

Natural numbers and Whole numbers

- The collection of all counting numbers is known as **natural numbers**.

These are 1, 2, 3, 4 ... and so on.

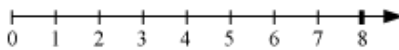
- All natural numbers along with zero are called **whole numbers**.

These are 0, 1, 2, 3, 4 ... and so on.

- All natural numbers are whole numbers, but all whole numbers are not natural numbers.
- We can write a natural number using 10 symbols 0, 1, 2, 3, 4, 5, 6, 7, 8, and 9. Each of such symbols is called a **digit** or a **figure**.

- **Number line:**

To draw a number line, we take a line and mark a point on it, labelling it 0. Then, we mark the points to the right of zero at equal intervals and label them as 1, 2, 3 ..., as follows:

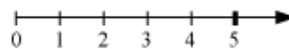


On the number line, we can say that out of any two whole numbers, the number on the right of the other number is greater.

Example: Place predecessor of 6 on the number line.

Solution:

The predecessor of 6 is 5. On the number line, we can show 5 as follows:



- According to fundamental theorem of arithmetic, a number can be represented as the product of primes having a unique factorisation.

Example:

Check whether 15^n is divisible by 10 or not for any natural number n . Justify your answer.

Solution:

A number is divisible by 10 if it is divisible by both 2 and 5.

$$15^n = (3 \cdot 5)^n$$

3 and 5 are the only primes that occur in the factorisation of 15^n

By uniqueness of fundamental theorem of arithmetic, there is no other prime except 3 and 5 in the factorisation of 15^n .

2 does not occur in the factorisation of 15^n .

Hence, 15^n is not divisible by 10.

- If we subtract 1 from a whole number, then we will get its **predecessor** and if we add 1 to a whole number, then we will find its **successor**.

For example, the predecessor of 15 is $15 - 1 = 14$ and its successor is $15 + 1 = 16$.

- Each whole number has a successor. All whole numbers, except zero, has a predecessor.
- **Closure Property of whole numbers:**
 - Whole numbers are closed under addition. For example, the sum of whole numbers 3 and 8 is 11 ($3 + 8 = 11$), which is again a whole number.
 - Whole numbers are closed under multiplication. For example, the multiplication of whole numbers 4 and 7 is 28 ($4 \times 7 = 28$), which is again a whole number.
 - Whole numbers are not closed under subtraction. For example, $5 - 2 = 3$ is a whole number, but $1 - 2 = -1$ is not a whole number.
 - Whole numbers are not closed under division. For example, $98 \div 4 = 2$ is a whole number, but $2 \div 5 = \frac{2}{5}$ is not a whole number.

- **Properties of whole numbers:**

We can add or multiply two whole numbers in any order, that is, $12 + 5 = 5 + 12 = 17$ and $9 \times 8 = 8 \times 9 = 72$.

This property of addition and multiplication of whole numbers is known as **commutative**.

Addition and multiplication of whole numbers are **associative**.

For example: $(17 + 19) + 25 = 17 + (19 + 25) = 61$.

Similarly, $(6 \times 13) \times 19 = 6 \times (13 \times 19) = 1482$.

These properties help some mathematical calculations easier.

Example: Find the value of $4 \times 17 \times 25$.

Solution:

$$\begin{aligned} 4 \times 17 \times 25 &= 4 \times 25 \times 17 \quad (\text{commutative over multiplication}) \\ &= (4 \times 25) \times 17 \\ &= 100 \times 17 \\ &= 1700 \end{aligned}$$

- **Distributive property of whole numbers for multiplication over addition:**

$$a \times (b + c) = a \times b + a \times c$$

The property also holds true for multiplication over subtraction.

This property also helps in making mathematical calculations easier.

Example:

Simplify $38 \times 68 + 32 \times 38$

Solution:

$$\begin{aligned} 38 \times 68 + 32 \times 38 &= 38 \times 68 + 38 \times 32 \quad (\text{Commutative property}) \\ &= 38 \times (68 + 32) \quad (\text{Distributive property}) \\ &= 38 \times 100 \\ &= 3800 \end{aligned}$$

- Addition of any whole number to zero gives the same whole number. Therefore, zero is the **additive identity** of whole numbers.

For example, $5 + 0 = 5$, $9 + 0 = 9$.

- Multiplication of any whole number with 1 gives the same whole number. Therefore, 1 is the **multiplicative identity** of whole numbers.

For example, $9 \times 1 = 9$.

- Multiplication of any whole number with zero, gives zero as the result.

For example, $5 \times 0 = 0$