NETWORKS TEST 4

Number of Questions: 25

Directions for questions 1 to 25: Select the correct alternative from the given choices.

1. Consider the circuit shown in figure



- The input impedance Z_{in} is _____. (A) 3.5 Ω (B) 2 Ω (C) 7 Ω (D) 5 Ω
- 2. The ideal transformer in figure is used to match the amplifier circuit to the loud speaker to achieve maximum power transfer.



If the output impedance of the amplifier is 192 Ω and the internal impedance of the speaker is 48 Ω . Then the required turns ratio ($N_1 : N_2$) is _____

(A) 2:1 (C) 1:3 (B) 1:2 (D) 1:4

3.



Two coils are mutually coupled with $L_1 = 10$ H and $L_2 = 40$ H and k = 0.5. Then the maximum possible equivalent inductance in between the terminals 'a' and 'b' is _____

(A)	30 H	(B)	4.28 H
(C)	5 H	(D)	8 H

4. Consider the parallel RLC circuit shown in below.



If resonant frequency $\omega_o = 2$ rad/sec, then the value of *L* is _____

- (A) 0.5 H (B) 2 H
- (C) A and B (D) 4 H
- 5. Consider the graph shown in below.



Match List – I with List – II:

List – I		List – II		
Р	Links	а	2, 5, 6, 8	
Q	f-loops	b	1, 4, 5, 9	
R	twigs	с	1, 2, 3, 4	
S	f-cut set	d	2, 3, 6, 7, 8	
		е	3, 4, 9	

(A)
$$P - d, Q - e, R - c, S - a$$

(B)
$$P-c, Q-d, R-a, S-e$$

(C)
$$F = c, Q = a, K = b, S = e$$

D)
$$F = a, Q = e, K = b, S = a$$



6.



The *h*-parameters $(h_{11} \text{ and } h_{21})$ of the circuit is _____ (A) 4 Ω and -2.2 (B) 4 Ω and $\frac{5}{11}$

(C) 2.5
$$\Omega$$
 and -2.2 (D) $\frac{11}{5} \Omega$ and 1.2

7. The RMS value of the current wave form *i*(*t*) is _____.



Section Marks: 90

 $e^{-2.5t}$ V

8. If $I_s = 5 \cos 500t$ A, In the circuit shown in figure



Then the circuit $i_1(t)$ is _

- (A) $2\cos(500t 26.56^\circ)$ A
- (B) $0.8 \sin (500t + 26^\circ) \text{ A}$
- (C) $5 \cos (500t + 30^\circ)$ A
- (D) None of these
- **9.** The response of a network is $i(t) = 2t \cdot e^{-5t} A$ for $t \ge 0$, the value of 't' at which the i(t) will become maximum, is
 - (A) 0.2 sec (B) 0.4 sec
 - (C) 0.25 sec (D) 0.8 sec
- 10. In the network shown below, it is given that $V_c = 2.5$ V and dV_c

 $\frac{dV_c}{dt} = -8$ V/s at a time 't', where t is the time constant

after the switch 'S' is closed. What is the value of 'C'?



A)	3.25 mF	(B)	1.25 mF
C)	1 μF	(D)	0.052 F

11. In an AC series RLC circuit, the voltage across *R* and *L* is 20V, voltage across *L* and *C* is 9V and voltage across

RLC	C is 15V. Then the	he ratio of $\frac{V_L}{V_C}$	is	$[Assume V_L]$
$> V_c$	<u>,</u>].			
(A)	0.64	(B)	2.52	
(C)	3.43	(D)	2.28	

12. Consider the circuit shown in figure



If A_1 , A_2 and A_3 are ideal ammeters. It A_1 and A_3 reads 8A and 3A respectively, then A_2 should read _____

		1	J)	2	
(A)	5 A			(B)	11 A
(C)	8.66 A			(D)	None

13. Consider the circuit shown in below.



- It is a (A) BSF (B) APF (C) BPF (D) HPF
- 14. The coil of a certain relay is operated by 15 V battery. If the coil has a resistance of 200 Ω and an inductance of 25 mH and the current needed to pull in is 40 mA, calculate the relay delay time.

15. If $i_c(t) = -5.e^{-2.5t}$ A, the voltage of the source of the given circuit, $V_{in}(t)$ is given by



(A)
$$-16.e^{-2.5t}$$
 V (B) $14.e^{-2.5t}$ (C) $8.e^{-2.5t}$ V (D) $-10.e^{-2.5t}$ V

16.



Find
$$V_{r}(t)$$
 for all t?

- (A) $1.6[1 e^{-150t}]u(t)$ mV
- (B) $80[1 e^{-150t}]u(t)$ mV
- (C) $2.5[1 e^{-75t}]u(t)$ V
- (D) $1.6[1 e^{-75t}]u(t)$ mV
- 17. Consider the circuit shown in below figure



Find the steady state values of voltage and current(A)10V, 8.1 A(B)18V, -8.1 A(C)8V, 4.5 A(D)6V, 9 A

3.90 | Networks Test 4

18. Consider the circuit shown in figure



If $i(t) = I_m \cos(2t + f)$ Amp and time constant of the circuit is $\frac{1}{2}$ sec.

At what value of f, the circuit gives transient free response?

(A) 135° (B) 1.356 rad

(C) 77.70° (D) B and C

19. Consider the circuit shown in figure



Determine the values of
$$\frac{dt_L(0)}{dt}$$
 and $\frac{dt_C(0)}{dt}$

- (A) -10 A/sec and 0
- (B) 10 A/sec and -60 V/sec
- (C) 12.5 A/sec and 45 V/sec
- (D) 0 and -60 V/sec

20.



21. For the circuit shown in figure below, the switch has been in position 1 for a long time. At t = 0, the switch is moved to position 2. Then, the capacitor voltage $V_c(t)$ for t > 0 is



22. In a linear network, a 1 Ω resistor consumes a power of 4 W, when voltage source of 4 V is applied to the circuit

and 16 W when the voltage source is replaced by an 8 V source the power consumed by the 1 Ω resistor when 10 V is applied will be





23. The network realization of *RC* impedance function, $2s^2 + 7s + 3$

 $Z(s) = \frac{2s^2 + 7s + 3}{s^2 + 3s + 1}$ is as shown below what are the val-

ues of R and C?



(A)	1 Ω, 1 F	(B)	2 Ω, 0.5 F
(C)	1 Ω, 0.5 F	(D)	2Ω, 2F

24. Consider the circuit shown in below.



The value of
$$Z(s)$$
 is ______
(A) $\frac{3(8+2s)}{3s^2+10s+8}$ (B) $\frac{(8+3s)}{s^2+10s+8}$
(C) $\frac{2(8+3s)}{3s^2+10s+8}$ (D) $\frac{2(8+3s)}{s^2+10s+8}$

25. For the circuit shown below the resonant frequency f_0 is



(C) 830 kHz (D) 133 kHz

Answer Keys									
1. B	2. A	3. B	4. C	5. D	6. A	7. A	8. A	9. A	10. D
11. D	12. B	13. C	14. A	15. B	16. A	17. B	18. D	19. D	20. A
21. B	22. A	23. A	24. C	25. D					

HINTS AND EXPLANATIONS

- 1. We know *T*-parameters are defined interms of $V_1 = AV_2 - BI_2$ $I_1 = CV_2 - DI_2$ $Z_{in} = \frac{V_1}{I_1} = \frac{AV_2 - BI_2}{CV_2 - DI_2}$ But $V_2 = -Z_L I_2$ $\therefore \quad Z_{in} = \frac{AZ_L + B}{CZ_L + D}$ $= \frac{5+2}{2.5+1} = \frac{7}{3.5} = 2 \Omega$. Choice (B)
- 2. Replace the amplifier circuit with the thevenins equivalent circuit.



4.
$$Y = 0.2 + j\omega(0.1) + \frac{1}{2 + j\omega L}$$

 $Y = 0.2 + j\omega(0.1) + \frac{2 - j\omega L}{4 + (\omega_0 L)^2}$
At resonance Img $\{Y\} = 0$

$$\omega = \omega_{o}$$

$$\omega_{o}(0.1) = \frac{\omega_{0}L}{4 + (\omega_{0}L)^{2}}$$

$$4 + (\omega_{o}L)^{2} = 10 L$$

But given $\omega_{o} = 2 \text{ r/s}$

$$4L^{2} = 10L - 4$$

$$2L^{2} - 5L + 2 = 0$$

$$2L^{2} - 4L - L + 2 = 0$$

$$2L\{L - 2\} - 1\{L - 2\} = 0$$

$$L = 2 \text{ and } L = \frac{1}{2}$$

Choice (C)

- **5.** Tree branches are called twigs
 - $\therefore \quad \text{no. of twigs} = N 1$ Here N = 5
 - ∴ Twigs = 4
 Select the twigs, without forming closed loop.
 Co-tree branches are called links
 - ∴ Total branches = Twigs + links
 f loops:- It consists only one link and one or more than one twigs
 f-cut set:- It is a removal of one tree branch at a time.
 It consists only one tree branch and others links.
 - Choice (D)
- 6. *h*-parameters are defined interms of V = h + L + h + V

$$V_{1} - H_{11}I_{1} + H_{12}V_{2}$$

$$I_{2} = h_{21}I_{1} + h_{22}V_{2}$$
Let $V_{2} = 0$

$$h_{11} = \frac{V_{1}}{I_{1}}$$

$$V_{1} = 10I_{1} - 1.5V_{1}$$

$$2.5V_{1} = 10I_{1}$$

$$V_{1}/I_{1} = 4\Omega$$

$$I_{1} + I_{2} = \frac{-1.5V_{1}}{5}$$
But $V_{1} = 4I_{1}$

$$I_{1} + I_{2} = -0.3 \times 4I_{1}$$

$$2.2I_{1} = -I_{2}$$

$$\frac{I_{2}}{I_{1}} = -2.2$$
Choice (A)
7. $I_{rms} = \sqrt{\frac{1}{T}\int_{0}^{T} i^{2}(t) . dt}$

Consider one period of i(t)



$$i_{L}(t) = \frac{V_{L}}{X_{L}} = \frac{3}{5} \times \frac{75 \cos 500t}{(1 - j2)(j10)}$$

$$i_{L}(t) = \frac{4.5 \cos 500t}{(2 + j1)}$$

$$i_{L}(t) = 2 \cos(500t - 26.56^{\circ}) \text{ Amp} \qquad \text{Choice (A)}$$
9. For $i(t)$ to be maximum only when
$$\frac{di(t)}{dt} = 0 \text{ and } \frac{d^{2}i(t)}{dt^{2}} < 0$$
Given $i(t) = 2t.e^{-5t} A$

$$\frac{di}{dt} = 2\{e^{-5t} + t.(-5).e^{-5t}\} = 0$$

$$1 - 5t = 0$$

$$t = \frac{1}{5} \text{ sec} \qquad \text{Choice (A)}$$

10. After closing the switch the given circuit becomes

11. From the given data

$$V_{s} \stackrel{+}{\sim} V_{s} \stackrel{-}{\sim} V_{s} \stackrel{+}{\sim} V_{s} \stackrel{-}{\sim} V_{s} \stackrel{-}{\sim}$$

8.



$$V(t) = 15 i(t) = 75 \cos 500t V.$$

$$\omega = 500$$

$$\frac{V_L - V(t)}{20} + \frac{V_L}{j\omega L} + \frac{V(t)}{50} = 0$$

$$5[V_L - V(t)] + (-j10V_L) + 2V(t) = 0$$

$$5V_L - 5V(t) - j10 V_L + 2 V(t) = 0$$

$$V_L (5 - j10) = 3V(t)$$

$$V_L = \frac{3}{5} \frac{V(t)}{(1 - j2)}$$

Networks Test 4 | 3.93

12. From the given circuit

$$I_1 = I_s = 8A$$

 $I_3 = I_L = 3A$
 \therefore we know $I_S = \sqrt{I_R^2 + (I_L - I_C)^2}$
But $I_R = 0$
 $I_S = (I_L - I_C)$ or $I_C - I_L$
 \therefore $I_C = I_L + I_S = 11$ Amp Choice (B)
13. At low frequencies $f \rightarrow 0$ Hz
 $L \rightarrow$ short circuit
 $C \rightarrow$ open circuit
 $I_S = 0$ Amp

$$T_{R} = 0 \text{ volts at high frequencies}$$

$$f \to \infty$$

$$L \to \text{ open circuit}$$

$$C \to \text{ short circuit}$$

$$I_{R} = 0$$

$$\therefore V_{o} = 0$$

$$V_{0} \uparrow$$

$$f_{c1} \qquad f_{c2} \longrightarrow F$$

BPF

Choice (C)

14. The current through the coil is given by

$$i(t) = i(\infty) + \{i(0) - i(\infty)\} \cdot e^{\frac{-t}{\tau}}$$

$$i(0) = 0, i(\infty) = \frac{15}{200} = 75 \text{ mA}$$

$$\tau = \frac{L}{R} = \frac{30 \times 10^{-3}}{200} = 0.15 \text{ms}$$

$$i(t) = 75[1 - e^{-t/\tau}] \text{ mA}$$

If $i(td) = 40 \text{ mA}$, then $t_d = ?$

$$40 = 75[1 - e^{-t/\tau}]$$

$$e^{-t/\tau} = 0.466$$

$$-\frac{t_d}{\tau} = \ln(0.466)$$

$$t_d = 0.7621\tau = 0.11 \text{ msec}$$
 Choice (A)
15. We know

$$i_{c} = C \cdot \frac{dv_{c}}{dt}$$

$$V_{c} = \frac{1}{c} \int i_{c}(t) \cdot dt$$

$$= \frac{1}{1} \int -5 \cdot e^{-2.5} \cdot dt$$

$$V_{c} = \frac{-5}{-2.5} \cdot e^{-2.5t} = 2 \cdot e^{-2.5t} \text{ volts}$$

$$I_{R} = \frac{V_{C}}{R} = 2 \cdot e^{-2.5t} \text{ Amp}$$

$$I_{in} = I_{C} + I_{R} = -3.e^{-2.5t}$$

$$V_{in-}I_{in} \times 1 - L.\frac{dI_{in}}{dt} - V_{C} = 0$$

$$V_{in} = I_{in} + V_{C} + V_{L}$$

$$V_{L} = 2.\frac{d}{dt} \{-3.e^{-2.5t}\}$$

$$V_{L} = 6 \times 2.5.e^{-2.5t} \text{ volts}$$

$$V_{in} = -3.e^{-2.5t} + 2.e^{-2.5t} + 15.e^{-2.5t}$$

$$V_{in} = 14.e^{-2.5t} \text{ volts}$$
Choice (B)

16. For t < 0:-The independent current source deactivates (open circuit) $\therefore \quad i_r(0^-) = 0 \text{ Amp} = i_r(0^+)$

For
$$t > 0$$
:-



If $t \to \infty$, the circuit is in steady state $L \to$ short circuit

$$-80 \text{mA} + \frac{0.5V_x}{25} + i_L(\infty) = 0$$

$$V_x = \frac{i_L(\infty)}{50}$$

$$80 \times 10^{-3} = \frac{i_L(\infty)}{50} \times \frac{1}{50} + i_L(\infty)$$

$$i_L(\infty) \left[1 + \frac{1}{25 \times 10^2}\right] = 80 \times 10^{-3}$$

$$i_L(\infty) = 79.96 \text{ mA}$$

$$\therefore \quad i_L(t) = i(\infty) + [i(0^-) - i(\infty)].e^{-t/\tau}$$

$$i_L(t) = i(\infty)[1 - e^{-t/\tau}] u(t)$$

$$\tau = \frac{L_{eq}}{R_{eq}}$$

Res:-

- (i) Deactivate all the independent sources.
- (ii) Connect one test source
- (iii) Find the equivalent resistance

$$V$$

$$\therefore \quad R_{\text{th}} = \frac{V_t}{I_t}$$

$$V_t + V_x - 25 I_t - 0.5 V_x = 0$$

$$V_t = 25 I_t + 50 I_t$$

$$\frac{V_t}{I_t} = R_{th} = 75 \ \Omega$$

$$\tau = \frac{0.5}{75} = \frac{1}{150} \sec$$

$$\therefore \quad i_L(t) = 79.96[1 - e^{-150t}].u(t) \ \text{mA}$$

$$\therefore \quad V_x = \frac{i_L(t)}{50}$$

$$V_x(t) \approx 1.6[1 - e^{-150t}].u(t) \ \text{mV} \qquad \text{Choice (A)}$$

17. In steady state

- $C \rightarrow \text{open circuit}$
- $L \rightarrow$ short circuit

The equivalent circuit is

S.C S.C

$$4\Omega = \underbrace{V_{c}(\infty)}_{V_{c}(\infty)} = 18V$$

$$\frac{18}{4} + \frac{18}{5} + i(\infty) = 0$$

$$18 \times 9 = -20 \ i(\infty)$$

$$i(\infty) = -8.1 \text{ Amp}$$
Choice (B)

18. We know, the transient free conditions $\omega t_o + \phi = \tan^{-1} (\omega \tau + p / 2) \text{ [for cosinusoidal input]}$ $2 t_o + \phi = \left\{ \tan^{-1} \left[2 \times \frac{1}{2} \right] + \frac{\pi}{2} \right\}$ $t_o = 1 \text{ sec}$ $\phi = \frac{\pi}{4} + \frac{\pi}{2} - \frac{\pi}{4} + \frac{\pi}{2} - \frac{\pi}{4} + \frac{\pi}{2} + \frac{\pi}{4} + \frac{\pi}{4}$

$$\phi = \frac{3\pi}{4} - 2 = 1.356$$
 rad or 77.70°. Choice (D)

19. For *t* < 0:

In steady state the equivalent circuit becomes



$$-10 + \frac{V_x}{4} + i_c + i_L = 0$$

$$i_c = \frac{CdV_c}{dt}$$

$$V_L = L.\frac{di_L}{dt}$$
But $V_x = V_C$

$$-10 + \frac{V_c}{4} + C.\frac{dV_c}{dt} + i_L = 0$$
at $t = 0^+$

$$C\frac{dV_c(0^+)}{dt} = 10 - \frac{V_c(0^+)}{4} - i_L(0^+) = 10 - 15 - 10$$

$$\frac{dV_c(0^+)}{dt} = \frac{-15}{\frac{1}{4}}$$

$$\frac{dV_c(0^+)}{dt} = -60 \text{ V/sec}$$

$$V_x = V_L + 6i_L$$

$$V_x = V_C$$

$$V_c(0^+) = L\frac{di_L(0^+)}{dt} + 6i_L(0^+)$$

$$60 - 6 \times 10 = \frac{Ldi_L}{dt}$$

$$\frac{di_L}{dt} = 0 \text{ A/sec}$$
Choice (D)
For $t < 0$:-

20. For *t* < 0:-Switch opened;

$$\therefore \quad V_c(0^-) = 0 = V_c(0^+)$$

For $t > 0$:-
At $t = 0^+$ switch closed
 $V_c(0^+) = OV$

 $\therefore \text{ As } t \to \infty; \text{ circuit is in steady state} \\ \text{ In } S.S \text{ capacitor behaves like a open circuit.}$



$$V_{c}(t) = 4.83[1 - e^{-t/t}] \cdot u(t)$$

$$T_{t} = RC$$

$$R = R_{th}:-$$

$$-I_{t} + \frac{V_{t}}{250} + \frac{V_{t}}{50} - 0.1V_{x} = 0$$

$$V_{t} + V_{x} = 0$$

$$V_{t} + V_{x} = 0$$

$$V_{x} = -V_{t}$$

$$\frac{6V_{t}}{250} = I_{t} - 0.1V_{t}$$

$$6V_{t} = 250 I_{t} - 25 V_{t}$$

$$31V_{t} = 250 I_{t}$$

$$R_{th} = \frac{V_{t}}{I_{t}} = \frac{250}{31} = 8.064 \Omega$$

$$T = 8.064 \times 1 \text{ m sec}$$

$$T = 8.064 \text{ m sec}$$

$$V_{c}(t) = 4.83[1 - e^{-124t}]u(t) \text{ at } t = 2 \text{ m sec}$$

$$V_{c}(2m) = 1.06 \text{ volts}$$
Choice (A)

21. For t < 0:- The switch connected to position 1. at $t = 0^{-}$



:.
$$V_{C}(0^{-}) = \frac{3}{10} \times 30 = 9 \text{V} = V_{C}(0^{+})$$

For
$$t > 0$$
:- Switch \rightarrow position 2.
The circuit becomes of $t \rightarrow \infty$ (in steady state)



$$\therefore \quad V_{c}(\infty) = 20V$$

$$\therefore \quad V_{c}(t) = V_{c}(\infty) + \{V_{c}(0^{+}) - V_{c}(\infty)\} \cdot e^{-t/\tau}$$

$$\tau = RC = 5 \times \frac{1}{4} = 1.25 \text{ sec}$$

$$V_{c}(t) = 20 + \{9 - 20\} \cdot e^{-t/1.25} \text{ volts}$$

$$V_{c}(t) = 20 - 11 \cdot e^{-4t/5} \text{ volts}$$

Choice (B)

$$I_{1}^{-} = CV_{2}^{2} + D\tilde{I}_{2}^{2}$$
When $V_{1} = 4V$ and $P = 4W$
 $\therefore P = I_{2}^{2}R_{L}$

$$I_{2} = \sqrt{\frac{P}{R_{L}}} \text{ and } P = \frac{V_{2}^{2}}{R_{L}}$$

$$V_{2} = \sqrt{P.R_{L}} \text{ as } R_{L} = 2$$

$$4 = A\sqrt{P.R_{L}} + B.\sqrt{\frac{P}{R}}$$

$$4 = A\sqrt{4} + B\sqrt{4}$$

$$2A + 2B = 4$$

$$A + B = 2$$

$$A + AB = 2$$

$$V_{1} = 10$$

$$10 = 5A + 5B$$
 $\therefore V_{2} = 5 \text{ and } I_{2} = 5$

$$P = I_{2}^{2}R_{L}$$

$$= 25 \times 1 = 25W$$
Choice (A)
23. $Z(S) = 2 + \left[\frac{1}{SC} || \left\{1 || \left(R + \frac{1}{S}\right)\right\}\right]$
 \therefore By comparison we can get

$$R = 1 \Omega \text{ and } C = 1F$$
Choice (A)
24. $Z(s) = \left(\frac{2}{s}\right) || [1 + (2 + s) || 2]$

$$= \frac{2}{s} || \left[1 + \frac{4 + 2s}{4 + s}\right]$$

$$= \left(\frac{2}{s}\right) || \left[1 + \frac{4 + 2s}{4 + s}\right]$$

$$= \frac{2(8 + 3s)}{\frac{2}{s^{2} + 8s + 3s^{2}}}$$

$$Z(s) = \frac{2(8 + 3s)}{3s^{2} + 10s + 8}$$
Choice (C)

22. $V_1 = AV_2 + BI_2$

25.



3.96 | Networks Test 4

But
$$V_x = 0.5V_1 \times 1/sc$$

 $V_1 = 5 I_t$
 $V_x = \frac{2.5I_t}{sC}$
 $V_t = I_t \left[5 + sL + \frac{1}{sc} + \frac{2.5}{sc} \right]$
 $\frac{V_t}{I_t} = Z(s)$

$$Z(s) = 5 + j\omega \ 1 \times 10^{-3} - \frac{j3.5}{\omega \times 5 \times 10^{-9}}$$

at resonance image $Z(s) = 0$
$$\therefore \quad \omega^2 = \frac{3.5}{5 \times 10^{-9} \times 10^{-3}}$$

$$w^2 = \frac{3.5}{5} \times 10^{12}$$

$$\omega = 836.66 \times 10^3 \text{ rad/sec}$$

$$f_o = 133.158 \text{ kHz}$$
 Choice (D)