

## Chapter – 02

### Linear Equations in One Variable

#### Exercises 2.5

**Question 1.** Solve the following linear equations.

$$\frac{x}{2} - \frac{1}{5} = \frac{x}{3} + \frac{1}{4}$$

**Answer:**

$$\frac{x}{2} - \frac{1}{5} = \frac{x}{3} + \frac{1}{4}$$

L.C.M of 2 and 5 = 10 and L.C.M of 3 and 4 = 12 Therefore,  $\frac{5x-2}{10} = \frac{4x+3}{12}$

Cross Multiplying we get,  $12(5x - 2) = 10(4x + 3)$   
 $60x - 24 = 40x + 30$   
 $60x - 40x = 30 + 24$   
 $20x = 54$

$$x = \frac{54}{20}$$

$$= 54$$

$$x = \frac{27}{10}$$

**Question 2.** Solve the following linear equations.

$$\frac{n}{2} - \frac{3n}{4} + \frac{5n}{6} = 21$$

**Answer:**

$$\frac{n}{2} - \frac{3n}{4} + \frac{5n}{6} = 21$$

L.C.M. of 2,6, and 4 is 12

$$\frac{6n-9n+10n}{12} = 21$$

$$\frac{7n}{12} = 21$$

Cross multiplying we get,

Thus,

$$7n = 12 \times 21$$

$$n = \frac{12 \times 21}{7}$$

$$n = 12 \times 3$$

$$n = 36$$

**Question 3.** Solve the following linear equations.

$$x + 7 - \frac{8x}{3} = \frac{17}{6} - \frac{5x}{2}$$

**Answer:**

$$x + 7 - \frac{8x}{3} = \frac{17}{6} - \frac{5x}{2}$$

As the equation contains variable as well as constants. First step should be taking variables at one side and constants at other side. Therefore, the equation becomes

$$x - \frac{8x}{3} + \frac{5x}{2} = \frac{17}{6} - 7$$

L.C.M of 3 and 2 = 6 and on right hand side L.C.M. will be just 6

$$\frac{6x-2 \times 8x+5x \times 3}{6} = \frac{17-7 \times 6}{6}$$

$$\frac{6x-16x+15x}{6} = \frac{17-42}{6}$$

As the denominator is same, it gets cancelled out.

$$5x = -25$$

$$x = \frac{-25}{5}$$

$$x = -5$$

**Question 4.** Solve the following linear equations.

$$\frac{x-5}{3} = \frac{x-3}{5}$$

**Answer:**

Method 1:

$$\frac{x-5}{3} = \frac{x-3}{5}$$

Cross multiplying we get,

$$5(x - 5) = 3(x - 3) \\ 5x - 25 = 3x - 9 \\ 5x - 3x = 25 - 9 \\ 2x = 16 \\ x = 16/2 \\ x = 8$$

**Question 5.** Solve the following linear equation.

$$\frac{3t-2}{4} - \frac{2t+3}{3} = \frac{2}{3} - t$$

**Answer:**

$$\left( \frac{3t-2}{4} - \frac{2t+3}{3} \right) = \frac{2}{3} - t$$

L.C.M of 4 and 3 is 12

Thus,

$$\frac{3(3t-2)-4(2t+3)}{12} = \frac{2-3t}{3}$$

$$\frac{9t-6-8t-12}{12} = \frac{2-3t}{3}$$

$$\frac{t-18}{12} = \frac{2-3t}{3}$$

Cross Multiplying, we get,

$$3(t-18) = 12(2-3t)$$

$$3t-54 = 24-36t$$

$$39t = 78$$

$$t = \frac{78}{39}$$

$$t = 2$$

**Question 6.** Solve the following linear equations.

$$m - \frac{m-1}{2} = 1 - \frac{m-2}{3}$$

**Answer:**

$$\text{To Solve: } m - \frac{m-1}{2} = 1 - \frac{m-2}{3}$$

Taking L.C.M on both sides we get,

$$\frac{2m-(m-1)}{2} = \frac{3-(m-2)}{3}$$

$$\frac{2m-m+1}{2} = \frac{3-m+2}{3}$$

$$\frac{m+1}{2} = \frac{5-m}{3}$$

$$\begin{aligned} \text{Cross Multiplying we get, } 3(m+1) &= 2(5-m) \\ 3m+3 &= 10-2m \\ 3m+2m &= 10-3 \\ 5m &= 7 \end{aligned}$$

$$m = \frac{7}{5}$$

**Question 7.** Simplify and solve the following linear equations.

$$3(t - 3) - 5(2t + 1)$$

**Answer:**

Opening the brackets, we write,

$$3t - 9 = 10t + 5$$

$$-9 - 5 = 10t - 3t$$

$$-14 = 7t$$

$$t = -2$$

**Question 8.** Simplify and solve the following linear equations.

$$15(y - 4) - 2(y - 9) + 5(y + 6) - 0$$

**Answer:**

$$15(y - 4) - 2(y - 9) + 5(y + 6) = 0$$

Opening brackets  $15y - 15 \times 4 - 2y + 2 \times 9 + 5y + 5 \times 6 = 0$

$$15y - 60 - 2y + 18 + 5y + 30 = 0 \quad (15y - y = \frac{12}{18} 2y + 5y) + 30 + 18 - 60 = 0$$

$$18y - 12 = 0$$

**Question 9.** Simplify and solve the following linear equations.

$$3(5z - 7) - 2(9z - 11) - 4(8z - 13) - 17$$

**Answer:**

$$3(5z - 7) - 2(9z - 11) = 4(8z - 13) - 17$$

Opening the brackets, we write,

$$15z - 21 - 18z + 22 = 32z - 52 - 17$$

$$15z - 18z - 21 + 22 = 32z - 69$$

$$-3z + 1 = 32z - 69$$

$$-3z - 32z = -69 - 1 \quad -35z = -70 \quad 35z = 70 \quad z = 2$$

**Question 10.** Simplify and solve the following linear equations.

$$0.25(4f - 3) - 0.05(10f - 9)$$

**Answer:**

$$0.25(4f - 3) = 0.05(10f - 9)$$

Opening Brackets, Multiply Component-wisely

$$0.25 \times 4f - 0.25 \times 3 = 0.05 \times 10f - 0.05 \times 9$$

$$1f - 0.75 = 0.5f - 0.45$$

$$1f - 0.5f = 0.75 - 0.45$$

$$0.5f = 0.30$$

$$0.5f / 0.5 = 0.30 / 0.5$$

$$f = 0.6$$