
CBSE Sample Paper-05 (Solved)
SUMMATIVE ASSESSMENT –I
MATHEMATICS
Class – IX

Time allowed: 3 hours

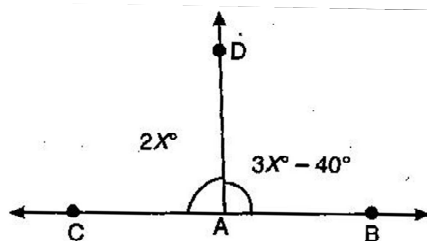
Maximum Marks: 90

General Instructions:

- a) All questions are compulsory.
 - b) The question paper consists of 31 questions divided into four sections – A, B, C and D.
 - c) Section A contains 4 questions of 1 mark each which are multiple choice questions, Section B contains 6 questions of 2 marks each, Section C contains 10 questions of 3 marks each and Section D contains 11 questions of 4 marks each.
 - d) Use of calculator is not permitted.
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Section A

1. If $x = \frac{\sqrt{7}}{5}$ and $\frac{5}{x} = P\sqrt{7}$, then the value of P is:
- (a) $\frac{7}{25}$ (b) $\frac{25}{7}$ (c) $\frac{15}{7}$ (d) $\frac{7}{15}$
2. In the figure, AB and AC are opposite rays. What is the value of x :

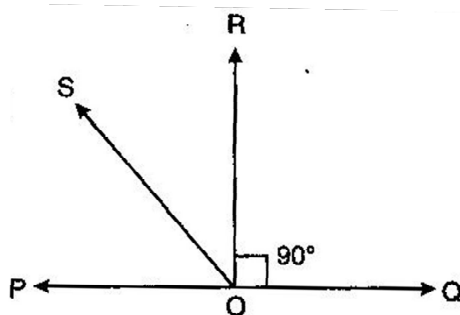


- (a) 44° (b) 54° (c) 64° (d) None of these
3. A triangle cannot have more than:
- (a) one right angle (b) two right angles
(c) two obtuse angles (d) None of these
4. Area of triangle whose base = 35 cm and height = 12.8 cm:
- (a) 224 sq. cm (b) 422 sq. cm (c) 424 sq. cm (d) 242 sq. cm

Section B

5. Write the following numbers in ascending order: $\sqrt[6]{6}, \sqrt[3]{7}, \sqrt[4]{8}$
6. Find the zeroes of the polynomial $p(x) = x^2 - 5x + 6$.
7. Find the remainder when $2x^4 + 6x^3 + 2x^2 - x + 2$ is divided by $(x + 2)$.
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8. In figure, POQ is a line. Ray OR is perpendicular to line PQ. OS is another ray lying between rays OP and OR. Prove that: $\angle ROS = \frac{1}{2} (\angle QOS - \angle POS)$



9. In a $\triangle ABC$, $30A + 6B = 5C$. Determine $\angle A$, $\angle B$ and $\angle C$.
10. Draw a triangle ABC where vertices A, B and C are $(0, 2)$, $(2, -2)$ and $(-2, 2)$ respectively.

Section C

11. Find five rational numbers between $\frac{3}{5}$ and $\frac{4}{5}$.

12. Simplify: $\frac{1}{2}\sqrt{486} - \sqrt{\frac{27}{2}}$

Or

Simplify: $\frac{\sqrt{a^2 - b^2} + a}{\sqrt{a^2 + b^2} + b} \div \frac{\sqrt{a^2 + b^2} - b}{a - \sqrt{a^2 - b^2}}$

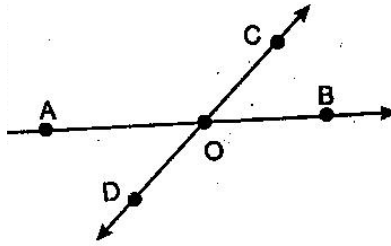
13. Divide $f(y) = 3y^4 - 8y^3 - y^2 - 5y - 5$ by $y - 3$.
14. If the polynomials $px^3 + 4x^2 + 3x - 4$ and $x^3 - 4x + p$ are divided by $x - 3$, then the remainder in each case is the same. Find the value of p .

Or

What must be added to $(x^3 - 3x^2 + 4x - 13)$ to obtain a polynomial which is exactly divisible by $(x - 3)$?

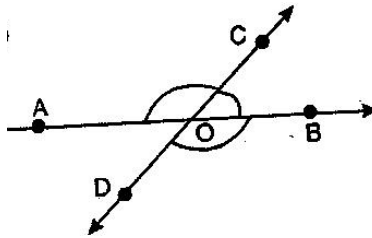
15. Factorize: $a^2px + 2a^2qx - 2apy - 4aqy + pz + 2qz$
16. If a point C lies between two points A and B such that $AC = BC$, then point C is called the mid-point of line segment AB. Prove that every line segment has one and only one mid-point.

17. In the figure, if $\angle AOC + \angle BOD = 266^\circ$, then find all the four angles.

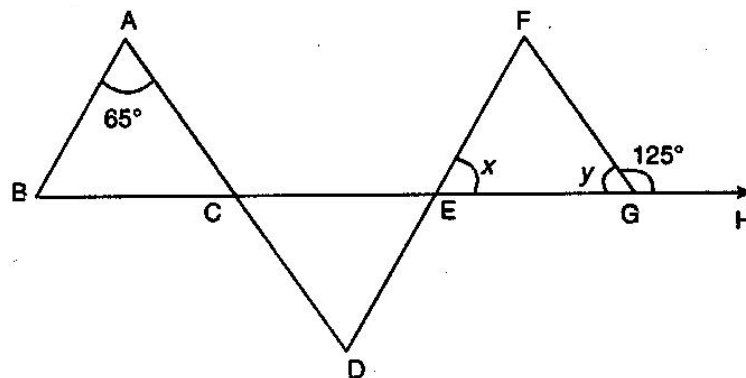


Or

- If the figure, if $\angle AOC + \angle BOC = \angle BOD = 338^\circ$, then find the all four angles.



18. If a line is perpendicular to one of the two given parallel lines then prove that it is also perpendicular to the other line.
19. In a triangle ABC, $\angle A + \angle B = 84^\circ$ and $\angle B + \angle C = 146^\circ$. Find the measure of each of the angles of the triangle.
20. In the figure, find x and y , if $AB \parallel DF$ and $AD \parallel FG$.



Section D

21. Represent $\sqrt{5}$ on number line.
22. Rationalize the denominator of $\frac{1}{\sqrt{2} + \sqrt{3} + \sqrt{10}}$.

Or

Simplify:
$$\frac{7\sqrt{3}}{\sqrt{10} + \sqrt{3}} - \frac{2\sqrt{5}}{\sqrt{6} + \sqrt{5}} - \frac{3\sqrt{2}}{\sqrt{15} + 3\sqrt{2}}$$

23. Ram has two rectangles in which their areas are given:

(a) $25a^2 - 35a + 12$

(b) $35y^2 + 13y - 12$

(i) Give possible expressions for the length and breadth of each of the rectangles.

(ii) Which mathematical concept is used in this problem?

(iii) Which value is depicted in this problem?

[Value Based Question]

24. Factorize $x^3 - 23x^2 + 142x - 120$, if $x - 1$ is a factor of it.

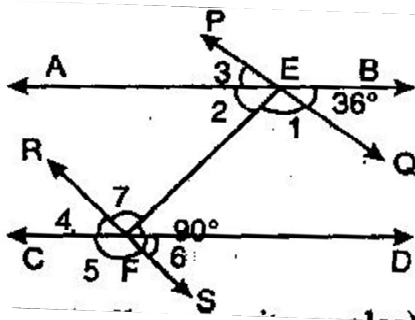
Or

Factorize by using factor theorem: $y^3 - 7y + 6$

25. Factorize : $x^3 + \frac{1}{x^3} - 2$

26. If lines AB, AC, AD and AE are parallel to a line l , then points A, B, C, D and E are collinear.

27. In the figure, $AB \parallel CD$ and $PQ \parallel RS$, find the angles marked.



28. Two plane mirrors are placed perpendicular to each other, as shown in the figure. An incident ray AB to the first mirror is first reflected in the direction of BC and then reflected by the second mirror in the direction of CD. Prove that $AB \parallel CD$.

29. In the figure, it is given that $\angle A = \angle C$ and $AB = BC$. Prove that $\triangle ABD \cong \triangle CBE$.

30. Draw the graph of linear equation: $8x - 3y + 4 = 0$

31. The side of a square exceeds the side of another square by 4 cm and the sum of the areas of the two squares is 400 sq. cm. Find the dimensions of the squares.

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(Solutions)

SECTION-A

1. (b)

2. (a)

3. (a)

4. (a)

5. L.C.M. of 6, 3 and 4 is 12.

$$\begin{aligned}\Rightarrow \sqrt[6]{6} &= \sqrt[12]{36} & \sqrt[3]{7} &= \sqrt[12]{2401} & \text{and} & \sqrt[4]{8} &= \sqrt[12]{512} \\ \Rightarrow 36 &< 512 < 2401 & \Rightarrow \sqrt[12]{36} &< \sqrt[12]{512} < \sqrt[12]{2401} \\ \therefore \sqrt[6]{6} &< \sqrt[4]{8} < \sqrt[3]{7}\end{aligned}$$

$$6. \quad x^2 - 5x + 6 = 0 \quad \Rightarrow \quad x^2 - 3x - 2x + 6 = 0$$

$$\Rightarrow x(x-3) - 2(x-3) = 0 \quad \Rightarrow \quad (x-3)(x-2) = 0$$

\therefore Zeroes are 2 and 3.

7. By remainder theorem,

$$\begin{aligned}f(-2) &= 2(-2)^4 + 6(-2)^3 + 2(-2)^2 - (-2) + 2 \\ \Rightarrow f(-2) &= 32 - 48 + 8 + 2 + 2 = -4\end{aligned}$$

$$\begin{aligned}8. \quad \angle QOS - \angle POS &= (\angle QOR + \angle ROS) - \angle POS \\ &= 90^\circ + \angle ROS - \angle POS \\ &= (90^\circ - \angle POS) + \angle ROS \\ &= (\angle ROP - \angle POS) + \angle ROS \\ &= 2 \angle ROS\end{aligned}$$

$$\text{Hence, } \angle ROS = \frac{1}{2} (\angle QOS - \angle POS)$$

9. Given $30A = 6B = 5C$

$$\Rightarrow \frac{A}{1} = \frac{B}{5} = \frac{C}{6} \quad [\text{Dividing by 30}]$$

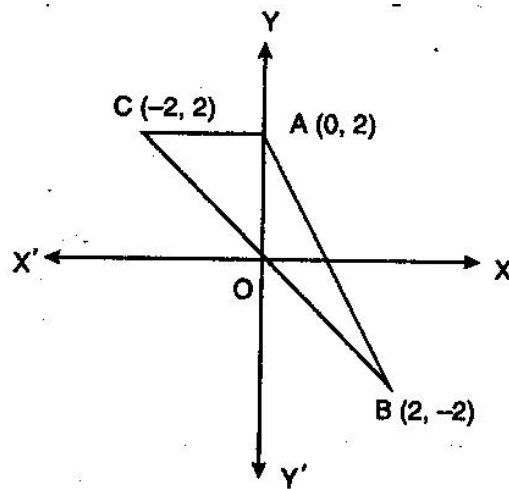
$$\Rightarrow \angle A : \angle B : \angle C = 1 : 5 : 6$$

Let $\angle A = x$, $\angle B = 5x$ and $\angle C = 6x$

$$\Rightarrow x + 5x + 6x = 180^\circ \quad \Rightarrow \quad 12x = 180^\circ \quad \Rightarrow \quad x = 15^\circ$$

Hence $\angle A = 15^\circ$, $\angle B = 75^\circ$ and $\angle C = 90^\circ$

10.



11. A rational number between r and s is $\frac{r+s}{2}$.

Therefore a rational number between $\frac{3}{5}$ and $\frac{4}{5} = \frac{1}{2} \left(\frac{3}{5} + \frac{4}{5} \right) = \frac{7}{10}$

A rational number between $\frac{3}{5}$ and $\frac{7}{10} = \frac{1}{2} \left(\frac{3}{5} + \frac{7}{10} \right) = \frac{13}{20}$

Hence five rational numbers between $\frac{3}{5}$ and $\frac{4}{5}$ are $\frac{5}{8}, \frac{13}{20}, \frac{27}{40}, \frac{7}{10}, \frac{31}{40}$.

$$\begin{aligned}
 12. \quad & \frac{1}{2} \sqrt{486} - \sqrt{\frac{27}{2}} = \frac{1}{2} \sqrt{9^2 \times 6} - \sqrt{\frac{54}{4}} \\
 & = \frac{1}{2} \sqrt{9^2} \times \sqrt{6} - \sqrt{\frac{3^2 \times 6}{2^2}} = \frac{1}{2} \times 9 \times \sqrt{6} - \frac{3}{2} \sqrt{6} = \sqrt{6} \left(\frac{9}{2} - \frac{3}{2} \right) = 3\sqrt{6}
 \end{aligned}$$

Or

$$\begin{aligned}
 & \frac{\sqrt{a^2 - b^2} + a}{\sqrt{a^2 + b^2} + b} \times \frac{a - \sqrt{a^2 - b^2}}{\sqrt{a^2 + b^2} - b} = \frac{a^2 - (a^2 - b^2)}{(a^2 + b^2) - b^2} \\
 & = \frac{b^2}{a^2}
 \end{aligned}$$

13.

$$\begin{array}{r}
 3y^3 + y^2 + 2y + 1 \\
 \hline
 y-3 \quad 3y^4 - 8y^3 - y^2 - 5y - 5 \\
 \quad 3y^4 - 9y^3 \\
 \quad \hline
 \quad \quad y^3 - y^2 - 5y - 5 \\
 \quad \quad y^3 - 3y^2 \\
 \quad \quad \hline
 \quad \quad \quad 2y^2 - 5y - 5 \\
 \quad \quad \quad 2y^2 - 6y \\
 \quad \quad \quad \hline
 \quad \quad \quad \quad y - 5 \\
 \quad \quad \quad \quad y - 3 \\
 \quad \quad \quad \quad \hline
 \quad \quad \quad \quad \quad - 2
 \end{array}$$

14. Let $A(x) = px^3 + 4x^2 + 3x - 4$

$$B(x) = x^3 - 4x + p$$

$$g(x) = x - 3$$

According to question, $A(3) = B(3)$

$$\Rightarrow p(3)^3 + 4(3)^2 + 3(3) - 4 = (3^3) - 4(3) + p$$

$$\Rightarrow 27p + 41 = 15 + p$$

$$\Rightarrow 27p - p = 15 - 41$$

$$\Rightarrow p = -1$$

Or

Let $f(x) = x^3 - 3x^2 + 4x - 13$ and $g(x) = x - 3$

Let k be added to $f(x)$ so that it may be exactly divisible by $(x - 3)$.

$$\therefore p(x) = (x^3 - 3x^2 + 4x - 13) + k$$

$$\therefore p(3) = (3)^3 - 3(3)^2 + 4(3) - 13 + k = 0$$

$$\Rightarrow 27 - 27 + 12 - 13 + k = 0$$

$$\Rightarrow -1 + k = 0 \quad \Rightarrow \quad k = 1$$

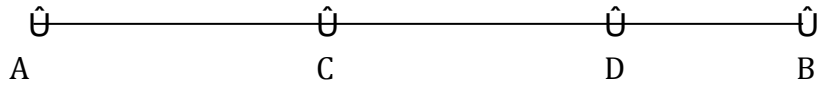
15. $a^2px + 2a^2qx - 2apy - 4aqy + pz + 2qz$

$$= (a^2px + 2a^2qx) + (-2apy - 4aqy) + (pz + 2qz)$$

$$= a^2x(p + 2q) - 2ay(p + 2q) + z(p + 2q)$$

$$= (p + 2q)(a^2x - 2ay + z)$$

16. Given $AC = BC$ (i)



If possible let D be another mid-point of AB

$\therefore AD = DB$ (ii)

Subtracting eq. (i) from eq. (ii), we get

$$AD - AC = DB - CB$$

$$\Rightarrow -CD = CD$$

$$\Rightarrow 2CD = 0$$

$$\Rightarrow CD = 0$$

\therefore C and D coincide.

Hence every line segment has one and only one mid-point.

17. $\angle AOC + \angle BOD = 266^\circ$ (i)

But $\angle BOD = \angle AOC$ [Vertically opposite]

$$\therefore \angle AOC + \angle AOC = 266^\circ$$

$$\Rightarrow \angle AOC = 133^\circ$$

Now $\angle AOC + \angle BOC = 180^\circ$ [Linear pair]

$$\Rightarrow 133^\circ + \angle BOC = 180^\circ$$

$$\Rightarrow \angle BOC = 47^\circ$$

$$\Rightarrow \angle AOD = \angle BOC$$

$$\Rightarrow \angle AOD = 47^\circ$$

Or

$$\angle AOC + \angle BOC + \angle BOD = 338^\circ \quad \text{.....(i)}$$

$$\angle AOC + \angle BOC + \angle BOD + \angle AOD = 360^\circ \quad \text{.....(ii)}$$

From eq. (i) and eq. (ii), we get,

$$338^\circ + \angle AOD = 360^\circ$$

$$\Rightarrow \angle AOD = 22^\circ$$

$$\therefore \angle BOC = 22^\circ, \angle BOD = 158^\circ \text{ and } \angle AOC = 158^\circ$$

18. Given : l, m, n are three lines such that $m \parallel n$ and $l \perp m$.

To prove: $l \perp n$

Proof : Since $l \perp m$

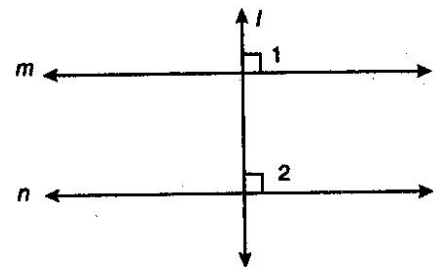
$$\Rightarrow \angle 1 = 90^\circ \quad \text{.....(i)}$$

Now, $m \parallel n$ and transversal intersects them.

$$\Rightarrow \angle 2 = \angle 1 \quad \text{.....(ii)} \quad \text{[Corresponding angles]}$$

From eq. (i) and (ii), we get,

$$\angle 2 = \angle 1 = 90^\circ \quad \Rightarrow \quad \angle 2 = 90^\circ$$



$$\therefore l \perp n$$

19. Given $\angle A + \angle B = 84^\circ$ (i)

And $\angle B + \angle C = 146^\circ$ (ii)

Adding eq. (i) and (ii), we get,

$$\angle A + \angle B + \angle B + \angle C = 230^\circ$$

$$\Rightarrow (\angle A + \angle B + \angle C) + \angle B = 230^\circ$$

$$\Rightarrow 180^\circ + \angle B = 230^\circ$$

$$\Rightarrow \angle B = 50^\circ$$

Putting the value of $\angle B$ in eq. (i), we get,

$$\angle A + 50^\circ = 84^\circ \Rightarrow \angle A = 34^\circ$$

Putting the value of $\angle B$ in eq. (ii), we get,

$$50^\circ + \angle C = 146^\circ \Rightarrow \angle C = 96^\circ$$

20. $\angle y + 125^\circ = 180^\circ$ [Straight angle]

$$\Rightarrow \angle y = 55^\circ$$
(i)

Now AB is parallel to FD and transversal AD cuts them.

$$\angle D = \angle A$$
 [Alternate angles]

$$\angle D = 65^\circ$$

Again AD || FG, transversal FD cuts them.

$$\angle F = \angle D$$

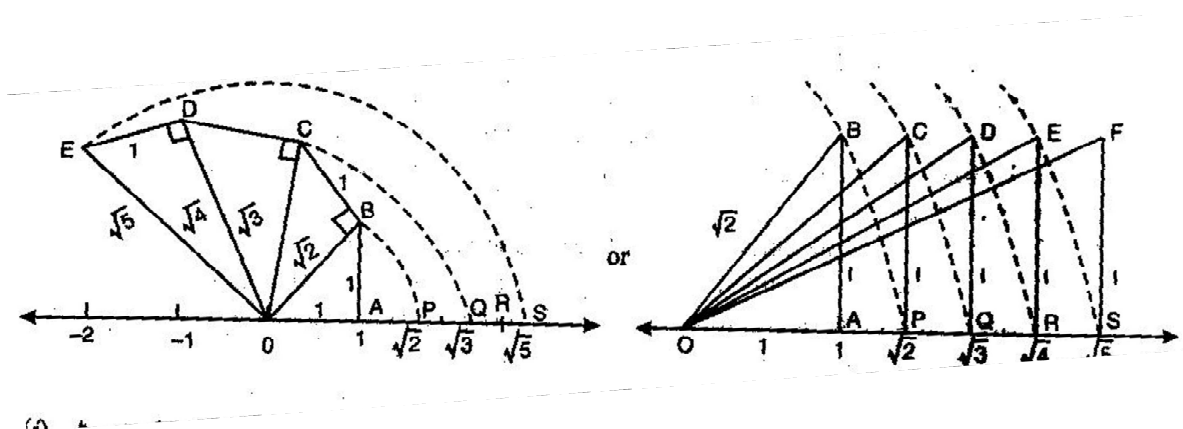
$$\angle F = 65^\circ$$
(ii)

In triangle EFG, $\angle x + \angle F + \angle y = 180^\circ$

$$\Rightarrow \angle x + 65^\circ + 55^\circ = 180^\circ$$

$$\Rightarrow \angle x = 60^\circ$$

21.



$$\begin{aligned}
22. \quad & \frac{1}{\sqrt{2}+\sqrt{3}+\sqrt{10}} \cdot \frac{(\sqrt{2}+\sqrt{3})-\sqrt{10}}{(\sqrt{2}+\sqrt{3})-\sqrt{10}} \\
&= \frac{\sqrt{2}+\sqrt{3}-\sqrt{10}}{(\sqrt{2}+\sqrt{3})^2-(\sqrt{10})^2} = \frac{\sqrt{2}+\sqrt{3}-\sqrt{10}}{2\sqrt{6}-5} \\
&= \frac{\sqrt{2}+\sqrt{3}-\sqrt{10}}{2\sqrt{6}-5} \times \frac{2\sqrt{6}+5}{2\sqrt{6}+5} = \frac{(\sqrt{2}+\sqrt{3}-\sqrt{10})(2\sqrt{6}+5)}{(2\sqrt{6})^2-(5)^2} \\
&= \frac{2\sqrt{12}+5\sqrt{2}+2\sqrt{18}+5\sqrt{3}-2\sqrt{60}-5\sqrt{10}}{24-25} = -4\sqrt{3}-5\sqrt{2}-6\sqrt{2}-5\sqrt{3}+4\sqrt{15}+5\sqrt{10} \\
&= -11\sqrt{2}-9\sqrt{3}+5\sqrt{0}+4\sqrt{15}
\end{aligned}$$

Or

$$\begin{aligned}
& \frac{7\sqrt{3}}{\sqrt{10}+\sqrt{3}} \times \frac{\sqrt{10}-\sqrt{3}}{\sqrt{10}-\sqrt{3}} - \frac{2\sqrt{5}}{\sqrt{6}+\sqrt{5}} \times \frac{\sqrt{6}-\sqrt{5}}{\sqrt{6}-\sqrt{5}} - \frac{3\sqrt{2}}{\sqrt{15}+3\sqrt{2}} \times \frac{\sqrt{15}-3\sqrt{2}}{\sqrt{15}-3\sqrt{2}} \\
&= \frac{7\sqrt{30}-21}{10-3} - \frac{2\sqrt{30}-10}{6-5} - \frac{3\sqrt{30}-18}{15-18} \\
&= \sqrt{30}-3-2\sqrt{30}+10+\sqrt{30}-6 \\
&= (\sqrt{30}-2\sqrt{30}+\sqrt{30})+(-3+10-6) \\
&= 1
\end{aligned}$$

23. (i) (a) Area = $25a^2 - 35a + 12 = 25a^2 - 15a - 20a + 12$
 $= 5a(5a-3) - 4(5a-3) = (5a-3)(5a-4)$

So possible length and breadth are $(5a-3)$ and $(5a-4)$ units respectively.

(b) Area = $35y^2 + 13y - 12 = 35y^2 + 28y - 15y - 12$
 $= 7y(5y+4) - 3(5y+4) = (7y-3)(5y+4)$

So possible length and breadth are $(7y-3)$ and $(5y+4)$.

(ii) Factorization of Polynomials.

(iii) Expression of one's desires and news is very necessary.

24. Let us divide $x^3 - 23x^2 + 142x - 120$ by $x-1$ to get the other factors.

$$\begin{array}{r}
 x^2 - 22x + 120 \\
 x-1 \overline{) x^3 - 23x^2 + 142x - 120} \\
 \underline{x^3 - x^2} \\
 -22x^2 + 142x - 120 \\
 \underline{-22x^2 + 22x} \\
 120x - 120 \\
 \underline{120x - 120} \\
 0
 \end{array}$$

$$\begin{aligned}
 x^3 - 23x^2 + 142x - 120 &= (x-1)(x^2 - 22x + 120) \\
 &= (x-1)(x^2 - 12x - 10x + 120) \\
 &= (x-1)[x(x-12) - 10(x-12)] \\
 &= (x-1)(x-12)(x-10)
 \end{aligned}$$

Or

Let $f(y) = y^3 - 7y + 6$

The constant term in $f(y)$ is 6 and its factors are $\pm 1, \pm 2, \pm 3, \pm 6$.

On putting $y = -1$ in given expression, we get,

$$f(-1) = (-1)^3 - 7(-1) + 6 = -1 + 7 + 6 \neq 0$$

$$f(+1) = (1)^3 - 7(1) + 6 = 0$$

So $(y-1)$ is a factor of $f(y)$.

Now we divide $f(y) = y^3 - 7y + 6$ by $y-1$ to get other factors.

$$\begin{array}{r}
 y^2 + y - 6 \\
 y-1 \overline{) y^3 - 7y + 6} \\
 \underline{y^3 - y^2} \\
 y^2 - 7y + 6 \\
 \underline{y^2 - y} \\
 -6y + 6 \\
 \underline{-6y + 6} \\
 0
 \end{array}$$

$$\begin{aligned}
\therefore y^3 - 7y + 6 &= (y-1)(y^2 + y - 6) \\
&= (y-1)(y^2 + 3y - 2y - 6) \\
&= (y-1)[y(y+3) - 2(y+3)] \\
&= (y-1)(y+3)(y-2)
\end{aligned}$$

$$\begin{aligned}
25. \quad x^3 + \frac{1}{x^3} - 2 &= x^3 + \left(\frac{1}{x}\right)^3 + 1 - 3 \\
&= x^3 + \left(\frac{1}{x}\right)^3 + (1)^3 - 3 \times x \times \frac{1}{x} \times 1 \\
&= \left(x + \frac{1}{x} + 1\right) \left[x^2 + \left(\frac{1}{x}\right)^2 + 1 - x \times \frac{1}{x} - \frac{1}{x} \times 1 - 1 \times x\right] \\
&= \left(x + \frac{1}{x} + 1\right) \left(x^2 + \left(\frac{1}{x}\right)^2 + 1 - 1 - \frac{1}{x} - x\right) \\
&= \left(x + \frac{1}{x} + 1\right) \left(x^2 + \frac{1}{x^2} - \frac{1}{x} - x\right)
\end{aligned}$$

26. Given : Lines AB, AC, AD and AE are parallel to line l .

To prove: A, B, C, D and E are collinear.

Proof : Since AB, AC, AD and AE are all parallel to line l . Therefore point A is outside l and lines AB, AC, AE are drawn through A and each line is parallel to l .

But by parallel lines axiom, one and only one line can be drawn through A outside it and parallel to l .

This is possible only when A, B, C, D and E all lie on the same line. Hence A, B, C, D and E are collinear.

$$27. \quad PQ \parallel RS \quad \Rightarrow \quad \angle 1 + \angle EFS = 180^\circ$$

[consecutive interior angles are supplementary when lines are parallel]

$$\begin{aligned}
&\angle 1 = 90^\circ \\
&\angle 7 + \angle EFS = 180^\circ \quad \text{[Linear pair]} \\
\Rightarrow \quad &\angle 7 + 90^\circ = 180^\circ \quad \Rightarrow \quad \angle 7 = 90^\circ \\
&\angle 3 = \angle BEQ \quad \text{[Vertically opposite angles]} \\
\Rightarrow \quad &\angle 3 = 36^\circ \\
&\angle 1 + \angle 2 + \angle 3 = 180^\circ \quad \text{[Straight angles]} \\
\Rightarrow \quad &90^\circ + \angle 2 + 36^\circ = 180^\circ \quad \Rightarrow \quad \angle 2 = 54^\circ \\
&\angle EFD = \angle 2 = 54^\circ \\
&\angle 6 + \angle EFD = 90^\circ \quad \Rightarrow \quad \angle 6 + 54^\circ = 90^\circ \quad \Rightarrow \quad \angle 6 = 36^\circ \\
&\angle 4 = \angle 6 = 36^\circ \quad \text{[Vertically opposite angles]} \\
&\angle 4 + \angle 5 = 180^\circ \quad \Rightarrow \quad \angle 5 = 144^\circ
\end{aligned}$$

28. Let BO and CO be the normals to the mirrors. As mirrors are perpendicular to each other. SO their normals BO and CO are perpendicular.

$$\therefore \angle BOC = 90^\circ$$

In right angled triangle OBC, $\angle 2 + \angle 3 = 90^\circ$ (i)

$$\angle 1 = \angle 2$$

[Angle of incident = Angle of reflection]

$$\angle 3 = \angle 4$$

[Angle of incident = Angle of reflection]

On adding, $\angle 1 + \angle 4 = \angle 2 + \angle 3$

$$\Rightarrow \angle 1 + \angle 4 = 90^\circ \text{(ii)}$$

On adding eq. (i) and (ii), we get,

$$\angle 2 + \angle 3 + \angle 1 + \angle 4 = 180^\circ$$

$$\angle ABC + \angle BCD = 180^\circ$$

But $\angle ABC$ and $\angle BCD$ are consecutive interior angles formed when the transversal BC intersect AB and CD.

$$\therefore AB \parallel CD$$

29. In Δ s AOE and COD,

$$\angle A = \angle C \quad \text{and} \quad \angle AOE = \angle COD \quad \text{[Vertically opposite angles]}$$

$$\therefore \angle A + \angle AOE = \angle C + \angle COD$$

$$\Rightarrow 180^\circ - \angle AEO = 180^\circ - \angle CDO \quad \text{[} \because \angle A + \angle AEO = 180^\circ \text{ and} \\ \angle C + \angle COD + \angle CDO = 180^\circ \text{]}$$

$$\Rightarrow \angle AEO = \angle CDO \quad \text{.....(i)}$$

$$\text{Now, } \angle AEO + \angle OEB = 180^\circ \quad \text{[Angles of a linear pair]}$$

$$\text{And } \angle CDO + \angle ODB = 180^\circ \quad \text{[Angles of a linear pair]}$$

$$\Rightarrow \angle AEO + \angle OEB = \angle CDO + \angle ODB$$

$$\Rightarrow \angle OEB = \angle ODB$$

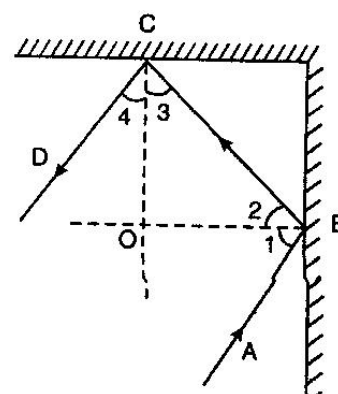
$$\Rightarrow \angle CEB = \angle ADB \quad \text{.....(ii)} \quad \text{[} \because \angle OEB = \angle CEB \text{ and } \angle ODB = \angle ADB \text{]}$$

$$\text{In } \Delta ADB \text{ and } \Delta CBE, \quad \angle A = \angle C \quad \text{[Given]}$$

$$\angle ADB = \angle CEB \quad \text{[From eq. (ii)]}$$

$$\text{And } AB = BC \quad \text{[Given]}$$

$$\Delta ADB \cong \Delta CBE \quad \text{[By AAS]}$$



30. We have, $8x - 3y + 4 = 0$

$$\Rightarrow 3y = 8x + 4$$

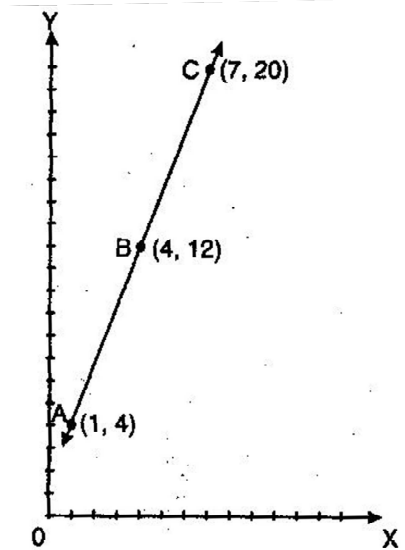
$$\Rightarrow y = \frac{8x}{3} + \frac{4}{3}$$

Table of coordinates:

x	1	4	7
y	4	12	20
Points	A	B	C

Join the points A, B, C.

The straight line AC is the graph of the linear equation $8x - 3y + 4 = 0$.



31. Let S_1 and S_2 be the two squares. Let the side of the square S_2 be x cm in length.

Then the side of square S_1 is $(x + 4)$ cm.

$$\therefore \text{Area of square } S_1 = (x + 4)^2$$

$$\text{And Area of square } S_2 = x^2$$

We are given that, Area of square S_1 + Area of square $S_2 = 400 \text{ cm}^2$

$$\Rightarrow (x + 4)^2 + x^2 = 400 \quad \Rightarrow x^2 + 8x + 16 + x^2 = 400$$

$$\Rightarrow 2x^2 + 8x - 384 = 0 \quad \Rightarrow x^2 + 4x - 192 = 0$$

$$\Rightarrow x^2 + 16x - 12x - 192 = 0 \quad \Rightarrow x(x + 16) - 12(x + 16) = 0$$

$$\Rightarrow (x + 16)(x - 12) = 0 \quad \Rightarrow x = -16, 12$$

As the length of the side of a square cannot be negative, therefore $x = 12$

$$\therefore \text{Side of square } S_1 = x + 4 = 12 + 4 = 16 \text{ cm and side of square } S_2 = 12 \text{ cm.}$$