Activity 4 Area of triangle

Objective

To show that the area of a triangle is half the product of the base and the height using paper cutting and pasting.

Pre-requisite knowledge

- 1. Familiarity with activity 1A.
- 2. Formula for the area of a rectangle.
- 3. A diagonal of a parallelogram divides it into two congruent triangles.

Material Required

Chart paper, pencil, compass, scale, a pair of scissors, cello tape.

Procedure

For Right angle triangle

- 1. Cut a right angle triangle. [Fig 4 (a)]
- 2. Cut a triangle congruent to the right angle triangle.
- 3. Align the hypotenuse of the two triangles to obtain a rectangle. [Fig 4 (b)]

Observations

The students observe that two congruent triangles aligned on hypotenuse forms a rectangle.

They can see that area of rectangle = area of two congruent triangles.

Area of rectangle = base × height.

Therefore, Area of triangle = $\frac{1}{2}$ × Area of rectangle = $\frac{1}{2}$ × base × height.

Procedure

For Acute Angle Triangle

- 1. Cut an acute angle triangle and draw the perpendicular from the vertex to the opposite side. [Fig 4 (c)]
- 2. Cut a triangle congruent to it and cut this triangle along the perpendicular. [Fig 4 (d)]
- 3. Align the hypotenuse of these cut outs to the given triangle in order to obtain a rectangle. [Fig 4 (e)]

Observations

The students observe that two congruent triangles aligned in a specific way forms a rectangle.

They can see that area of rectangle = area of two congruent triangles.

Area of rectangle = base × height.

Therefore, Area of triangle = $\frac{1}{2}$ × Area of rectangle = $\frac{1}{2}$ × base × height.

Procedure

For Obtuse Angle Triangle

- 1. Cut an obtuse angle triangle. [Fig 4 (f)]
- 2. Cut a triangle congruent to this obtuse angle triangle.
- 3. Align the greatest side of the two triangles in order to obtain parallelogram. [Fig 4 (g)]

Observations

The students observe that aligning these two congruent triangles forms a parallelogram.

They can see that area of the parallelogram = area of two congruent triangles. Area of parallelogram = base × height.

Area of triangle = $\frac{1}{2}$ × area of parallelogram = $\frac{1}{2}$ × base × height.

Learning Outcome

The students may infer that area of each triangle is half the product of its base and height irrespective of the sides and angles of triangle.

