# Class X Session 2023-24 Subject - Mathematics (Standard) Sample Question Paper - 1

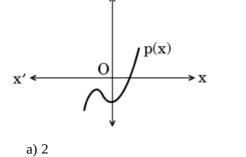
## **Time Allowed: 3 hours**

#### **General Instructions:**

- 1. This Question Paper has 5 Sections A, B, C, D and E.
- 2. Section A has 20 MCQs carrying 1 mark each
- 3. Section B has 5 questions carrying 02 marks each.
- 4. Section C has 6 questions carrying 03 marks each.
- 5. Section D has 4 questions carrying 05 marks each.
- 6. Section E has 3 case based integrated units of assessment (04 marks each) with sub- parts of the values of 1, 1 and 2 marks each respectively.
- 7. All Questions are compulsory. However, an internal choice in 2 Qs of 5 marks, 2 Qs of 3 marks and 2 Questions of 2 marks has been provided. An internal choice has been provided in the 2marks questions of Section E
- 8. Draw neat figures wherever required. Take  $\pi = \frac{22}{7}$  wherever required if not stated.

#### Section A

- 1. The HCF and the LCM of 12, 21, 15 respectively are:
  - a) 3, 140 b) 420, 3
  - c) 12, 420 d) 3, 420
- 2. Number of zeroes of the polynomial p(x) shown in the Figure, are:



c) 0

3. A system of linear equations is said to be consistent, if it has

b) 1

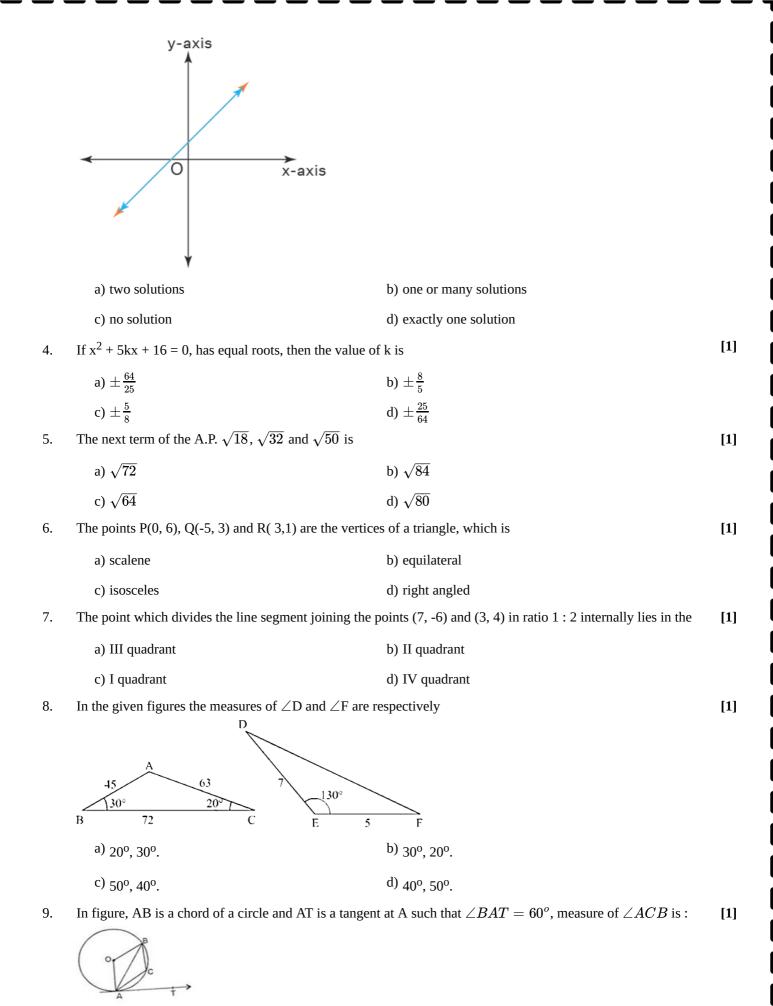
d) 3

Maximum Marks: 80

[1]

[1]

[1]





b) 150°

	c) 90°	d) 110°	
10.	In a right triangle ABC, right angled at triangle (in cm) is	B, BC = 12 cm and AB = 5 cm. The radius of the circle inscribed in the	[1]
	a) 4	b) 1	
	c) 2	d) 3	
11.	$9 \sec^2 A - 9 \tan^2 A =$		[1]
	a) 1	b) 9	
	c) 0	d) 8	
12.	The value of $(1 + \tan^2 \theta)(1 - \sin \theta)(1 + \sin \theta)$	in $ heta$ ) is	[1]
	a) $\sqrt{2}$	b) 1	
	c) 2	d) 0	
13.	The upper part of a tree broken by the v	vindfalls to the ground without being detached. The top of the broken part	[1]
	touches the ground at an angle of $30^{\circ}$ at	t a point 8m from the foot of the tree. The original height of the tree is	
	a) $8\sqrt{3}$ m	b) $24\sqrt{3}$ m	
	c) 8 m	d) 24 m	
14.	A chord of a circle of radius 10 cm subt = 3.14) is	tends a right angle at the centre. The area of the minor segments (given, $\pi$	[1]
	a) 32.5 cm <sup>2</sup>	b) 34.5 cm <sup>2</sup>	
	c) 30.5 cm <sup>2</sup>	d) 28.5 cm <sup>2</sup>	
15.	If AB is a chord of a circle of length $5_{\mathrm{V}}$	$/\overline{3}$ cm with centre O and radius 5 cm, then area of sector OAB is	[1]
	a) $rac{25\pi}{3}\mathrm{cm}^2$	b) $25\pi\mathrm{cm}^2$	
	c) $rac{8\pi}{3}cm^2$	d) $\frac{3\pi}{8}$ cm <sup>2</sup>	
16.		25 are placed in a box and mixed thoroughly and one card is drawn at hat the number on the card is a multiple of 3 and 5 is	[1]
	a) $\frac{12}{25}$	b) $\frac{4}{25}$	
	c) $\frac{1}{25}$	d) $\frac{8}{25}$	
17.	Two dice are rolled together. The proba	bility that the sum of the numbers that appeared is 9, is:	[1]
	a) $\frac{5}{9}$	b) $\frac{1}{9}$	
	c) $\frac{4}{9}$	d) $\frac{2}{9}$	
18.	The mean of the first 10 prime numbers	sis	[1]
	a) 129	b) 1.29	
	c) 12.9	d) 11.9	
19.	Assertion (A): If we join two hemisphe	eres of same radius along their bases, then we get a sphere.	[1]
	<b>Reason (R):</b> A tank is made of the shap	be of a cylinder with a hemispherical depression at one end. The height of	

the cylinder is 1.45 m and radius is 30 cm. The total surface area of the tank is 3.3  $\ensuremath{m^2}\xspace$ 

- a) Both A and R are true and R is the correct explanation of A.
- b) Both A and R are true but R is not the correct explanation of A.

[2]

[2]

d) A is false but R is true.

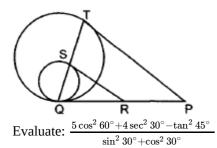
c) A is true but R is false.

20. **Assertion (A):** The sum of the first n terms of an AP is given by  $S_n = 3n^2 - 4n$ . Then its nth term  $a_n = 6n - 7$  [1] **Reason (R):** nth term of an AP, whose sum to n terms is  $S_n$ , is given by  $a_n = S_n - S_{n-1}$ 

a) Both A and R are true and R is the correct	b) Both A and R are true but R is not the
explanation of A.	correct explanation of A.
c) A is true but R is false.	d) A is false but R is true.

## Section B

- 21. Define HCF of two positive integers and find the HCF of the pair of numbers: 105 and 120. [2]
- 22. If ABC and DEF are similar triangles such that  $\angle A = 57^{\circ}$  and  $\angle E = 73^{\circ}$ , what is the measure of  $\angle C$ ? [2]
- In the following figure, PQ is the common tangent to both the circles. SR and PT are tangent to both the circles. [2]If SR = 4 cm, PT = 7 cm, then find RP.



24.

OR

Prove that:  $(\sqrt{3} + 1) (3 - \cot 30^\circ) = \tan^3 60^\circ - 2 \tan 60^\circ$ 

25. What is the angle subtended at the centre of a circle of radius 6 cm by an arc of length  $3\pi$  cm?

OR

Write the formula for the area of a segment in a circle of radius r given that the sector angle is  $\theta$  (in degrees).

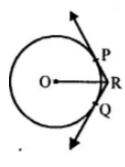
## Section C

- 26. Amita, Suneha and Raghav start preparing cards for greeting each person of an old age home on new year. In order to complete one card, they take 10, 16 and 20 minutes respectively. If all of them started together, after what time will they start preparing a new card together ? Why do you think there is a need to show elders that the young generation cares for them and remembers the contribution made by them in the prime of their life?
- 27. If one root of the quadratic polynomial  $2x^2 3x + p$  is 3, find the other root. Also, find the value of p. [3]
- 28. Draw the Graphs of the equations x = 3, x = 5 and 2x y 4 = 0. Also find the area of the quadrilateral formed [3] by the lines and the x-axis.

OR

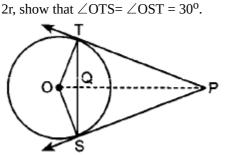
Check graphically whether the pair of equations x + 3y = 6 and 2x - 3y = 12 is consistent. If so, solve them graphically.

29. In the given figure, two tangents RQ and RP are drawn from an external point R to the circle with centre O. If (3)  $\angle$  PRQ = 120°, then prove that OR = PR + RQ.



OR

In figure, from an external point P, two tangents PT and PS are drawn to a circle with centre O and radius r. If OP =



30. Find the acute angle  $\theta$ , when  $\frac{\cos \theta - \sin \theta}{\cos \theta + \sin \theta} = \frac{1 - \sqrt{3}}{1 + \sqrt{3}}$ .

31. Find the median of the following frequency distribution:

	Marks	0 - 10	10 - 20	20 - 30	30 - 40	40 - 50
Number of students         6         16         30         9         4	Number of students	6	16	30	9	4

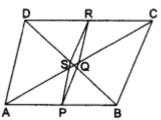
#### Section D

32. At t minutes past 2 p.m, the time needed by the minute hand of a clock to show 3 p.m. was found to be 3 minutes [5] less than  $\frac{t^2}{4}$  minutes. Find t.

OR

A cottage industry produces a certain number of pottery articles in a day. It was observed on a particular day that cost of production of each article (in rupees) was 3 more than twice the number of articles produced on that day. If, the total cost of production on that day was ₹ 90, find the number of articles produced and the cost of each article.

33. ABCD is a quadrilateral in which AD = BC. If P, Q, R, S be the midpoints of AB, AC, CD and BD respectively, [5] show that PQRS is a rhombus.



34. A tent is of the shape of a right circular cylinder upto a height of 3 metres and then becomes a right circular cone **[5]** with a maximum height of 13.5 metres above the ground. Calculate the cost of painting the inner side of the tent at the rate of Rs.2 per square metre, if the radius of the base is 14 metres.

OR

A tent is in the form of a right circular cylinder surmounted by a cone. The diameter of the base of the cylinder or the cone is 24 m. The height of the cylinder is 11 m. If the vertex of the cone is 16 m above the ground, find the area of the canvas required for making the tent. (Use  $\pi = \frac{22}{7}$ )

35. Find the mean from the following frequency distribution of marks at a test in statistics:

[5]

[3] [3]

Marks (x):	5	10	15	20	25	30	35	40	45	50
No. of students (f):	15	50	80	76	72	45	39	9	8	6

# Section E

# 36. **Read the text carefully and answer the questions:**

Your elder brother wants to buy a car and plans to take loan from a bank for his car. He repays his total loan of ₹

1,18,000 by paying every month starting with the first instalment of ₹ 1000. If he increases the instalment by ₹ 100 every month , answer the following:



- (i) Find the amount paid by him in 30<sup>th</sup> installment.
- (ii) Find the amount paid by him in 30 installments.

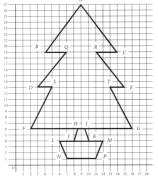
# OR

Find the  $10^{\text{th}}$  installment, if the  $1^{\text{st}}$  installment is of ₹ 2000.

(iii) If total installments are 40 then amount paid in the last installment?

# 37. **Read the text carefully and answer the questions:**

The design of Christmas tree is shown in the following graph:



- (i) What is the distance of point A from x-axis?
- (ii) What is the Length of BC?

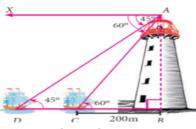
# OR

What is the perimeter of its trunk LMPN?

(iii) What is the Length of FG?

# 38. **Read the text carefully and answer the questions:**

A man is watching a boat speeding away from the top of a tower. The boat makes an angle of depression of 60° with the man's eye when at a distance of 200 m from the tower. After 10 seconds, the angle of depression becomes 45°.



(i) What is the approximate speed of the boat (in km/hr), assuming that it is sailing in still water?

[4]

[4]

[4]

(ii) How far is the boat when the angle is 45°?

# OR

As the boat moves away from the tower, angle of depression will decrease/increase?

(iii) What is the height of tower?

# Solution

## Section A

#### 1.

(d) 3, 420 Explanation: We have, 12 = 2 × 2 × 3 21 = 3 × 7 15 = 5 × 3 HCF = 3 and L.C.M = 2 × 2 × 3 × 5 × 7 = 420

#### 2.

**(b)** 1

**Explanation:** We see that the graph cuts the x-axis at 1 point which implies p(x) is zero at this 1 point only.

# 3.

# (b) one or many solutions

**Explanation:** A system of linear equations is said to be consistent if it has at least one solution or can have many solutions. If a consistent system has an infinite number of solutions, it is dependent. When you graph the equations, both equations represent the same line. If a system has no solution, it is said to be inconsistent. The graphs of the lines do not intersect, so the graphs are parallel and there is no solution.

4.

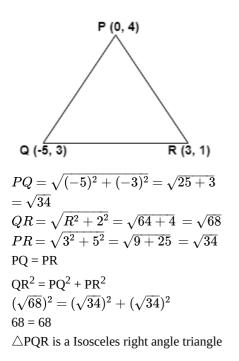
(b)  $\pm \frac{8}{5}$ Explanation: Here, a = 1, b = 5k, c = 16 If  $x^2 + 5kx + 16 = 0$  has equal roots, then, b<sup>2</sup> - 4ac = 0  $\Rightarrow (5k)^2 - 4 \times 1 \times 16 = 0$   $\Rightarrow 25k^2 - 64 = 0$   $\Rightarrow 25k^2 = 64$   $\Rightarrow k^2 = \frac{64}{25}$   $\Rightarrow k = \pm \frac{8}{5}$ (a)  $\sqrt{72}$ Explanation: Given:  $\sqrt{18}$ ,  $\sqrt{32}$ ,  $\sqrt{50}$   $\Rightarrow 3\sqrt{2}$ ,  $4\sqrt{2}$ ,  $5\sqrt{2}$   $\therefore d = 4\sqrt{2} - 3\sqrt{2} = \sqrt{2}$ Therefore, next term is  $5\sqrt{2} + \sqrt{2}$ 

6.

5.

(d) right angled **Explanation**:

 $= 6\sqrt{2} = \sqrt{72}$ 





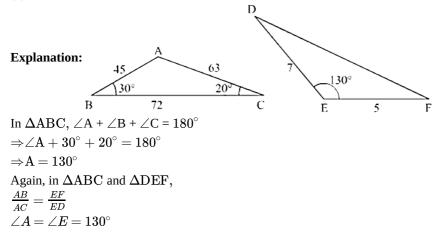
#### (d) IV quadrant

**Explanation:** Let A and B be the joining point and P is the dividing point; Let's assume the co - ordinates of point P = x and y By using Section formula; x coordinate of point P will be  $x = \frac{mx_2 + nx_1}{m+n}$  and

y co - ordinate of point P will be  $y = \frac{my_2 + ny_1}{m+n}$   $\therefore x = \frac{1(3) + 2(7)}{1+2}$   $y = \frac{1(4) + 2(-6)}{1+2}$ Given that,  $x_1 = 7, y_1 = -6,$   $x_2 = 3, y_2 = 4$  m = 1 and n = 2  $x = \frac{3+14}{3} = \frac{17}{3}$   $y = \frac{4-12}{3} = -\frac{8}{3}$ So,  $(x, y) = \frac{17}{3}, -\frac{8}{3}$  lies in IV quadrant.

[Since, in IV quadrant, x - coordinate is positive and y - coordinate is negative]

8. **(a)** 20°, 30°.



 $\triangle ABC \sim \Delta EFD$  (SAS Similarity)  $\therefore \angle F = \angle B = 30^{\circ}$  $\angle D = \angle C = 20^{\circ}$ 

# 9. **(a)** 120°

**Explanation:** Since OA is perpendicular to AT, then  $\angle OAT = 90^{\circ}$  $\Rightarrow \angle OAB + \angle BAT = 90^{\circ}$  $\Rightarrow \angle OAB + 60^{\circ} = 90^{\circ} \Rightarrow \angle OAB = 30^{\circ}$  $\therefore \angle OAB = \angle OBA = 30^{\circ}$  [Angles opposite to radii]  $\therefore \angle AOB = 180^{\circ} - (30^{\circ} + 30^{\circ}) = 120^{\circ}$  [Angle sum property of a triangle]

 $\therefore \text{Reflex} \angle \text{AOB} = 360^{\circ} - 120^{\circ} = 240^{\circ}$ 

Now, since the arc AB of a circle makes an angle which is equal to twice the angle ACB subtended by it at the circumference.  $\therefore$  Reflex $\angle$ AOB = 2 $\angle$ ACB

 $\Rightarrow$ 240° = 2 $\angle$ ACB

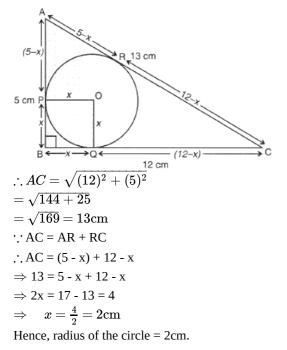
 $\Rightarrow \angle ACB = 120^{\circ}$ 

#### 10.

**(c)** 2

# **Explanation:**

Here, AB = 5cm, BC = 12 and  $\angle B = 90^{\circ}$ Let the radius of circle be x cm



# 11.

**(b)** 9

**Explanation:** 9 ( $\sec^2 A - \tan^2 A$ ) = 9 × 1 ( $\sec^2 A - \tan^2 A$ =1) = 9

# 12.

**(b)** 1

**Explanation:** Given:  $(1 + \tan^2\theta)(1 - \sin\theta)(1 + \sin\theta)$ =  $(\sec^2\theta)(1 - \sin^2\theta)$ =  $(\sec^2\theta)(\cos^2\theta)$ =  $\frac{1}{\cos^2\theta} \times \cos^2\theta = 1$ 

13. **(a)**  $8\sqrt{3}$  m **Explanation:** In right triangle ABC,  $\cos 30^\circ = \frac{BC}{AC}$ 

D (Top of the tree)  
B  
(Foot of 
$$\frac{8}{9}$$
 m  
the tree) ground  
 $\Rightarrow \frac{\sqrt{3}}{2} = \frac{8}{AC} \Rightarrow AC = \frac{16}{\sqrt{3}}$  m  
Again,  $\tan 30^{\circ} = \frac{AB}{BC}$   
 $\Rightarrow \frac{1}{\sqrt{3}} = \frac{AB}{8} \Rightarrow AB = \frac{8}{\sqrt{3}}$  m  
 $\therefore$  Height of the tree = AB + AC =  $\frac{8}{\sqrt{3}} + \frac{16}{\sqrt{3}} = \frac{24}{\sqrt{3}}$   
 $= \frac{24}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} = 8\sqrt{3}$  m  
The height of the tree is  $8\sqrt{3}$ m.

14.

# (**d**) 28.5 cm<sup>2</sup>

# **Explanation:**

ar(minor segment A C B A)=ar(sector O A C B O) - ar( $\Delta OAB$ )

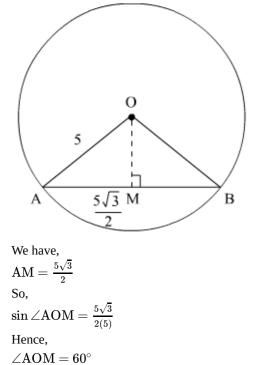
$$= \left(\frac{\pi r^{2\theta}}{360} - \frac{1}{2} \times r \times r\right)$$

$$= \left(\frac{3.14 \times 10 \times 10 \times 90}{360} - \frac{1}{2} \times 10 \times 10\right) \text{ cm}^{2}$$

$$= (78.5 - 50) \text{ cm}^{2} = 28.5 \text{ cm}^{2}$$

15. **(a)**  $\frac{25\pi}{3}$  cm<sup>2</sup>

**Explanation:** We have to find the area of the sector OAB.



 $\Rightarrow \angle AOB = 120^{\circ}$ Area of sector AOB =  $\frac{120}{360} \times \pi \times 5^2 \text{ cm}^2 = \frac{25\pi}{3} \text{ cm}^2$ 

16.

# 6

(c)  $\frac{1}{25}$  **Explanation:** Multiples of 3 = 3, 6, 9, 12, 15, 18, 21, 24 Multiples of 5 = 5, 10, 15, 20, 25 Number of possible outcomes (multiple of 3 and 5) = {15} = 1 Number of Total outcomes = 25  $\therefore$  Required Probability =  $\frac{1}{25}$ 

# 17.

# **(b)** $\frac{1}{9}$

**Explanation:** Number of possible outcomes = {(3, 6), (5, 4), (4, 5), (6, 3)} = 4 Number of Total outcomes =  $6 \times 6 = 36$  $\therefore$  Required Probability =  $\frac{4}{36} = \frac{1}{9}$ 

## 18.

(c) 12.9 Explanation: The first 10 prime numbers are 2, 3, 5, 7, 11, 13, 17, 19, 23, 29  $\therefore \text{ Mean} = \frac{\text{Sum of first 10 prime numbers}}{10} = \frac{2+3+5+7+11+13+17+19+23+29}{10} = \frac{129}{10} = 12.9$ 

19.

**(b)** Both A and R are true but R is not the correct explanation of A. **Explanation:** Both A and R are true but R is not the correct explanation of A.

20. **(a)** Both A and R are true and R is the correct explanation of A. **Explanation:** nth term of an AP be  $a_n = S_n - S_{n-1}$ 

$$a_n = 3n^2 - 4n - 3(n - 1)^2 + 4(n - 1)$$

a<sub>n</sub> = 6n - 7

So, both A and R are true and R is the correct explanation of A.

# Section B

21. HCF of two or more numbers is the greatest common factor which can divide all the numbers exactly. On applying Euclid's division lemma on 120 and 105 we get

 $120 = 105 \times 1 + 15.$ 

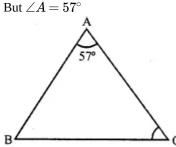
Since remainder ≠ 0, apply division lemma on divisor 105 and remainder 15

 $105 = 15 \times 7 + 0.$ 

Therefore, H.C.F. of 105 and 120 = 15.

22. It is given that  $\Delta ABC \sim \Delta DEF$ 

Their corresponding angles are equal,  $\angle A = \angle D, \angle B = \angle E$  and  $\angle C = \angle F$ 

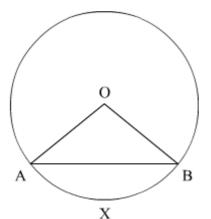


D 73° E4  $\therefore \angle D = 57^{\circ}$  $\therefore \angle \mathrm{E} = 73^{\circ}$  $\therefore \angle B = 73^{\circ}$ Now in  $\triangle ABC$  $\angle A + \angle B + \angle C = 180^{\circ}$  (Sum of angles of a triangle)  $\Rightarrow 57^{\circ} + 73^{\circ} + \angle C = 180^{\circ}$  $\Rightarrow 130^{\circ} + \angle C = 180^{\circ} \Rightarrow \angle C = 180^{\circ} - 130^{\circ}$  $\therefore \angle C = 50^{\circ}$ 23. ∵ PT = PQ .:. PQ = 7 cm Also SR = QR ∴ QR =4 Now, RP = PQ - QR = 7 - 4 = 3 cm24. Given:  $\frac{5\cos^2 60^\circ + 4\sec^2 30^\circ - \tan^2 45^\circ}{12}$ Ven:  $\frac{5}{\sin^2 30^\circ + \cos^2 30^\circ}$  $5\left(\frac{1}{2}\right)^2 + 4\left(\frac{2}{\sqrt{3}}\right)^2 - (1)^2$  $\left(\frac{1}{2}\right)^2 + \left(\frac{\sqrt{3}}{2}\right)$  $5 \times \frac{1}{4} + 4 \times$  $= \frac{\frac{1}{4} + \frac{1}{4} + \frac{1}{4}}{\frac{16}{3} - \frac{1}{3}}$ =  $\frac{\frac{1+3}{4}}{15+64-12}$  $\frac{\frac{1+6}{12}}{\frac{4}{4}}$ 67  $= \frac{\frac{61}{12}}{\frac{1}{12}}$  $= \frac{67}{12}$ We have to prove that:  $(\sqrt{3} + 1) (3 - \cot 30^\circ) = \tan^3 60^\circ - 2 \tan 60^\circ$ Here, LHS =  $(\sqrt{3} + 1)(3 - \cot 30^\circ)$  $=(\sqrt{3}+1)(3-\sqrt{3})$  $=\sqrt{3}(3-\sqrt{3})+1(3-\sqrt{3})$  $=3\sqrt{3}-3+3-\sqrt{3}$  $=2\sqrt{3}$  $RHS = \tan^3 60^\circ - 2\sin 60^\circ$  $=(\sqrt{3})^3-2 imesrac{\sqrt{3}}{2}$  $=3\sqrt{3}-\sqrt{3}$  $=2\sqrt{3}$  $\Rightarrow$  LHS = RHS Hence, proved. 25. We have R = 6 cmLength of the arc =  $3\pi$ cm as we know that arc length  $= rac{ heta}{360} imes 2\pi r$ Substituting the values we get,

OR

 $\begin{aligned} &3\pi = \frac{\theta}{360} \times 2\pi \times 6 \dots (1) \\ &\text{Now we will simplify the equation (1) as below,} \\ &3\pi = \frac{\theta}{360} \times 12\pi \\ &3\pi = \frac{\theta}{30} \times \pi \\ &3 = \frac{\theta}{30} \\ &\theta = 90^{\circ} \end{aligned}$ 

Therefore, the angle subtended at the centre of the circle is  $90^{\circ}$ .



In this figure, centre of the circle is *O*, radius OA = r and  $\angle AOB = \theta$ We are going to find the area of the segment *AXB*. Area of the segment AXB = Area of the sector OAXB - Area of  $\triangle AOB$  ....(i) We know that area of sector  $OAXB = \frac{\theta}{360} \times \pi r^2$ We also know that area of  $\triangle AOB = r^2 \sin \frac{\theta}{2} \cos \frac{\theta}{2}$ Substituting these values in equation (1) we get, Area of the segment  $AXB = \frac{\theta}{360} \times \pi r^2 - r^2 \sin \frac{\theta}{2} \cos \frac{\theta}{2}$ Area of the segment  $AXB = \left(\frac{\theta}{360} \times \pi - \sin \frac{\theta}{2} \cos \frac{\theta}{2}\right) r^2$ So, Area of the segment  $AXB = \left(\frac{\pi\theta}{360} - \sin \frac{\theta}{2} \cos \frac{\theta}{2}\right) r^2$ Therefore, area of the segment is  $\left(\frac{\pi\theta}{360} - \sin \frac{\theta}{2} \cos \frac{\theta}{2}\right) r^2$ 

#### Section C

OR

- 26. (i) The required number of minutes after which they start preparing a new card together = LCM of 10,16 and 20 minutes Prime factorisation of  $10 = 2 \times 5$ 
  - and prime factorisation of  $16 = 2 \times 2 \times 2 \times 2$

and prime factorisation of  $20 = 2 \times 2 \times 5$ 

Now, LCM(10,16,20) = 2 × 2 × 2 × 2 × 5 = 80

Therefore, Number of minutes after which they start preparing a new card together = 80 minutes.

(ii) Recognition and care for elders removes the loneliness due to age related diseases. Moreover they feel happy to help young minds through their experience.

27. The given quadratic polynomial is  $p(x) = 2x^2 - 3x + p$ 

```
Since, 3 is a root (zero) of p(x)

\Rightarrow 2(3)^2 - 3 \times 3 + p = 0
\Rightarrow 18 - 9 + p = 0
\Rightarrow 9 + p = 0
\Rightarrow p = -9
Now p(x) = 2x^2 - 3x - 9
= 2x^2 - 6x + 3x - 9
= 2x (x - 3) + 3 (x - 3)
= (x - 3) (2x + 3)
For roots of polynomial, p(x) = 0
\Rightarrow (x - 3) (2x + 3) = 0
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 $\Rightarrow$  x = 3 or x =  $-\frac{3}{2}$ Hence the other root is  $-\frac{3}{2}$ .

28. 
$$2x - y = 4$$

8. $2x - y = 4$								
	x 2 3 5							
	y 0 2 6							
	6 (5, 6) 5 (5, 6) 3 (3, 2) 1 (2, 0)							

Quadrilateral is like trapezium whose parallel sides are 2 units and 6 units. Distance between parallel sides is 2 units. So, area of trapezium =  $\frac{1}{2}$  × (sum of parallel sides) × (Distance between parallel sides)  $=\frac{1}{2}(2+6) imes 2 = 8$ sq. units

The solution of pair of linear equations:

$$x + 3y = 6$$
 and  $2x - 3y = 12$ 

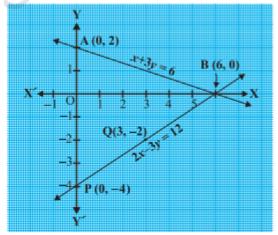
х	0	6
$y = \frac{6-x}{3}$	2	0

OR

and

Х	0	3
$y=rac{2x-12}{3}$	-4	-2

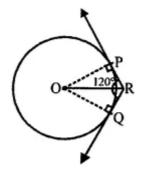
Plot the points A(0, 2), B(6, 0), P(0, -4) and Q(3, -2) on graph paper, and join the points to form the lines AB and PQ



We observe that there is a point B (6, 0) common to both the lines AB and PQ. So, the solution of the pair of linear equations is x = 6 and y = 0, i.e., the given pair of equations is consistent.

29. In the given figure, two tangents RQ and RP are drawn from the external point R to the circle with centre O.

 $\angle PRQ = 120^{\circ}$ To prove: OR = PR + RQConstruction: Join OP and OQ. Also join OR.



Proof: OR bisects the  $\angle$  PRQ  $\therefore \angle PRO = \angle QRO = \frac{120^{\circ}}{2} = 60^{\circ}$ : OP and OQ are radii and RP and RQ are tangents.  $\therefore$  OP  $\perp$  PR and OQ  $\perp$  QR In right riangle OPR  $\angle \mathrm{POR} = 180^\circ - (90^\circ + 60^\circ)$  $=180^\circ-150^\circ=30^\circ$ Similarly,  $\angle \mathrm{QOR} = 30^{\circ}$ and  $\cos \theta = \frac{PR}{OR}$   $\Rightarrow \cos 60^\circ = \frac{PR}{OR} \Rightarrow \frac{1}{2} = \frac{PR}{OR}$  $\Rightarrow$  2PR=OR .....(i) Similarly, in right riangle OQR $\Rightarrow$  2QR=OR .....(ii) Adding (i) and (ii)  $\Rightarrow$  2PR + 2QR = 2OR  $\Rightarrow$  OR = PR + RQ Hence Proved.

Given,

C O S In riangle OTS, OT = OS $\Rightarrow \angle OTS = \angle OST$  ...(i) In right riangle OTP,  $\frac{OT}{OP} = \sin \angle TPO$  $\Rightarrow \frac{r}{2r} = \sin \angle \text{TPO}$  $\sin \angle \text{TPO} = \frac{1}{2} \Rightarrow \angle \text{TPO} = 30^{\circ}$ Similarly  $\angle OPS = 30^{\circ}$  $\Rightarrow \angle TPS = 30^{\circ} + 30^{\circ} = 60^{\circ}$ Also  $\angle TPS + \angle SOT = 180^{\circ}$  $\angle \mathrm{SOT} = 120^{\circ}$  $\Rightarrow$ In  $\triangle$ SOT,  $\angle SOT + \angle OTS + \angle OST = 180^{\circ}$  $\Rightarrow 120^{\circ} + 2 \angle \mathrm{OTS} = 180^{\circ}$  $\Rightarrow \angle \text{OTS} = 30^{\circ}$  ...(ii)

OR

From (i) and (ii)  $\angle \mathrm{OTS} = \angle \mathrm{OST} = 30^\circ$ 

30. According to question

 $\frac{\cos\theta - \sin\theta}{\cos\theta + \sin\theta} = \frac{1 - \sqrt{3}}{1 + \sqrt{3}}$ 

 $\frac{(\cos\theta - \sin\theta) + (\cos\theta + \sin\theta)}{(\cos\theta - \sin\theta) - (\cos\theta + \sin\theta)} = \frac{(1 - \sqrt{3}) + (1 + \sqrt{3})}{(1 - \sqrt{3}) - (1 + \sqrt{3})}$  [Applying componendo and dividendo]  $\Rightarrow$ 

$$\Rightarrow \frac{2\cos\theta}{2\cos\theta} = \frac{2}{2}$$

 $-2\sin\theta$   $-2\sqrt{3}$  $\cot heta = rac{1}{\sqrt{3}} \Rightarrow \tan heta = \sqrt{3} \Rightarrow \tan heta = \tan 60^\circ \Rightarrow heta = 60^\circ$  $\Rightarrow$ 

31.

Class Interval	Frequency	Cumulative Frequency
0 - 10	6	6
10 - 20	16	22
20 - 30	30	52
30 - 40	9	61
40 - 50	4	65

Here, N =  $65 \Rightarrow \frac{N}{2} = 32.5$ 

The cumulative frequency just greater than 32.5 is 52.

Hence, median class is 20 - 30.

:. l = 20, h = 10, f = 30, cf = cf of preceding class = 22  
Now, Median = 
$$l + \left\{ h \times \frac{\left(\frac{N}{2} - cf\right)}{f} \right\}$$
  
= 20 +  $\left\{ 10 \times \frac{(32.5 - 22)}{30} \right\}$   
= 20 +  $\left\{ 10 \times \frac{10.5}{30} \right\}$   
= 20 + 3.5  
= 23.5

Thus, the median of the data is 23.5.

#### Section D

32. Total time taken by minute hand from 2 p.m. to 3 p.m. is 60 min.

According to question,  $t + \left(\frac{t^2}{4} - 3\right) = 60$  $\Rightarrow 4t + t^2 - 12 = 240$  $\Rightarrow t^2 + 4t - 252 = 0$  $\Rightarrow$  t<sup>2</sup> + 18t - 14t - 252 = 0  $\Rightarrow$  t(t + 18) - 14(t + 18) = 0  $\Rightarrow$  (t + 18) (t - 14) = 0  $\Rightarrow$  t + 18 = 0 or t - 14 = 0  $\Rightarrow$  t = -18 or t = 14 min. As time can't be negative. Therefore, t = 14 min.

OR

Let cost of production of each article be Rs x We are given total cost of production on that particular day = Rs 90 Therefore, total number of articles produced that day = 90/x

According to the given conditions,

 $x = 2\left(rac{90}{x}
ight) + 3$  $\Rightarrow x = \frac{180}{x} + 3$  $\Rightarrow x = \frac{180 + 3x}{x}$  $\Rightarrow x^2 = 180 + 3x$  $\Rightarrow x^2 - 3x - 180 = 0$   $\Rightarrow x^2 - 15x + 12x - 180 = 0$ 

 $\Rightarrow x (x - 15) + 12 (x - 15) = 0$ 

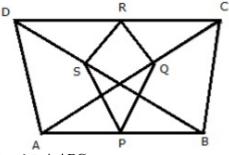
 $\Rightarrow (x - 15) (x + 12) = 0 \Rightarrow x = 15, -12$ 

Cost cannot be in negative, therefore, we discard x = -12

Therefore, x = Rs 15 which is the cost of production of each article.

Number of articles produced on that particular day =  $\frac{90}{15} = 6$ 

33. Given: ABCD is a quadrilateral in which AD = BC. P, Q, R, S are the midpoints of AB, AC, CD and BD. To prove: PQRS is a rhombus



Proof: In $\triangle ABC$ ,

Since P and Q are mid points of AB and AC

Therefore,  $PQ ||BC, PQ = \frac{1}{2}BC$  ......(1) (Mid-point theorem)

Similarly,

In  $\triangle CDA$ ,

Since R and Q are mid points of CD and AC

Therefore,  $RQ \parallel DA$ ,  $RQ = \frac{1}{2}DA = \frac{1}{2}BC$ .....(2)

In  $\triangle BDA$ ,

Since S and P mid points of BD and AB

Therefore, SP||DA,,SP= $\frac{1}{2}$ DA= $\frac{1}{2}$ BC .....(3)

In riangle CDB,

Since S and R are mid points of BD and CD

Therefore, SR||BC ,SR $=\frac{1}{2}BC$  .....(4)

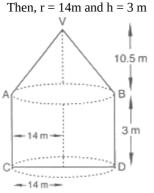
From (1) (2),(3)and (4) PQ || SR and (3) RQ || SP

PQ=RQ=SP=SR

So the opposite sided of PQRS are parallel and all sides are equal

Hence, PQRS is a rhombus.

34. Let r metres be the radius of the base of the cylinder and h metres be its heigh  $\Rightarrow l_1 = \sqrt{306.25}$ m = 17.5m



Now we have Curved surface area of the cylinder  $..= 2\pi rhm^2 = \left(2 \times \frac{22}{7} \times 14 \times 3\right)m^2 = 264 m^2$ 

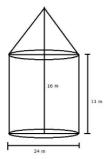
Let  $r_1$  m be the radius of the base,  $h_1$  m be the height and Z m be the slant height of the cone. Then,  $r_1 = 14$ m,  $h_1 = (13.5 - 3)$ m = 10.5m

 $I_{1} = \sqrt{r_{1}^{2} + h_{1}^{2}}$   $\Rightarrow l_{1} = \sqrt{14^{2} + (10.5)^{2}} \text{m} = \sqrt{196 + 110.25} \text{m}$ Therefore Curved surface area of the cone =  $\pi r_{1} l_{1}$  $= \frac{22}{7} \times 14 \times 17.5 \text{m}^{2} = 770 \text{m}^{2}$  So, Total area which is to be painted = Curved surface area of the cylinder + Curved surface area of the cone....

 $= (264 + 770) \text{ m2} = 1034 \text{ m}^2$ 

Now for Flence, total cost of painting = Rs. $(1034 \times 2)$  = Rs.2068 .

OR



Diameter of cyliner = 24m  $\therefore$  radius of cylinder = radius of cone = 12m Height of cylinder = 11m Total height of tent = 16m  $\therefore$  Height of cone = 16 - 11 = 5m Now,  $l^2 = r^2 + h^2$   $\Rightarrow l^2 = 12^2 + 5^2$   $\Rightarrow l^2 = 144 + 25 = 169$   $\Rightarrow l = \sqrt{169} = 13m$   $\therefore$  Canvas required for tent = curved surface area of cone + curved surface area of cylinder  $= \pi rl + 2\pi rh$   $= \frac{22}{7} \times 12 \times 13 + 2 \times \frac{22}{7} \times 12 \times 11$   $= \frac{22}{7} \times 12 [13 + 2 \times 11]$  $= \frac{22}{7} \times 12 \times 35$ 

 $= 22 \times 12 \times 5 = 1320 \text{m}^2$ 

35. Let the assumed mean be A = 25 and h = 5.

marks (x <sub>1</sub> ):	no. of students (f <sub>1</sub> ):	$d_1 = x_1 = A = x_1 - 25$	$u_1 = \frac{1}{h}(d_1)$	f <sub>1</sub> u <sub>1</sub>
5	15	-20	-4	-60
10	50	-15	-3	-150
15	80	-10	-2	-160
20	76	-5	-1	-76
25	72	0	0	0
30	45	5	1	45
35	39	10	2	78
30	9	15	3	27
45	8	20	4	32
50	6	25	5	30
	$\sum f_1 = 400$			$\sum f_1 u_1 = -234$

We know that mean,  $\overline{X} = A + h\left(\frac{1}{N}\sum_{i=1}^{n}f_{i}u_{i}\right)$ 

Now, we have  $N = \sum f_1 = 400$ , = -234, h = 5 and A = - 234, h = 5 and A = 25.

Putting the values in the above formula, we get

$$\bar{X} = \mathbf{A} + \mathbf{h}\left(\frac{1}{N}\sum_{i=1}^{n}f_{i}u_{i}\right)$$

 $= 25 + 5\left(\frac{1}{400} \times (-234)\right)$ = 25 -  $\frac{234}{80}$ = 25 - 2.925 = 22.075 Hence, the mean marks is 22.075

#### Section E

## 36. Read the text carefully and answer the questions:

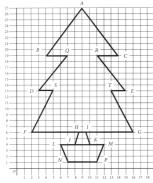
Your elder brother wants to buy a car and plans to take loan from a bank for his car. He repays his total loan of  $\gtrless$  1,18,000 by paying every month starting with the first instalment of  $\gtrless$  1000. If he increases the instalment by  $\gtrless$  100 every month , answer the following:

OR

BANK 11891 111 11 11 一面 (i) a = 1000 d = 100  $S_n = 1,18,000$  $t_{30} = a + 29 d$  $= 1000 + 29 \times 100$ = 1000 + 2900t<sub>30</sub> = 3900 i.e., he will pay ₹ 3900 in 30<sup>th</sup> installment. (ii)  $S_n = \frac{n}{2} \{2a + (n - 1)d\}$  $S_{30} = \frac{30}{2} \{2 \times 1000 + (30 - 1) \times 100\}$  $S_{30} = 15 \{2000 + 2900\}$  $S_{30} = 15 \times 4900$  $S_{30} = 73,500$ i.e., he will pay ₹ 73500 in 30 installments.  $t_{10} = a + 9d$  $= 2000 + 9 \times 100$  $t_{10} = 2000 + 900$ t<sub>10</sub> = ₹ 2900 (iii)S<sub>n</sub> =  $\frac{n}{2}$  {a + 1}  $1,18,000 = \frac{40}{2} \{1000 + 1\}$ 1,18,000 = 20,000 + 20198,000 = 20 1 l = 4900i.e., the last installment will be of ₹ 4900.

37. Read the text carefully and answer the questions:

The design of Christmas tree is shown in the following graph:



(i) The coordinates of point A are (9, 27), therefore its distance from x-axis = 27 units.

(ii) Coordinates of B and C are (4, 19) and (14, 19)

:. Required distance = 
$$\sqrt{(14 - 4)^2 + (19 - 19)^2}$$
  
=  $\sqrt{10^2}$  = 10 units

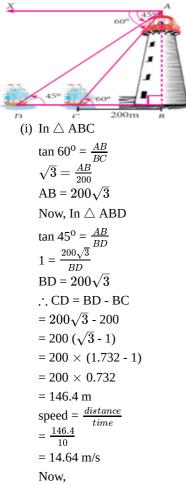
Coordinates of L and N are (6, 4) and (7, 1) respectively. Length of  $LN = \sqrt{(7-6)^2 + (1-4)^2}$   $= \sqrt{1+9} = \sqrt{10}$  units  $\Rightarrow$  Length of MP =  $\sqrt{10}$  units Now, perimeter of LMPN = LN + LM + MP + NP  $= \sqrt{10} + 6 + \sqrt{10} + 4 = (2\sqrt{10} + 10)$  units [ $\because$  LM = 12 - 6 = 6 units and NP = 11 - 7 = 4 units] (iii)Coordinates of F and G are (2, 6) and (16, 6) respectively.  $\therefore$  Required distance =  $\sqrt{(16-2)^2 + (6-6)^2}$ 

$$=\sqrt{14^2} = 14$$
 units

# 38. Read the text carefully and answer the questions:

A man is watching a boat speeding away from the top of a tower. The boat makes an angle of depression of  $60^{\circ}$  with the man's eye when at a distance of 200 m from the tower. After 10 seconds, the angle of depression becomes  $45^{\circ}$ .

OR



speed =  $14.64 \times \frac{18}{5}$  km/hr = 52.7 ≈ 53 km/hr (ii) In  $\triangle$  ABD  $\tan 45^{\circ} = \frac{AB}{BD}$   $1 = \frac{200\sqrt{3}}{BD}$ BD =  $200\sqrt{3}$  m  $\therefore$  CD =  $200\sqrt{3} - 200$ =  $200 (\sqrt{3} - 1)$ =  $200 (\sqrt{3} - 1)$ =  $200 \times 0.732$ = 146.4≈ 147 m  $\therefore$  boat is at a distance of 147 m from its actual position.

OR

As boat moves away from the tower angle of depression decreases. (iii)In  $\bigtriangleup$  ABC

 $\tan 60^{0} = \frac{AB}{BC}$  $\sqrt{3} = \frac{AB}{200}$  $AB = 200\sqrt{3} m$ Hence, height of tower =  $200\sqrt{3}$  m