

**Instructions:**

- All the questions are compulsory.
- The question paper consists of 16 questions divided into 4 sections A,B,C and D.
- Section A comprises of 3 questions :
  - Q.No.1 consists of 16 Multiple Choice Questions carrying 1 mark each.
  - Q.No.2 consists of 8 Fill in the Blank type questions with options carrying 1 mark each.
  - Q.No.3 consists of 8 True/False type questions carrying 1 mark each.
- Section B comprises of 5 questions of 2 marks each.
- Section C comprises of 5 questions of 4 marks each.
- Section D comprises of 3 questions of 6 marks each.
- There is no overall choice. However, an internal choice has been provided in three questions of 2 marks, three questions of 4 marks and three questions of 6 marks each. You have to attempt only one of the alternatives in all such questions.
- Use of calculator is not permitted.

**Section – A**

**Q1** Choose the correct options in the following questions :

- (i) Function  $f: R \rightarrow R$ ,  $f(x) = 3x - 5$  is :  
 (a) one-one only (b) onto only (c) one-one and onto (d) none of these 1
- (ii) Relation given by  $R = \{(1, 1), (2, 2), (1, 2), (2, 1)\}$  is  
 (a) reflexive only (b) symmetric only (c) transitive only (d) equivalence relation 1
- (iii)  $\cos^{-1}(-\cos \frac{2\pi}{3})$  is equal to :  
 (a)  $\frac{\pi}{5}$  (b)  $\frac{2\pi}{3}$  (c)  $\frac{\pi}{2}$  (d)  $\frac{\pi}{3}$  1
- (iv) If  $\begin{bmatrix} 1 & -x \\ 4 & -3 \end{bmatrix} = \begin{bmatrix} 1 & 8 \\ 4 & -3 \end{bmatrix}$  then value of  $x$  is:  
 (a) 8 (b) -4 (c) 3 (d) -8 1
- (v) If order of matrix  $A$  is  $2 \times 3$  and order of matrix  $B$  is  $3 \times 5$  then order of matrix  $B'A'$  is :  
 (a)  $5 \times 2$  (b)  $2 \times 5$  (c)  $5 \times 3$  (d)  $3 \times 2$  1
- (vi) If  $f(x) = \begin{cases} kx + 1, & x \leq 5 \\ 3x - 5, & x > 5 \end{cases}$  is continuous then value of  $k$  is :  
 (a)  $\frac{9}{5}$  (b)  $\frac{5}{9}$  (c)  $\frac{5}{3}$  (d)  $\frac{3}{5}$  1
- (vii)  $\frac{d}{dx} \{\tan^{-1}(e^x)\}$  is equal to :  
 (a)  $e^x \tan^{-1} e^x$  (b)  $\frac{e^x}{1+e^{2x}}$  (c) 0 (d)  $e^x \sec^{-1} x$  1
- (viii) Slope of tangent to the curve  $y = x^2 - 2x + 1$  at  $x = 3$  is:  
 (a) 4 (b) 6 (c) 0 (d) 2 1
- (ix)  $\int 3x^2 dx$  is equal to :  
 (a)  $x + c$  (b)  $x^2 + c$  (c)  $x^3 + c$  (d)  $x^4 + c$  1
- (x)  $\int_0^{\pi/2} \frac{\sin^{1/2} x}{\sin^{1/2} x + \cos^{1/2} x} dx$  is equal to :  
 (a) 0 (b)  $\frac{\pi}{2}$  (c)  $\frac{\pi}{3}$  (d)  $\frac{\pi}{4}$  1
- (xi) Degree of differential equation  $\frac{d^2y}{dx^2} - 2\frac{dy}{dx} + 3y = 0$  is :  
 (a) 3 (b) 2 (c) 1 (d) 0 1
- (xii) If  $\vec{a} \cdot \vec{b} = |\vec{a} \times \vec{b}|$  then angle between vector  $\vec{a}$  and vector  $\vec{b}$  is :  
 (a)  $\frac{\pi}{2}$  (b)  $\frac{\pi}{6}$  (c)  $\frac{\pi}{4}$  (d)  $\frac{\pi}{3}$  1
- (xiii) If  $\vec{a} \cdot \vec{b} = 0$  then angle between vectors  $\vec{a}$  and  $\vec{b}$  is :  
 (a)  $\frac{\pi}{2}$  (b)  $\frac{\pi}{6}$  (c)  $\frac{\pi}{4}$  (d)  $\frac{\pi}{3}$  1
- (xiv) Direction ratios of line given by  $\frac{x-1}{3} = \frac{2y+6}{12} = \frac{1-z}{-7}$  are :  
 (a)  $\langle 3, 12, -7 \rangle$  (b)  $\langle 3, -6, 7 \rangle$  (c)  $\langle 3, 6, 7 \rangle$  (d)  $\langle 3, 6, -7 \rangle$  1

- (xv) Maximum value of  $Z = 3x + y$  for the constraints  $x + y \leq 4, x \geq 0, y \geq 0$  is: 1  
 (a)12 (b)16 (c)4 (d)10
- (xvi) If  $P(A) = \frac{1}{2}, P(B) = \frac{3}{8}$  and  $P(A \cap B) = \frac{1}{5}$  then  $P(A|B)$  is equal to : 1  
 (a) $\frac{2}{5}$  (b) $\frac{8}{15}$  (c) $\frac{2}{3}$  (d) $\frac{5}{8}$

Q2 Fill in the blanks from the given options

0, 1,  $\langle 3, -1, 2 \rangle$ ,  $\frac{\pi}{2}$ , 6, 2, 5, 4,  $-\sin x$ ,  $\tan x$

- (i) Value of  $\sin^{-1}(1)$  is \_\_\_\_\_ 1
- (ii) If  $A = [a_{ij}]_{2 \times 3}$  such that  $a_{ij} = i + j$  then  $a_{11} =$  \_\_\_\_\_ 1
- (iii) If  $\begin{vmatrix} x & 0 \\ 7 & 1 \end{vmatrix} = \begin{vmatrix} 3 & 0 \\ 7 & 2 \end{vmatrix}$  then  $x =$  \_\_\_\_\_ 1
- (iv) If  $y = \cos x$  then at  $x = 0, \frac{dy}{dx} =$  \_\_\_\_\_ 1
- (v)  $\int_0^5 dx =$  \_\_\_\_\_ 1
- (vi) Order of the differential equation  $\frac{d^2y}{dx^2} - \left(\frac{dy}{dx}\right)^3 + y = 0$  is \_\_\_\_\_ 1
- (vii) Direction ratios of a line which is perpendicular to the plane  $3x - y + 2z = 9$  are \_\_\_\_\_ 1
- (viii) Probability of occurrence of impossible event = \_\_\_\_\_ 1

Q3 State true or false for the following statements :

- (i) If  $A$  is a square matrix then  $(A + A')$  is a skew-symmetric matrix. 1
- (ii) If  $y = 10x$  then  $\frac{dy}{dx} = 0$ . 1
- (iii) If  $y = \tan x$  then  $\frac{dy}{dx} = \sec^2 x$  1
- (iv)  $\int dx = x^2 + c$  1
- (v)  $xdy - ydx = 0$  is a variable separable type of differential equation. 1
- (vi) Scalar product of two perpendicular vectors is zero. 1
- (vii) Point  $(3, -4, 2)$  lies in the plane  $2x + y - z = 0$  1
- (viii) If  $P(E) = 0.4$  then  $P(\text{not } E) = 0.6$  1

#### Section – B

- Q4 If  $A = \begin{bmatrix} 2 & 3 \\ 1 & 4 \end{bmatrix}$  and  $f(x) = x^2 + 2x + 3$  then find  $f(A)$ . 2
- Q5 Find the interval in which function  $f(x) = x^2 + 2x - 7$  is increasing. 2  
 OR  
 Find the slope of the normal to the curve  $y = x^3 - x + 1$  at the point whose  $x$ -coordinate is 2. 2
- Q6 Evaluate  $\int e^x \left( \log x + \frac{1}{x} \right) dx$ . 2  
 OR  
 Evaluate  $\int x \sin x dx$  2
- Q7 Using integration find the area bounded by the parabola  $y^2 = 4x$  straight lines  $x = 1, x = 4$  in the first quadrant. 2
- Q8 Find the unit vector in the direction of diagonal of the parallelogram whose sides are given by the vectors  $\vec{a} = 2\hat{i} - \hat{j} - 3\hat{k}, \vec{b} = 5\hat{i} + 2\hat{j} - \hat{k}$  2  
 OR  
 If  $\vec{a} = 2\hat{i} + 3\hat{j} - 5\hat{k}, \vec{b} = 7\hat{i} - 2\hat{j} - 4\hat{k}$  then find  $\vec{a} \times \vec{b}$ . 2

#### Section – C

- Q9 Find the value of:  $2 \tan^{-1}(1) - \cos^{-1}\left(\frac{-1}{2}\right) + 3 \sin^{-1}\left(\frac{1}{\sqrt{2}}\right) + 2 \sec^{-1}\left(\frac{2}{\sqrt{3}}\right)$  4

**Q10** If  $y = x^{\sin x} + (\sin x)^x$  then find  $\frac{dy}{dx}$ . 4

OR

If  $y = (\tan^{-1} x)^2$ , show that  $(x^2 + 1)^2 y_2 + 2x(x^2 + 1)y_1 = 2$  4

**Q11** Evaluate  $\int \frac{dx}{(x-1)(x-2)(x-3)}$ . 4

OR

Evaluate  $\int \frac{\sec^2 x}{\tan^2 x - 4 \tan x + 7} dx$  4

**Q12** Find the general solution of the differential equation  $x^2 dy - (x^2 + xy + y^2) dx = 0$ . 4

OR

Find the general solution of the differential equation  $\sec^2 x \tan y dx - \sec^2 y \tan x dy = 0$ . 4

**Q13** Bag I contains 3 red and 4 white balls. Bag II contains 7 red and 5 white balls. A bag is selected at random and a ball is drawn from it, which is found to be red. Find the probability that ball is drawn from bag II.

### Section – D

**Q14** Solve the following system of linear equations by matrix method : 6  
 $2x + 3y - 5z = 13$  ,  $x - y + z = -2$  ,  $3x + 2y - z = 8$

OR

Express  $A = \begin{bmatrix} 2 & 3 & 5 \\ 0 & 2 & 9 \\ 3 & 2 & 8 \end{bmatrix}$  as the sum of a symmetric matrix and a skew-symmetric matrix. 6

**Q15** Find the shortest distance between the lines 6

$\vec{r} = 6i - j + 3k + \lambda(i + 3j + 2k)$  and  $\vec{r} = 9i + j - 4k + \mu(i - 2j + k)$  6

OR

Find the foot of perpendicular drawn from the point  $(2, -3, 5)$  on the plane  $3x + 4y - 2z = 20$  6

**Q16** Solve the following linear programming problem graphically: 6  
Maximize and minimize  $Z = 4x + 3y$  subject to the constraints

$$x + y \leq 8, \quad 4x + y \geq 8, \quad x - y \geq 0, \quad x \geq 0, \quad y \geq 0$$

OR

Solve the following linear programming problem graphically: 6  
Maximize and minimize  $Z = 5x + 2y - 2$  subject to the constraints

$$x + y \leq 10, \quad x + y \geq 3, \quad x \leq 8, \quad y \leq 8, \quad x \geq 0, \quad y \geq 0$$