Ex 3.1

Answer 1.

(i) Rs25000 for $1\frac{1}{2}$ years at 10% per annum. Here P = Rs25000, t = $1\frac{1}{2}$ years, r = 10% Now, Amount after 1 year = $P\left(1 + \frac{r}{100}\right) = 25000\left(1 + \frac{10}{100}\right)$ $= 25000\left(1 + \frac{1}{10}\right) = 25000\left(\frac{11}{10}\right)$ = 27500Thus, principle for the next 6 months = Rs27500 Interest for the next 6 months = $\frac{27500 \times 6 \times 10}{100 \times 12}$ = 1375 Therefore, amount after $1\frac{1}{2}$ years = Rs27500 + Rs1375 = Rs28875 And CI = A - P = Rs28875 - Rs25000 = Rs3875 (ii) Rs32000 for 2 years at $7\frac{1}{2}$ % per annum. Here $P_1 = Rs32000$ and $r = 7\frac{1}{2}\% = \frac{15}{2}\%$ So, Amount after 1 year = $P\left(1 + \frac{r}{100}\right) = 32000\left(1 + \frac{15}{2 \times 100}\right)$ $= 32000\left(1 + \frac{3}{40}\right) = 32000\left(\frac{43}{40}\right)$ = 34400 Thus, $P_2 = Rs34400$ and $r = \frac{15}{2}\%$ So, Amount after 2 year = $P\left(1 + \frac{r}{100}\right) = 34400\left(1 + \frac{15}{2 \times 100}\right)$ $= 34400\left(1 + \frac{3}{40}\right) = 34400\left(\frac{43}{40}\right)$ = 36980 Hence, Amount = Rs 36980 Also, CI = A - P = Rs 36980 - Rs 32000 = Rs 4980

(iii) Rs10000 for $2\frac{1}{2}$ years at 6% per annum. Here $P_1 = Rs10000$ and r = 6%So, Amount after 1 year = $P\left(1 + \frac{r}{100}\right) = 10000\left(1 + \frac{6}{100}\right)$ $= 10000 \times \frac{106}{100} = 10600$ Thus, P2 = Rs10600 and r = 6% Amount after 2 year = $P\left(1 + \frac{r}{100}\right) = 10600\left(1 + \frac{6}{100}\right)$ $= 10600 \times \frac{106}{100} = 11236$ Thus, principle for the next 6 months = Rs11236 Interest for the next 6 months = $\frac{11236 \times 6 \times 6}{100 \times 12}$ = 337.08 Therefore, amount after $1\frac{1}{2}$ years = Rs11236 + Rs337.08 = Rs11573.08 And CI = A - P = Rs11573.08 - Rs10000 = Rs1573.08 (iv) Rs24000 for $1\frac{1}{2}$ years at $7\frac{1}{2}$ % per annum. Here P = Rs24000, t = $1\frac{1}{2}$ years, r = $7\frac{1}{2}\% = \frac{15}{2}\%$ Now, Amount after 1 year = $P\left(1 + \frac{r}{100}\right) = 24000\left(1 + \frac{15}{2 \times 100}\right)$ $= 24000\left(1 + \frac{3}{40}\right) = 24000\left(\frac{43}{40}\right)$ = 25800 Thus, principle for the next 6 months = Rs25800 Interest for the next 6 months = $\frac{25800 \times 15 \times 6}{200 \times 12}$ = 967.50 Therefore, amount after $1\frac{1}{2}$ years = Rs25800 + Rs967.50 = Rs26767.50 And CI = A - P = Rs26767.50 - Rs24000 = Rs2767.50

Answer 2A.

For 1st year: P = Rs. 16000, R = 15% and T = 1 year :. Interest = Rs. $\frac{16000 \times 15 \times 1}{100}$ = Rs. 2400 And, amount = Rs. 16000 + Rs. 2400 = Rs. 18400

For 2nd year: P = Rs. 18400, R = 12% and T = 1 year :. Interest = Rs. $\frac{18400 \times 12 \times 1}{100}$ = Rs. 2208 And, amount = Rs. 18400 + Rs. 2208 = Rs. 20608

:. Required amount = Rs. 20608 And, Compound Interest = A - P = Rs. 20608 - Rs. 16000 = Rs. 4608

Answer 2B.

For 1st year: P = Rs. 17500, R = 8% and T = 1 year :. Interest = Rs. $\frac{17500 \times 8 \times 1}{100}$ = Rs. 1400 And, amount = Rs. 17500 + Rs. 1400 = Rs. 18900

For 2nd year: P = Rs. 18900, R = 10% and T = 1 year :. Interest = Rs. $\frac{18900 \times 10 \times 1}{100}$ = Rs. 1890 And, amount = Rs. 18900 + Rs. 1890 = Rs. 20790

For 3rd year: P = Rs. 20790, R = 12% and T = 1 year :. Interest = Rs. $\frac{20790 \times 12 \times 1}{100}$ = Rs. 2494.80 And, amount = Rs.20790 + Rs.2494.80 = Rs.23284.80

:. Required amount = Rs. 23284.80 And, Compound Interest = A - P = Rs. 23284.80 - Rs. 17,500 = Rs. 5784.80

Answer 3.

Here P₁ = Rs20000 and r = 10%
So, Amount after 1 year = P
$$\left(1 + \frac{r}{100}\right)$$
 = 20000 $\left(1 + \frac{10}{100}\right)$
= 20000 × $\frac{110}{100}$ = 22000
Thus, P₂ = Rs22000 and r = 10%
Amount after 2 year = P $\left(1 + \frac{r}{100}\right)$ = 22000 $\left(1 + \frac{10}{100}\right)$
= 22000 × $\frac{110}{100}$ = 24200
Thus, P₃ = Rs24200 and r = 10%
Amount after 3 year = P $\left(1 + \frac{r}{100}\right)$ = 24200 $\left(1 + \frac{10}{100}\right)$
= 24200 × $\frac{110}{100}$ = 26620

Hence, Amount = Rs 26620 Also, CI = A - P = Rs 26620 - Rs 20000 = Rs 6620

Answer 4.

For 1st year: P = Rs. 5000, R = 10% and T = 1 year :. Interest = Rs. $\frac{5000 \times 10 \times 1}{100}$ = Rs. 500 And, amount = Rs.5000 + Rs.500 = Rs.5500 For 2nd year: P = Rs. 5500, R = 10% and T = 1 year :. Interest = Rs. $\frac{5500 \times 10 \times 1}{100}$ = Rs. 550 And, amount = Rs.5500 + Rs.550 = Rs.6050 For 3rd year: P = Rs. 6050, R = 10% and T = 1 year :. Interest = Rs. $\frac{6050 \times 10 \times 1}{100}$ = Rs. 605

:. Compound interest for 3rd year is Rs. 605.

Answer 5.

For 1st year: P = Rs. 25600, R = 5% and T = 1 year :. Interest = Rs. $\frac{25600 \times 5 \times 1}{100}$ = Rs. 1280 And, amount = Rs.25600 + Rs.1280 = Rs.26880

For 2nd year: P = Rs. 26880, R = 5% and T = 1 year :. Interest = Rs. $\frac{26880 \times 5 \times 1}{100}$ = Rs. 1344 And, amount = Rs.26880 + Rs.1344 = Rs.28224

:: Amount at the end of 2nd year is Rs. 28224.

Answer 6.

Here P₁ = Rs7500 and rate of interest for half year (r) = 4%
So, Amount after
$$\frac{1}{2}$$
 year = P $\left(1 + \frac{r}{100}\right)$ = 7500 $\left(1 + \frac{4}{100}\right)$
= 7500 x $\frac{104}{100}$ = 7800

Thus, P₂ = Rs/800 and r = 4%
Amount after 1 year = P
$$\left(1 + \frac{r}{100}\right)$$
 = 7800 $\left(1 + \frac{4}{100}\right)$
= 7800 × $\frac{104}{100}$ = 8112
Thus, P₃ = Rs8112 and r = 4%

Amount after
$$1\frac{1}{2}$$
 year = $P\left(1 + \frac{r}{100}\right) = 8112\left(1 + \frac{4}{100}\right)$
= $8112 \times \frac{104}{100} = 8436.48$

Hence, Amount = Rs 8436.48 Also, CI = A - P = Rs 8436.48 - Rs 7500 = Rs 936.48

Answer 7.

Since, Amount after 1 year =
$$P\left(1 + \frac{r}{100}\right)$$

$$\Rightarrow 27600 = 24000 \left(1 + \frac{r}{100}\right)$$

$$\Rightarrow 1 + \frac{r}{100} = \frac{27600}{24000} = \frac{23}{20}$$

$$\Rightarrow \frac{r}{100} = \frac{23}{20} - 1 = \frac{3}{20}$$

$$\Rightarrow r = \frac{100 \times 3}{20} = 15$$

Amount after 2 year = P $\left(1 + \frac{r}{100}\right) = 27600 \left(1 + \frac{15}{100}\right)$

$$= 27600 \times \frac{115}{100} = 31740$$

Answer 8.

Here P₁ = Rs14000 and r = 5%
So, Amount after 1 year = P
$$\left(1 + \frac{r}{100}\right)$$
 = 14000 $\left(1 + \frac{5}{100}\right)$
= 14000 × $\frac{105}{100}$ = 14700
Thus, P₂ = Rs14700 and r = 8%
Amount after 2 year = P $\left(1 + \frac{r}{100}\right)$ = 14700 $\left(1 + \frac{8}{100}\right)$
= 14700 × $\frac{108}{100}$ = 15876

Hence, Amount = Rs 15876

Answer 9.

Here P₁ = Rs17500 and r = 4%
So, Amount after 1 year = P
$$\left(1 + \frac{r}{100}\right)$$
 = 17500 $\left(1 + \frac{4}{100}\right)$
= 17500 × $\frac{104}{100}$ = 18200
Thus, P₂ = Rs18200 and r = 5%
Amount after 2 year = P $\left(1 + \frac{r}{100}\right)$ = 18200 $\left(1 + \frac{5}{100}\right)$
= 18200 × $\frac{105}{100}$ = 19110
Thus, P₃ = Rs19110 and r = 6%
Amount after 3 year = P $\left(1 + \frac{r}{100}\right)$ = 19110 $\left(1 + \frac{6}{100}\right)$

$$= 19110 \times \frac{106}{100} = 20256.60$$

Hence, Amount = Rs 20256.60 Also, CI = A - P = Rs 20256.60 - Rs 17500 = Rs2756.60

Answer 10.

For 1st half-year: P = Rs. 4000, R = 14% and T = $\frac{1}{2}$ year Interest = Rs. $\frac{4000 \times 14 \times 1}{100 \times 2}$ = Rs. 280 And, amount = Rs. 4000 + Rs. 280 = Rs. 4280

For 2nd half-year: P = Rs. 4280, R = 14% and T = $\frac{1}{2}$ year Interest = Rs. $\frac{4280 \times 14 \times 1}{100 \times 2}$ = Rs. 299.60 And, amount = Rs. 4280 + Rs. 299.60 = Rs. 4579.60

For 3rd half-year: P = Rs. 4579.60, R = 14% and T = $\frac{1}{2}$ year Interest = Rs. $\frac{4579.60 \times 14 \times 1}{100 \times 2}$ = Rs. 320.572 And, amount = Rs. 4579.60 + Rs. 320.572 = Rs. 4900.172

Thus, the amount to be paid at the end of $1\frac{1}{2}$ years is Rs. 4900.172.

Answer 11.

Here P₁ = Rs42000 and rate of interest for half year = 4%, t = 4 half years So, Amount after $\frac{1}{2}$ year = P $\left(1 + \frac{r}{100}\right)$ = 42000 $\left(1 + \frac{4}{100}\right)$ = 42000 × $\frac{104}{100}$ = 43680 Thus, P₂ = Rs43680 Amount after 1 year = P $\left(1 + \frac{r}{100}\right)$ = 43680 $\left(1 + \frac{4}{100}\right)$ = 43680 × $\frac{104}{100}$ = 45427.20 Thus, P₃ = Rs45427.20 Amount after 1 $\frac{1}{2}$ year = P $\left(1 + \frac{r}{100}\right)$ = 45427.20 $\left(1 + \frac{4}{100}\right)$ = 45427.20 × $\frac{104}{100}$ = 47244.29 Thus, P₄ = Rs47244.29 Amount after 2 year = P $\left(1 + \frac{r}{100}\right)$ = 47244.29 $\left(1 + \frac{4}{100}\right)$ = 47244.29 × $\frac{104}{100}$ = 49134.06

Hence, Amount = Rs 49134.06 Also, CI = A - P = Rs 49134.06 - Rs 42000 = Rs 7134.06

Answer 12.

Case I: Here P = Rs15000 and r = 10.5% So, Amount after 1 year = P $\left(1 + \frac{r}{100}\right)$ = 15000 $\left(1 + \frac{10.5}{100}\right)$ = 15000 × $\frac{110.5}{100}$ = 16575

Case II: Here P₁ = Rs15000 and rate of interest for half year (r) = 5% So, Amount after $\frac{1}{2}$ year = P $\left(1 + \frac{r}{100}\right)$ = 15000 $\left(1 + \frac{5}{100}\right)$ = 15000 × $\frac{105}{100}$ = 15750 Thus, P₂ = Rs15750 and r = 5%

Amount after 1 year = $P\left(1 + \frac{r}{100}\right) = 15750\left(1 + \frac{5}{100}\right)$ = $15750 \times \frac{105}{100} = 16537.50$

Hence the first man gains by Rs16575 - Rs16537.50 = Rs37.50

Answer 13.

Case I: Here P₁ = Rs20000 and r = 12% So, Amount after 1 year = $P\left(1 + \frac{r}{100}\right) = 20000\left(1 + \frac{12}{100}\right)$ $= 20000 \times \frac{112}{100} = 22400$ Thus, P₂ = Rs22400 and r = 12% Amount after 2 year = $P\left(1 + \frac{r}{100}\right) = 22400\left(1 + \frac{12}{100}\right)$ $= 22400 \times \frac{112}{100} = 25088$ Thus, P₃ = Rs25088 and r = 12% Amount after 3 year = $P\left(1 + \frac{r}{100}\right) = 25088\left(1 + \frac{12}{100}\right)$ $= 25088 \times \frac{112}{100} = 28098.56$ Hence, Amount = Rs 28098.56 Also, CI = A - P = Rs 28098.56 - Rs 20000 = Rs 8098.56 Case II:

Simple interest = $\frac{20000 \times 12 \times 3}{100}$ = 7200 Difference between C.I. and S.I. = Rs 8098.56 - Rs 7200 = Rs 898.56

Answer 14.

Since, Simple interest =
$$\frac{P \times r \times t}{100}$$

 $\Rightarrow 1500 = \frac{P \times 4 \times 2}{100} \Rightarrow P = \frac{150000}{8} = 18750$
Now for CI, P = Rs 18750, r = 4%, t = 2 year
Here P₁ = Rs 18750 and r = 4%
So, Amount after 1 year = $P\left(1 + \frac{r}{100}\right) = 18750\left(1 + \frac{4}{100}\right)$
 $= 18750 \times \frac{104}{100} = 19500$
Thus, P₂ = Rs19500 and r = 4%
Amount after 2 year = $P\left(1 + \frac{r}{100}\right) = 19500\left(1 + \frac{4}{100}\right)$
 $= 19500 \times \frac{104}{100} = 20280$

Hence, Amount = Rs 20280 Also, CI = A – P = Rs 20280 – Rs 18750 = Rs 1530

Answer 15.

Case I: Here P₁ = Rs 5000 and r = 6% So, Amount after 1 year = P $\left(1 + \frac{r}{100}\right)$ = 5000 $\left(1 + \frac{6}{100}\right)$ = 5000 × $\frac{106}{100}$ = 5300 Amount after 2 year = P $\left(1 + \frac{r}{100}\right)$ = 5300 $\left(1 + \frac{6}{100}\right)$ = 5300 × $\frac{106}{100}$ = 5618 Thus, P₃ = Rs 5618 and r = 6% Amount after 3 year = P $\left(1 + \frac{r}{100}\right)$ = 5618 $\left(1 + \frac{6}{100}\right)$ = 5618 × $\frac{106}{100}$ = 5955.08 Hence, Amount = Rs 5955.08

Also, CI = A - P = Rs 5955.08 - Rs 5000 = Rs 955.08

Case II: Simple interest = $\frac{5000 \times 6 \times 3}{100}$ = 900 Difference between C.I. and S.I. = Rs 955.08 - Rs 900 = Rs 55.08

Answer 16.

Since Simple interest =
$$\frac{P \times r \times t}{100}$$

 $\Rightarrow 450 = \frac{P \times 4 \times 2}{100} \Rightarrow P = \frac{45000}{8} = 5625$
Now for CI, P = Rs 5625, r = 4, t = 1 year
Here P₁ = Rs5625 and rate of interest for half-yearly = 2%
So, Amount after $\frac{1}{2}$ year = $P\left(1 + \frac{r}{100}\right) = 5625\left(1 + \frac{2}{100}\right)$
 $= 5625 \times \frac{102}{100} = 5737.50$
Thus, P₂ = Rs 5737.50 and r = 2%
Amount after 1 year = $P\left(1 + \frac{r}{100}\right) = 5737.50\left(1 + \frac{2}{100}\right)$
 $= 102$

Hence, Amount = Rs 5852.25

Also, CI = A - P = Rs 5852.25 - Rs 5625 = Rs 227.25

Answer 17.

Case I: Simple interest = $\frac{62500 \times 8 \times 2}{100}$ = 10000 Amount = Rs 62500 + Rs 10000 = Rs 72500 Case II: Here P₁ = Rs 62500 and r = 8% So, Amount after 1 year = P $\left(1 + \frac{r}{100}\right)$ = 62500 $\left(1 + \frac{8}{100}\right)$ = 62500 × $\frac{108}{100}$ = 67500 Thus, P₂ = Rs 67500 and r = 8% Amount after 2 year = P $\left(1 + \frac{r}{100}\right)$ = 67500 $\left(1 + \frac{8}{100}\right)$ = 67500 × $\frac{108}{100}$ = 72900 Hence, Amount = Rs 72900

Thus, gain in amount = Rs 72900 – Rs 72500 = Rs 400

Answer 18.

For 1st year: P = Rs. 100, R = 10% and T = 1 year Interest = Rs. $\frac{100 \times 10 \times 1}{100}$ = Rs. 10 Amount = Rs. 100 + Rs. 10 = Rs. 110

For 2nd year: P = Rs. 110, R = 15% and T = 1 year Interest = Rs. $\frac{110 \times 15 \times 1}{100}$ = Rs. 16.50 Amount = Rs. 110 + Rs. 16.50 = Rs. 126.50

When amount is Rs. 126.50, Principal is Rs. 100. Hence, when amount is Rs. 10120, Principal = Rs. $\frac{10120 \times 100}{126.50}$ = Rs. 8000

Answer 19.

To calculate the S.I. paid by Sunil: P = Rs.50000, R = 10% and T = $1\frac{1}{2}$ years = $\frac{3}{2}$ years \therefore S.I. = Rs. $\frac{50000 \times 10 \times 3}{100 \times 2}$ = Rs. 7500

To calculate the C.I. earned by Sunil: For 1st year: P = Rs.50000, R = 10% and T = 1 year :. Interest = Rs. $\frac{50000 \times 10 \times 1}{100}$ = Rs. 5000 And, amount = Rs.50000 + Rs.5000 = Rs.55000

For next half year: P = Rs. 55000, R = 10% and T = $\frac{1}{2}$ year :. Interest = Rs. $\frac{55000 \times 10 \times 1}{100 \times 2}$ = Rs. 2750 And, amount = Rs. 55000 + Rs. 2750 = Rs. 57750 :. Total CL correct _ Ro. 57750 _ Ro. 50000 _ Ro. 7750

Answer 20.

Let the value of mobile in the beginning be Rs. 100. For 1st year, depreciation = 5% of Rs. $100 = \frac{5}{100} \times 100 =$ Rs. 5 Value of machine for second year = Rs. 100 - Rs. 5 = Rs. 95

For 2nd year, depreciation = 5% of Rs. $95 = \frac{5}{100} \times 95 = Rs. 4.75$ Value of machine for third year = Rs. 95 - Rs. 4.75 = Rs. 90.25

For 3rd year, depreciation = 10% of Rs. $90.25 = \frac{10}{100} \times 90.25 = Rs. 9.025$ Value of machine at the end of third year = Rs. 90.25 - Rs. 9.025 = Rs. 81.225

Net depreciation = Rs. 100 - Rs. 81.225 = Rs. 18.775 or 18.775%

Answer 21.

For 1sthalf year : P = Rs. 6500, R = 10% and T = $\frac{1}{2}$ year Interest = Rs. $\frac{6500 \times 10 \times 1}{100 \times 2}$ = Rs. 325 Amount = Rs. 6500 + Rs. 325 = Rs. 6825

Money paid at the end of 1^{s} half year = Rs. 2000. Balance money for 2^{nd} half year = Rs. 6825 - Rs. 2000 = Rs. 4825.

For 2ndhalf year : P = Rs. 4825; R = 10% and T = $\frac{1}{2}$ year Interest = Rs. $\frac{4825 \times 10 \times 1}{100 \times 2}$ = Rs. 241.25 Amount = Rs. 4825 + Rs. 241.25 = Rs. 5066.25

Money paid at the end of 2^{nd} half year = Rs. 2000 Balance money for 3^{rd} half year = Rs. 5066.25 - Rs. 2000 = Rs. 3066.25

For 3rdhalf year : P = Rs. 3066.25; R = 10% and T = $\frac{1}{2}$ year Interest = Rs. $\frac{3066.25 \times 10 \times 1}{100 \times 2}$ = Rs. 153.3125 Amount = Rs. 3066.25 + Rs. 153.3125 = Rs. 3219.5625

Money paid at the end of 3rdhalf year = Rs. 2000 Amount outstanding at the end of 3rdpayment

- = Rs. 3219.5625 Rs. 2000
- = Rs. 1219.5625
- = Rs. 1220 (nearest rupee)

Answer 22.

For 1sthalf year : P = Rs. 20000, R = 10% and T = 1 year Interest = Rs. $\frac{20000 \times 10 \times 1}{100}$ = Rs. 2000 Amount = Rs. 20000 + Rs. 2000 = Rs. 22000

Money paid at the end of 1^{s} half year = Rs. 5000 Balance money for 2^{nd} half year = Rs. 22000 – Rs. 5000 = Rs. 17000

For 2ndhalf year : P = Rs. 17000; R = 10% and T = 1 year Interest = Rs. $\frac{17000 \times 10 \times 1}{100}$ = Rs. 1700 Amount = Rs. 17000 + Rs. 1700 = Rs. 18700

Money paid at the end of 2ndhalf year = Rs. 10000 Balance money for 3rdhalf year = Rs. 18700 - Rs. 10000 = Rs. 8700

For 3rdhalf year : P = Rs. 8700; R = 10% and T = 1 year Interest = Rs. $\frac{8700 \times 10 \times 1}{100}$ = Rs. 870 Amount = Rs. 8700 + Rs. 870 = Rs. 9570

A man should pay Rs. 9570 at the end of 3rd year to clear the account.

Answer 23.

Let the value of ring (P₁) = Rs. 100. Appreciation (C.I.) for the 1st year = Rs. $\frac{100 \times 10 \times 1}{100}$ = Rs. 10 \therefore Value of the ring at the end of 1st year (A₁) = Rs.100 + Rs.10 = Rs. 110

:. Value of the ring at the beginning of 2^{nd} year (P₂) = Rs. 110 Appreciation (C.I.) for the 2^{nd} year = Rs. $\frac{110 \times 10 \times 1}{100}$ = Rs. 11

Sum of the appreciation (C.I.) of 1^{st} year and appreciation (C.I.) of 2^{nd} year = Rs. (10 + 11) = Rs. 21

Thus, when sum of appreciation is Rs.21, then value of the ring (P_1) = Rs. 100 And, when sum of appreciation is Rs. 6300, then value of the ring

= Rs. $\frac{100 \times 6300}{21}$ = Rs. 30000

So, the value of the ring is Rs. 30000.

Answer 24.

For 1st year : P = Rs. 15500, R = 10% and T = 1 year Interest = Rs. $\frac{15500 \times 10 \times 1}{100}$ = Rs. 1550 Amount = Rs. 15500 + Rs. 1550 = Rs. 17050 For 2nd year : P = Rs. 17050; R = 15% and T = 1 year Interest = Rs. $\frac{17050 \times 15 \times 1}{100}$ = Rs. 2557.50 Amount = Rs. 17050 + Rs. 2557.50 = Rs. 19607.50 For 3rd year : P = Rs. 19607.50; R = 20% and T = 1 year Interest = Rs. $\frac{19607.50 \times 20 \times 1}{100}$ = Rs. 3921.50 Amount = Rs. 19607.50 + Rs. 3921.50 = Rs. 23529 Difference between the C.I. of the 2nd year and the 3rd year

= Rs. (3921.50 – 2557.50) = Rs. 1364

Answer 25.

For 1st year : P = Rs. 7500, R = 30% and T = 1 year Interest = Rs. $\frac{7500 \times 30 \times 1}{100}$ = Rs. 2250 Amount = Rs. 7500 + Rs. 2250 = Rs. 9750

For 2^{nd} year : P = Rs. 9750; R = 30% and T = 1 year Interest = Rs. $\frac{9750 \times 30 \times 1}{100}$ = Rs. 2925 Amount = Rs. 9750 + Rs. 2925 = Rs. 12675

Thus, total amount to be paid by Samidha = Rs. 12675 But, Samidha gave Rs. 10000 + juicer to Shreya. \Rightarrow Rs. 10000 + Cost of juicer = Rs. 12675 \Rightarrow Cost of juicer = Rs. (12675 - 10000) = Rs. 2675

Ex 3.2

Answer 1.

(i) Rs 8000 for 3 years at 10% per annum compounded annually. Here P = Rs 8000, t = 3 years, r = 10% 2

Now, Amount =
$$P\left(1 + \frac{r}{100}\right)^{c} = 8000\left(1 + \frac{10}{100}\right)^{3}$$

= $8000\left(\frac{11}{10}\right)^{3}$
= $8000 \times \frac{1331}{1000} = 10648$
Hence, Amount = Rs 10648
Also, CI = A - P = Rs 10648 - Rs 8000 = Rs 2648

.

(ii) Rs 15000 for 2 years at 8% per annum compounded semi-annually. Here P = Rs 15000, t = 2 years, r = 8% Since interest is compounded semi-annually, so

Amount =
$$P\left(1 + \frac{r}{200}\right)^{2t} = 15000\left(1 + \frac{8}{200}\right)^{4}$$

= $15000\left(\frac{26}{25}\right)^{4}$
= $15000 \times \frac{26}{25} \times \frac{26}{25} \times \frac{26}{25} \times \frac{26}{25} = 17547.88$
Hence, Amount = Rs 17547.88
Also, CI = A - P = Rs 17547.88 - Rs 15000 = Rs 2547.88

(iii) Rs12000 for $1\frac{1}{2}$ years at 5% per annum compounded annually. Here P = Rs 12000, t = $1\frac{1}{2}$ years, r = 5% Now, Amount after 1 year = $P\left(1 + \frac{r}{100}\right)^t = 12000\left(1 + \frac{5}{100}\right)$ $= 12000 \left(\frac{105}{100} \right)$ = 12600

Now interest for the next half year = $=\frac{12600 \times 5}{100 \times 2} = 315$ Hence, Amount = Rs 12600 + Rs 315 = Rs 12915 Also, CI = A-P = Rs 12915 - Rs 12000 = Rs 915

(iv) Rs 25000 for 2 years at 6% per annum compounded semi-annually. Here P = Rs25000, t = 2 years, r = 6% Since interest is compounded semi-annually, so

Amount = $P\left(1 + \frac{r}{200}\right)^{2t} = 25000\left(1 + \frac{6}{200}\right)^{4}$ = $25000\left(\frac{103}{100}\right)^{4}$ = 28137.72 Hence, Amount = Rs 28137.72 Also, CI = A - P = Rs 28137.72 - Rs 25000 = Rs 3137.72

(v) Rs16000 for 3 years at 10%, 8% and 6% for successive years. Here P = Rs 16000, t = 3 years, r = 10%, 8%, 6% successively.

Now, Amount =
$$P\left(1 + \frac{r_1}{100}\right)\left(1 + \frac{r_2}{100}\right)\left(1 + \frac{r_3}{100}\right)$$

= $16000\left(1 + \frac{10}{100}\right)\left(1 + \frac{8}{100}\right)\left(1 + \frac{6}{100}\right)$
= $16000\left(\frac{11}{10}\right)\left(\frac{108}{100}\right)\left(\frac{106}{100}\right)$
= 20148.48
Hence, Amount = Rs 20148.48

Also, CI = A - P = Rs 20148.48 - Rs 16000 = Rs 4148.48

Answer 2.

Here P = Rs15000, t =
$$2\frac{1}{2}$$
 years, r = 10%
Now, Amount after 2 year = $P\left(1 + \frac{r}{100}\right)^{t} = 15000\left(1 + \frac{10}{100}\right)^{2}$
= $15000\left(\frac{11}{10}\right)^{2}$
= 18150

Now interest for the next half year = $\frac{18150 \times 10}{100 \times 2}$ = 907.5 Hence, Amount = Rs 18150 + Rs 907.50 = Rs19057.50 Also, CI = A - P = Rs 19057.50 - Rs 15000 = Rs 4057.50

Answer 3.

Here P = Rs 36000, t = 2 years, r = 15%
Now, Amount = P
$$\left(1 + \frac{r}{100}\right)^{t}$$
 = 36000 $\left(1 + \frac{15}{100}\right)^{2}$
= 36000 $\left(\frac{115}{100}\right)^{2}$
= 47610
Hence, Amount = Rs 47610

Answer 4.

Here P = Rs50000, t = $1\frac{1}{2}$ years, r = 8% Since interest is compounded half-yearly, so Now, Amount = $P\left(1 + \frac{r}{200}\right)^{2t} = 50000\left(1 + \frac{8}{200}\right)^{3}$ = $50000\left(\frac{104}{100}\right)^{3}$ = 56243.20Hence, Amount = Rs 56243.20 Also, CI = A - P = Rs 56243.20 - Rs 50000 = Rs 6243.20

Answer 5.

Here P = Rs25000, t = 2 years, r = 4%, 5% successively
Now, Amount = P
$$\left(1 + \frac{r_1}{100}\right)\left(1 + \frac{r_2}{100}\right)$$

= 25000 $\left(1 + \frac{4}{100}\right)\left(1 + \frac{5}{100}\right)$
= 25000 $\left(\frac{104}{100}\right)\left(\frac{105}{100}\right)$
= 27300
Hence, Amount = Rs 27300

Answer 6.

Here P = Rs31250, t = 3 years, r = 8%, 10%, 12% successively.

Now, Amount =
$$P\left(1 + \frac{r_1}{100}\right)\left(1 + \frac{r_2}{100}\right)\left(1 + \frac{r_3}{100}\right)$$

= $31250\left(1 + \frac{8}{100}\right)\left(1 + \frac{10}{100}\right)\left(1 + \frac{12}{100}\right)$
= $31250\left(\frac{108}{100}\right)\left(\frac{110}{100}\right)\left(\frac{112}{100}\right)$
= 41580

Hence, Amount = Rs 41580

Answer 7.

Here P = Rs 28000, A = 30870, t = 2 years
Now, P
$$\left(1 + \frac{r}{100}\right)^{t} = A \Rightarrow 28000 \left(1 + \frac{r}{100}\right)^{2} = 30870$$

 $\Rightarrow \left(1 + \frac{r}{100}\right)^{2} = \frac{30870}{28000} = \frac{441}{400} = \left(\frac{21}{20}\right)^{2}$

$$\Rightarrow 1 + \frac{r}{100} = \frac{21}{20} \Rightarrow \frac{r}{100} = \frac{21}{20} - 1 = \frac{1}{20} \Rightarrow R = \frac{100}{20} = 5$$

Hence rate of interest is 5%.

Answer 8.

Here P = Rs 15625, A = 17576, r = 4%
Now, P
$$\left(1 + \frac{r}{100}\right)^{t} = A \Rightarrow 15625 \left(1 + \frac{4}{100}\right)^{t} = 17576$$

 $\Rightarrow \left(\frac{26}{25}\right)^{t} = \frac{17576}{15625} = \left(\frac{26}{25}\right)^{3}$

By comparing powers, t = 3 Hence time is 3 years.

Answer 9.

Here P = Rs 2000, A = Rs 2662, r = 10%
Now,
$$P\left(1 + \frac{r}{100}\right)^{t} = A \Rightarrow 2000\left(1 + \frac{10}{100}\right)^{t} = 2662$$

 $\Rightarrow \left(\frac{11}{10}\right)^{t} = \frac{2662}{2000} = \frac{1331}{1000} = \left(\frac{11}{10}\right)^{3}$
By comparing powers, t = 3
Hence time is 3 years.

Answer 10.

Since, Simple interest = $\frac{P \times r \times t}{100}$ $\Rightarrow 600 = \frac{P \times 4 \times 3}{100} \Rightarrow P = \frac{60000}{12} = 5000$ Now for CI, P = Rs 5000, r = 4%, t = 3 year Amount = P $\left(1 + \frac{r}{100}\right)^t = 5000 \left(1 + \frac{4}{100}\right)^3$

$$= 5000 \times \left(\frac{26}{25}\right)^3 = 5624.32$$

Hence, Amount = Rs 5624.32 Also, CI = A - P = Rs 5624.32 - Rs 5000 = Rs 624.32

Answer 11.

Let sum be Rs P and r % be the rate of interest. We have t = 2 years, CI = Rs 40.80 and SI = Rs 40 Since, Simple interest = $\frac{P \times r \times t}{100}$ $\Rightarrow 40 = \frac{P \times r \times 2}{100} \Rightarrow Pr = \frac{4000}{2} = 2000$

Now,

$$CI = A - P = P\left(1 + \frac{r}{100}\right)^{t} - P = P\left[\left(1 + \frac{r}{100}\right)^{t} - 1\right]$$

$$\Rightarrow 40.80 = P\left[\left(1 + \frac{r}{100}\right)^{2} - 1\right]$$

$$\Rightarrow 40.80 = P\left(1 + \frac{r^{2}}{10000} + \frac{2r}{100} - 1\right)$$

$$\Rightarrow 40.80 = P\left(1 + \frac{r^{2}}{10000} + \frac{2r}{100} - 1\right)$$

$$\Rightarrow 40.80 = P\left(\frac{r^{2}}{10000} + \frac{2r}{100}\right)$$

$$\Rightarrow 40.80 = Pr\left(\frac{r}{10000} + \frac{2}{100}\right)$$

$$\Rightarrow 40.80 = Pr\left(\frac{r}{10000} + \frac{2}{100}\right)$$

$$\Rightarrow 40.80 = 2000\left(\frac{r + 200}{10000}\right)$$

$$\Rightarrow 40.80 = \frac{r + 200}{5}$$

$$\Rightarrow r = 40.80 \times 5 - 200 = 204 - 200 = 4$$

Hence, $r = 4\%$.

Now, Pr = $2000 \Rightarrow P = \frac{2000}{r} = \frac{2000}{4} = 500$. Thus, sum is Rs500 and rate of interest is 4%.

Answer 12.

Since, C.I. = A - P
C.I. =
$$P\left(1 + \frac{8}{100}\right)^2 - P = P\left(\frac{108}{100}\right)^2 - P = \frac{11664P}{10000} - P = \frac{11664P - 10000P}{10000} = \frac{1664P}{10000}$$

S.I. = $\frac{P \times 8 \times 2}{100} = \frac{16P}{100}$
Now, C.I. - S.I. = Rs. 448
 $\Rightarrow \frac{1664P}{10000} - \frac{16P}{100} = Rs. 448$
 $\Rightarrow \frac{1664P - 1600P}{10000} = Rs. 448$
 $\Rightarrow 64P = Rs. 4480000$
 $\Rightarrow P = Rs. 70000$

Hence, the sum is Rs. 70000.

Answer 13.

Let the rate of interest per year be r%. S.I. in 2 years = Rs. $\frac{50000 \times r \times 2}{100}$ = Rs. 1000r And, C.I. in 2 years = A - P = Rs. $50000 \left(1 + \frac{r}{100}\right)^2$ - Rs. 50000 Given, C.I. - S.I. = Rs. 125 $\Rightarrow 50000 \left(1 + \frac{r}{100}\right)^2$ - 50000 - 1000r = 125 $\Rightarrow 50000 \left(1 + \frac{r^2}{10000} + \frac{2r}{100}\right)$ - 50000 - 1000r = 125 $\Rightarrow 50000 + 5r^2 + 1000r - 50000 - 1000r = 125$ $\Rightarrow 5r^2 = 125$ $\Rightarrow r^2 = 25$ $\Rightarrow r = \pm 5$ But the rate of interest cannot be negative.

... Rate of interest is 5%.

Answer 14.

Given: Amount = Rs. 15729, n = 2 years, $r_1 = 5$ and $r_2 = 7\%$ $A = P\left(1 + \frac{r_1}{100}\right)\left(1 + \frac{r_2}{100}\right)$ $\Rightarrow 15729 = P\left(1 + \frac{5}{100}\right)\left(1 + \frac{7}{100}\right)$ $\Rightarrow 15729 = P\left(\frac{105}{100}\right)\left(\frac{107}{100}\right)$ $\Rightarrow P = \frac{15729 \times 100 \times 100}{105 \times 107}$ $\Rightarrow P = Rs. 14000$

Answer 15.

Given : A = Rs. 13891.50, P = Rs. 12000, n = 3 years
13891.50 = 12000
$$\left(1 + \frac{r}{100}\right)^3$$

 $\Rightarrow \frac{13891.50}{12000} = \left(1 + \frac{r}{100}\right)^3$
 $\Rightarrow \frac{1389150}{12000 \times 100} = \left(1 + \frac{r}{100}\right)^3$
 $\Rightarrow \frac{9261}{8000} = \left(1 + \frac{r}{100}\right)^3$
 $\Rightarrow \frac{21}{20} = 1 + \frac{r}{100}$
 $\Rightarrow \frac{21}{20} - 1 = \frac{r}{100}$
 $\Rightarrow \frac{1}{20} = \frac{r}{100}$
 $\Rightarrow r = 5\%$

Answer 16.

Let the share of A be Rs. x. Then, the share of B = Rs. (16820 - x)

For A: P = Rs. x, r = 5% and n = (40 - 27) years = 13 years

$$\therefore A = P\left(1 + \frac{r}{100}\right)^n = Rs. \times \left(1 + \frac{5}{100}\right)^{13} = Rs. \times \left(\frac{21}{20}\right)^{13}$$

For B: P = Rs. (16820 - x), r = 5% and n = (40 - 25) years = 15 years

$$\therefore A = P\left(1 + \frac{r}{100}\right)^{n} = Rs. (16820 - x)\left(1 + \frac{5}{100}\right)^{15} = Rs. (16820 - x)\left(\frac{21}{20}\right)^{15}$$

Given; both receive equal sums on reaching the age of 40 years.

$$\therefore \times \left(\frac{21}{20}\right)^{13} = (16820 - \times) \left(\frac{21}{20}\right)^{15}$$

⇒ x = (16820 - x) × $\left(\frac{21}{20}\right)^{2}$

⇒ x = Rs. 8820

⇒ 16820 - x = 16820 - 8820 = 8000

:. Share of A = Rs. 8820 and Share of B = Rs. 8000