

Apt i

- 100 balls $\begin{cases} 99 \text{ balls (ok)} & 10 \text{ gm each} \\ 1 \text{ ball (faulty)} & 9 \text{ gm} \end{cases}$

$\Rightarrow$ minimum no. of weighings on a beam balance is $\underline{\hspace{2cm}}$ [Power of 3 will control answer]

$\Rightarrow$ Spring balance $\rightarrow$ Power of 2

CHAPTER - 1 [NUMBER SYSTEM]

- $N = a^p b^q c^r$

$\Rightarrow$ no. of factors = $(p+1)(q+1)(r+1)$

a, b, c are distinct prime nos

p, q, r natural no.

- $N = \cancel{2^3} \times \textcircled{3^2} \times \textcircled{5^3}$

even factors $\rightarrow$ Total - odd

odd factor = $(2+1)(3+1) = 12$

$$N = 2^3 \times 3^2 \times 5^3$$

$$\begin{array}{ccc} \swarrow & \swarrow & \swarrow \\ 0 & 2 & 0 \end{array} \quad \begin{array}{ccc} \swarrow & \swarrow & \swarrow \\ 0 & 2 & 0 \end{array} \quad \begin{array}{ccc} \swarrow & \swarrow & \swarrow \\ 0 & 2 & 0 \end{array}$$

$$2 \times 2 \times 2 = 8 \text{ perfect square}$$

$$N = 2^3 \times 3^2 \times 5^3$$

$$\begin{array}{ccc} \swarrow & \swarrow & \swarrow \\ 0 & 3 & 0 \end{array} \quad \begin{array}{ccc} \swarrow & \swarrow & \swarrow \\ 0 & 0 & 3 \end{array}$$

$$2 \times 1 \times 2 = 4 \text{ perfect cube}$$

CHAPTER [FACTORIAL]

- Highest Power of a no. 'n' in $N!$ is calculate by dividing repeatedly & adding Quotient.

ex:- 100! have how many zeros

or 100! have what highest Power of 5

$$\Rightarrow \frac{100}{5} = 20$$

$$\frac{20}{5} = \frac{4}{24}$$

- If n is not prime, break it in prime, then the no. in shortage will decide the answer

CHAPTER [BASE SYSTEM]

- Que $32 + 24 = 100$ find base

$$\begin{array}{r} 32 \\ 24 \\ \hline 100 \end{array}$$

$$2 + 4 = 0$$

$$\Rightarrow \text{base} = 6$$

$$1 + 3 + 2 = 0$$

$$\Rightarrow \text{base} = 6$$

ex:-

$$\begin{array}{r} 137 \\ 276 \\ \hline 435 \end{array}$$

↓
base = 8

then,

$$\begin{array}{r} \textcircled{1} \\ 731 \\ 672 \\ \hline 1623 \end{array}$$

CHAPTER [REMINDER]

- Rule-1 $\Rightarrow$ If $a = b \text{ mod } c$
 $d = e \text{ mod } c$
 $f = g \text{ mod } c$

[∵ when a is divided by c, b is the remainder]

then, $\frac{a \times d \times f}{c} = \frac{b \times e \times g}{c} \text{ mod } c$

applicable on
+, -, ×, ÷ also

or change by dividing by c

- Rule-2 $\Rightarrow$ If $a \equiv b \pmod{c}$
 $a^n \equiv b^n \pmod{c}$

CHAPTER [Cyclicity]

- | | | | | |
|--------|---|---|---|---|
| | 2 | 3 | 7 | 8 |
| $4n+1$ | 2 | 3 | 7 | 8 |
| $4n+2$ | 4 | 9 | 9 | 4 |
| $4n+3$ | 8 | 7 | 3 | 2 |
| $4n$ | 6 | 1 | 1 | 6 |

	4	9
odd power	4	9
even power	6	1
- 0, 1, 5, 6 have no cyclicity, they appear themselves

CHAPTER [Proportions]

- $a : b :: c : d \Rightarrow \frac{a}{b} = \frac{c}{d}$

means $\swarrow \searrow$
 Extremes

- a, b, c are in continued proportion $\Rightarrow a : b :: b : c$

CHAPTER [MIXTURES]

- Quantity of milk left after n operation $= \left(\frac{a-b}{a}\right)^n \times \text{initial Quantity}$

a = Initial quantity

b = Quantity replaced in each operation

CHAPTER [PERCENTAGE]

- If $R = a \times b \Rightarrow \% \text{ in } R = x + y + \frac{xy}{100}$
 $\downarrow \quad \quad \downarrow$
 $x\% \quad y\%$
 change change

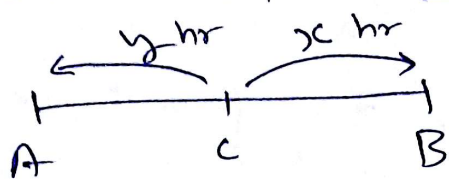
$\Rightarrow$ use -ve sign for reduction

CHAPTER [TIME, SPEED, DISTANCE]

- when N equal distances are covered with diff. speeds $(x_1, x_2, x_3, x_4 \dots)$ then

$$(\text{Speed})_{\text{average}} = \frac{N}{\frac{1}{x_1} + \frac{1}{x_2} + \frac{1}{x_3} \dots \frac{1}{x_n}} \Rightarrow \text{Harmonic mean}$$

- Relative speed concept



$$\frac{S_A}{S_B} = \sqrt{\frac{y}{x}}$$

$\Rightarrow$ A goes towards B & B comes towards A

$\Rightarrow$ meets at C

$\Rightarrow$ A takes x hrs to reach B [After meeting]

$\Rightarrow$ B takes y hrs to reach A [at C]

- Linear races

put values in Ratio, $\frac{A}{B} = \text{given}$, $\frac{B}{C} = \text{give}$

$$\text{then, } \frac{A}{C} = \frac{A}{B} \times \frac{B}{C} = \underline{\hspace{2cm}}$$

- Circular races

$\Rightarrow$ meeting @ SP for 1st time [independent of dir.]

$$\text{Time taken} = A = \text{LCM}(t_A, t_B)$$

$$= \text{LCM}\left(\frac{\text{Circum}}{S_A}, \frac{\text{Circum}}{S_B}\right)$$

$\Rightarrow$ meeting for 1st time anywhere on track

$$\text{Time taken} = \frac{\text{Circum}}{\text{relative Speed}} = B$$

$$\Rightarrow \text{Total \& diff. meeting points} = \frac{A}{B}$$

CHAPTER [Calendar]

- Every multiple of 4 is L.Y.
- Every century is not L.Y.
- Every 4th century is L.Y.
ex:- 1600, 2000, 2400
- 1 normal year $\Rightarrow$ 1 odd day
- 1 leap year $\Rightarrow$ 2 odd day
- 100 years $\Rightarrow$ 5 odd day [when observed century is not a L.Y.]
- upto 1600, 2000, 2400 $\Rightarrow$ 0 odd day
- upto 1900 $\rightarrow$ 1 odd day

odds	Day
1	mon
2	Tues
3	wed
4	Thurs
5	Fri
6	Sat
0	Sun

CHAPTER [ALGEBRA]

- If $x + y = \text{const.}$
then, $xy \Rightarrow$ maximum when $x = y$
- If $x + y + z = \text{const}$
 $xyz \Rightarrow \text{max. when } x = y = z$
- for All $x, y, z > 0$
 $AM > GM > HM$
- Geometric Progression

$$a, ar, ar^2, \dots, ar^{n-1}$$

$$S_n = \frac{a(1-r^n)}{1-r} \Rightarrow |r| < 1$$

$$S_n = \frac{a(r^n-1)}{r-1} \Rightarrow |r| > 1$$

$$S_{\infty} = \frac{a}{1-r} \Rightarrow r < 1$$

- Arithmetic Progression (AP)

$$a, a+d, a+2d, \dots, [a+(n-1)d]$$

$$S_n = \frac{n}{2} [2a + (n-1)d] = \frac{n}{2} (a+l)$$

- $\Sigma n = \frac{n(n+1)}{2}$ [when $T_n = n$]

$$\Sigma n^2 = \frac{n(n+1)(2n+1)}{6}$$
 [when $T_n = n^2$]

$$\Sigma n^3 = \left[\frac{n(n+1)}{2} \right]^2$$
 [when $T_n = n^3$]

$$\Sigma \Sigma n = \frac{n(n+1)(n+2)}{6}$$
 [$\because$ when $T_n = \Sigma n = \frac{n(n+1)}{2}$]

CHAPTER [CUBES]

Total blocks = $l \times b \times h$ [$\because$ Dipped in ink]

3S painted = 8

2s painted = $4 [(l-2) + (b-2) + (h-2)]$

1s painted = $2 [(l-2)(b-2) + (b-2)(h-2) + (h-2)(l-2)]$

0s painted = $(l-2)(b-2)(h-2)$

CHAPTER [Permutation & Combination]

- ${}^n P_r = \frac{n!}{(n-r)!}$; ${}^n C_r = \frac{n!}{r!(n-r)!}$

- whole no. solun $\Rightarrow$ when '0' allocations is allowed
'n' identical objects distributed among 'r' people
can be done in
ways = $\binom{n+r-1}{r-1}$

- Natural no. Soluⁿ $\Rightarrow$ when '0' allocation not allowed
 $\Rightarrow$ allote the required no. to each as per question
 $\Rightarrow$ find new 'n'

$$\text{i.e. } n_{\text{new}} = n' = n - (\text{sum of all allocation})$$

$$\text{ways} = {}^{n' + r - 1}C_{r-1}$$

- 12 points, How many lines can be formed

$$\Rightarrow {}^{12}C_2$$

if 5 are collinear

$$\Rightarrow {}^{12}C_2 - {}^5C_2 + 1$$

- 12 points, ~~are~~ How many Δ s

$$\Rightarrow {}^{12}C_3$$

if 5 are collinear points

$$\Rightarrow {}^{12}C_3 - {}^5C_3$$

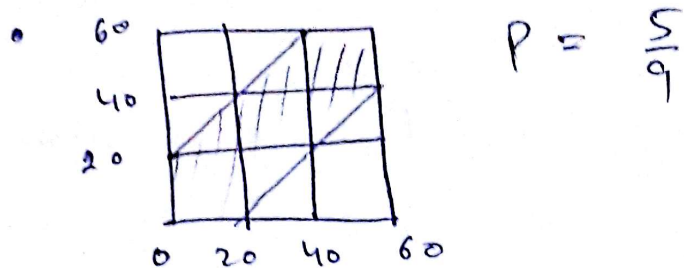
Chess board

- $n \times n$ board
- no. of squares = $\sum n^2$
- no. of rectangles = $\sum n^3$
- no of types of rectangle = $\sum n$

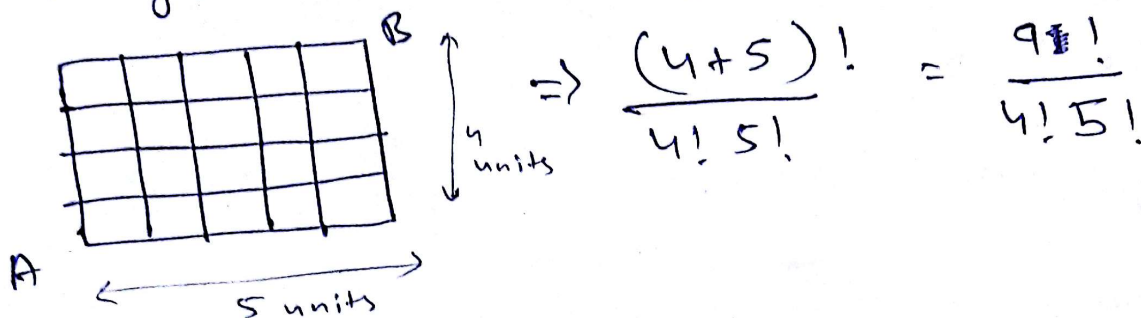
Ques: All five digit no. are formed from 5 single digit natural no. without repetition then, sum of all those no.s = ?

$$\Rightarrow \text{Sum} = \underbrace{(n-1)!}_{\substack{\downarrow \\ \text{no. of} \\ \text{digits}}} \times \underbrace{11111}_{\substack{\downarrow \\ \text{equal to} \\ \text{no. of digits}}} \times \underbrace{(\sum d)}_{\substack{\downarrow \\ \text{Sum of} \\ \text{digits}}}$$

CHAPTER (Probability)



- no. of shortest distance from A $\rightarrow$ B



CHAPTER [BLOOD RELATIONS]

1. family hierarchy tree
 2. Keep on marking gender
 3. Keep on writing relation
 4. A^+ $\rightarrow$ for male
 A^- $\rightarrow$ for female
 5. Don't judge gender by name
- Bhanja, Bhateja $\Rightarrow$ nephew
 - Bhanji, Bhatiji $\Rightarrow$ niece
 - Relation from mother side $\Rightarrow$ maternal
 - Relation from father side $\Rightarrow$ paternal

Clock

- 12 hrs $\rightarrow$ 11 coincides
12 hrs $\rightarrow$ 11 opposites
12 hrs $\rightarrow$ 22 right angles

CHAPTER [Simple interest & compound interest]

- $SI = \frac{PRT}{100}$
- $CA = P \left(1 + \frac{R}{100}\right)^n$

eg:- Amount is compounded half yearly

$$R = 10\% \text{ per annum} ; T = 2 \text{ years}$$

$$\text{then } CA = P \left(1 + \frac{5}{100} \right)^{4 \leftarrow \times 2}$$

- $(CI - SI)_{\text{upto 1 year}} = 0$
- $(CI - SI)_{\text{upto 2 year}} = P \left(\frac{R}{100} \right)^2$
- $(CI - SI)_{\text{upto 3 year}} = P \left(\frac{R}{100} \right)^3 + 3P \left(\frac{R}{100} \right)^2$

Miscellaneous

- $Ax^3 + Bx^2 + Cx + D = 0$

$$\alpha + \beta + \gamma = -\frac{B}{A}$$

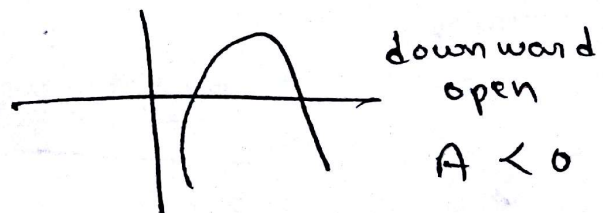
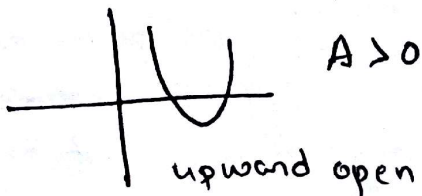
$$\alpha\beta + \beta\gamma + \gamma\alpha = +\frac{C}{A}$$

$$\alpha\beta\gamma = -\frac{D}{A}$$

+
-
+
...

Start with -ve
and move alternatively

- $y = Ax^2 + Bx + C = 0$ is a parabola



- $n(A \cup B \cup C) = + (n(A) + n(B) + n(C))$
 $- (n(A \cap B) + n(B \cap C) + n(C \cap A))$
 $+ (n(A \cap B \cap C))$
 $- \vdots$
 $+ \vdots$