



# Assignment

Area of Bounded Region

## Basic Level

- Area under the curve  $y = x^2 - 4x$  within the  $x$ -axis and the line  $x=2$ , is [SCRA 1991]
  - $\frac{16}{3}$  sq. units
  - $-\frac{16}{3}$  sq. units
  - $\frac{4}{7}$  sq. units
  - Cannot be calculated
- The area bounded by the curve  $y = 4x - x^2$  and the  $x$ -axis is [MP PET 1999, 2003]
  - $\frac{30}{7}$  sq. units
  - $\frac{31}{7}$  sq. units
  - $\frac{32}{3}$  sq. units
  - $\frac{34}{3}$  sq. units
- The area between the curve  $y = 4 + 3x - x^2$  and  $x$ -axis is [Rajasthan PET 2001]
  - $\frac{125}{6}$
  - $\frac{125}{3}$
  - $\frac{125}{2}$
  - None of these
- Area under the curve  $y = \sqrt{3x+4}$  between  $x=0$  and  $x=4$ , is [AI CBSE 1979, 1980]
  - $\frac{56}{9}$  sq. units
  - $\frac{64}{9}$  sq. units
  - 8 sq. units
  - None of these
- The area bounded by the curve  $y = x^3$ ,  $x$ -axis and two ordinates  $x=1$  to  $x=2$  equal to [MP PET 1999]
  - $\frac{15}{2}$  sq. units
  - $\frac{15}{4}$  sq. units
  - $\frac{17}{2}$  sq. units
  - $\frac{17}{4}$  sq. units
- If the area above the  $x$ -axis, bounded by the curves  $y = 2^{kx}$  and  $x=0$  and  $x=2$  is  $\frac{3}{\ln 2}$ , then the value of  $k$  is [Orissa JEE 2003]
  - $\frac{1}{2}$
  - 1
  - 1
  - 2
- Area bounded by curve  $y = x^3$ ,  $x$ -axis and ordinates  $x=1$  and  $x=4$ , is
  - 64 sq. units
  - 27 sq. units
  - $\frac{127}{4}$  sq. units
  - $\frac{255}{4}$  sq. units
- Area bounded by curve  $xy = c$ ,  $x$ -axis between  $x=1$  and  $x=4$ , is
  - $c \log 3$  sq. units
  - $2 \log c$  sq. units
  - $2c \log 2$  sq. units
  - $2c \log 5$  sq. units
- The measurement of the area bounded by the coordinate axes and the curve  $y = \log_e x$  is [MP PET 1998]
  - 1
  - 2
  - 3
  - $\infty$
- The area bounded by the curve  $y = \log x$ , the  $x$ -axis and ordinate  $x=e$  is [MP PET 1994]
  - $e$
  - 1
  - $\infty$
  - None of these
- Area bounded by the curve  $y = \log x$ ,  $x$ -axis and the ordinates  $x=1$ ,  $x=2$  is
  - $\log 4$  sq. units
  - $\log 4+1$  sq. units
  - $\log 4-1$  sq. units
  - None of these
- Area bounded by the curve  $y = x e^{x^2}$ ,  $x$ -axis and the ordinates  $x=0$ ,  $x=a$  is
  - $\frac{e^{a^2}+1}{2}$  sq. units
  - $\frac{e^{a^2}-1}{2}$  sq. units
  - $e^{a^2}+1$  sq. units
  - $e^{a^2}-1$  sq. units
- If area bounded by the curves  $y^2 = 4ax$  and  $y = mx$  is  $\frac{a^2}{3}$ , then the value of  $m$  is
  - 2
  - 2
  - 1/2
  - None of these
- The area of the region (in the square units) bounded by the curve  $x^2 = 4y$ , line  $x=2$  and  $x$ -axis is [MP PET 2002]
  - 2
  - 2
  - 1/2
  - None of these

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- (a) 1 (b)  $\frac{2}{3}$  (c)  $\frac{4}{3}$  (d)  $\frac{8}{3}$
15. Area bounded by the parabola  $y = 4x^2$ ,  $y$ -axis and the lines  $y = 1$ ,  $y = 4$  is  
(a) 3 sq. units (b)  $\frac{7}{5}$  sq. units (c)  $\frac{7}{3}$  sq. units (d) None of these
16. Area bounded by parabola  $y^2 = x$  and straight line  $2y = x$  is [MP PET 1996]  
(a)  $\frac{4}{3}$  (b) 1 (c)  $\frac{2}{3}$  (d)  $\frac{1}{3}$
17. Area enclosed by the parabola  $ay = 3(a^2 - x^2)$  and  $x$ -axis is  
(a)  $4a^2$  sq. units (b)  $12a^2$  sq. units (c)  $4a^3$  sq. units (d) None of these
18. The area enclosed by the curve  $y = \sin x$ ,  $y = 0$ ,  $x = 0$  and  $x = \frac{\pi}{2}$  is [MP PET 1995]  
(a)  $\pi$  (b)  $2\pi$  (c) 1 (d) 2
19. Area bounded by the curve  $y = \sin x$  between  $x = 0$  and  $x = 2\pi$  is  
(a) 2 sq. units (b) 4 sq. units (c) 8 sq. units (d) None of these
20. Area bounded by the curve  $y = k \sin x$  between  $x = \pi$  and  $x = 2\pi$ , is  
(a)  $2k$  sq. units (b) 0 (c)  $\frac{k^2}{2}$  sq. units (d)  $k$  sq. units
21. The area of the region bounded by the  $x$ -axis and the curves defined by  $y = \tan x$   $\left(-\frac{\pi}{3} \leq x \leq \frac{\pi}{3}\right)$  is [Kurukshetra CEE 1998]  
(a)  $\log \sqrt{2}$  (b)  $-\log \sqrt{2}$  (c)  $2 \log 2$  (d) 0
22. The area between the curve  $y = \sin^2 x$ ,  $x$ -axis and the ordinates  $x=0$  and  $x = \frac{\pi}{2}$  is [Rajasthan PET 1996]  
(a)  $\frac{\pi}{2}$  (b)  $\frac{\pi}{4}$  (c)  $\frac{\pi}{8}$  (d)  $\pi$
23. Area of the region bounded by the curve  $y = \tan x$ , tangent drawn to the curve at  $x = \frac{\pi}{4}$  and the  $x$ -axis is [DCE 2002]  
(a)  $\frac{1}{4}$  (b)  $\log \sqrt{2} - \frac{1}{4}$  (c)  $\log \sqrt{2} + \frac{1}{4}$  (d) None of the above
24. The ratio of the areas bounded by the curves  $y = \cos x$  and  $y = \cos 2x$  between  $x = 0$ ,  $x = \frac{\pi}{3}$  and  $x$ -axis, is [MP PET 1997]  
(a)  $\sqrt{2} : 1$  (b) 1:1 (c) 1:2 (d) 2:1
25. The area bounded by the curve  $y = \sec x$ , the  $x$ -axis and the lines  $x=0$  and  $x = \frac{\pi}{4}$  is [Tamilnadu PCEE 2002]  
(a)  $\log(\sqrt{2} + 1)$  (b)  $\log(\sqrt{2} - 1)$  (c)  $\frac{1}{2} \log 2$  (d)  $\sqrt{2}$
26. The area bounded by  $y = [x]$  and the two ordinates  $x=1$  and  $x=1.7$  is  
(a)  $\frac{17}{10}$  (b) 1 (c)  $\frac{17}{5}$  (d)  $\frac{7}{10}$
27. The value of  $k$  for which the area of the figure bounded by the curve  $y = 8x^2 - x^5$ , the straight line  $x = 1$  and  $x = k$  and the  $x$ -axis is equal to  $\frac{16}{3}$   
(a) 2 (b)  $\sqrt[3]{8 - \sqrt{17}}$  (c) 3 (d) -1

28. The area of the region bounded by the curves  $y = |x - 2|$ ,  $x = 1$ ,  $x = 3$  and the  $x$ -axis is [AIEEE 2004]  
 (a) 4 (b) 2 (c) 3 (d) 1
29. The area of the region bounded by  $y = |x - 1|$  and  $y = 1$  is [IIT Screening 1994]  
 (a) 2 (b) 1 (c)  $1/2$  (d) None of these
30. Area bounded by lines  $y = 2 + x$ ,  $y = 2 - x$  and  $x = 2$  is [MP PET 1996]  
 (a) 3 (b) 4 (c) 8 (d) 16
31. Area enclosed between the curve  $y^2(2a - x) = x^3$  and line  $x = 2a$  above  $x$ -axis is [MP PET 2001]  
 (a)  $\pi a^2$  (b)  $\frac{3\pi a^2}{2}$  (c)  $2\pi a^2$  (d)  $3\pi a^2$
32. Area bounded by the curve  $xy - 3x - 2y - 10 = 0$ ,  $x$ -axis and the lines  $x = 3$ ,  $x = 4$  is [AI CBSE 1991]  
 (a)  $16 \log 2 - 3$  (b)  $16 \log 2 - 13$  (c)  $16 \log 2 + 3$  (d) None of these
33. The area of the triangle formed by the tangent to the hyperbola  $xy = a^2$  and coordinate axes is [Rajasthan PET 2000]  
 (a)  $a^2$  (b)  $2a^2$  (c)  $3a^2$  (d)  $4a^2$
34. If a curve  $y = a\sqrt{x} + bx$  passes through the point (1, 2) and the area bounded by the curve, line  $x = 4$  and  $x$ -axis is 8 square units, then [MP PET 2002]  
 (a)  $a = 3, b = -1$  (b)  $a = 3, b = 1$  (c)  $a = -3, b = 1$  (d)  $a = -3, b = -1$
35. The area bounded by the curve  $y = f(x)$ ,  $x$ -axis and ordinates  $x = 1$  and  $x = b$  is  $(b - 1)\sin(3b + 4)$  then  $f(x)$  is [Rajasthan PET 2000]  
 (a)  $3(x - 1)\cos(3x + 4) + \sin(3x + 4)$  (b)  $(b - 1)\sin(3x + 4) + 3\cos(3x + 4)$   
 (c)  $(b - 1)\cos(3x + 4) + 3\sin(3x + 4)$  (d) None of these
36. The area enclosed by the parabola  $y^2 = 4ax$  and the straight line  $y = 2ax$ , is [MP PET 1993]  
 (a)  $\frac{a^2}{3}$  sq. units (b)  $\frac{1}{3a^2}$  sq. units (c)  $\frac{1}{3a}$  sq. units (d)  $\frac{2}{3a}$  sq. units
37. The area bounded by the curve  $x = at^2$ ,  $y = 2at$  and the  $x$ -axis in  $1 \leq t \leq 3$  is. [Pb. CET 1998]  
 (a)  $26a^2$  (b)  $8a^2$  (c)  $\frac{26a^2}{3}$  (d)  $\frac{104a^2}{3}$
38. If  $A_n$  be the area bounded by the curve  $y = (\tan x)^n$  and the lines  $x = 0$ ,  $y = 0$  and  $x = \frac{\pi}{4}$ , then for  $n > 2$  [IIT 1996, Him. UCET 2002]  
 (a)  $A_n + A_{n-2} = \frac{1}{n-1}$  (b)  $A_n + A_{n-2} < \frac{1}{n-1}$  (c)  $A_n - A_{n-2} = \frac{1}{n-1}$  (d) None of these
39. The area between the curve  $y = 2x^4 - x^2$ , the axis and the ordinates of two minima of the curve is  
 (a)  $\frac{7}{120}$  (b)  $\frac{9}{120}$  (c)  $\frac{11}{120}$  (d) None of these
40. The slope of the tangent to a curve  $y = f(x)$  at  $(x, f(x))$  is  $2x + 1$ . If the curve passes through the point (1, 2), then the area of the region bounded by the curve, the  $x$ -axis and the line  $x = 1$  is [IIT 1995]  
 (a)  $\frac{5}{6}$  (b)  $\frac{6}{5}$  (c) 6 (d)  $\frac{1}{6}$

## Symmetrical Area

## Basic Level

41. The area bounded by the  $x$ -axis and the curve  $y = \sin x$  and  $x = 0$ ,  $x = \pi$  is [Kerala (Engg.) 2002]  
 (a) 1 (b) 2 (c) 3 (d) 4
42. The area of the curve  $xy^2 = a^2(a - x)$  bounded by  $y$ -axis is [Rajasthan PET 1996]  
 (a)  $\pi a^2$  (b)  $2\pi a^2$  (c)  $3\pi a^2$  (d)  $4\pi a^2$

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43. The area bounded by the parabola  $y^2 = 4ax$ , its axis and two ordinates  $x = 4$ ,  $x = 9$  is  
 (a)  $4a^2$  (b)  $4a^2 \cdot 4$  (c)  $4a^2(9 - 4)$  (d)  $\frac{152\sqrt{a}}{3}$
44. Area bounded by the parabola  $y^2 = 2x$  and the ordinates  $x = 1$ ,  $x = 4$  is  
 (a)  $\frac{4\sqrt{2}}{3}$  sq. units (b)  $\frac{28\sqrt{2}}{3}$  sq. units (c)  $\frac{56}{3}$  sq. units (d) None of these
45. Area bounded by the parabola  $y^2 = 4ax$  and its latus rectum is [Rajasthan PET 1997, 2000, 2002]  
 (a)  $\frac{2}{3}a^2$  sq. units (b)  $\frac{4}{3}a^2$  sq. units (c)  $\frac{8}{3}a^2$  sq. units (d)  $\frac{3}{8}a^2$  sq. units
46. The area between the curve  $y^2 = 4ax$ ,  $x$ -axis and the ordinates  $x = 0$  and  $x = a$  is [Rajasthan PET 1996]  
 (a)  $\frac{4}{3}a^2$  (b)  $\frac{8}{3}a^2$  (c)  $\frac{2}{3}a^2$  (d)  $\frac{5}{2}a^2$
47. Area of the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  is [Karnataka CET 1993]  
 (a)  $\pi ab$  sq. units (b)  $\frac{1}{2}\pi ab$  sq. units (c)  $\frac{1}{4}\pi ab$  sq. units (d) None of these
48. The area of the smaller segment cut off from the circle  $x^2 + y^2 = 9$  by  $x = 1$  is [Rajasthan PET 2002]  
 (a)  $\frac{1}{2}(9 \sec^{-1} 3 - \sqrt{8})$  (b)  $9 \sec^{-1}(3) - \sqrt{8}$  (c)  $\sqrt{8} - 9 \sec^{-1} 3$  (d) None of these
49. The area of the upper half of the circle whose equation is  $(x - 1)^2 + y^2 = 1$  is given by [Kurukshetra CEE 1995]  
 (a)  $\int_0^2 \sqrt{2x - x^2} dx$  (b)  $\int_0^1 \sqrt{2x - x^2} dx$  (c)  $\int_1^2 \sqrt{2x - x^2} dx$  (d)  $\frac{\pi}{4}$

#### Advance Level

50. The area bounded by the curves  $y = \ln x$ ,  $y = \ln |x|$ ,  $y = |\ln x|$  and  $y = |\ln |x||$  is [AIEEE 2002]  
 (a) 4 sq. units (b) 6 sq. units (c) 10 sq. units (d) None of these
51. Ratio of the area cut off a parabola by any double ordinate is that of the corresponding rectangle contained by that double ordinate and its distance from the vertex is  
 (a)  $\frac{1}{2}$  (b)  $\frac{1}{3}$  (c)  $\frac{2}{3}$  (d) 1
52. The area bounded by the curves  $x = a \cos^3 t$ ,  $y = a \sin^3 t$  is  
 (a)  $\frac{3\pi a^2}{8}$  (b)  $\frac{3\pi a^2}{16}$  (c)  $\frac{3\pi a^2}{32}$  (d)  $3\pi a^2$

#### Area between Two curves

#### Basic Level

53. The area bounded by the curves  $y = \sqrt{x}$ ,  $2y + 3 = x$  and  $x$ -axis in the 1<sup>st</sup> quadrant is [IIT 2003]  
 (a) 9 (b)  $\frac{27}{4}$  (c) 36 (d) 18
54. The area of region  $\{(x, y) : x^2 + y^2 \leq 1 \leq x + y\}$  is [Kerala (Engg.) 2002]  
 (a)  $\frac{\pi^2}{5}$  (b)  $\frac{\pi^2}{2}$  (c)  $\frac{\pi^2}{3}$  (d)  $\frac{\pi}{4} - \frac{1}{2}$
55. The area bounded by the curve  $y = x$ ,  $x$ -axis and ordinates  $x = -1$  to  $x = 2$  is [Rajasthan PET 2001]

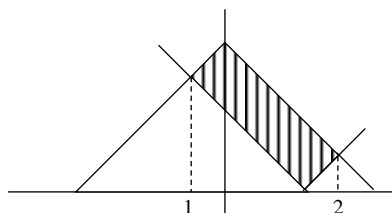
- (a) 0 (b)  $\frac{1}{2}$  (c)  $\frac{3}{2}$  (d)  $\frac{5}{2}$   
**56.** The area bounded by the curves  $y = |x| - 1$  and  $y = -|x| + 1$  is [IIT Screening 2002]
- (a) 1 (b) 2 (c)  $2\sqrt{2}$  (d) 4  
**57.** The area bounded by the straight lines  $x = 0, x = 2$  and the curves  $y = 2^x, y = 2x - x^2$  is [AMU 2001]
- (a)  $\frac{4}{3} - \frac{1}{\log 2}$  (b)  $\frac{3}{\log 2} + \frac{4}{3}$  (c)  $\frac{4}{\log 2} - 1$  (d)  $\frac{3}{\log 2} - \frac{4}{3}$   
**58.** The area of figure bounded by  $y = e^x, y = e^{-x}$  and the straight line  $x = 1$  is [Karnataka CET 1999]
- (a)  $e + \frac{1}{e}$  (b)  $e - \frac{1}{e}$  (c)  $e + \frac{1}{e} - 2$  (d)  $e + \frac{1}{e} + 2$   
**59.** The area bounded by the curves  $y = \log_e x$  and  $y = (\log_e x)^2$  is [Rajasthan PET 2000]
- (a)  $3 - e$  (b)  $e - 3$  (c)  $\frac{1}{2}(3 - e)$  (d)  $\frac{1}{2}(e - 3)$   
**60.** The area bounded by the curves  $y^2 - x = 0$  and  $y - x^2 = 0$  is [MP PET 1997]
- (a)  $\frac{7}{3}$  (b)  $\frac{1}{3}$  (c)  $\frac{5}{3}$  (d) 1  
**61.** The area enclosed by the parabolas  $y = x^2 - 1$  and  $y = 1 - x^2$  is [AMU 1999]
- (a)  $\frac{1}{3}$  (b)  $\frac{2}{3}$  (c)  $\frac{4}{3}$  (d)  $\frac{8}{3}$   
**62.** The area bounded by curve  $y^2 = x$ , line  $y = 4$  and y-axis is [Roorkee 1995; Rajasthan PET 2003]
- (a)  $\frac{16}{3}$  (b)  $\frac{64}{3}$  (c)  $7\sqrt{2}$  (d) None of these  
**63.** Area included between the two curves  $y^2 = 4ax$  and  $x^2 = 4ay$ , is [SCRA 1986; Roorkee 1984; Rajasthan PET 1999; Kerala (Engg.) 2002]
- (a)  $\frac{32}{3}a^2$  sq. units (b)  $\frac{16}{3}$  sq. units (c)  $\frac{32}{3}$  sq. units (d)  $\frac{16}{3}a^2$  sq. units  
**64.** Area bounded by the curve  $x^2 = 4y$  and the straight line  $x = 4y - 2$ , is [SCRA 1986; IIT 1981]
- (a)  $\frac{8}{9}$  sq. units (b)  $\frac{9}{8}$  sq. units (c)  $\frac{4}{3}$  sq. units (d) None of these  
**65.** What is the area bounded by the curves  $x^2 + y^2 = 9$  and  $y^2 = 8x$  [DCE 1999]
- (a) 0 (b)  $\frac{2\sqrt{2}}{3} + \frac{9\pi}{2} - 9 \sin^{-1}\left(\frac{1}{3}\right)$  (c)  $16\pi$  (d) None of these  
**66.** The area bounded by the circle  $x^2 + y^2 = 4$ , line  $x = \sqrt{3}y$  and x-axis lying in the first quadrant, is [Rajasthan PET 1997; Kurukshetra CEE 1998]
- (a)  $\frac{\pi}{2}$  (b)  $\frac{\pi}{4}$  (c)  $\frac{\pi}{3}$  (d)  $\pi$   
**67.** The area in the first quadrant between  $x^2 + y^2 = \pi^2$  and  $y = \sin x$  is [MP PET 1997]
- (a)  $\frac{(\pi^3 - 8)}{4}$  (b)  $\frac{\pi^3}{3}$  (c)  $\frac{(\pi^3 - 16)}{4}$  (d)  $\frac{(\pi^3 - 8)}{2}$   
**68.** For  $0 \leq x \leq \pi$ , the area bounded by  $y = x$  and  $y = x + \sin x$ , is [Roorkee Ququalifying 1998]
- (a) 2 (b) 4 (c)  $2\pi$  (d)  $4\pi$   
**69.** Area bounded by  $y = x \sin x$  and x-axis between  $x = 0$  and  $x = 2\pi$ , is [Roorkee 1981; Rajasthan PET 1995]
- (a) 0 (b)  $2\pi$  sq. units (c)  $\pi$  sq. units (d)  $4\pi$  sq. units  
**70.** The area bounded by curves  $y = \cos x$  and  $y = \sin x$  and ordinates  $x = 0$  and  $x = \frac{\pi}{4}$  is [Karnataka CET 2002]
- (a)  $\sqrt{2}$  (b)  $\sqrt{2} + 1$  (c)  $\sqrt{2} - 1$  (d)  $\sqrt{2}(\sqrt{2} - 1)$   
**71.** The area formed by triangular shaped region bounded by the curves  $y = \sin x, y = \cos x$  and  $x = 0$  is [MP PET 2000]
- (a)  $\sqrt{2} - 1$  (b) 1 (c)  $\sqrt{2}$  (d)  $1 + \sqrt{2}$

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72. Area between the curve  $y = \cos x$  and  $x$ -axis when  $0 \leq x \leq 2\pi$ , is [MP PET 1997]  
 (a) 2 (b) 4 (c) 3 (d) 0
73.  $AOB$  is the positive quadrant of the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  where  $OA = a$ ,  $OB = b$ . Then area between the arc  $AB$  and chord  $AB$  of the ellipse is  
 (a)  $\pi ab$  (b)  $(\pi - 2)ab$  (c)  $\frac{ab(\pi - 2)}{4}$  (d)  $\frac{ab(\pi + 2)}{4}$

#### Advance Level

74. For which of the following values of  $m$ , the area of the region bounded by the curve  $y = x - x^2$  and the line  $y = mx$  equals  $\frac{9}{2}$  [IIT 1999]  
 (a) -4 (b) -2 (c) 2 (d) 4
75. The area of the figure bounded by the curves  $y = |x - 1|$  and  $y = 3 - |x|$ , is [AIEEE 2003; Orissa JEE 2003]



- (a) 2 sq. units (b) 3 sq. units (c) 4 sq. units (d) 1 sq. units
76. If the ordinate  $x = a$  divides the area bounded by the curve  $y = \left(1 + \frac{8}{x^2}\right)$ ,  $x$ -axis and the ordinates  $x = 2$ ,  $x = 4$  into two equal parts, then  $a =$  [IIT 1983]  
 (a) 8 (b)  $2\sqrt{2}$  (c) 2 (d)  $\sqrt{2}$
77. The area of the region lying inside  $x^2 + (y - 1)^2 = 1$  and out side  $c^2 x^2 + y^2 = c^2$ , where  $c = (\sqrt{2} - 1)$  is [Roorkee 1999]  
 (a)  $(4 - \sqrt{2})\frac{\pi}{4} + \frac{1}{\sqrt{2}}$  (b)  $(4 + \sqrt{2})\frac{\pi}{4} - \frac{1}{\sqrt{2}}$  (c)  $(4 + \sqrt{2})\frac{\pi}{4} + \frac{1}{\sqrt{2}}$  (d) None of these
78. The area enclosed between the curves  $y = \log_e(x + e)$ ,  $x = \log_e(x + e)$ ,  $x = \log_e\left(\frac{1}{y}\right)$  and the  $x$ -axis, is [Roorkee 1990; Pb. CET 2002]  
 (a) 2 (b) 1 (c) 4 (d) None of these
79. The area of the region formed by  $x^2 + y^2 - 6x - 4y + 12 \leq 0$ ,  $y \leq x$  and  $x \leq \frac{5}{2}$  is [Roorkee 1996; PUCET 2002]  
 (a)  $\frac{\pi}{6} - \frac{\sqrt{3} + 1}{8}$  (b)  $\frac{\pi}{6} + \frac{\sqrt{3} - 1}{8}$  (c)  $\frac{\pi}{6} - \frac{\sqrt{3} - 1}{8}$  (d) None of these
80. If the area bounded by the curves  $y = x - bx^2$  and  $y = \frac{1}{b}x^2$ , where  $b > 0$  is maximum, then  $b =$  [IIT 1997]  
 (a) 0 (b) 1 (c) 2 (d) None of these
81. Let  $f(x) = \text{Maximum}[x^2, (1 - x^2), 2x(1 - x)]$  where  $0 \leq x \leq 1$ . The area of the region bounded by the curves  $y = f(x)$ ,  $x$ -axis,  $x = 0$  and  $x = 1$  is [IIT 1997; IIT Hyderabad 2002]  
 (a)  $\frac{17}{27}$  (b)  $\frac{14}{27}$  (c)  $\frac{19}{27}$  (d) None of these
82. The area of the closed figure bounded by  $x = -1$  and  $x = 2$  and  $y = \begin{cases} -x^2 + 2, & x \leq 1 \\ 2x - 1, & x > 1 \end{cases}$  and the abscissa axis is  
 (a)  $\frac{16}{3}$  sq. units (b)  $\frac{10}{3}$  sq. units (c)  $\frac{13}{3}$  sq. units (d)  $\frac{7}{3}$  sq. units

83. The volume of the solid formed by rotating the area enclosed between the curve  $y = x^2$  and the line  $y = 1$  about  $y = 1$  is (in cubic units)  
 (a)  $\frac{9\pi}{5}$  (b)  $\frac{7\pi}{3}$  (c)  $\frac{8\pi}{3}$  (d) None of these
84. The volume of the solid obtained by rotating the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  about the axis of  $x$  is [MNR 1995]  
 (a)  $\pi^2 b$  (b)  $\pi - b^2$  (c)  $\frac{4}{3}\pi a^2 b$  (d)  $\frac{4}{3}\pi ab^2$
85. The part of the parabola between the parabola  $y^2 = 4ax$  and the line  $x = c$  is revolved about  $x$ -axis. The volume of the resulting solid is  
 (a)  $2\pi ac^2$  (b)  $\pi ac^2$  (c)  $\frac{\pi c^2}{4}$  (d)  $4\pi ac^2$
86. The volume of the solid generated by revolving about the  $y$ -axis the figure bounded by the parabola  $y = x^2$  and  $x = y^2$  is [UPSEAT 2002]  
 (a)  $\frac{21}{5}\pi$  (b)  $\frac{24}{5}\pi$  (c)  $\frac{5}{24}\pi$  (d) None of these
87. The volume of the frustum of a cone of height 6 cm., and radii are 5 cms and 8 cms is  
 (a) 258 cc (b) 250 cc (c) 268 cc (d) 275 cc
88. The part of the circle  $x^2 + y^2 = 4$  between  $x = 1$  and  $x = 2$  is revolved about  $x$ -axis. The curved surface of the resulting solid is  
 (a)  $2\pi$  (b)  $4\pi$  (c)  $6\pi$  (d)  $8\pi$

### Advance Level

89. The volume of a solid obtained by revolving about  $y$ -axis enclosed between the ellipse  $x^2 + 9y^2 = 9$  and the straight line  $x + 3y = 3$  in the first quadrant is [MNR 1994]  
 (a)  $3\pi$  (b)  $4\pi$  (c)  $6\pi$  (d)  $9\pi$
90. The volume of the frustum of a right circular cone. The radii of whose ends are respectively 10 cms and 16 cms and thickness is 4 cms, is  
 (a)  $1232\pi$  (b)  $332\pi$  (c)  $1032\pi$  (d)  $1132\pi$
91. The line segment joining the points  $(1, m)$  and  $(2, 2m)$  is revolved round the  $y$ -axis to form a frustum of a cone of the volume of the frustum is  $14\pi$  then the value of  $m$  is equal to  
 (a) 2 (b) 4 (c) 6 (d) 8
92. A frustum of sphere is made by cutting two parallel planes of any sphere. If radius of sphere is 5 cm and distance between the plane is 1 cm, then what will be the curved surface of frustum when the distance of first plane from the centre of sphere is 2 cm [UPSEAT 1999]  
 (a)  $5\pi m^2$  (b)  $10\pi m^2$  (c)  $15\pi m^2$  (d)  $40\pi m^2$

# Answer Sheet

### *Assignment (Basic and Advance Level)*

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
a	c	a	d	b	b	d	c	d	b	c	b	a	b	c	a	a	c	b	a
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40
c	b	d	d	a	d	b	d	b	b	b	c	b	a	a	c	d	a	a	a
41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60
b	a	d	b	c	b	a	b	a	a	c	a	a	d	d	b	d	c	a	b
61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80
d	b	d	b	b	c	a	a	d	c	a	b	c	b	c	b	a	a	c	b
81	82	83	84	85	86	87	88	89	90	91	92								
a	a	d	d	a	d	a	b	a	c	c	b								