

NATURE OF PHYSICAL WORLD AND MEASUREMENT

"Education is not the learning of facts, but the training of the mind to think" - **Albert Einstein**



LEARNING OBJECTIVES

In this unit, the student is exposed to

- excitement generated by the discoveries in Physics
- an understanding of physical quantities of importance
- different system of units
- an understanding of errors and corrections in physics measurements
- the importance of significant figures
- usage of dimensions to check the homogeneity of physical quantities



1.1

SCIENCE—INTRODUCTION

The word 'science' has its root in the Latin verb *scientia*, meaning "to know". In Tamil language, it is '**அ**றிவியல்' (Ariviyal) meaning 'knowing the truth'. The human mind is always curious to know and understand different phenomena like the bright celestial objects in nature, cyclic changes in the seasons, occurrence of rainbow, etc. The inquisitive mind looks for meaningful patterns and relations in such phenomena. Today's modern science and technology is an offshoot of the understanding of nature. Science is the systematic organization of knowledge gained through observation, experimentation and logical reasoning. The knowledge of science dealing with non-living things is physical science

(Physics and Chemistry), and that dealing with living things is biological science (Botany, Zoology etc.).

Curiosity-driven observations of natural happenings was the origin of science. The word 'science' was coined only in the 19th century. Natural philosophy was the earlier name given to science, when ancient civilization knew and practised astronomy, chemistry, human physiology agriculture. Oral communication was the mode of conveying knowledge when writing systems were not yet developed. One of the oldest forerunners of scientific advancements, from astronomy to medicine, were the Egyptians. Scientific and mathematical excellence in India dates back to prehistoric human activity in the Indus Valley Civilization (3300 – 1300 BC(BCE).



According to part IV Article 51A (h) of Indian Constitution "It shall be the duty of every citizen of India to develop scientific temper, humanism and spirit of inquiry and reform". This is the aim of our Science Education.

The name Physics was introduced by Aristotle in the year 350 BC

1.1.1 The Scientific Method

The scientific method is a step-by-step approach in studying natural phenomena and establishing laws which govern these phenomena. Any scientific method involves the following general features.

- (i) Systematic observation
- (ii) Controlled experimentation
- (iii) Qualitative and quantitative reasoning
- (iv) Mathematical modeling
- (v) Prediction and verification or falsification of theories

Example

Consider a metalic rod being heated. When one end of the rod is heated, heat is felt at the other end. The following questions can be asked on this observation

- a) What happens within the rod when it is heated?
- b) How does the heat reach the other end?
- c) Is this effect true for all materials?
- d) If heat flows through the material, is it possible to visualize heat?

The process of finding the answers to these queries is scientific investigation.

The basic phenomenon of heat is discussed in unit 8.

1.2

PHYSICS - INTRODUCTION

The word 'physics' is derived from the Greek word "Fusis", meaning nature. The study of nature and natural phenomena is dealt within physics. Hence physics is considered as the most basic of all sciences.

Unification and Reductionism are the two approaches in studying physics. Attempting to explain diverse physical phenomena with a few concepts and laws is unification. For example, Newton's universal law of gravitation (in unit 6) explains the motion of freely falling bodies towards the Earth, motion of planets around the Sun, motion of the Moon around the Earth, thus unifying the fundamental forces of nature.

An attempt to explain a macroscopic system in terms of its microscopic constituents is *reductionism*. For example, thermodynamics (unit 8) was developed to explain macroscopic properties like temperature, entropy, etc., of bulk systems. The above properties have been interpreted in terms of the molecular constituents (microscopic) of the bulk system by kinetic theory (unit 9) and statistical mechanics.

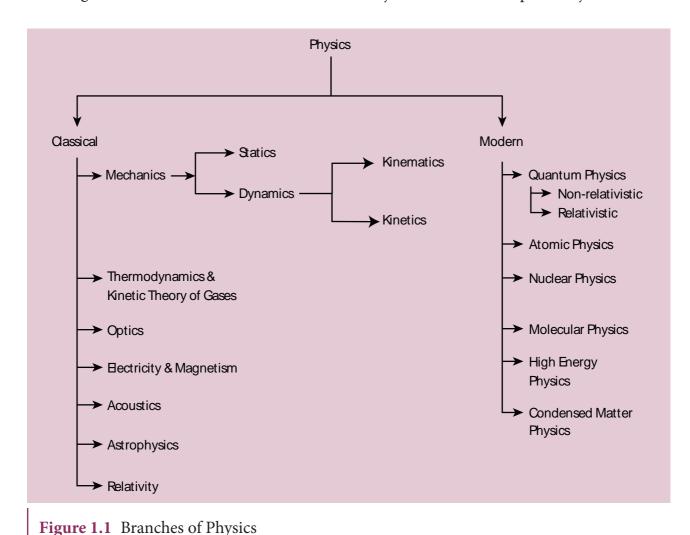


UNIT 1 NATURE OF PHYSICAL WORLD AND MEASUREMENT

1.2.1 Branches of Physics

Physics as a fundamental science helps to uncover the laws of nature. The language of its expression is mathematics. In ancient times, humans lived with nature - their lifestyles were integrated with nature. They could understand the signals from the movement of the stars and other celestial bodies. They could determine the time to sow and reap by watching the sky. Thus, astronomy and mathematics were the first disciplines to be developed. The chronological development of various branches of physics is presented in Appendix A1.1. The various branches of physics are schematically shown in figure 1.1. The essential focus of different areas is given in Table 1.1.

Some of the fundamental concepts of basic areas of physics are discussed in higher secondary first year physics books volume 1 and 2. Mechanics is covered in unit 1 to 6. Unit 1 gives an idea of the development of physics along with discussion on basic elements such as measurement, units etc. Unit 2 gives the basic mathematics needed to express the impact of physical principles and their governing laws. The impact of forces acting on objects in terms of the fundamental laws of motion of Newton are very systematically covered in unit 3. Work and energy which are the basic parameters of investigation of the mechanical world are presented in unit 4. Unit 5 deals with the mechanics of rigid bodies (in contrast, objects are viewed as point objects in units



UNIT 1 NATURE OF PHYSICAL WORLD AND MEASUREMENT



Та	ble 1.1 Branches of P	'hysics	
Classical Physics		Refers to traditional physics that was recognized and developed before the beginning of the 20th century	
	Branch	Major focus	
1.	Classical mechanics	The study of forces acting on bodies whether at rest or in motion	
2.	Thermodynamics	The study of the relationship between heat and other forms of energy	
3.	Optics	The study of light	
4.	Electricity and magnetism	The study of electricity and magnetism and their mutual relationship	
5.	Acoustics	The study of the production and propagation of sound waves	
6.	Astrophysics	The branch of physics which deals with the study of the physics of astronomical bodies	
7.	Relativity	One of the branches of theoretical physics which deals with the relationship between space, time and energy particularly with respect to objects moving in different ways.	
Mo	odern Physics	Refers to the concepts in physics that have surfaced since the beginning of the 20 th century.	
1.	*Quantum mechanics	The study of the discrete nature of phenomena at the atomic and subatomic levels	
2.	Atomic physics	The branch of physics which deals with the structure and properties of the atom	
3.	Nuclear physics	The branch of physics which deals with the structure, properties and reaction of the nuclei of atoms.	
4.	Condensed matter physics	The study of the properties of condensed materials (solids, liquids and those intermediate between them and dense gas). It branches into various sub-divisions including	
		developing fields such as nano science, photonics etc.	
		It covers the basics of materials science, which aims at	
		developing new material with better properties for promising applications.	
		applications.	
5.	High energy physics	The study of the nature of the particles.	

Detailed explanation is beyond the scope of this book.

3 and 4). The basics of gravitation and its consequences are discussed in unit 6. Older branches of physics such as different properties of matter are discussed in unit 7. The impact of heat and investigations of its consequences are covered in units 8 and 9. Important features of oscillations and wave motion are covered in units 10 and 11.



1.2.2 Scope and Excitement of Physics

Discoveries in physics are of two types; accidental discoveries and well-analysed research outcome in the laboratory based on intuitive thinking and prediction. For magnetism was accidentally example, observed but the reason for this strange behavior of magnets was later analysed theoretically. This analysis revealed the underlying phenomena of magnetism. With this knowledge, artificial magnets were prepared in the laboratories. Theoretical predictions are the most important contribution of physics to the developments in technology and medicine. For example, the famous equation of Albert Einstein, E=mc² was a theoretical prediction in 1905 and experimentally proved in 1932 by Cockcroft and Walton. Theoretical predictions aided with recent simulation and computation procedures are widely used to identify the most suited materials for robust applications. The pharmaceutical industry uses this technique very effectively to design new drugs. Biocompatible materials for organ replacement are predicted using quantum prescriptions of physics before fabrication. Thus, experiments and theory work hand in hand complimenting one another.

Physics has a huge scope as it covers a tremendous range of magnitude of various physical quantities (length, mass, time, energy etc). It deals with systems of very large magnitude as in astronomical phenomena as well as those with very small magnitude involving electrons and protons.

Range of time scales: astronomical scales to microscopic scales, 10¹⁸s to 10⁻²²s.

■ Range of masses: from heavenly bodies to electron, 10⁵⁵ kg (mass of known observable universe) to 10⁻³¹ kg (mass of an electron) [the actual mass of an electron is 9.11×10⁻³¹ kg].

The study of physics is not only educative but also exciting in many ways.

- A small number of basic concepts and laws can explain diverse physical phenomena.
- The most interesting part is the designing of useful devices based on the physical laws.

For example i) use of robotics ii) journey to Moon and to nearby planets with controls from the ground iii) technological advances in health sciences etc.

- Carrying out new challenging experiments to unfold the secrets of nature and in verifying or falsifying the existing theories.
- Probing and understanding the science behind natural phenomena like the eclipse, and why one feels the heat when there is a fire? (or) What causes the wind, etc.

In today's world of technological advancement, the building block of all engineering and technical education is physics which is explained with the help of mathematical tools.





PHYSICS IN RELATION TO TECHNOLOGY AND SOCIETY

Technology is the application of the principles of physics for practical purposes. The application of knowledge for practical purposes in various fields to invent and produce useful products or to solve problems is known as technology. Thus, physics and technology can both together impact our society directly or indirectly. For example,

- i. Basic laws of electricity and magnetism led to the discovery of wireless communication technology which has shrunk the world with effective communication over large distances.
- The launching of satellite into space has revolutionized the concept of communication.
- iii. Microelectronics, lasers, computers, superconductivity and nuclear energy have comprehensively changed the thinking and living style of human beings.

Physics being a fundamental science has played a vital role in the development of all other sciences. A few examples:

1. Physics in relation to Chemistry: In physics, we study the structure of atom, radioactivity, X-ray diffraction etc. Such studies have enabled researchers in chemistry to arrange elements in the periodic table on the basis of their atomic numbers. This has further helped to know the nature of valency, chemical

- bonding and to understand the complex chemical structures. Inter-disciplinary branches like Physical chemistry and Quantum chemistry play important roles here.
- 2. Physics in relation to biology: Biological studies are impossible without a microscope designed using physics principles. The invention of the electron microscope has made it possible to see even the structure of a cell. X-ray and neutron diffraction techniques have helped understand the structure of nucleic acids, which help to control vital life processes. X-rays are used for diagnostic purposes. Radio-isotopes are used in radiotherapy for the cure of cancer and other diseases. In recent years, biological processes are being studied from the physics point of view.
- 3. Physics in relation to mathematics: Physics is a quantitative science. It is most closely related to mathematics as a tool for its development.
- 4. Physics in relation to astronomy: Astronomical telescopes are used to study the motion of planets and other heavenly bodies in the sky. Radio telescopes have enabled the astronomers to observe distant points of the universe. Studies of the universe are done using physical principles.
- 5. Physics in relation to geology:
 Diffraction techniques help to study
 the crystal structure of various rocks.
 Radioactivity is used to estimate the age
 of rocks, fossils and the age of the Earth.
- 6. **Physics in relation to oceanography:** Oceanographers seek to understand the physical and chemical processes of the



7. Physics in relation to psychology: All psychological interactions can be derived from a physical process. The movements of neurotransmitters are governed by the physical properties of diffusion and molecular motion. The functioning of our brain is related to our underlying waveparticle dualism.

Nature teaches true science with physics as an efficient tool. Science and technology should be used in a balanced manner so that they do not become weapons to destroy nature which taught us science. Global warming and other negative impacts of technology need to be checked. Safe science with moderate and appropriate use of technology is the need of this century.

The scope and opportunities for higher education in physics and various fellowships offered is given in the beginning of the book.



1.4

MEASUREMENT

"When you can measure what you are speaking about and can express it in numbers, you know something about it; but when you cannot express it in numbers, your knowledge is of a meager and unsatisfactory kind" - Lord Kelvin

The comparison of any physical quantity with its standard unit is known as measurement.

Measurement is the basis of all scientific studies and experimentation. It plays an important role in our daily life. Physics is a quantitative science and physicists always deal with numbers which are the measurement of physical quantities.

1.4.1 Definition of Physical Quantity

Quantities that can be measured, and in terms of which, laws of physics are described are called physical quantities. Examples are length, mass, time, force, energy, etc.

1.4.2 Types of Physical Quantities

Physical quantities are classified into two types. They are fundamental and derived quantities.

Fundamental or base quantities are quantities which cannot be expressed in terms of any other physical quantities. These are length, mass, time, electric current, temperature, luminous intensity and amount of substance.

Quantities that can be expressed in terms of fundamental quantities are called derived quantities. For example, area, volume, velocity, acceleration, force, etc.

UNIT 1 NATURE OF PHYSICAL WORLD AND MEASUREMENT

1.4.3 Definition of Unit and its Types

The process of measurement is basically a process of comparison. To measure a quantity, we always compare it with some reference standard. For example, when we state that a rope is 10 meter long, it is to say that it is 10 times as long as an object whose length is defined as 1 metre. Such a standard is known as the unit of the quantity. Here 1 metre is the unit of the quantity 'length'.

An arbitrarily chosen standard of measurement of a quantity, which is accepted internationally is called unit of the quantity.

The units in which the fundamental quantities are measured are called fundamental or base units and the units of measurement of all other physical quantities, which can be obtained by a suitable multiplication or division of powers of fundamental units, are called derived units.

1.4.4 Different types of Measurement Systems

A complete set of units which is used to measure all kinds of fundamental and derived quantities is called a system of units. Here are the common system of units used in mechanics:

- (a) **the f.p.s. system** is the British Engineering system of units, which uses *foot*, *pound* and *second* as the three basic units for measuring length, mass and time respectively.
- (b) **The c.g.s system** is the Gaussian system, which uses *centimeter*, *gram*

- and *second* as the three basic units for measuring length, mass and time respectively.
- (c) The m.k.s system is based on *metre*, *kilogram* and *second* as the three basic units for measuring length, mass and time respectively.



The cgs, mks and SI are metric or decimal system of units. The fps system is not a metric system.

1.4.5 SI unit System

The system of units used by scientists and engineers around the world is commonly called *the metric system* but, since 1960, it has been known officially as the International System, or SI (the abbreviation for its French name, Système International). The SI with a standard scheme of symbols, units and abbreviations, were developed and recommended by the General Conference on Weights and Measures in 1971 for international usage in scientific, technical, industrial and commercial work. The advantages of the SI system are,

- i) This system makes use of only one unit for one physical quantity, which means a rational system of units.
- ii) In this system, all the derived units can be easily obtained from basic and supplementary units, which means it is a coherent system of units.



UNIT 1 NATURE OF PHYSICAL WORLD AND MEASUREMENT

iii) It is a metric system which means that multiples and submultiples can be expressed as powers of 10.

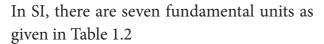




Table 1.2	SI Base Qua	antities an	d Units			
Base		SI Units				
Quantity	Unit	Symbol	Definition			
Length	metre	m	One metre is the length of the path travelled by light in vacuum in 1/299,792,458 of a second (1983)			
Mass	kilogram	kg	One kilogram is the mass of the prototype cylinder of platinum iridium alloy (whose height is equal to its diameter), preserved at the International Bureau of Weights and Measures at Serves, near Paris, France. (1901)			
Time	second	S	One second is the duration of 9,192,631,770 periods of radiation corresponding to the transition between the two hyperfine levels of the ground state of Cesium-133 atom.(1967)			
Electric current	ampere	A	One ampere is the constant current, which when maintained in each of the two straight parallel conductors of infinite length and negligible cross section, held one metre apart in vacuum shall produce a force per unit length of 2×10^{-7} N/m between them. (1948)			
Temperature	kelvin	K	One kelvin is the fraction $\left(\frac{1}{273.16}\right)$ of the			
			thermodynamic temperature of the triple point* of the water. (1967)			
Amount of substance	mole	mol	One mole is the amount of substance which contains as many elementary entities as there are atoms in 0.012 kg of pure carbon-12. (1971)			
Luminous intensity	candela	cd	One candela is the luminous intensity in a given direction, of a source that emits monochromatic radiation of			
			frequency $5.4 \times 10^{14} \text{Hz}$ and that has a radiant intensity			
			of $\frac{1}{683}$ watt/steradian in that direction. (1979)			

^{*} Triple point of water is the temperature at which saturated vapour, pure water and melting ice are all in equilibrium. The triple point temperature of water is 273.16K



Table 1.3 lists some of the derived quantities and their units.

Table 1.3 Derived Quantities and their Units			
Physical quantity	Expression	Unit	
Plane angle	arc / radius	rad	
Solid angle	surface area/radius ²	sr	
Area	$length \times breadth$	m^2	
Volume	area \times height	m^3	
Velocity	displacement / time	$m s^{-1}$	
Acceleration	velocity / time	m s ⁻²	
Angular velocity	angular displacement / time	rad s ⁻¹	
Angular acceleration	angular velocity / time	rad s ⁻²	
Density	mass / volume	kg m ⁻³	
Linear momentum	$mass \times velocity$	kg m s ⁻¹	
Moment of inertia	$mass \times (distance)^2$	kg m²	
Force	$mass \times acceleration$	$kg m s^{-2} or N$	
Pressure	force / area	N m ⁻² or Pa	
Energy (work)	force × distance	N m or J	
Power	Work / time	J s ⁻¹ or watt (W)	
Impulse	$force \times time$	N s	
Surface tension	force / length	$N m^{-1}$	
Moment of force (torque)	force × distance	N m	
Electric charge	current × time	A s or C	
Current density	current / area	$A m^{-2}$	
Magnetic induction	force / (current \times length)	$N\ A^{-1}\ m^{-1}$ or tesla	
Force constant	force / displacement	N m ⁻¹	
Plank's constant	energy of photon / frequency	Js	
Specific heat (S)	heat energy / (mass × temperature)	J kg ⁻¹ K ⁻¹	
Boltzmann constant (k)	energy/temperature	J K ⁻¹	





 π radian = 180°

1 radian =
$$\frac{180^{\circ}}{\pi} = \frac{180^{\circ} \times 7}{22} = 57.27^{\circ}$$

Also, 1° (degree of arc) = 60' (minute of arc) and 1' (minute of arc) = 60'' (seconds of arc)

Relations between radian, degree and minutes:

$$1^{\circ} = \frac{\pi}{180} \text{ rad} = 1.745 \times 10^{-2} \text{ rad}$$

$$\therefore 1' = \frac{1^{\circ}}{60} = \frac{1.745 \times 10^{-2}}{60} = 2.908 \times 10^{-4} rad$$
$$\approx 2.91 \times 10^{-4} rad$$

$$\therefore 1'' = \frac{1^{\circ}}{3600} = \frac{1.745 \times 10^{-2}}{3600} = 4.847 \times 10^{-6} rad$$

$$\approx 4.85 \times 10^{-6} rad$$

1.5

MEASUREMENT OF BASIC QUANTITIES

1.5.1 Measurement of length

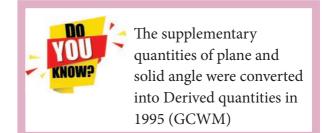
The concept of length in physics is related to the concept of distance in everyday life. Length is defined as the distance between any two points in space. The SI unit of length is metre. The objects of our interest vary widely in sizes. For example, large objects like the galaxy, stars, Sun, Earth, Moon etc., and their distances constitute a *macrocosm*. It refers to a large world,

The Radian (rad): One radian is the angle subtended at the centre of a circle by an arc equal in length to the radius of the circle.

The Steradian (sr): One steradian is the solid angle subtended at the centre of a sphere, by that surface of the sphere, which is equal in area, to the square of radius of the sphere

in which both objects and distances are large. On the contrary, objects like molecules, atoms, proton, neutron, electron, bacteria etc., and their distances constitute *microcosm*, which means a small world in which both objects and distances are small-sized.

Distances ranging from 10^{-5} m to 10^{2} m can be measured by direct methods. For example, a metre scale can be used to measure the distance from $10^{-3}\,\mathrm{m}$ to 1 m, vernier calipers up to 10⁻⁴ m, a screw gauge up to 10^{-5} m and so on. The atomic and astronomical distances cannot be measured by any of the above mentioned direct methods. Hence, to measure the very small and the very large distances, indirect methods have to be devised and used. In Table 1.4, a list of powers of 10 (both positive and negative powers) is given. Prefixes for each power are also mentioned. These prefixes are used along with units of length, and of mass.



UNIT 1 NATURE OF PHYSICAL WORLD AND MEASUREMENT

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Table 1.4 P	refixes for Pov	vers of Ten			
Multiple	Prefix	Symbol	Sub multiple	Prefix	Symbol
10^{1}	deca	da	10^{-1}	deci	d
10^{2}	hecto	h	10^{-2}	centi	С
10^{3}	kilo	k	10^{-3}	milli	m
10^{6}	mega	M	10^{-6}	micro	μ
10^{9}	giga	G	10^{-9}	nano	n
10^{12}	tera	T	10^{-12}	pico	p
10^{15}	peta	P	10^{-15}	femto	f
10^{18}	exa	E	10^{-18}	atto	a
10^{21}	zetta	Z	10^{-21}	zepto	Z
10^{24}	yotta	Y	10^{-24}	yocto	у

i) Measurement of small distances: screw gauge and vernier caliper

Screw gauge: The screw gauge is an instrument used for measuring accurately the dimensions of objects up to a maximum of about 50 mm. The principle of the instrument is the magnification of linear motion using the circular motion of a screw. The least count of the screw gauge is 0.01 mm *Vernier caliper:* A vernier caliper is a versatile instrument for measuring the dimensions of an object namely diameter of a hole, or a depth of a hole. The least count of the vernier caliper is 0.01 cm

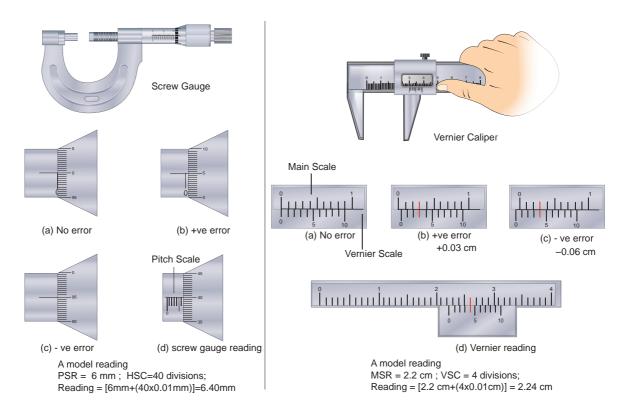


Figure 1.2 Screw gauge and vernier caliper with errors



For measuring larger distances such as the height of a tree, distance of the Moon or a planet from the Earth, some special methods are adopted. Triangulation method, parallax method and radar method are used to determine very large distances.

Triangulation method for the height of an accessible object

Let AB = h be the height of the tree or tower to be measured. Let C be the point of observation at distance x from B. Place a range finder at C and measure the angle of elevation, $\angle ACB = \theta$ as shown in Figure 1.3.

From right angled triangle ABC, $\tan \theta = \frac{AB}{BC} = \frac{h}{x}$

(or)

height
$$h = x \tan \theta$$

Knowing the distance *x*, the height h can be determined.

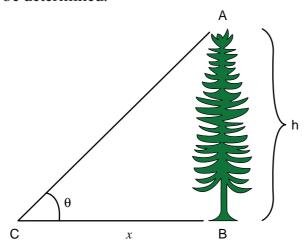


Figure 1.3 Triangulation method

Range and order of lengths of various objects are listed in Table 1.5

EXAMPLE 1.1

From a point on the ground, the top of a tree is seen to have an angle of elevation 60° . The distance between the tree and a point is 50 m. Calculate the height of the tree?

Solution

Angle
$$\theta = 60^{\circ}$$

The distance between the tree and a point x = 50 m

Height of the tree (h) = ?

For triangulation method tan $\theta = \frac{h}{x}$

$$h = x \tan \theta$$
$$= 50 \times \tan 60^{\circ}$$
$$= 50 \times 1.732$$
$$h = 86.6 \text{ m}$$

The height of the tree is 86.6 m.

Parallax method

Very large distances, such as the distance of a planet or a star from the Earth can be measured by the parallax method. *Parallax is the name given to the apparent change in the position of an object with respect to the background, when the object is seen from two different positions*. The distance between the two positions (i.e., points of observation) is called the basis (b). Consider any object at the location O (Figure 1.4)

Let L and R represent the positions of the left and right eyes of the observer respectively.

The object (O) is viewed with the left eye (L) keeping the right eye closed and the same object (O) is viewed with the right eye (R) keeping the left eye closed.

In Figure 1.4, LO and RO are the lines drawn from the positions of the left and right eyes to the object. These two lines make an angle θ at O. This angle θ is called the angle of parallax.

OL and OR are considered as the radii (x) of a circle. For astronomical calculation, the distance LR = b (basis) can be treated as an arc of this circle, then

$$OL = OR = x$$

as LR = b

$$\theta = \frac{b}{x}$$

Knowing b and θ , x can be calculated which is approximately the distance of the object from the observer.

If the object is the Moon or any near by star, then the angle θ will be too small due to the large astronomical distance and the place of observation. In this case, the two points of observation should be sufficiently spaced on the surface of the Earth.

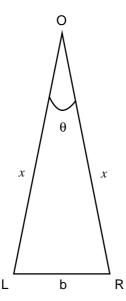


Figure 1.4 Parallax method

Determination of distance of Moon from Earth

In Figure 1.5, C is the centre of the Earth. A and B are two diametrically opposite

places on the surface of the Earth. From A and B, the parallaxes θ_1 and θ_2 respectively of Moon M with respect to some distant star are determined with the help of an astronomical telescope. Thus, the total parallax of the Moon subtended on Earth $\angle AMB = \theta_1 + \theta_2 = \theta$.

If θ is measured in radians, then $\theta = \frac{AB}{AM}$; AM \approx MC (AM is approximately equal to MC)

$$\theta = \frac{AB}{MC}$$
 or $MC = \frac{AB}{\theta}$; Knowing the values of AB and θ , we can calculate the

values of AB and θ , we can calculate the distance MC of Moon from the Earth.

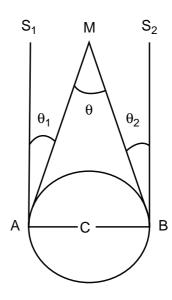


Figure 1.5 Parallax method: determination of distance of Moon from Earth

EXAMPLE 1.2

The Moon subtends an angle of 1° 55' at the base line equal to the diameter of the Earth. What is the distance of the Moon from the Earth? (Radius of the Earth is $6.4 \times 10^6 m$)

14

UNIT 1 NATURE OF PHYSICAL WORLD AND MEASUREMENT

Solution

angle
$$\theta = 1^{\circ} 55' = 115'$$

= $(115 \times 60)'' \times (4.85 \times 10^{-6})$ rad
= 3.34×10^{-2} rad
since $1'' = 4.85 \times 10^{-6}$ rad

Radius of the Earth = $6.4 \times 10^6 m$ From the Figure 1.5, AB is the diameter of the Earth (b)= $2 \times 6.4 \times 10^6 m$ Distance of the Moon from the Earth x = ?

$$x = \frac{b}{\theta} = \frac{2 \times 6.4 \times 10^6}{3.34 \times 10^{-2}}$$
$$x = 3.83 \times 10^8 \text{m}$$

RADAR method

The word RADAR stands for radio detection and ranging. A radar can be used to measure accurately the distance of a nearby planet such as Mars. In this method, radio waves are sent from transmitters which, after reflection from the planet, are detected by the receiver. By measuring, the time interval (t) between the instants the radio waves are sent and received, the distance of the planet can be determined as

Speed = distance travelled / time taken
(Speed is explained in unit 2)
Distance(d) = Speed of radio
waves × time taken

$$d = \frac{v \times t}{2}$$

where v is the speed of the radio wave. As the time taken (t) is for the distance covered during the forward and backward path of the radio waves, it is divided by 2 to get the actual distance of the object. This method can also be used to determine the height, at which an aeroplane flies from the ground.

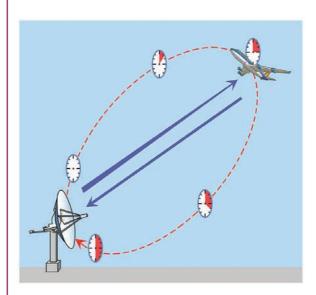


Figure 1.6 RADAR method

EXAMPLE 1.3

A RADAR signal is beamed towards a planet and its echo is received 7 minutes later. If the distance between the planet and the Earth is 6.3×10^{10} m. Calculate the speed of the signal?

Solution

The distance of the planet from the Earth $d = 6.3 \times 10^{10} \text{ m}$

Time
$$t = 7$$
 minutes $= 7 \times 60$ s.
the speed of signal $v = ?$

The speed of signal

$$v = \frac{2d}{t} = \frac{2 \times 6.3 \times 10^{10}}{7 \times 60} = 3 \times 10^8 \, \text{ms}^{-1}$$



Table 1.5 Range and Order of Lengths	
Size of objects and distances	Length (m)
Distance to the boundary of observable	10^{26}
universe	
Distance to the Andromeda galaxy	10^{22}
Size of our galaxy	10^{21}
Distance from Earth to the nearest star	10^{16}
(other than the Sun)	
Average radius of Pluto's orbit	10^{12}
Distance of the Sun from the Earth	10^{11}
Distance of Moon from the Earth	10^{8}
Radius of the Earth	10^{7}
Height of the Mount Everest above sea level	10^4
Length of a football field	10^{2}
Thickness of a paper	10^{-4}
Diameter of a red blood cell	10^{-5}
Wavelength of light	10^{-7}
Length of typical virus	10^{-8}
Diameter of the hydrogen atom	10^{-10}
Size of atomic nucleus	10^{-14}
Diameter of a proton	10^{-15}

Some Common Practical Units

- (i) Fermi = $1 \text{ fm} = 10^{-15} \text{ m}$
- (ii) 1 angstrom = $1 \text{ Å} = 10^{-10} \text{ m}$
- (iii) 1 nanometer = $1 \text{ nm} = 10^{-9} \text{ m}$
- (iv) 1 micron = $1 \mu m = 10^{-6} m$
- (v) 1 Light year (Distance travelled by light in vacuum in one year) 1 Light Year = 9.467×10^{15} m
- (vi) 1 astronomical unit (the mean distance of the Earth from the Sun) $1 \text{ AU} = 1.496 \times 10^{11} \text{ m}$
- (vii) 1 parsec (Parallactic second) (Distance at which an arc of length 1 AU subtends an angle of 1 second of arc)
 1 parsec = 3.08 × 10¹⁶ m = 3.26 light year

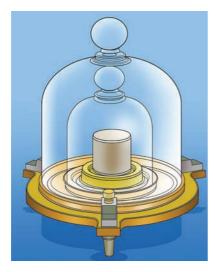


Figure 1.7 The international 1 kg standard of mass, a platinum-iridium (9:1) cylinder 3.9 cm in height and diameter.



Why is the cylinder used in defining kilogram made up of platinum-iridium alloy?

This is because the platinum-iridium alloy is least affected by environment and time.

Chandrasekhar Limit (CSL) is the largest practical unit of mass.

1 CSL = 1.4 times the mass of the Sun

The smallest practical unit of time is Shake.

 $1 \text{ Shake} = 10^{-8} \text{ s}$





Mass is a property of matter. It does not depend on temperature, pressure and location of the body in space. Mass of a body is defined as the quantity of matter contained in a body. The SI unit of mass is kilogram (kg). The masses of objects which we shall study in this course vary over a wide range. These may vary from a tiny mass of electron $(9.11 \times 10^{-31} \text{kg})$ to the huge mass of the known universe $(=10^{55} \text{kg})$. The order of masses of various objects is shown in Table 1.6.

Ordinarily, the mass of an object is determined in kilograms using a common balance like the one used in a grocery shop. For measuring larger masses like

Table 1.6 Range of masses			
Object	Order of mass (kg)		
Electron	10^{-30}		
Proton or Neutron	10^{-27}		
Uranium atom	10^{-25}		
Red blood corpuscle	10^{-14}		
A cell	10^{-10}		
Dust particle	10^{-9}		
Raindrop	10^{-6}		
Mosquito	10^{-5}		
Grape	10^{-3}		
Frog	10^{-1}		
Human	10^{2}		
Car	10^{3}		
Ship	10^{5}		
Moon	10^{23}		
Earth	10^{25}		
Sun	10^{30}		
Milky way	10^{41}		
Observable Universe	10 ⁵⁵		

that of planets, stars etc., we make use of gravitational methods. For measurement of small masses of atomic/subatomic particles etc., we make use of a mass spectrograph.

Some of the weighing balances commonly used are common balance, spring balance, electronic balance, etc.

1.5.3 Measurement of Time intervals

"Time flows uniformly forward"

– Sir Issac Newton

"Time is what a clock reads"

– Albert Einstein

A clock is used to measure the time interval. An atomic standard of time, is based on the periodic vibration produced in a Cesium atom. Some of the clocks developed later are electric oscillators, electronic oscillators, solar clock, quartz crystal clock, atomic clock, decay of elementary particles, radioactive dating etc. The order of time intervals are tabulated in Table 1.7.

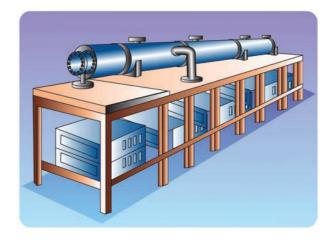


Figure 1.8 The atomic clock, which keeps time on the basis of radiation from cesium atoms is accurate to about three millionths of a second per year.

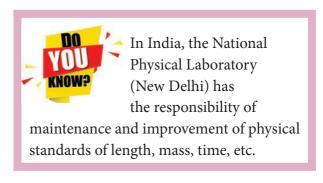


Table 1.7 Order of Time Intervals	
Event	Order of time interval (s)
Lifespan of the most unstable particle	10^{-24}
Time taken by light to cross a distance of nuclear size	10^{-22}
Period of X-rays	10^{-19}
Time period of electron in hydrogen atom	10^{-15}
Period of visible light waves	10^{-15}
Time taken by visible light to cross through a window pane	10^{-8}
Lifetime of an excited state of an atom	10^{-8}
Period of radio waves	10^{-6}
Time period of audible sound waves	10^{-3}
Wink of an eye	10^{-1}
Time interval between two successive heart beats	10^{0}
Travel time of light from Moon to Earth	10^{0}
Travel time of light from Sun to Earth	10^{2}
Halflife time of a free neutron	10^{3}
Time period of a satellite	10^4
Time period of rotation of Earth around its axis (one day)	105
Time period of revolution of Earth around the Sun (one year)	10^{7}
Average life of a human being	10^{9}
Age of Egyptian pyramids	10^{11}
Age of Universe	10^{17}

1.6

THEORY OF ERRORS

The foundation of all experimental science and technology is measurement. The result obtained from any measurement will contain some uncertainty. Such an uncertainty is termed *error*. Any calculation made using the measured values will also have an error. It is not possible to make exact measurements in an experiment. In measurements, two different terms, accuracy and precision are used and need



to be distinguished at this stage. Accuracy refers to how far we are from the true value, and precision refers to how well we measure.



1.6.1 Accuracy and Precision

Let us say, you know your true height is exactly 5'9". You first measure your height with a yardstick and get the value 5'0". Your measurement is hence not accurate. Now you measure your height with a laser yardstick and get 5'9" as the value. Now your measurement is accurate. The true value is also called theoretical value. The level of accuracy required for each application varies greatly. Highly accurate data can be very difficult to produce and compile. For example, if you consistently measure your height as 5'0" with a yard stick, your measurements are precise. The level of precision required for different applications vary to a great extent. Engineering projects such as road and utility construction require very precise information measured to the millimeter or one-tenth of an inch.

If a measurement is precise, that does not necessarily mean that it is accurate. However, if the measurement is consistently accurate, it is also precise.

For example, if the temperature outside a building is 40°C as measured by a weather thermometer and if the real outside

temperature is 40°C, the thermometer is accurate. If the thermometer consistently registers this exact temperature in a row, the thermometer is precise.

Consider another example. Let the temperature of a refrigerator repeatedly measured by a thermometer be given as 10.4°C, 10.2°C, 10.3°C, 10.1°C, 10.2°C, 10.1°C, 10.1°C. However, if the real temperature inside the refrigerator is 9°C, we say that the thermometer is not accurate (it is almost one degree off the true value), but since all the measured values are close to 10°C, hence it is precise.

A visual example:

Target shooting is an example which explains the difference between accuracy and precision. In Figure 1.9 (a), the shots are focused so as to reach the bull's eye (midpoint), but the arrows have reached only around this point. Hence the shots are not accurate and also not precise.

In Figure 1.9 (b), all the shots are close to each other but not at the central point. Hence the shots are said to be precise but not accurate. In Figure 1.9 (c), the shots are closer and also at the central point. Hence the shots are both precise and accurate.

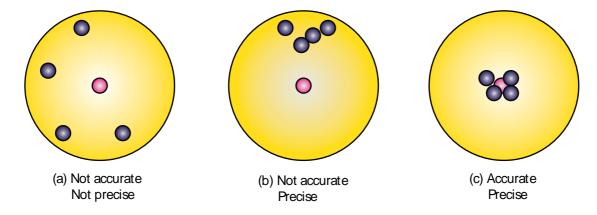


Figure 1.9 Visual example of accuracy and precision





A numerical example

The true value of a certain length is nearly 5.678 cm. In one experiment, using a measuring instrument of resolution 0.1 cm, the measured value is found to be 5.5 cm. In another experiment using a measuring instrument of greater resolution, say 0.01 cm, the length is found to be 5.38 cm. We find that the first measurement is more accurate as it is closer to the true value, but it has lesser precision. On the contrary, the second measurement is less accurate, but it is more precise.

1.6.2 Errors in Measurement

The uncertainty in a measurement is called an error. Random error, systematic error and gross error are the three possible errors.

i) Systematic errors

Systematic errors are reproducible inaccuracies that are consistently in the same direction. These occur often due to a problem that persists throughout the experiment. Systematic errors can be classified as follows

1) Instrumental errors

When an instrument is not calibrated properly at the time of manufacture, instrumental errors may arise. If a measurement is made with a meter scale whose end is worn out, the result obtained will have errors. These errors can be corrected by choosing the instrument carefully.

2) Imperfections in experimental technique or procedure

These errors arise due to the limitations in the experimental arrangement. As an example, while

performing experiments with a calorimeter, if there is no proper insulation, there will be radiation losses. This results in errors and to overcome these, necessary correction has to be applied.

3) Personal errors

These errors are due to individuals performing the experiment, may be due to incorrect initial setting up of the experiment or carelessness of the individual making the observation due to improper precautions.

4) Errors due to external causes

The change in the external conditions during an experiment can cause error in measurement. For example, changes in temperature, humidity, or pressure during measurements may affect the result of the measurement.

5) Least count error

Least count is the smallest value that can be measured by the measuring instrument, and the error due to this measurement is least count error. The instrument's resolution hence is the cause of this error. Least count error can be reduced by using a high precision instrument for the measurement.

ii) Random errors

Random errors may arise due to random and unpredictable variations in experimental conditions like pressure, temperature, voltage supply etc. Errors may also be due to personal errors by the observer who performs the experiment. Random errors are sometimes called "chance error". When different readings are obtained by a person every time he



UNIT 1 NATURE OF PHYSICAL WORLD AND MEASUREMENT



repeats the experiment, personal error occurs. For example, consider the case of the thickness of a wire measured using a screw gauge. The readings taken may be different for different trials. In this case, a large number of measurements are made and then the arithmetic mean is taken.

$$a_m = \frac{a_1 + a_2 + a_3 + \dots a_n}{n} \quad (1.1)$$

or

$$a_m = \frac{1}{n} \sum_{i=1}^n a_i$$
 (1.2)

Usually this arithmetic mean is taken as the best possible true value of the quantity.

Certain procedures to be followed to minimize experimental errors, along with examples are shown in Table 1.8.

iii) Gross Error

The error caused due to the shear carelessness of an observer is called gross error.

For example

- (i) Reading an instrument without setting it properly.
- (ii) Taking observations in a wrong manner without bothering about the sources of errors and the precautions.
- (iii) Recording wrong observations.
- (iv) Using wrong values of the observations in calculations.

These errors can be minimized only when an observer is careful and mentally alert.

Table 1.8 Minimizing Experimental Error				
Type of error	Example	How to minimize it		
Random error	Suppose you measure the mass of a ring three times using the same balance and get slightly different values. 15.46 g, 15.42 g, 15.44 g	Take more data. Random errors can be evaluated through statistical analysis and can be reduced by averaging over a large number of observations.		
Systematic error	Suppose the cloth tape measure that you use to measure the length of an object has been stretched out from years of use. (As a result all of the length measurements are not correct).	Systematic errors are difficult to detect and cannot be analysed statistically, because all of the data is in the same direction. (Either too high or too low)		



i) Absolute Error

The magnitude of difference between the true value and the measured value of a quantity is called absolute error. If a_1 , a_2 , a_3 , a_n are the measured values of any quantity 'a' in an experiment performed n times, then the arithmetic mean of these values is called the true value (a_m) of the quantity.

$$a_m = \frac{a_1 + a_2 + a_3 + \dots + a_n}{n}$$
 or $a_m = \frac{1}{n} \sum_{i=1}^n a_i$

The absolute error in measured values is given by

$$|\Delta a_1| = |a_m - a_1|$$

$$|\Delta a_2| = |a_m - a_2|$$

$$\dots$$

$$|\Delta a_n| = |a_m - a_n|$$

ii) Mean Absolute error

The arithmetic mean of absolute errors in all the measurements is called the mean absolute error.

$$\Delta a_m = \frac{\left|\Delta a_1\right| + \left|\Delta a_2\right| + \left|\Delta a_3\right| + \dots + \left|\Delta a_n\right|}{n}$$

$$or = \frac{1}{n} \sum_{i=1}^n \left|\Delta a_i\right|$$

If $a_{\rm m}$ is the true value and $\Delta a_{\rm m}$ is the mean absolute error then the magnitude of the quantity may lie between $a_{\rm m}$ + $\Delta a_{\rm m}$ and $a_{\rm m}$ - $\Delta a_{\rm m}$

iii) Relative error

The ratio of the mean absolute error to the mean value is called relative error. This is also called as fractional error. Thus

Relative error =
$$\frac{Mean \ absolute \ error}{Mean \ value}$$
$$= \frac{\Delta a_m}{a_m}$$

Relative error expresses how large the absolute error is compared to the total size of the object measured. For example, a driver's speedometer shows that his car is travelling at 60 km h⁻¹ when it is actually moving at 62 km h⁻¹. Then absolute error of speedometer is $62-60 \text{ km h}^{-1} = 2 \text{ km h}^{-1}$ Relative error of the measurement is $2 \text{ km h}^{-1} / 60 \text{ km h}^{-1} = 0.033$.

iv) Percentage error

The relative error expressed as a percentage is called percentage error.

Percentage error =
$$\frac{\Delta a_m}{a_m} \times 100\%$$

A percentage error very close to zero means one is close to the targeted value, which is good and acceptable. It is always necessary to understand whether error is due to impression of equipment used or a mistake in the experimentation.

EXAMPLE 1.4

In a series of successive measurements in an experiment, the readings of the period of oscillation of a simple pendulum were found to be 2.63s, 2.56 s, 2.42s, 2.71s and 2.80s. Calculate (i) the mean value of the period of oscillation (ii) the absolute error in each measurement (iii) the mean absolute error (iv) the relative error (v) the percentage error. Express the result in proper form.

Solution

$$t_1 = 2.63 \, s, t_2 = 2.56 \, s, t_3 = 2.42 \, s,$$

 $t_4 = 2.71 \, s, t_5 = 2.80 \, s$

(i)
$$T_{m} = \frac{t_{1} + t_{2} + t_{3} + t_{4} + t_{5}}{5}$$

$$= \frac{2.63 + 2.56 + 2.42 + 2.71 + 2.80}{5}$$

$$T_{m} = \frac{13.12}{5} = 2.624s$$

$$T_{m} = 2.62s \quad \text{(Rounded off to 2}^{\text{nd}}$$

$$\text{decimal place)}$$

(ii) Absolute error $|\Delta T| = |T_m - t|$

$$\begin{aligned} |\Delta T_1| &= |2.62 - 2.63| = +0.01s \\ |\Delta T_2| &= |2.62 - 2.56| = +0.06s \\ |\Delta T_3| &= |2.62 - 2.42| = +0.20s \\ |\Delta T_4| &= |2.62 - 2.71| = +0.09s \\ |\Delta T_5| &= |2.62 - 2.80| = +0.18s \end{aligned}$$

(iii) Mean absolute error = $\frac{\sum |\Delta T_i|}{n}$

$$\Delta T_m = \frac{0.01 + 0.06 + 0.20 + 0.09 + 0.18}{5}$$

$$\Delta T_m = \frac{0.54}{5} = 0.108s = 0.11s \quad (Rounded)$$
off to 2nd decimal place)

(iv) Relative error:

$$S_{T} = \frac{\Delta T_{m}}{T_{m}} = \frac{0.11}{2.62} = 0.0 419$$

 $S_{T} = 0.04$

- (v) Percentage error in T = 0.04 $\times 100\% = 4\%$
- (vi) Time period of simple pendulum = $T = (2.62 \pm 0.11)s$

1.6.4 Propagation of errors

A number of measured quantities may be involved in the final calculation of an experiment. Different types of instruments might have been used for taking readings. Then we may have to look at the errors in measuring various quantities, collectively.

The error in the final result depends on

- (i) The errors in the individual measurements
- (ii) On the nature of mathematical operations performed to get the final result. So we should know the rules to combine the errors.

The various possibilities of the propagation or combination of errors in different mathematical operations are discussed below:

(i) Error in the sum of two quantities

Let ΔA and ΔB be the absolute errors in the two quantities A and B respectively. Then,

Measured value of $A = A \pm \Delta A$ Measured value of $B = B \pm \Delta B$ Consider the sum, Z = A + B

(

$$Z \pm \Delta Z = (A \pm \Delta A) + (B \pm \Delta B)$$

$$= (A + B) \pm (\Delta A + \Delta B)$$

$$= Z \pm (\Delta A + \Delta B)$$
(or)
$$\Delta Z = \Delta A + \Delta B$$
 (1.3)

The maximum possible error in the sum of two quantities is equal to the sum of the absolute errors in the individual quantities.

EXAMPLE 1.5

Two resistances $R_1 = (100 \pm 3) \Omega$, $R_2 = (150 \pm 2) \Omega$, are connected in series. What is their equivalent resistance?

Solution

$$R_1 = 100 \pm 3\Omega; R_2 = 150 \pm 2\Omega$$

Equivalent resistance R = ?Equivalent resistance $R = R_1 + R_2$

$$= (100 \pm 3) + (150 \pm 2)$$
$$= (100 + 150) \pm (3 + 2)$$
$$R = (250 \pm 5) \Omega$$

(ii) Error in the difference of two quantities

Let ΔA and ΔB be the absolute errors in the two quantities, A and B, respectively. Then,

Measured value of $A = A + \Delta A$

Measured value of $A = A \pm \Delta A$ Measured value of $B = B \pm \Delta B$ Consider the difference, Z = A - BThe error ΔZ in Z is then given by $Z \pm \Delta Z = (A \pm \Delta A) - (B \pm \Delta B)$

$$= (A - B)) \pm \Delta A \mp \Delta B$$

$$= Z \pm \Delta A \mp \Delta B$$
(or) $\Delta Z = \Delta A + \Delta B$(1.4)

The maximum error in difference of two quantities is equal to the sum of the absolute errors in the individual quantities.

EXAMPLE 1.6

The temperatures of two bodies measured by a thermometer are $t_1 = (20 + 0.5)^{\circ}$ C, $t_2 = (50 \pm 0.5)^{\circ}$ C. Calculate the temperature difference and the error therein.

Solution

$$t_1 = (20 \pm 0.5)^{\circ}C$$
 $t_2 = (50 \pm 0.5)^{\circ}C$

temperature difference t=?

$$t = t_2 - t_1 = (50 \pm 0.5) - (20 \pm 0.5)$$
°C
(Using equation 1.4)

$$= (50 - 20) \pm (0.5 + 0.5)$$

$$t = (30 \pm 1)^{\circ}C$$

(iii) Error in the product of two quantities

Let ΔA and ΔB be the absolute errors in the two quantities A, and B, respectively. Consider the product Z = AB

The error ΔZ in Z is given by $Z \pm \Delta Z = (A \pm \Delta A) (B \pm \Delta B)$

$$= (AB) \pm (A \Delta B) \pm (B \Delta A) \pm (\Delta A \cdot \Delta B)$$

Dividing L.H.S by Z and R.H.S by AB, we get,

$$1 \pm \frac{\Delta Z}{Z} = 1 \pm \frac{\Delta B}{B} \pm \frac{\Delta A}{A} \pm \frac{\Delta A}{A} \cdot \frac{\Delta B}{B}$$

$$\frac{\Delta Z}{Z} = \pm \left(\frac{\Delta A}{A} + \frac{\Delta B}{B}\right) \tag{1.5}$$

The maximum fractional error in the product of two quantities is equal to the sum of the fractional errors in the individual quantities.

[Alternative method is given in Appendix A1.2]

EXAMPLE 1.7

The length and breadth of a rectangle are (5.7 ± 0.1) cm and (3.4 ± 0.2) cm respectively. Calculate the area of the rectangle with error limits.

Solutions

Length
$$\ell = (5.7 \pm 0.1) \text{ cm}$$

Breadth b = (3.4 ± 0.2) cm

Area A with error limit = A $\pm \Delta A$ = ?

Area A =
$$\ell \times b = 5.7 \times 3.4 = 19.38 = 19.4 \text{ cm}^2$$

$$\frac{\Delta A}{A} = \frac{\Delta l}{l} + \frac{\Delta b}{b}$$
$$\Delta A = \left(\frac{\Delta l}{l} + \frac{\Delta b}{b}\right) A$$

$$\Delta A = \left(\frac{0.1}{5.7} + \frac{0.2}{3.4}\right) 19.4$$

 $= (0.0175 + 0.0588) \times 19.4$

= 1.48 = 1.5

Area with error limit

$$A = (19.4 \pm 1.5) \text{ cm}^2$$

(iv) Error in the division or quotient of two quantities

Let ΔA and ΔB be the absolute errors in the two quantities A and B respectively.

Consider the quotient, $Z = \frac{A}{B}$

The error ΔZ in Z is given by

$$Z \pm \Delta Z = \frac{A \pm \Delta A}{B \pm \Delta B} = \frac{A \left(1 \pm \frac{\Delta A}{A}\right)}{B \left(1 \pm \frac{\Delta B}{B}\right)}$$
$$= \frac{A}{B} \left(1 \pm \frac{\Delta A}{A}\right) \left(1 \pm \frac{\Delta B}{B}\right)^{-1}$$

or
$$Z \pm \Delta Z = Z \left(1 \pm \frac{\Delta A}{A} \right) \left(1 \mp \frac{\Delta B}{B} \right)$$
 [using

 $(1+x)^n \approx 1+nx$, when x<<1]

Dividing both sides by Z, we get,

$$1 \pm \frac{\Delta Z}{Z} = \left(1 \pm \frac{\Delta A}{A}\right) \left(1 \mp \frac{\Delta B}{B}\right)$$
$$= 1 \pm \frac{\Delta A}{A} \mp \frac{\Delta B}{B} \pm \frac{\Delta A}{A} \cdot \frac{\Delta B}{B}$$

As the terms $\Delta A/A$ and $\Delta B/B$ are small, their product term can be neglected.

The maximum fractional error in Z is

given by
$$\frac{\Delta Z}{Z} = \left(\frac{\Delta A}{A} + \frac{\Delta B}{B}\right)$$
 (1.6)

The maximum fractional error in the quotient of two quantities is equal to the sum of their individual fractional errors.

(Alternative method is given in Appendix A1.2)

EXAMPLE 1.8

The voltage across a wire is (100 ± 5) V and the current passing through it is (10 ± 0.2) A. Find the resistance of the wire.

Solution

Voltage
$$V = (100\pm5)V$$

Current I =
$$(10\pm0.2)$$
 A

Resistance R = ?

Then resistance R is given by Ohm's law, $R = \frac{V}{I}$

$$=\frac{100}{10}=10\Omega$$

$$\frac{\Delta R}{R} = \left(\frac{\Delta V}{V} + \frac{\Delta I}{I}\right)$$

$$\Delta R = \left(\frac{\Delta V}{V} + \frac{\Delta I}{I}\right) R$$

$$= \left(\frac{5}{100} + \frac{0.2}{10}\right) 10$$

$$=(0.05+0.02)10$$

$$= 0.07 \times 10 = 0.7$$

The resistance $R = (10 \pm 0.7)\Omega$

(v) Error in the power of a quantity Consider the nth power of A, $Z = A^n$ The error ΔZ in Z is given by

$$Z \pm \Delta Z = (A \pm \Delta A)^{n} = A^{n} \left(1 \pm \frac{\Delta A}{A} \right)^{n}$$
$$= Z \left(1 \pm n \frac{\Delta A}{A} \right)$$

We get $[(1+x)^n \approx 1+nx$, when x << 1] neglecting remaining terms, Dividing both sides by Z

$$1 \pm \frac{\Delta Z}{Z} = 1 \pm n \frac{\Delta A}{A} \text{ or}$$

$$\frac{\Delta Z}{Z} = n \cdot \frac{\Delta A}{A}$$
(1.7)

(h

The fractional error in the nth power of a quantity is n times the fractional error in that quantity.

General rule: If $Z = \frac{A^p B^q}{C^r}$ Then

maximum fractional error in Z is

given by
$$\frac{\Delta Z}{Z} = p \frac{\Delta A}{A} + q \frac{\Delta B}{B} + r \frac{\Delta C}{C}$$

The percentage error in Z is given by

$$\frac{\Delta Z}{Z} \times 100 = p \frac{\Delta A}{A} \times 100 + q \frac{\Delta B}{B} \times 100$$
$$+ r \frac{\Delta C}{C} \times 100$$

EXAMPLE 1.9

A physical quantity x is given by $x = \frac{a^2b^3}{c\sqrt{d}}$. If the percentage errors of measurement in a, b, c and d are 4%, 2%, 3% and 1% respectively, then calculate the percentage error in the calculation of x. (NEET 2013)

Solution

Given
$$x = \frac{a^2b^3}{c\sqrt{d}}$$

The percentage error in x is given by

$$\frac{\Delta x}{x} \times 100 = 2\frac{\Delta a}{a} \times 100 + 3\frac{\Delta b}{b} \times 100$$
$$+ \frac{\Delta c}{c} \times 100 + \frac{1}{2}\frac{\Delta d}{d} \times 100$$

$$= (2 \times 4\%) + (3 \times 2\%) + (1 \times 3\%) + (\frac{1}{2} \times 1\%)$$

The percentage error is x = 17.5%

1.7

SIGNIFICANT FIGURES

1.7.1 Definition and Rules of Significant Figures

Suppose we ask three students to measure the length of a stick using metre scale (the least count for metre scale is 1 mm or 0.1 cm). So, the result of the measurement (length of stick) can be any of the following, 7.20 cm or 7.22 cm or 7.23 cm. Note that all the three students measured first two digits correctly (with confidence) but last digit varies from person to person. So, the number of meaningful digits is 3 which communicate both measurement (quantitative) and also the precision of the instrument used. Therefore, significant number or significant digit is 3. It is defined as the number of meaningful digits which contain numbers that are known reliably and first uncertain number.

Examples: The significant figure for the digit 121.23 is 5, significant figure for the digit 1.2 is 2, significant figure for the digit 0.123 is 3, significant digit for 0.1230 is 4, significant digit for 0.0123 is 3, significant

digit for 1230 is 3, significant digit for 1230 (with decimal) is 4 and significant digit for 200000000 is 1 (because 20000000= 2×10^7 has only one significant digit, that is, 2).

In physical measurement, if the length of an object is l = 1230 m, then significant digit for l is 4.

The rules for counting significant figures are given in Table 1.9.

EXAMPLE 1.10

State the number of significant figures in the following

- i) 600800
- iv) 5213.0

ii) 400

v) $2.65 \times 10^{24} m$

iii) 0.007

vi) 0.0006032

Solution: i) four ii) one iii) one

iv) five v) three vi) four

1.7.2 Rounding Off

Calculators are widely used now-a-days to do calculations. The result given by a calculator has too many figures. In no case should the result have more significant figures than the figures involved in the data used for calculation. The result of calculation with numbers containing more than one uncertain digit should be rounded off. The rules for rounding off are shown in Table 1.10.

EXAMPLE 1.11

Round off the following numbers as indicated

- i) 18.35 up to 3 digits
- ii) 19.45 up to 3 digits
- iii) 101.55×10^6 up to 4 digits
- iv) 248337 up to digits 3 digits
- v) 12.653 up to 3 digits.

UNIT 1 NATURE OF PHYSICAL WORLD AND MEASUREMENT



ant figures
Example
1342 has four significant figures
are significant 2008 has four significant figures
digit but 30700. has five significant figures
nificant.
al point, the a) 30700 has three significant figures
ot significant.
b) 30700 m has five significant figures
o (s) on the 0.00345 has three significant figures
of the first
oint and 40.00 has four significant figures and
nificant. 0.030400 has five significant figures
nes not 1.53 cm, 0.0153 m, 0.0000153 km,
all have three significant figures

Note: 1 Multiplying or dividing factors, which are neither rounded numbers nor numbers representing measured values, are exact and they have infinite numbers of significant figures as per the situation. For **example,** circumference of circle $S = 2\pi r$, Here the factor 2 is exact number. It can be written as 2.0, 2.00 or 2.000 as required.

Note: 2 The power of 10 is irrelevant to the determination of significant figures.

For **example** $x = 5.70 \text{ m} = 5.70 \times 10^2 \text{ cm} = 5.70 \times 10^3 \text{ mm} = 5.70 \times 10^{-3} \text{ km}$.

In each case the number of significant figures is three.

Table 1.10	Rules for Rounding C)ff
	raico foi ficalianing	711

Ruie	Examp
i) If the digit to be dropped is smaller than 5, then	i) 7.3
the preceding digit should be left unchanged.	ii) 8.9

- ii) If the digit to be dropped is greater than 5, then the preceding digit should be increased by 1
- iii) If the digit to be dropped is 5 followed by digits other than zero, then the preceding digit should be raised by 1
- iv) If the digit to be dropped is 5 or 5 followed by zeros, then the preceding digit is not changed if it is even
- v) If the digit to be dropped is 5 or 5 followed by zeros, then the preceding digit is raised by 1 if it is odd

Example

- i) 7.32 is rounded off to 7.3
- ii) 8.94 is rounded off to 8.9
- i) 17.26 is rounded off to 17.3
- ii) 11.89 is rounded off to 11.9
- i) 7.352, on being rounded off to first decimal becomes 7.4
- ii) 18.159 on being rounded off to first decimal, become 18.2
- i) 3.45 is rounded off to 3.4
- ii) 8.250 is rounded off to 8.2
- i) 3.35 is rounded off to 3.4
- ii) 8.350 is rounded off to 8.4





- i) 18.4 ii) 19.4 iii) 101.6×10^6
- iv) 248000
- v) 12.7

1.7.3 Arithmetical Operations with Significant Figures

(i) Addition and subtraction

In addition and subtraction, the final result should retain as many decimal places as there are in the number with the smallest number of decimal places.

Example:

1. 3.1 + 1.780 + 2.046 = 6.926

Here the least number of significant digits after the decimal is one. Hence the result will be 6.9.

2. 12.637 - 2.42 = 10.217

Here the least number of significant digits after the decimal is two. Hence the result will be 10.22

(ii) Multiplication and Division

In multiplication or division, the final result should retain as many significant figures as there are in the original number with smallest number of significant figures.

Example:

1. $1.21 \times 36.72 = 44.4312 = 44.4$

Here the least number of significant digits in the measured values is three. Hence the result when rounded off to three significant digits is 44.4

2. $36.72 \div 1.2 = 30.6 = 31$

Here the least number of significant digits in the measured values is two. Hence the result when rounded off to significant digit becomes 31.

1.8

DIMENSIONAL ANALYSIS

1.8.1 Dimension of Physical Quantities

In mechanics, we deal with the physical quantities like mass, time, length, velocity, acceleration, etc. which can be expressed in terms of three independent base quantities such as M, L and T. So, the dimension of a physical quantity can be defined as 'any physical quantity which is expressed in terms of base quantities whose exponent (power) represents the dimension of the physical quantity. The notation used to denote the dimension of a physical quantity is [(physical quantity within square bracket)]. For an example, [length] means dimension of length, [area] means dimension of area, etc. The dimension of length can be expressed in terms of base quantities as

$$[length] = M^0 LT^0 = L$$

Similarly,
$$[area] = M^0 L^2 T^0 = L^2$$

Similarly, [volume] =
$$M^0 L^3 T^0 = L^3$$

Note that in all the cases, the base quantity L is same but exponent (power) are different, which means dimensions are different. For a pure number, exponent of base quantity is zero. For example, consider the number 2, which has no dimension and can be expressed as

$$\Rightarrow$$
[2]= $M^0 L^0 T^0$ (dimensionless)

Let us write down the dimensions of a few more physical quantities.

Speed,
$$s = \frac{\text{distance}}{\text{time taken}} \Rightarrow [s] = \frac{L}{T} = LT^{-1}$$

Velocity,
$$\vec{v} = \frac{\text{displacement}}{\text{time taken}} \Rightarrow [\vec{v}] = \frac{L}{T} = LT^{-1}$$

Note that speed is a scalar quantity and velocity is a vector quantity (scalar and vector will be discussed in Unit 2) but both of them have the same dimensional formula.

Acceleration,
$$\vec{a} = \frac{\text{velocity}}{\text{time taken}} \Rightarrow [\vec{a}] = \frac{LT^{-1}}{T} = LT^{-2}$$

Acceleration is velocity per time. Linear momentum or Momentum,

$$\left[\vec{p}\right] = m\vec{v} \Rightarrow \left[\vec{p}\right] = MLT^{-1}$$

Force,
$$\vec{F} = m\vec{a} \Rightarrow [\vec{F}] = MLT^{-2} = \frac{\text{Momentum}}{\text{time}}$$

This is true for any kind of force. There are only four types of forces that exist in nature viz strong force, electromagnetic force, weak force and gravitational force. Further, frictional force, centripetal force, centrifugal force, all have the dimension MLT⁻².

Impulse,
$$\vec{I} = \vec{F}t \Rightarrow [\vec{I}] = MLT^{-1}$$

= dimension of momentum

Angular momentum is the moment of linear momentum (discussed in unit 5).

Angular Momentum, $\vec{L} = \vec{r} \times \vec{p} \Rightarrow [\vec{L}] = ML^2T^{-1}$ Work done,

$$W = \vec{F} \cdot \vec{d} \Rightarrow [W] = ML^2T^{-2}$$

Kinetic energy

$$KE = \frac{1}{2}mv^2 \Rightarrow [KE] = \left[\frac{1}{2}\right][m][v^2]$$

Since, number $\frac{1}{2}$ is dimensionless, the dimension of kinetic energy $[KE] = [m][v^2] = ML^2T^{-2}$. Similarly, to get the dimension of potential energy, let us consider the gravitational potential energy, $PE = mgh \Rightarrow [PE] = [m][g][h]$, where, m is the mass of the particle, g is the acceleration due to gravity and h is the height from the ground

level. Hence, $[PE] = [m][g][h] = ML^2T^{-2}$. Thus, for any kind of energy (such as for internal energy, total energy etc.), the dimension is

$$[Energy] = ML^2T^{-2}$$

The moment of force is known as torque, $\vec{\tau} = \vec{r} \times \vec{F} \Rightarrow [\vec{\tau}] = ML^2T^{-2}$ (Read the symbol τ as tau – Greek alphabet). Note that the dimension of torque and dimension of energy are identical but they are different physical quantities. Further one of them is a scalar (energy) and another one is a vector (torque). This means that the dimensionally same physical quantities need not be the same physical quantities.



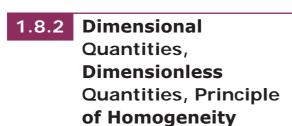
1. We may come across dimensions in different situations in physics, so we often confuse with the term

'dimension'. For instance, we come across terms like 'dimension of energy,' motion in one dimension' and 'dimension of atom'. It should be kept in mind that dimension of physical quantity means expressing physical quantity in terms of exponent of the base quantity. Motion in one dimension, two dimensions and three dimensions implies that it gives dimension of space. Dimension of atom implies the size of the atom. So, simply writing dimension is meaningless. Hence, the meaning should be taken with the context we write.

2. All the trigonometric functions like $\sin \theta$, $\cos \theta$ etc. are dimensionless (θ is dimensionless), exponential function e^x and logarithm function $\ln x$ are dimensionless (x must be dimensionless). Suppose we expand a function in series expansion (finite or infinite) which contain terms like, x^0, x^1, x^2, \ldots then x must be dimensionless quantity.



Table 1.11 Dimensional Formula		
Physical quantity	Expression	Dimensional formula
Area (Rectangle)	$length \times breadth$	$[L^2]$
Volume	Area × height	$[L^3]$
Density	mass / volume	$[ML^{-3}]$
Velocity	displacement/time	$[LT^{-1}]$
Acceleration	velocity / time	$[LT^{-2}]$
Momentum	$mass \times velocity$	$[MLT^{-1}]$
Force	$mass \times acceleration$	$[MLT^{-2}]$
Work	force \times distance	$[\mathrm{ML^2T^{-2}}]$
Power	work / time	$[\mathrm{ML^2T^{-3}}]$
Energy	Work	$[\mathrm{ML^2T^{-2}}]$
Impulse	force \times time	$[MLT^{-1}]$
Radius of gyration	Distance	[L]
Pressure (or) stress	force / area	$[ML^{-1}T^{-2}]$
Surface tension	force / length	$[MT^{-2}]$
Frequency	1 / time period	$[T^{-1}]$
Moment of Inertia	$mass \times (distance)^2$	$[ML^2]$
Moment of force (or torque)	$force \times distance$	$[ML^2T^{-2}]$
Angular velocity	angular displacement / time	$[\mathrm{T}^{-1}]$
Angular acceleration	angular velocity / time	$[T^{-2}]$
Angular momentum	linear momentum \times distance	$[\mathrm{ML^2T^{-1}}]$
Co-efficient of Elasticity	stress/strain	$[ML^{-1}T^{-2}]$
Co-efficient of viscosity	(force \times distance) / (area \times velocity)	$[ML^{-1}T^{-1}]$
Surface energy	work / area	$[\mathrm{MT}^{-2}]$
Heat capacity	heat energy / temperature	$[ML^2T^{-2}K^{-1}]$
Charge	current × time	[AT]
Magnetic induction	force / (current × length)	$[MT^{-2}A^{-1}]$
Force constant	force / displacement	$[MT^{-2}]$
Gravitational constant	[force \times (distance) ²] / (mass) ²	$[M^{-1}L^3T^{-2}]$
Planck's constant	energy / frequency	$[\mathrm{ML^2T^{-1}}]$
Faraday constant	avogadro constant × elementary charge	[AT mol ⁻¹]
Boltzmann constant	energy / temperature	$[ML^2T^{-2}K^{-1}]$



On the basis of dimension, we can classify quantities into four categories.

(1) Dimensional variables

Physical quantities, which possess dimensions and have variable values are called dimensional variables. Examples are length, velocity, and acceleration etc.

(2) Dimensionless variables

Physical quantities which have no dimensions, but have variable values are called dimensionless variables. Examples are specific gravity, strain, refractive index etc.

(3) Dimensional Constant

Physical quantities which possess dimensions and have constant values are called dimensional constants. Examples are Gravitational constant, Planck's constant etc.

(4) Dimensionless Constant

Quantities which have constant values and also have no dimensions are called dimensionless constants. Examples are π , e (Euler's number), numbers etc.

Principle of homogeneity of dimensions

The principle of homogeneity of dimensions states that the dimensions of all the terms in a physical expression should be the same. For example, in the physical expression $v^2 = u^2 + 2as$, the dimensions of v^2 , u^2 and 2 as are the same and equal to $[L^2T^{-2}]$.

1.8.3 Application and Limitations of the Method of Dimensional Analysis.

This method is used to

- (i) Convert a physical quantity from one system of units to another.
- (ii) Check the dimensional correctness of a given physical equation.
- (iii) Establish relations among various physical quantities.

(i) To convert a physical quantity from one system of units to another

This is based on the fact that the product of the numerical values (n) and its corresponding unit (u) is a constant. i.e, n [u] = constant (or) $n_1[u_1] = n_2[u_2]$.

Consider a physical quantity which has dimension 'a' in mass, 'b' in length and 'c' in time. If the fundamental units in one system are M_1 , L_1 and T_1 and the other system are M_2 , L_2 and T_2 respectively, then we can write, n_1 [M_1^a L_1^b T_1^c] = n_2 [M_2^a L_2^b T_2^c]

We have thus converted the numerical value of physical quantity from one system of units into the other system.

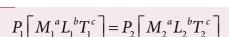
EXAMPLE 1.12

Convert 76 cm of mercury pressure into Nm⁻² using the method of dimensions.

Solution

In cgs system 76 cm of mercury pressure = $76 \times 13.6 \times 980$ dyne cm⁻²

The dimensional formula of pressure P is $\left[ML^{-1}T^{-2}\right]$



We have
$$P_2 = P_1 \left[\frac{M_1}{M_2} \right]^a \left[\frac{L_1}{L_2} \right]^b \left[\frac{T_1}{T_2} \right]^c$$

$$M_1 = 1g, M_2 = 1kg$$

 $L_1 = 1 cm, L_2 = 1m$
 $T_1 = 1 s, T_2 = 1s$

As
$$a = 1$$
, $b = -1$, and $c = -2$

Then

$$P_{2} = 76 \times 13.6 \times 980 \left[\frac{1g}{1kg} \right]^{1} \left[\frac{1cm}{1m} \right]^{-1} \left[\frac{1s}{1s} \right]^{-2}$$

$$= 76 \times 13.6 \times 980 \left[\frac{10^{-3} kg}{1kg} \right]^{1} \left[\frac{10^{-2} m}{1m} \right]^{-1} \left[\frac{1s}{1s} \right]^{-2}$$

$$= 76 \times 13.6 \times 980 \times [10^{-3}] \times 10^{2}$$

$$P_{2} = 1.01 \times 10^{5} \text{ Nm}^{-2}$$

EXAMPLE 1.13

If the value of universal gravitational constant in SI is $6.6x10^{-11}$ Nm² kg⁻², then find its value in CGS System?

Solution

Let G_{SI} be the gravitational constant in the SI system and G_{cgs} in the cgs system. Then

$$G_{SI} = 6.6 \times 10^{-11} \text{Nm}^2 \text{kg}^{-2}$$

$$G_{cgs} = ?$$

$$n_2 = n_1 \left\lceil \frac{M_1}{M_2} \right\rceil^a \left\lceil \frac{L_1}{L_2} \right\rceil^b \left\lceil \frac{T_1}{T_2} \right\rceil^c$$

$$G_{cgs} = G_{SI} \left[\frac{M_1}{M_2} \right]^a \left[\frac{L_1}{L_2} \right]^b \left[\frac{T_1}{T_2} \right]^c$$

$$M_1 = 1 \text{ kg}$$
 $L_1 = 1 \text{m}$ $T_1 = 1 \text{s}$
 $M_2 = 1 \text{ g}$ $L_2 = 1 \text{ cm}$ $T_2 = 1 \text{s}$

The dimensional formula for G is $M^{-1}L^3T^{-2}$

$$a = -1 b = 3 \text{ and } c = -2$$

$$G_{cgs} = 6.6 \times 10^{-11} \left[\frac{1kg}{1g} \right]^{-1} \left[\frac{1m}{1cm} \right]^{3} \left[\frac{1s}{1s} \right]^{-2}$$

$$= 6.6 \times 10^{-11} \left[\frac{1kg}{10^{-3}kg} \right]^{-1} \left[\frac{1m}{10^{-2}m} \right]^{3} \left[\frac{1s}{1s} \right]^{-2}$$

$$= 6.6 \times 10^{-11} \times 10^{-3} \times 10^{6} \times 1$$

$$G_{cgs} = 6.6 \times 10^{-8} \, dyne \, \text{cm}^{2} \, g^{-2}$$

(ii) To check the dimensional correctness of a given physical equation

Let us take the equation of motion v = u + at

Apply dimensional formula on both sides $[LT^{-1}] = [LT^{-1}] + [LT^{-2}] [T]$

$$[LT^{-1}] = [LT^{-1}] + [LT^{-1}]$$

(Quantities of same dimension only can be added)

We see that the dimensions of both sides are same. Hence the equation is dimensionally correct.

EXAMPLE 1.14

Check the correctness of the equation $\frac{1}{2}mv^2 = mgh$ using dimensional analysis method.

Solution

Dimensional formula for

$$\frac{1}{2}mv^2 = [M][LT^{-1}]^2 = [ML^2T^{-2}]$$

Dimensional formula for

$$mgh = [M][LT^{-2}][L] = [ML^2T^{-2}]$$

 $[ML^2T^{-2}] = [ML^2T^{-2}]$

Both sides are dimensionally the same, hence the equations $\frac{1}{2}mv^2 = mgh$ is dimensionally correct.

(iii) To establish the relation among various physical quantities

If the physical quantity Q depends upon the quantities Q_1 , Q_2 and Q_3 ie. Q is proportional to Q_1 , Q_2 and Q_3 .

Then,

$$Q \propto Q_1^{a} Q_2^{b} Q_3^{c}$$

 $Q = k Q_1^{a} Q_2^{b} Q_3^{c}$

where k is a dimensionless constant. When the dimensional formula of Q, Q_1 , Q_2 and Q_3 are substituted, then according to the principle of homogeneity, the powers of M, L, T are made equal on both sides of the equation. From this, we get the values of a, b, c

EXAMPLE 1.15

Obtain an expression for the time period T of a simple pendulum. The time period T depends on (i) mass 'm' of the bob (ii) length 'l' of the pendulum and (iii) acceleration due to gravity g at the place where the pendulum is suspended. (Constant $k = 2\pi$) i.e

Solution

$$T \alpha m^{a} l^{b} g^{c}$$
 $T = k. m^{a} l^{b} g^{c}$

Here k is the dimensionless constant. Rewriting the above equation with dimensions

$$[T^1] = [M^a] [L^b] [LT^{-2}]^c$$

$$[M^0L^0T^1] = [M^a L^{b+c} T^{-2c}]$$

Comparing the powers of M, L and T on both sides, a=0, b+c=0, -2c=1

Solving for a,b and c a = 0, b = 1/2, and c = -1/2

From the above equation T=k. m^0 $\ell^{1/2} g^{-1/2}$

$$T = k \left(\frac{\ell}{g}\right)^{1/2} = k \sqrt{\frac{\ell}{g}}$$

Experimentally $k = 2\pi$, hence $T = 2\pi \sqrt{\frac{\ell}{g}}$

Limitations of Dimensional analysis

- 1. This method gives no information about the dimensionless constants in the formula like 1, 2, π , e (Euler number), etc.
- 2. This method cannot decide whether the given quantity is a vector or a scalar.
- 3. This method is not suitable to derive relations involving trigonometric, exponential and logarithmic functions.
- 4. It cannot be applied to an equation involving more than three physical quantities.
- 5. It can only check on whether a physical relation is dimensionally correct but not the correctness of the relation. For example using dimensional analysis, $s = ut + \frac{1}{3} at^2$ is dimensionally correct whereas the correct relation is $s = ut + \frac{1}{2} at^2$.

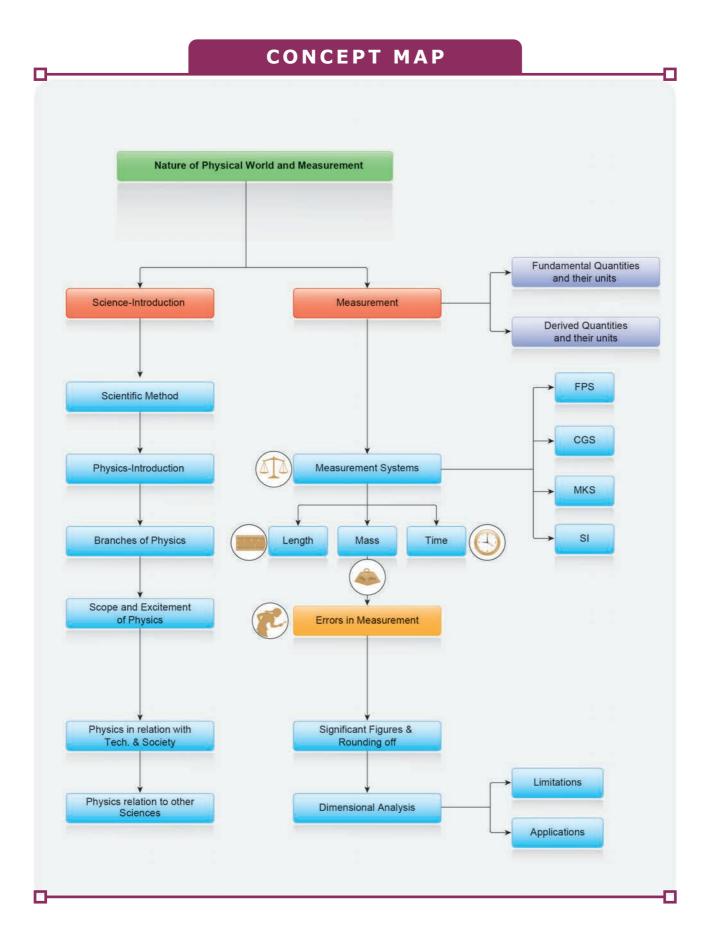


- Physics is an experimental science in which measurements made must be expressed in units.
- All physical quantities have a magnitude (size) and a unit.
- The SI unit of length, mass, time, temperature, electric current, amount of substance and luminous intensity are metre, kilogram, second, kelvin, ampere, mole and candela respectively.
- Units of all mechanical, electrical, magnetic and thermal quantities are derived in terms of these base units.
- Screw gauge, vernier caliper methods are available for the measurement of length in the case of small distances.
- Parallax, RADAR methods are available for the measurement of length in the case of long distances.
- The uncertainty in a measurement is called error. The accuracy of a measurement is a measure of how close the measured value is to the true value of the quantity. Every accurate measurement is precise but every precise measurement need not be accurate.
- When two or more quantities are added or subtracted, the result can be as precise as the least of the individual precisions. When the quantities are multiplied or divided, the result has the same number of significant figures as the quantity with the smallest number of significant figures.
- Dimensional analysis is used to perform quick check on the validity of equations. Whenever the quantities are added, subtracted or equated, they must have the same dimension. A dimensionally correct equation may not be a true equation but every true equation is necessarily dimensionally correct.









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I. Multiple Choice Questions

1. One of the combinations from the fundamental physical constants is $\frac{hc}{G}$.

The unit of this expression is

a) kg²

b) m³

c) s^{-1}

- d) m
- 2. If the error in the measurement of radius is 2%, then the error in the determination of volume of the sphere will be
 - a) 8%

b) 2%

c) 4%

- d) 6%
- 3. If the length and time period of an oscillating pendulum have errors of 1% and 3% respectively then the error in measurement of acceleration due to gravity is
 - a) 4%

[Related to AMPMT 2008]

- b) 5%
- c) 6%
- d) 7%
- 4. The length of a body is measured as 3.51 m, if the accuracy is 0.01m, then the percentage error in the measurement is
 - a) 351%
- b) 1%
- c) 0.28%
- d) 0.035%
- **5.** Which of the following has the highest number of significant figures?
 - a) 0.007 m²
 - b) 2.64x10²⁴ kg
 - c) 0.0006032 m²
 - d) 6.3200 J
- **6.** If $\pi = 3.14$, then the value of π^2 is
 - a) 9.8596
- b) 9.860

c) 9.86

d) 9.9

7. Which of the following pairs of physical quantities have same dimension?



- a) force and power
- b) torque and energy
- c) torque and power
- d) force and torque
- **8.** The dimensional formula of Planck's constant h is [AMU, Main, JEE, NEET]
 - a) $[ML^2T^{-1}]$
- b) [ML²T⁻³]
- c) [MLT⁻¹]
- d) $[ML^3T^{-3}]$
- **9.**The velocity of a particle v at an instant t is given by $v = at + bt^2$. The dimensions of b is
 - a) [L]

- b) [LT⁻¹]
- c) [LT⁻²]
- d) [LT⁻³]
- **10.** The dimensional formula for gravitational constant *G* is [Related to AIPMT 2004]
 - a) $[ML^3T^{-2}]$
- b) $[M^{-1}L^3T^{-2}]$
- c) $[M^{-1}L^{-3}T^{-2}]$
- d) $[ML^{-3}T^2]$
- 11. The density of a material in CGS system of units is 4 g cm⁻³. In a system of units in which unit of length is 10 cm and unit of mass is 100 g, then the value of density of material will be
 - a) 0.04

b) 0.4

c) 40

- d) 400
- **12.** If the force is proportional to square of velocity, then the dimension of proportionality constant is [JEE-2000]
 - a) [MLT⁰]
- b) [MLT⁻¹]
- c) [ML⁻²T]
- d) $[ML^{-1}T^{0}]$

- 13. The dimension of $(\mu_0 \varepsilon_0)^{-\frac{1}{2}}$ is [Main AIPMT 2011]
 - (a) length
- (b) time
- (c) velocity
- (d) force
- 14. Planck's constant (h), speed of light in vacuum (c) and Newton's gravitational constant (G) are taken as three fundamental constants. Which of the following combinations of these has the dimension of length?.

[NEET 2016 (phase II)]

(a)
$$\frac{\sqrt{hG}}{c^{\frac{3}{2}}}$$

(b)
$$\frac{\sqrt{hG}}{c^{\frac{5}{2}}}$$

(c)
$$\sqrt{\frac{hc}{G}}$$

(d)
$$\sqrt{\frac{Gc}{h^{\frac{3}{2}}}}$$

15. A length-scale (l) depends on the permittivity (ε) of a dielectric material, Boltzmann constant (k_B), the absolute temperature (T), the number per unit volume (n) of certain charged particles,

II. Short Answer Questions

- **1.** Briefly explain the types of physical quantities.
- **2.** How will you measure the diameter of the Moon using parallax method?
- **3.** Write the rules for determining significant figures.
- **III. Long Answer Questions**
 - 1. i) Explain the use of screw gauge and vernier caliper in measuring smaller distances.
 - ii) Write a note on triangulation method and radar method to measure larger distances.

and the charge (q) carried by each of the particles. Which of the following expression for l is dimensionally correct?. [JEE (advanced) 2016]

(a)
$$l = \sqrt{\frac{nq^2}{\varepsilon k_B T}}$$

(b)
$$l = \sqrt{\frac{\varepsilon k_B T}{nq^2}}$$

(c)
$$l = \sqrt{\frac{q^2}{\varepsilon n^{\frac{2}{3}} k_B T}}$$

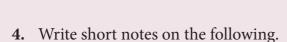
(d)
$$l = \sqrt{\frac{q^2}{\varepsilon n k_B T}}$$

Answers:

- 1) a 2) d
- 3) d
- 4) c

- 5) d
- 6) c
- 7) b
- 8) a

- 9) d
- 10) b
- 11) c
- 12) d
- 13) c 14) a 15) b
- **4.** What are the limitations of dimensional analysis?
- **5.** Define precision and accuracy. Explain with one example.
- **2.** Explain in detail the various types of errors.
- **3.** What do you mean by propagation of errors? Explain the propagation of errors in addition and multiplication.



- a) Unit
- b) Rounding off
- c) Dimensionless quantities

5. Explain the principle of homogeniety of dimensions. What are its uses? Give example.

IV. Numerical Problems

- 1. In a submarine equipped with sonar, the time delay between the generation of a pulse and its echo after reflection from an enemy submarine is observed to be 80 s. If the speed of sound in water is 1460 ms⁻¹. What is the distance of enemy submarine? Ans: (58.40 km)
- 2. The radius of the circle is 3.12 m. Calculate the area of the circle with regard to significant figures. Ans: (30.6 m²)
- 3. Assuming that the frequency γ of a vibrating string may depend upon i) applied force (F) ii) length (ℓ) iii) mass

per unit length (m), prove that $\gamma \alpha$ $\frac{1}{l} \sqrt{\frac{F}{m}}$ using dimensional analysis. (related to JIPMER 2001)

- 4. Jupiter is at a distance of 824.7 million km from the Earth. Its angular diameter is measured to be 35.72". Calculate the diameter of Jupiter. Ans: $(1.428 \times 10^5 \text{ km})$
- 5. The measurement value of length of a simple pendulum is 20 cm known with 2 mm accuracy. The time for 50 oscillations was measured to be 40 s within 1 s resolution. Calculate the percentage accuracy in the determination of acceleration due to gravity 'g' from the above measurement.

 Ans: (6%)

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Screw Gauge and Vernier Caliper

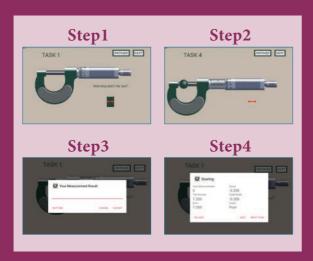
Measure with Pleasure

STEPS:

- Get into/Access the application with the help of the link given below or the given QR code.
- To measure the given object's diameter / thickness, place the object as it should be fitted between the screw and anvil. The object can be fitted properly by adjusting the screw.
- After clicking the Answer button, You will get a
 box showing Your Measurement Result. Input
 your measured value in it and click Submit
 button. There you can verify your measurement
 if it is right or wrong.
- You can measure the diameter of various objects by clicking Next button.

STEPS:

- Use the given URL to access 'Vernier Caliper' simulation page. Click 'Play Button' to launch the simulation.
- Select the unit and set the 'Zero Error' from the dropdown above the scale.
- Click and drag the secondary scale and place the blue coloured object in between them. Find the measurement and enter it in the answer box above the scale.
- Change the size of the object by clicking and dragging the edge of the blue object and practice the measurement using Vernier Caliper.





Screw Gauge stimulation URL:

https://play.google.com/store/apps/details?id=com.priantos.screwgaugegames&hl=en

Vernier caliper stimulation URL:

 $\frac{http://iwant2study.org/ospsg/index.php/interactive-resources/physics/01-measurements/5-vernier-caliper\#faqnoanchor}{}$

- * Pictures are indicative only.
- * If browser requires, allow **Flash Player** or **Java Script** to load the page.





UNIT 1 NATURE OF PHYSICAL WORLD AND MEASUREMENT