\Rightarrow r^2 = 12.25$$

$$\Rightarrow r = 3.5 \text{ m}$$

16. (a) $\frac{1}{2}$

Explanation: $\frac{1}{2}$

17.

(d) 15625

Explanation: $(-5)^4 \times (-5)^2$

$$= 625 \times 25$$

$$= 15625$$

18. (a) 4 days

Explanation: Given $(6M + 8B) \times 10 = (26M + 48B) \times 2$

$$\Rightarrow 60M + 80B = 52M + 96B$$

$$\Rightarrow 8M = 16B$$

$$\Rightarrow 1M = 2B$$

$$\therefore 15M + 20B = 30B + 20B = 50B$$

$$6M + 8B = 12B + 8B = 20B$$

Now

Boys	Days
20	10
50↓	x (Let)

$$\therefore x = \frac{20 \times 10}{50} = 4 \text{ days}$$

19.

(d) $7a^2b^4c^6$

Explanation: $\frac{49a^4b^6c^8}{7a^2b^2c^2}$

$$= 7a^{4-2}b^{6-2}c^{8-2}$$

$$= 7a^2b^4c^6$$

20. (a) $\frac{2a}{3c^3}$

Explanation: $\frac{(-6a^3b^5)(2a^2b^3)}{-18a^4b^8c^3}$

$$= \frac{12}{18} \frac{a^{3+2}b^{5+3}}{a^4b^8c^3}$$

$$= \frac{2}{3} \frac{a^5b^8}{a^4b^8c^3} = \frac{2}{3} \frac{a}{c^3}$$

Section B

21. $m - \frac{m-1}{2} = 1 - \frac{m-2}{3}$

It is a linear equation since it involves linear expressions only.

$$\therefore m - \frac{m}{2} + \frac{1}{2} = 1 - \frac{m}{3} + \frac{2}{3}$$

$$\therefore m - \frac{m}{2} + \frac{m}{3} = 1 + \frac{2}{3} - \frac{1}{2} \dots [\text{Transposing } \frac{-m}{3} \text{ to L.H.S. and } \frac{1}{2} \text{ to R.H.S.}]$$

$$\therefore \frac{6m-3m+2m}{6} = \frac{6+4-3}{6}$$

$$\therefore \frac{5m}{6} = \frac{7}{6}$$

$$\therefore m = \frac{7}{6} \times \frac{6}{5} \dots [\text{Multiplying both sides by } \frac{6}{5}]$$

$$\therefore m = \frac{7}{5} \text{ this is the required solution.}$$

22. Let the two adjacent angles be $3x^\circ$ and $2x^\circ$.

Then,

$$3x^\circ + 2x^\circ = 180^\circ (\because \text{Sum of the two adjacent angles of a parallelogram is } 180^\circ)$$

$$\Rightarrow 5x^\circ = 180^\circ$$

$$\Rightarrow x^\circ = \frac{180^\circ}{5}$$

$$\Rightarrow x^\circ = 36^\circ$$

$$\Rightarrow 3x^\circ = 3 \times 36^\circ = 108^\circ$$

$$\text{and } 2x^\circ = 2 \times 36^\circ = 72^\circ$$

Since, the opposite angles of a parallelogram are equal measure, therefore the measures of the angles of the parallelogram are 72° , 108° , 72° and 108° .

OR

Let ABCD be a quadrilateral, such that

$$\angle A = \angle C, \angle B = \angle D \text{ and also } \angle A + \angle C = 180^\circ, \angle B + \angle D = 180^\circ$$

$$\text{Now, } \angle A + \angle A = 180^\circ$$

$$\Rightarrow 2\angle A = 180^\circ$$

$$\Rightarrow \angle A = 90^\circ$$

$$\text{Similarly, } \angle B = 90^\circ$$

Hence, each angle is a right angle.

23. From the graph it is clear that

Sum of the central angles for Social Science and Mathematics.

$$= 65^\circ + 90^\circ$$

$$= 155^\circ$$

Sum of the central angles for Science and Hindi.

$$= 80^\circ + 70^\circ$$

$$= 150^\circ$$

Hence, the sum of the marks obtained in Social Science and Mathematics is more than in Science and Hindi.

24. We have, The prime factorization of 5832 is

2	5832
2	2916
2	1458
3	729
3	243
3	81
3	27
3	9
3	3
	1

$$5832 = 2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 3 \times 3 \times 3$$

$$\text{Therefore, } \sqrt[3]{5832} = \sqrt[3]{2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 3 \times 3 \times 3}$$

$$= 2 \times 3 \times 3$$

$$= 18$$

25. The first expression $= 4y(3y^2 + 5y - 7) = (4y \times 3y^2) + (4y \times 5y) + (4y \times (-7)) = 12y^3 + 20y^2 - 28y$

$$\text{The second expression} = 2(y^3 - 4y^2 + 5) = 2y^3 + 2 \times (-4y^2) + 2 \times 5 = 2y^3 - 8y^2 + 10$$

Adding the two expressions,

$$\begin{array}{r} 12y^3 \quad + \quad 20y^2 - 28y \\ + \quad 2y^3 \quad - \quad 8y^2 \quad + 10 \\ \hline 14y^3 \quad + \quad 12y^2 - 28y + 10 \end{array}$$

Thus, the sum is $14y^3 + 12y^2 - 28y + 10$

OR

Given, cost of a chocolate = ₹ $(x + 4)$

Rohit bought $(x + 4)$ chocolates

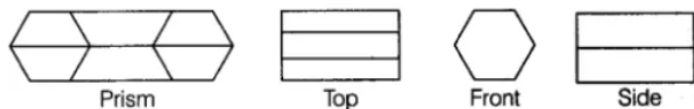
$$\therefore \text{The cost of } (x + 4) \text{ chocolates} = \text{Cost of one chocolate} \times \text{Number of chocolates} = (x + 4)(x + 4) = (x + 4)^2$$

$$\therefore \text{The total amount paid by Rohit} = ₹(x^2 + 8x + 16) [\because (a + b)^2 = a^2 + 2ab + b^2]$$

Now, if $x = 10$. Then, the amount paid by Rohit $= 10^2 + 8 \times 10 + 16 = 100 + 80 + 16 = ₹196$

26. The following figure shows a prism with its base as a regular hexagon with one of its faces to us.

And also, we show the top view, front view and side view of the prism.



27. Commutative property of multiplication is $x \times y = y \times x$

L.H.S

$$2 \times \frac{-7}{8} = \frac{-14}{8}$$

R.H.S

$$\frac{-7}{8} \times 2 = \frac{-14}{8}$$

Therefore, L.H.S = R.H.S

Hence, verified.

28. $\frac{3t-2}{4} - \frac{2t+3}{3} = \frac{2}{3} - t$ It is a linear equation since it involves linear expressions only.

$$\therefore \frac{3}{4}t - \frac{2}{4} - \frac{2}{3}t - \frac{3}{3} = \frac{2}{3} - t$$

$$\therefore \frac{3}{4}t - \frac{1}{2} - \frac{2}{3}t - 1 = \frac{2}{3} - t$$

$$\therefore \frac{3}{4}t - \frac{2}{3}t + t = \frac{2}{3} + \frac{1}{2} + 1 \dots [\text{Transposing } -t \text{ to L.H.S. and } -\frac{1}{2} \text{ and } -1 \text{ to R.H.S.}]$$

$$\therefore \frac{9t-8t+12t}{12} = \frac{4+3+6}{6}$$

$$\therefore \frac{13t}{12} = \frac{13}{6}$$

$$\therefore t = \frac{13}{6} \times \frac{12}{13} \dots [\text{Multiplying both sides by } \frac{12}{13}]$$

$\therefore t = 2$ this is the required solution.

29. $\sqrt{\sqrt{144} + \sqrt{25}}$

$$= \sqrt{\sqrt{3 \times 3 \times 4 \times 4} + \sqrt{5 \times 5}}$$

$$\sqrt{3 \times 4 + 5}$$

$$\sqrt{17}$$

OR

Let the number of plants in each row be x .

Then, number of rows = number of plants in each row = x

	32
3	<u>1024</u>
	9
62	<u>124</u>
	124
	0

$$\text{Total plants} = x \times x = x^2$$

$$\text{According to the question, } x^2 = 1024$$

$$\Rightarrow x = \sqrt{1024} = \sqrt{32 \times 32}$$

$\therefore x = 32$ Hence, there are 32 plants in each row.

30. We have given,

The total weight of sugar in three bags = 64.2 kg

Let the first bag contains x kg sugar

The second bag contains $= x \times \frac{4}{5}$ kg

$$= \frac{4x}{5} \text{ kg}$$

Third bag contains $= x \times \frac{4}{5} \times \frac{91}{2} \%$

$$= x \times \frac{4}{5} \times \frac{91}{100}$$

$$= \frac{91x}{250} \text{ kg}$$

According to the question,

$$\begin{aligned}
 x + \frac{4x}{5} + \frac{91x}{250} &= 64.2 \\
 \Rightarrow \frac{250x + 200x + 91x}{250} &= 64.2 \\
 \Rightarrow 541x &= 64.2 \times 250 \\
 541x &= 16050 \\
 x &= \frac{16050}{541} \\
 x &= 29.67\text{kg}
 \end{aligned}$$

So, the first bag contains the sugar = 23.73 kg

$$\begin{aligned}
 \text{Second bag contains the sugar} &= 29.67 \times \frac{4}{5} \\
 &= 23.73\text{kg}
 \end{aligned}$$

$$\begin{aligned}
 \text{and third bag contains the sugar} &= \frac{91}{250} \times 29.67 \\
 &= 10.8\text{kg}
 \end{aligned}$$

31. We have, product of two expressions $x^5 + x^3 + x$ and one is $x^2 + x + 1$

Let the other expression be A. Then, $A \cdot (x^2 + x + 1) = x^5 + x^3 + x$

$$\begin{aligned}
 \Rightarrow A &= \frac{x^5 + x^3 + x}{x^2 + x + 1} = \frac{x(x^4 + x^2 + 1)}{x^2 + x + 1} \\
 \Rightarrow A &= \frac{x(x^4 + 2x^2 - x^2 + 1)}{x^2 + x + 1} = \frac{x(x^4 + 2x^2 + 1 - x^2)}{x^2 + x + 1} \quad [\text{adding and subtracting } x^2 \text{ in numerator term}] \\
 &= \frac{x[(x^4 + 2x^2 + 1) - x^2]}{x^2 + x + 1} = \frac{x[(x^2 + 1)^2 - x^2]}{x^2 + x + 1} \\
 &= \frac{x(x^2 + 1 + x)(x^2 + 1 - x)}{x^2 + x + 1} \quad [\text{using the identity, } a^2 - b^2 = (a + b)(a - b)] \\
 &= x(x^2 + 1 - x)
 \end{aligned}$$

Hence, the other expression is $x(x^2 - x + 1)$

32. Let the radius and height of the cylinder be r and h , respectively.

$$\text{Curved surface area of cylinder} = 2\pi rh$$

$$\text{Area of base} = \pi r^2$$

$$\text{Sum of areas of bases} = 2\pi r^2$$

$$\text{According to the question, } 4 \times \text{Curved surface area} = 6 \times \text{Sum of areas of bases}$$

$$4 \times 2\pi rh = 6 \times 2\pi r^2$$

$$= 8\pi rh = 12\pi r^2$$

$$= 2h = 3r$$

$$\Rightarrow r = \frac{2}{3}h$$

$$\therefore r = \frac{2}{3} \times 12 = 8\text{cm} \quad [\because h = 12\text{ cm, given}]$$

$$\therefore \text{Curved surface area of the cylinder} = 2\pi rh$$

$$= 2 \times \frac{22}{7} \times 8 \times 12 = \frac{44 \times 8 \times 12}{7}$$

$$= 603.428\text{ cm}^2$$

OR

For milk tank

$$r = 1.5\text{ m}$$

$$h = 7\text{ m}$$

$$\therefore \text{Capacity} = \pi r^2 h$$

$$= \frac{22}{7} \times 1.5 \times 1.5 \times 7$$

$$= \frac{22}{7} \times \frac{15}{10} \times \frac{15}{10} \times 7$$

$$= 49.5\text{ m}^3$$

$$= 49.5 \times 1000\text{ L} \dots [\because 1\text{ m}^3 = 1000\text{ L}]$$

$$= 49500\text{ L}$$

Hence, the quantity of milk that can be stored in the tank is 49500 litres.

$$\begin{aligned}
 33. &\left\{ \left(\frac{-2}{3} \right)^{-2} \right\}^2 \\
 &= \left(\frac{-2}{3} \right)^{(-2) \times 2} \\
 &= \left(\frac{-2}{3} \right)^{-4}
 \end{aligned}$$

$$\begin{aligned}
&= \frac{(-2)^{-4}}{(3)^{-4}} \\
&= \frac{3^4}{(-2)^4} \\
&= \frac{3 \times 3 \times 3 \times 3}{(-2) \times (-2) \times (-2) \times (-2)} \\
&= \frac{81}{16} \\
&= 5 \frac{1}{16}
\end{aligned}$$

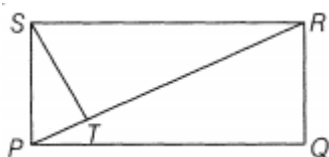
34. $24(x^2yz + xy^2z + xyz^2)$

$$\begin{aligned}
&= 2 \times 2 \times 2 \times 3 \times [(x \times x \times y \times z) + (x \times y \times y \times z) + (x \times y \times z \times z)] \\
&= 2 \times 2 \times 2 \times 3 \times x \times y \times z \times (x + y + z) \text{ [By taking out the common factor]} \\
&= 8 \times 3 \times xyz \times (x + y + z)
\end{aligned}$$

Now, $24(x^2yz + xy^2z + xyz^2) \div 8xyz$

$$= \frac{8 \times 3 \times xyz \times (x + y + z)}{8 \times xyz} = 3 \times (x + y + z) = 3(x + y + z)$$

35. Given ST is perpendicular on PR and ST divides $\angle S$ in the ratio 2 : 3
- So, sum of ratio = 2 + 3 = 5



Now, $\angle TSP = \frac{2}{5} \times 90^\circ = 36^\circ$, $\angle TSR = \frac{3}{5} \times 90^\circ = 54^\circ$

$\angle TPS = 180^\circ - (\angle STP + \angle TSP)$ [by the angle sum property of a triangle]

$$= 180^\circ - (90^\circ + 36^\circ) = 54^\circ$$

We know that, $\angle SPQ = 90^\circ$

$$\Rightarrow \angle TPS + \angle TPQ = 90^\circ$$

$$\Rightarrow 54^\circ + \angle TPQ = 90^\circ$$

$$\Rightarrow \angle TPQ = 90^\circ - 54^\circ = 36^\circ$$

OR

- i. Yes (opposite sides of a rectangle)
- ii. Yes, since, $AB \parallel CD$, AC is a transversal and they are alternate angles.
- iii. Since DQ and BP are perpendiculars from D and B, respectively on AC, therefore, $\angle DQA = \angle BPC = 90^\circ$.
Thus $DQ \parallel BP$ (if the alternate angles are equal the lines are parallel)
Also $AD \parallel BC$ and AC is the transversal.
 $\therefore \angle DAQ = \angle BCP$ (Alternate angles)
Since $\angle DQA = \angle BPC$ and $\angle DAQ = \angle BCP$,
 $\therefore \angle ADQ = \angle CBP$
Now in $\triangle DAQ$ and $\triangle BCP$, we have
 $\angle DAQ = \angle BCP$
 $\angle ADQ = \angle CBP$
 $DA = BC$
 $\therefore \triangle DAQ \cong \triangle BCP$ (by ASA condition of congruence)
- iv. Yes, (corresponding parts of congruent triangle $\triangle DAQ$ and $\triangle BCP$)

36. Monthly income = ₹50000

Category	Money spent
Housing	$\frac{30}{100} \times 50000 = 15000$
Food (including eating out)	$\frac{20}{100} \times 50000 = 10000$
Car loan and maintenance	$\frac{25}{100} \times 50000 = 12500$
Utilities	$\frac{10}{100} \times 50000 = 5000$
Phone	$\frac{5}{100} \times 50000 = 2500$
Clothing	$\frac{5}{100} \times 50000 = 2500$

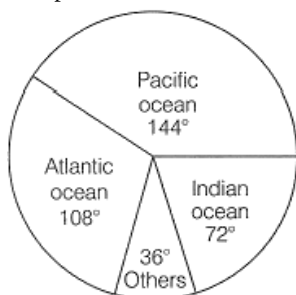
Entertainment

$$\frac{5}{100} \times 50000 = 2500$$

OR

Ocean	Central angle
Pacific	$\frac{40}{100} \times 360^\circ = 144^\circ$
Atlantic	$\frac{30}{100} \times 360^\circ = 108^\circ$
Indian	$\frac{20}{100} \times 360^\circ = 72^\circ$
Others	$\frac{10}{100} \times 360^\circ = 36^\circ$

The pie chart is as follows:



37. We have given that principal (P) = ₹40000

Rate of interest (R) = 8% per annum

i. Compound interest for one year,

$$\text{We know that, } A = P \left(1 + \frac{R}{100} \right)^n$$

$$= 40000 \left(1 + \frac{8}{100} \right)^1 [\because n = 1 \text{ yr}]$$

$$= 40000 \times \frac{108}{100}$$

$$\therefore \text{Amount, } A = 400 \times 108$$

$$= ₹43200$$

$$\therefore \text{Compound interest, CI} = A - P$$

$$= ₹43200 - ₹40000$$

$$= ₹3200$$

ii. Amount of 1st year = Principal of 1st year

$$= ₹43200$$

iii. Now, for 1st year,

$$\text{Principal} = ₹43200$$

Rate of interest, R = 8% per annum

Time, n = 1 yr

$$\text{Amount for 1st year} = 43200$$

$$= \left(1 + \frac{8}{100} \right)^1$$

$$= 43200 \times \frac{108}{100}$$

$$= ₹46656$$

$$\text{Compound interest, CI} = A - P$$

$$= ₹46656 - ₹43200$$

$$= ₹3456$$

iv. Now, if period i.e. time (n) = 2 yr,

$$\text{Principal} = ₹40000$$

and rate (R) = 8% per annum

$$\therefore A = P \left(1 + \frac{R}{100} \right)^n$$

$$\Rightarrow A = 40000 \left(1 + \frac{8}{100} \right)^2$$

$$= 40000 \times \frac{108}{100} \times \frac{108}{100}$$

$$= ₹46656$$

Therefore the total Amount, A = ₹46656

38. i. First Cuboidal Box

$$l = 60 \text{ cm}$$

$$b = 40 \text{ cm}$$

$$h = 50 \text{ cm}$$

∴ Total surface area

$$= 2 (lb + bh + hl)$$

$$= 2 (60 \times 40 + 40 \times 50 + 50 \times 60)$$

$$= 2 (2400 + 2000 + 3000)$$

$$= 2 (7400)$$

$$= 14800 \text{ cm}^2$$

ii. Second Cuboidal Box

$$l = 50 \text{ cm}$$

$$b = 50 \text{ cm}$$

$$h = 50 \text{ cm}$$

∴ Total surface area

$$= 2 (lb + bh + hl)$$

$$= 2 (50 \times 50 + 50 \times 50 + 50 \times 50)$$

$$= 2 (2500 + 2500 + 2500)$$

$$= 2 (7500)$$

$$= 15000 \text{ cm}^2$$

Hence, the box (a) requires the least amount of material to make.

39. Suppose the length of cloth is x metres and its cost, in ₹ is y

x	2	4	5	10	13
y	y ₂	y ₃	210	y ₄	y ₅

As the length of cloth increases, cost of the cloth also increases in the same ratio. It is a case of direct proportion.

We can use the relation of type $\frac{x_1}{y_1} = \frac{x_2}{y_2}$

i. Here $x_1 = 5$, $y_1 = 210$ and $x_2 = 2$

$$\text{Therefore, } \frac{x_1}{y_1} = \frac{x_2}{y_2}$$

$$\text{we get } \frac{5}{210} = \frac{2}{y_2}$$

$$\text{or } 5 y_2 = 2 \times 210$$

$$\text{or } y_2 = \frac{2 \times 210}{5}$$

$$y_2 = 84$$

ii. If $x_3 = 4$,

$$\text{then } \frac{5}{210} = \frac{4}{y_3}$$

$$\text{or } 5 y_3 = 4 \times 210$$

$$\text{or } y_3 = \frac{4 \times 210}{5}$$

$$y_3 = 168$$

iii. If $x_4 = 10$,

$$\text{then } \frac{5}{210} = \frac{10}{y_4}$$

$$\text{or } y_4 = \frac{10 \times 210}{5}$$

$$y_4 = 420$$

iv. If $x_5 = 13$,

$$\text{then } \frac{5}{210} = \frac{13}{y_5}$$

$$\text{or } y_5 = \frac{13 \times 210}{5}$$

$$y_5 = 546$$

40. a. On the basis of the given graph, cyclist II rest at 8 : 45 AM for 15 min.
b. Cyclist II is cycling faster after rest as he has covered a distance of 20 km in 1h.
c. Both cyclists meet at 9:00 AM.
d. Cyclist II had travelled 20 km, when he met cyclist I.
e. When cyclist II reached town A, the cyclist I was 10 km from town B.