

MIND MAP : LEARNING MADE SIMPLE CHAPTER - 10

1. When two lines are parallel their slopes are equal. Thus, any line parallel to $y = mx + c$ is of the type $y = mx + d$, where d is any parameter
2. Two lines $ax + by + c = 0$ and $a'x + b'y + c' = 0$ are parallel if $\frac{a}{a'} = \frac{b}{b'} \neq \frac{c}{c'}$
3. The distance between two parallel lines with equations $ax + by + c_1 = 0$ and $ax + by + c_2 = 0$ is $\left| \frac{c_1 - c_2}{\sqrt{a^2 + b^2}} \right|$

If m_1 and m_2 are the slopes of two intersecting lines ($m_1 m_2 \neq -1$) and θ be the acute angle between them then $\tan \theta = \left| \frac{m_1 - m_2}{1 + m_1 m_2} \right|$

- If θ is the angle at which a straight line is inclined to be +ve direction of x-axis and $0^\circ \leq \theta < 180^\circ$, $\theta \neq 90^\circ$, then the slope of the line, denoted by m , is defined by $m = \tan \theta$. If θ is 90° , m doesn't exist, but the line is parallel to y-axis. If $\theta = 0^\circ$, then $m = 0$ and the line is parallel to x-axis.
- If $A(x_1, y_1)$ and $B(x_2, y_2)$, $x_1 \neq x_2$ are points on straight line, then the slope m of the line is given by $m = (y_2 - y_1) / (x_2 - x_1)$

Area of triangle whose vertices are (x_1, y_1) , (x_2, y_2) and (x_3, y_3) is $\frac{1}{2} |x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)|$

The distance between the points $A(x_1, y_1)$ and $B(x_2, y_2)$ is $\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

The $P(x, y)$ divided the line joining $A(x_1, y_1)$ and $B(x_2, y_2)$ in the ratio $m:n$, then $x = \frac{mx_2 + nx_1}{m + n}$; $y = \frac{my_2 + ny_1}{m + n}$

Note: • If m/n is +ve, the division is internal, but if m/n is -ve, the division is external.
• If $m = n$, then P is the mid-point of the line segment joining A & B .

Straight Line

Parallel lines

Angle between two straight lines in terms of their slopes

Slope Formula

Area of Triangle

Distance Formula

Section Formula

Perpendicular lines

1. When two lines of the slope m_1 & m_2 are at right angles, the Product of their slope is -1 , i.e., $m_1 m_2 = -1$. Thus, any line perpendicular to $y = mx + c$ is of the form $y = -\frac{1}{m}x + d$ where d is any parameter.
2. Two lines $ax + by + c = 0$ and $a'x + b'y + c' = 0$ are perpendicular if $aa' + bb' = 0$. Thus, any line perpendicular to $ax + by + c = 0$ is of the form $bx - ay + k = 0$, where k is any parameter.

Reflection & foot of perpendicular a point about a line

Length of the perpendicular from a point on a line

Equation of Straight Line in various forms

1. The image of a point (x_1, y_1) about a line $ax + by + c = 0$ is:

$$\frac{x - x_1}{a} = \frac{y - y_1}{b} = -\frac{ax_1 + by_1 + c}{a^2 + b^2}$$

2. Similarly, foot of perpendicular from a point on the line is:

$$\frac{x - x_1}{a} = \frac{y - y_1}{b} = \frac{-(ax_1 + by_1 + c)}{a^2 + b^2}$$

The length of the perpendicular from $P(x_1, y_1)$ on $ax + by + c = 0$ is:

$$\left| \frac{ax_1 + by_1 + c}{\sqrt{a^2 + b^2}} \right|$$

1. **POINT-SLOPE FORM:** $y - y_1 = m(x - x_1)$ is the equation of a straight line whose slope is ' m ' and passes through the point (x_1, y_1) .
2. **SLOPE INTERCEPT FORM:** $y = mx + c$ is the equation of a straight line whose slope is ' m ' and makes an intercept c on the y-axis.
3. **TWO POINT FORM:** $y - y_1 = \frac{y_2 - y_1}{x_2 - x_1} (x - x_1)$ is the equation of a straight line which passes through (x_1, y_1) & (x_2, y_2) .
4. **INTERCEPT FORM:** $\frac{x}{a} + \frac{y}{b} = 1$ is the equation of a straight line which makes intercepts a & b on x and y axis respectively.
5. **NORMAL / PERPENDICULAR FORM:** $x \cos \alpha + y \sin \alpha = p$ (where $p > 0, 0 \leq \alpha < 2\pi$) is the equation of a straight line where the length of the perpendicular from origin O on the line is p and this perpendicular makes an angle α with +ve x-axis.
6. **GENERAL FORM:** $ax + by + c = 0$ is the equation of a straight line in general form. In this case, slope of line $= -\frac{a}{b}$