MATHEMATICS DPP

PRACTICE PROBLEMS

DPP No. 38

Total Marks : 32

Max. Time : 37 min.

Topics : Application of Derivatives, Limits

Type of Questions			M.M., Min.	
Single choice Objective (no negative marking) Q. 1(3 marks, 3 min.)Multiple choice objective (no negative marking) Q.2(5 marks, 4 min.)Subjective Questions (no negative marking) Q. 3,4,5,6,7,8(4 marks, 5 min.)		[3, [5,	3] 4]	
				(4 marks, 5 min.)
		1.	At (0, 0), the curve $y^2 = x^3 + x^2$	

At (0, 0), the curve y (A) touches X-axis (B) bisects the angle between the axes (C) makes an angle of 60° with OX (D) none of these Let $f(\theta) = \frac{1 + \sin \theta}{5 + 4 \cos \theta}$, then 2. (A) $\frac{1}{5} \leq f(\theta) \leq 1$ (B) $0 \le f(\theta) \le 3$ (C) in (0, $\pi/2$), f(θ) is increasing (D) none of these 3. Find the number of critical points of the following functions. $f(x) = -\frac{3}{4} x^4 - 8x^3 - \frac{45}{2} x^2 + 105 \qquad ; \qquad x \in R$ (i) : f(x) = |x - 2| + |x + 1|(ii) x∈R f(x) = min (tanx, cotx): (iii) $\mathbf{X} \in (\mathbf{0}, \pi)$ Q(x) = 2f $\left(\frac{x^2}{2}\right)$ + f (6 - x²), $\forall x \in R$ & f " > 0. Discuss monotonocity of the function Q(x), where 4.

- 5. The number of distinct tangents to the curve $y^2 2x^3 4y + 8 = 0$ which pass through the point (1, 2) is
- 6. If $\lim_{x \to 3} \left(\frac{\sqrt{2x+3}-x}{\sqrt{x+1}-x+1} \right)^{\frac{x-1-\sqrt{x^2-5}}{x^2-5x+6}}$ can be expressed in the form $\frac{a\sqrt{b}}{c}$ where a, b, c, \in N, then find the

least value of $(a^2 + b^2 + c^2)$.

- The graph of the derivative f' of a continuous function f is shown with f(0) = 0, then for f(x) find
 (i) Intervals of monotonicity
 - (ii) Points of local minima-maxima .
 - (iii) Intervals of concavity
 - (iv) Points of inflection
 - (v) Critical points



8. P(x) is a polynomial function with real coefficients. Let $a, b \in R$ with a < b, are two consecutive roots of the equation P(x) = 0, then show that there exists at least one 'c' such that $a \le c \le b$ and P'(c) + 100 P(c) = 0.

Answers Key

- **1.** (B) **2.** (B)(C)
- 3. (i) 3 points, x = 0, -3, -5 (ii) ∞ points, x ∈ [-1, 2]
 - (iii) 2 points, x = $\frac{\pi}{4}$, $\frac{3\pi}{4}$
- **4.** M.I. in [-2, 0] ∪ [2, ∞) & M.D. in (-∞, -2] ∪ [0, 2)
- **5.** 2 **6.** 29
- 7. (i) $MI x \in [0, 2] \cup [4, 6) \cup [8, 9]$, $MD [2, 4] \cup (6, 8]$
 - (ii) Local minima x = 0, 4, 8, Local maxima x = 2, 6, 9
 - (iii) Concaveup $x \in [3, 6) \cup (6, 9]$, Concavedown $x \in [0, 3)$
 - (iv) Inflection point x = 3
 - (v) Critical points 2, 4, 6, 8