

Topics : Wave on a String , Circular Motion, Relative Motion

Type of Questions

Single choice Objective ('-1' negative marking) Q.1 to Q.3

(3 marks, 3 min.)

M.M., Min.

[9, 9]

Multiple choice objective ('-1' negative marking) Q.4

(4 marks, 4 min.)

[4, 4]

Comprehension ('-1' negative marking) Q.5 to Q.7

(3 marks, 3 min.)

[9, 9]

- Three waves producing displacement in the same direction of same frequency and of amplitudes $10\mu\text{m}$, $4\mu\text{m}$ and $7\mu\text{m}$ arrive at a point with successive phase difference of $\pi/2$. The amplitude of the resultant wave is
(A) $2\mu\text{m}$ (B) $7\mu\text{m}$ (C) $5\mu\text{m}$ (D) 1
- A string fixed at both ends has consecutive standing wave modes for which the distances between adjacent nodes are 18 cm and 16 cm respectively. The length of the string is -
(A) 144 cm (B) 152 cm (C) 176 cm (D) 200 cm

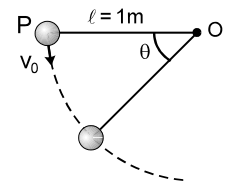
- The sphere at P is given a downward velocity v_0 and swings in a vertical plane at the end of a rope of $\ell = 1\text{m}$ attached to a support at O. The rope breaks at angle 30° from horizontal, knowing that it can withstand a maximum tension equal to three times the weight of the sphere. Then the value of v_0 will be :
($g = \pi^2 \text{ m/s}^2$)

(A) $\frac{g}{2} \text{ m/s}$

(B) $\frac{2g}{3} \text{ m/s}$

(C) $\sqrt{\frac{3g}{2}} \text{ m/s}$

(D) $\frac{g}{3} \text{ m/s}$



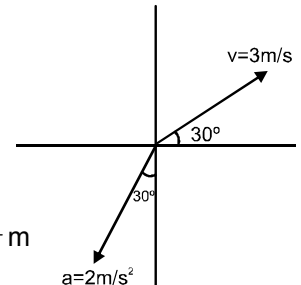
- Initial velocity and acceleration of a particle are as shown in the figure. Acceleration vector of particle remain constant. Then radius of curvature of path of particle :

(A) is 9m initially

(B) is $\frac{9}{\sqrt{3}} \text{ m}$ initially

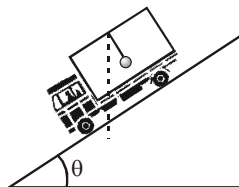
(C) will have minimum value of $\frac{9}{8} \text{ m}$

(D) will have minimum value $\frac{3}{8} \text{ m}$



COMPREHENSION

A van accelerates uniformly down an inclined hill going from rest to 30 m/s in 6 s. During the acceleration, a toy of mass $m = 0.1 \text{ kg}$ hangs by a light string from the van's ceiling. The acceleration is such that string remains perpendicular to the ceiling. (Take $g = 10 \text{ m/s}^2$)



- The angle θ of the incline is :
(A) 30° (B) 60° (C) 90° (D) 45°
- The tension in the string is
(A) 1.0 N (B) 0.5 N (C) $\frac{\sqrt{3}}{2} \text{ N}$ (D) $\sqrt{3} \text{ N}$
- The friction force on the van is
(A) Zero (B) $mg \cos\theta$ (C) $mg \sin\theta$ (D) $mg \tan\theta$

Answers Key

DPP NO. - 81

1. (C) 2. (A) 3. (C) 4. (A)(C)
5. (A) 6. (C) 7. (A)

Hint & Solutions

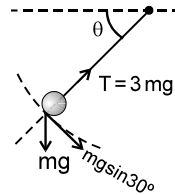
DPP NO. - 81

2. $L = \frac{m\lambda_1}{2}$ and $L(m+1) = \frac{\lambda_2}{2}$

Where m is no. of harmonic
 $m \cdot 36 = (m+1) 32$
 $\Rightarrow m = 8$
 $L = 8 \times 18 = 144 \text{ cm}$

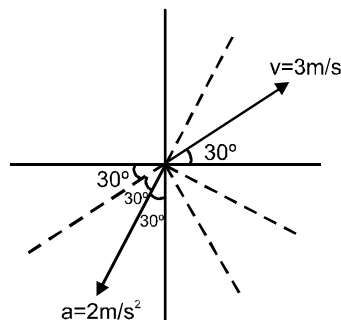
3. $T - mg \sin \theta = \frac{mv^2}{R}$
 $\Rightarrow 3mg - mg \sin 30^\circ$

$= \frac{m(u_0^2 + 2gl \sin 30^\circ)}{l}$



$\therefore u_0 = \sqrt{3g/2}$

4. Initially $ROC = \frac{v^2}{a \sin 30^\circ} = \frac{9}{1} m$



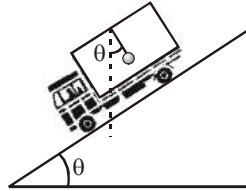
For minimum $ROC = \frac{(v \sin 30^\circ)^2}{a} = \frac{9}{8} m$.

5. to 7 Acceleration of the van = $\frac{30}{6} = 5 \text{ m/s}^2$

$$g \sin \theta = a$$

$$\Rightarrow \sin \theta = \frac{1}{2}$$

$$\Rightarrow \theta = 30^\circ$$



6. Tension

$$T = mg \cos \theta = \frac{\sqrt{3}}{2} N$$

7. Since acceleration of the van is $g \sin \theta$, there is no friction.