

Chapter **21**

Magnetic Effect of Current

Oersted found that a magnetic field is established around a current carrying conductor.

Magnetic field exists as long as there is current in the wire.



Biot-Savart's Law

Biot-Savart's law is used to determine the magnetic field at any point due to a current carrying conductor.

This law is although for infinitesimally small conductor yet it can be used for long conductors. In order to understand the Biot-Savart's law, we need to understand the term currentelement.

Current element

It is the product of current and length of infinitesimal segment of current carrying wire.

The current element is taken as



a vector quantity. Its direction is

same as the direction of current.

Current element $AB = i \vec{dl}$

According to Biot-Savart Law, magnetic field at point '*P* due to the current element \vec{idl} is given by the expression,

$$d\vec{B} = k \frac{i dl\sin\theta}{r^2} \hat{n}$$
 also $\vec{B} = \int d\vec{B} = \frac{\mu_0 i}{4\pi} \cdot \int \frac{dl\sin\theta}{r^2} \hat{n}$
In C.G.S. $k = 1$ and in S.I. : $k = \frac{\mu_0}{4\pi}$

where
$$\mu_0$$
 = Absolute permeability of air or vacuum
= $4\pi \times 10^{-7} \frac{Wb}{Amp - metre}$. It's other units are
 $\frac{Henry}{metre}$ or $\frac{N}{Amp^2}$ or $\frac{Tesla - metre}{Ampere}$
Vectorially, $d\vec{B} = \frac{\mu_0}{4\pi} \cdot \frac{i(\vec{dl} \times \hat{r})}{r^2} = \frac{\mu_0}{4\pi} \cdot \frac{i(\vec{dl} \times \vec{r})}{r^3}$ Fig. 21.2

Direction of Magnetic Field

The direction of magnetic field is determined with the help of the following simple laws :

(1) Maxwell's cork screw rule : According

to this rule, if we imagine a right handed



screw placed along the current carrying linear conductor, be rotated such that the screw moves in the direction of flow of current, then the direction of rotation of the thumb gives the direction of magnetic lines of force.

(2) Right hand thumb rule : According to this rule if a straight current carrying conductor is held in the right hand such that the thumb of the hand represents the direction of current flow, then the direction of folding fingers will represent the direction of magnetic lines of force.



(3) Right hand thumb rule of circular currents : According to

this rule if the direction of current in circular conducting coil is in the direction of folding fingers of right hand, then the direction of magnetic field will be in the direction of stretched thumb.



Fig. 21.5

(4) Right hand palm rule

If we stretch our right hand such that fingers point towards the point. At which magnetic field is required while thumb is in the direction of current then normal to the palm will show the direction of magnetic field.



Meaning of Cross ⊗ and dot ⊙

If magnetic field is directed perpendicular and into the plane of the paper it is represented by \otimes (cross) while if magnetic field



is directed perpendicular and out of the plane of the paper it is represented by ⊙ (dot)

In : Magnetic field is away from the observer or perpendicular inwards.

Out : Magnetic field is towards the observer or perpendicular outwards.

Ampere's Law

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Amperes law gives another method to calculate the magnetic field due to a given current distribution.

Line integral of the magnetic field \vec{B} around any closed curve is equal to μ_0 times the R net current *i* threading through . \odot the area enclosed by the curve \otimes i.e. \otimes b

)



$$\oint B \cdot dI = \mu_0 \sum i = \mu_0 (i_1 + i_3 - i_2)$$

Also using $\vec{B} = \mu_0 \vec{H}$ (where \vec{H} = magnetising field)

$$\oint \mu_0 \vec{H}.\vec{dl} = \mu_0 \Sigma i \Longrightarrow \oint \vec{H}.\vec{dl} = \Sigma i$$

Total current crossing the above area is $(i_1 + i_3 - i_2)$. Any current outside the area is not included in net current. (Outward $\odot \rightarrow + ve$, Inward $\otimes \rightarrow - ve$)

Table 21.1	:	Biot-Savart	's law	v/s /	Ampere':	s law
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Biot-Savart's law	Ampere's law		
this law is valid for all current distributions	This law is valid for symmetrical current distributions		
This law is the differential form of \vec{B} or \vec{H}	Basically this law is the integral from of \vec{B} or \vec{H}		
This law is based only on the principle of magnetism	This law is based on the principle of electromagnetism.		

Magnetic Field Due to Circular Current

If a coil of radius r, carrying current *i* then magnetic field on it's axis at a distance x from its centre given by (Application of



(1)
$$B_{axis} = \frac{\mu_0}{4\pi} \cdot \frac{2\pi Nir^2}{(x^2 + r^2)^{3/2}}$$
; where N = number of turns in coil

- (2) At centre $x = 0 \implies B_{centre} = \frac{\mu_0}{4\pi} \cdot \frac{2\pi Ni}{r} = \frac{\mu_0 Ni}{2r} = B_{max}$
- (3) The ratio of magnetic field at the centre of circular coil

and on it's axis is given by $\frac{B_{centre}}{B_{axis}} = \left(1 + \frac{x^2}{r^2}\right)$

(4) If
$$x >> r \Rightarrow B_{axis} = \frac{\mu_0}{4\pi} \cdot \frac{2\pi Nir^2}{x^3} = \frac{\mu_0}{4\pi} \cdot \frac{2NiA}{x^3}$$

where $A = \pi r^2$ = Area of each turn of the coil.

(5) *B-x* **curve** : The variation of magnetic field due to a circular coil as the distance x varies as shown in the figure.

B varies non-linearly with distance *x* as shown in figure and is maximum when $x^2 = \min = 0$, *i.e.*, the point is at the centre of the coil and it is zero at $x = \pm \infty$.



(6) Point of inflection (A and A') : Also known as points of curvature change or points of zero curvature. (i) At these points *B* varies linearly with $x \Rightarrow \frac{dB}{dx} =$

constant
$$\Rightarrow \frac{d^2 B}{dx^2} = 0$$

(ii) These are located at $x = \pm \frac{r}{2}$ from the centre of the coil and the magnetic field at $x = \frac{r}{2}$ is $B = \frac{4\mu_0 Ni}{5\sqrt{5} r}$

(7) Helmholtz coils

(i) This is the set-up of two coaxial coils of same radius such that distance between their centres is equal to their radius.

(ii) At axial mid point *O*, magnetic field is given by

$$B = \frac{8\mu_0 Ni}{5\sqrt{5}R} = 0.716 \frac{\mu_0 Ni}{R} = 1.432 B$$
, where $B = \frac{\mu_0 Ni}{2R}$

(iii) Current direction is same in both coils otherwise this arrangement is not called Helmholtz's coil arrangement.

(iv) Number of points of inflextion \Rightarrow Three (A, A', A'')



Magnetic Field at Centre *O* in Different Conditions of Circular Current

Condition	Figure	Magnetic field	
Arc subtends angle θ at the centre		$B = \frac{\mu_0}{4\pi} \cdot \frac{\theta i}{r}$	
Arc subtends			

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angle $(2\pi - \theta)$ at the centre		$B = \frac{\mu_0}{4\pi} \cdot \frac{(2\pi - \theta)i}{r}$	opposite direction				
Semi-circular arc	$ \begin{array}{c} $	$B = \frac{\mu_0}{4\pi} \cdot \frac{\pi i}{r} = \frac{\mu_0 i}{4r}$	Concentric loops but their planes are perpendicular to each other $B = \sqrt{B_1^2 + B_2^2}$ $= \frac{\mu_0}{2r} \sqrt{i_1^2 + i_2^2}$				
Three quarter semi-circular current carrying arc		$B = \frac{\mu_0}{4\pi} \cdot \frac{\left(2\pi - \frac{\pi}{2}\right)i}{r}$ $= \frac{3\mu_0 i}{8r}$	Concentric loops but their planes are at Q \dot{b} B_2 O \dot{b} B_1 $B = \sqrt{B_1^2 + B_2^2} + 2B_1B_2 \cos \theta$				
Circular current carrying arc		$B = \frac{\mu_0}{4\pi} \frac{2\pi i}{r}$ $= \frac{\mu_0 i}{2r}$	an angle θ with each other				
Concentric co-planer circular loops carries		$B_1 = \frac{\mu_0}{4\pi} 2\pi i \left(\frac{1}{r_1} + \frac{1}{r_2}\right)$	Distribution of current across the diameter $B=0$				
current in the same direction			Distribution of current between any two points on the				
Concentric co-planer circular loops carries current in the		$B_2 = \frac{\mu_0}{4\pi} 2\pi \left[\frac{1}{r_1} - \frac{1}{r_2} \right]$	circumference Magnetic Field Due to a Straight Wire				

Magnetic field due to a current carrying wire at a point *P* which lies at a perpendicular distance *r* from the wire as shown is given as $\frac{\mu_0}{i} \frac{i}{i} \frac{i}{i$

$$B = \frac{\mu_0}{4\pi} \cdot \frac{i}{r} (\sin\phi_1 + \sin\phi_2)$$

From figure $\alpha = (90^\circ - \phi_1)$
and $\beta = (90^\circ + \phi_2)$
Fig. 21.12

Hence
$$B = \frac{\mu_o}{4\pi} \cdot \frac{i}{r} (\cos \alpha - \cos \beta)$$

(1) For a wire of finite length : Magnetic field at a point which lies on perpendicular bisector of finite length wire



(2) For a wire of infinite length : When the linear conductor *XY* is of infinite length and the point *P* lies near the centre of the conductor $\phi_1 = \phi_2 = 90^{\circ}$.



(3) For a wire of semi-infinite length : When the linear conductor is of infinite length and the point *P* lies near the end *Y* or $Y \neq 00^{\circ}$ and $\phi = 0^{\circ}$

or X:
$$\phi_1 = 90^\circ$$
 and $\phi_2 = 0^\circ$
So, $B = \frac{\mu_0}{4\pi} \frac{i}{r} [\sin 90^\circ + \sin 0^\circ]$
 $= \frac{\mu_0 i}{4\pi r}$
Fig. 21.15

(4) For axial position of wire : When point *P* lies on axial position of current carrying conductor then magnetic field at *P* i P

Fig. 21.16

B = 0

Magnetic Field Due to a Cylindrical Wire

Magnetic field due to a cylindrical wire is obtained by the application of Ampere's law

(1) Outside the cylinder



In all above cases magnetic field outside the wire at P $\oint \vec{B}.\vec{dl} = \mu_0 i \implies B \int dl = \mu_0 i \implies B \times 2\pi r = \mu_0 i \implies B_{out} = \frac{\mu_0 i}{2\pi r}$ In all the above cases $B_{surface} = \frac{\mu_0 i}{2\pi R}$

(2) **Inside the hollow cylinder :** Magnetic field inside the hollow cylinder is zero.



(3) **Inside the solid cylinder :** Current enclosed by loop (/) is lesser then the total current (*)*



Current density is uniform *i.e.* $J = J \Rightarrow i' = i \times \frac{A'}{A} = i \left(\frac{r^2}{R^2} \right)$ Hence at inside point $\oint \vec{B_{in}} \cdot d\vec{l} = \mu_0 \vec{i} \Rightarrow B = \frac{\mu_0}{2\pi} \cdot \frac{ir}{R^2}$

(4) Inside the thick portion of hollow cylinder : Current

enclosed by loop is given as $i' = i \times \frac{A'}{A} = i \times \frac{(r^2 - R_1^2)}{(R_2^2 - R_1^2)}$



Fig. 21.20

Hence at point $Q \quad \oint \vec{B} \cdot d\vec{l} = \mu_0 \vec{i} \implies B = \frac{\mu_0 \vec{i}}{2\pi r} \cdot \frac{(r^2 - R_1^2)}{(R_2^2 - R_1^2)}$

Magnetic Field Due to an Infinite Sheet Carrying Current

The figure shows an infinite sheet of current with linear current density j (*A*/*m*). Due to symmetry the field line pattern above and below the sheet is uniform. Consider a square loop of side /as slown in the figure.





Fig. 21.21

 $\int_{a}^{b} \overrightarrow{B.dl} + \int_{b}^{c} \overrightarrow{B.dl} + \int_{c}^{d} \overrightarrow{B.dl} + \int_{d}^{d} \overrightarrow{B.dl} = \mu_{0}i \quad (By Ampere's law)$ Since $B \perp dl$ along the path $b \rightarrow c$ and $d \rightarrow a$, therefore,

 $\int_{b}^{c} \vec{B}.\vec{dl} = 0 ; \int_{d}^{a} \vec{B}.\vec{dl} = 0$

Also, $B \parallel dl$ along the path $a \rightarrow b$ and $c \rightarrow d$, thus $\int_{-}^{b} \vec{B} \cdot \vec{dl} + \int_{-}^{a} \vec{B} \cdot \vec{dl} = 2Bl$ The current enclosed by the loop is i = jl. Therefore, according to Ampere's law $2Bl = \mu_0(jl)$ or $B = \frac{\mu_0 j}{2}$

Solenoid



A cylinderical coil of many tightly wound turns of insulated wire with generally diameter of the coil smaller than its length is called a solenoid.



A magnetic field is produced around and within the solenoid. The magnetic field within the solenoid is uniform and parallel to the axis of solenoid.

(1) Finite length solenoid :

If N = total number of turns, / = length of the solenoid, n = number of turns per unit length

$$=\frac{N}{l}$$



(i) Magnetic field inside the

solenoid at point *P* is given by $B = \frac{\mu_0}{4\pi} (2\pi ni) [\sin\alpha + \sin\beta]$

(ii) Infinite length solenoid : If the solenoid is of infinite length and the point is well inside the solenoid i.e. $\alpha = \beta = (\pi/2).$

So $B_{in} = \mu_0 ni$

(iii) If the solenoid is of infinite length and the point is near one $\alpha = 0$ and $\beta = (\pi/2)$ so $B_{end} = \frac{1}{2}(\mu_0 n i)$ i.e. end $\left(B_{end} = \frac{1}{2} B_{in} \right)$

Toroid

A toroid can be considered as a ring shaped closed solenoid. Hence it is like an endless cylindrical solenoid.



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- (ii) Neutral particle *i.e.* $q = 0 \Rightarrow F = 0$
- (iii) Rest charge *i.e.* $v = 0 \Rightarrow F = 0$
- (iv) Moving charge *i.e.* $\theta = 0^\circ$ or $\theta = 180^\circ \Rightarrow F = 0$

(2) **Direction of force :** The force \vec{F} is always perpendicular to both the velocity \vec{v} and the field \vec{B} in accordance with Right Hand Screw Rule, though \vec{v} and \vec{B} themselves may or may not



Direction of force on charged particle in magnetic field can also be find by Fleming's Left Hand Rule (FLHR).



Here, First finger (indicates) → Direction of magnetic field

Middle finger \rightarrow Direction of motion of positive charge or direction, Opposite to the motion of negative charge.

Thumb \rightarrow Direction of force

Trajectory of a Charged Particle in a Magnetic Field

(1) Straight line : If the direction of a \vec{v} is parallel or antiparallel to \vec{B} , $\theta = 0$ or $\theta = 180^{\circ}$ and therefore F = 0. Hence the trajectory of the particle is a straight line.



Consider a toroid having *n* turns per unit length. Magnetic field at a point P in the figure is given as

$$B = \frac{\mu_0 N i}{2\pi r} = \mu_o n i$$
 where $n = \frac{N}{2\pi r}$

Force On a Charged Particle in Magnetic Field

If a particle carrying a positive charge q and moving with velocity v enters a magnetic field B then it experiences a force F which is given by the expression $\vec{F} = q(\vec{v} \times \vec{B}) \Rightarrow F = qvB\sin\theta$

where \vec{v} = velocity of the particle, \vec{B} = magnetic field



(1) Zero force : Force on charged particle will be zero (*i.e.*F = 0) if

(i) No field *i.e.* $B = 0 \Rightarrow F = 0$

(2) Circular path : If \vec{v} is perpendicular to \vec{B} *i.e.* $\theta = 90^{\circ}$, hence particle will experience a maximum magnetic force *F_{max} = qvB* which act's in a direction perpendicular to the motion of charged particle. Therefore the trajectory of the particle is a circle.



(i) In this case path of charged particle is circular and magnetic force provides the necessary centripetal force i.e. $qvB = \frac{mv^2}{r}$ \Rightarrow radius of path $r = \frac{mv}{qB} = \frac{p}{qB} = \frac{\sqrt{2mK}}{qB} = \frac{1}{B}\sqrt{\frac{2mV}{q}}$

where p = momentum of charged particle and K = kinetic energy of charged particle (gained by charged particle after accelerating through potential difference Ŵ then $p = mv = \sqrt{2mK} = \sqrt{2mqV}$

(ii) If *T* is the time period of the particle then $T = \frac{2\pi m}{aB}$ (*i.e.*, time period (or frequency) is independent of speed of particle).

(3) Helical path : When the charged particle is moving at an angle to the field (other than 0°, 90°, or 180°). Particle describes a path called helix.



Fig. 21.30

(i) The radius of this helical path is $r = \frac{m(vsin\theta)}{aB}$

(ii) Time period and frequency do not depend on velocity and so they are given by $T = \frac{2\pi m}{qB}$ and $v = \frac{qB}{2\pi m}$

(iii) The pitch of the helix, (i.e., linear distance travelled in one rotation) will be given by $p = T(v \cos \theta) = 2\pi \frac{m}{aB}(v \cos \theta)$

(iv) If pitch value is p, then number of pitches obtained in length /given as

Number of pitches =
$$\frac{l}{p}$$
 and time required $t = \frac{l}{v \cos \theta}$

Lorentz Force

When the moving charged particle is subjected simultaneously to both electric field \vec{E} and magnetic field \vec{B} , the moving charged particle will experience electric force $\vec{F}_e = q\vec{E}$ and magnetic force $\vec{F}_m = q(\vec{v} \times \vec{B})$; so the net force on it will be $\vec{F} = q (\vec{E} + (\vec{v} \times \vec{B}))$. Which is the famous 'Lorentz-force equation'.

Depending on the directions of \vec{v}, E and \vec{B} following situations are possible

(i) When \vec{v}, \vec{E} and \vec{B} all the three are collinear : In this situation the magnetic force on it will be zero and only electric force will act and so $\vec{a} = \frac{\vec{F}}{m} = \frac{q\vec{E}}{m}$

(ii) The particle will pass through the field following a straight-line path (parallel field) with change in its speed. So in this situation speed, velocity, momentum and kinetic energy all will change without change in direction of motion as shown



 $v\sin\theta \xrightarrow{P}_{\theta} \xrightarrow{P}_{$ (iii) \vec{v}, \vec{E} and \vec{B} are mutually perpendicular : In this Fig. 21.32

(2) Maximum energy of particle : Maximum energy gained

by the charged particle $E_{\text{max}} = \left(\frac{q^2 B^2}{2m}\right) r^2$

where r_0 = maximum radius of the circular path followed by the positive ion.

Hall Effect

The Phenomenon of producing a transverse emf in a current carrying conductor on applying a magnetic field perpendicular to the direction of the current is called Hall effect.

Hall effect helps us to know the nature and number of charge carriers in a conductor.

Consider a conductor having electrons as current carriers. The electrons move with drift velocity \vec{v} opposite to the direction of flow of current



Force acting on electron $F_m = -e(\vec{v} \times \vec{B})$. This force acts along *x*-axis and hence electrons will move towards face (2) and

Force On a Current Carrying Conductor In Magnetic Field

it becomes negatively charged.

In case of current carrying conductor in a magnetic field force experienced by its small length element is $\vec{dF} = i\vec{dl} \times \vec{B}$; $i\vec{dl}$ = current element $\vec{dF} = i(\vec{dl} \times \vec{B})$



as shown in figure, the particle will pass through the field with same velocity, without any deviation in path.

And in this situation, as $F_e = F_m$ *i.e.*, qE = qvB v = E/B

This principle is used in 'velocity-selector' to get a charged beam having a specific velocity.

Cyclotron

Cyclotron is a device used to accelerated positively charged particles (like, α -particles, deutrons *etc.*) to acquire enough energy to carry out nuclear disintegration *etc.*



It consists of two hollow *D*-shaped metallic chambers D_1 and D_2 called dees. The two dees are placed horizontally with a small gap separating them. The dees are connected to the source of high frequency electric field. The dees are enclosed in a metal box containing a gas at a low pressure of the order of 10^{-3} *mm* mercury. The whole apparatus is placed between the two poles of a strong electromagnet *NS* as shown in fig. The magnetic field acts perpendicular to the plane of the dees.

(1) **Cyclotron frequency** : Time taken by ion to describe a semicircular path is given by $t = \frac{\pi r}{v} = \frac{\pi m}{aB}$

If T = time period of oscillating electric field then $T = 2t = \frac{2\pi m}{qB}$ the cyclotron frequency $v = \frac{1}{T} = \frac{Bq}{2\pi m}$ Total magnetic force $\vec{F} = \int d\vec{F} = \int i(d\vec{l} \times \vec{B})$. If magnetic field is uniform *i.e.*, \vec{B} = constant $\vec{F} = i[\int d\vec{l}] \times \vec{B} = i(\vec{L} \times \vec{B})$

 $\int \vec{dl} = \vec{L}' = \text{ vector sum of all the length elements from initial}$ to final point. Which is in accordance with the law of vector addition is equal to length vector \vec{L} joining initial to final point.

(For a straight conductor $F = Bilsin\theta$)

Direction of force : The direction of force is always perpendicular to the plane containing \vec{idl} and \vec{B} and is same as that of cross-product of two vectors $(\vec{A} \times \vec{B})$ with $\vec{A} = \vec{idl}$.



The direction of force when current element $i\overline{dl}$ and \overline{B} are perpendicular to each other can also be determined by applying either of the following rules

Fleming's left-hand rule : Stretch the fore-finger, central finger and thumb of left hand mutually perpendicular. Then if the fore-finger points in the direction of field \vec{B} and the central in the direction of current *i*, the thumb will point in the direction of force.



Right-hand palm rule : Stretch the fingers and thumb of right hand at right angles to each other. Then if the fingers point in the direction of field \vec{B} and thumb in the direction of current *i*, then normal to the palm will point in the direction of force



Force Between Two Parallel Current Carrying Conductors

The force on a length / of each of two long, straight, parallel wires carrying currents \dot{h} and \dot{k} and separated by a distance a is



Force Between Two Moving Charges

If two charges q_1 and q_2 are moving with velocities v_1 and v_2 respectively and at any instant the distance between them is *r*, then





Magnetic force between them is $F_m = \frac{\mu_0}{4\pi} \cdot \frac{q_1 q_2 v_1 v_2}{r^2}$ (i) and Electric force between them is $F_e = \frac{1}{4\pi\varepsilon_0} \cdot \frac{q_1 q_2}{r^2}$ (ii) From equation (i) and (ii) $\frac{F_m}{F_e} = \mu_0 \varepsilon_0 v^2$ but $\mu_0 \varepsilon_0 = \frac{1}{c^2}$; where *c* is the velocity of light in vacuum. So $\frac{F_m}{F_e} = \left(\frac{v}{c}\right)^2$

As v < c so $F_m < F_e$

Standard Cases For Force on Current Carrying Conductors

Case 1: When an arbitrary current carrying loop placed in a magnetic field (\perp to the plane of loop), each element of loop experiences a magnetic force due to which loop stretches and open into circular loop and tension developed in it's each part.







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In both the situations for equilibrium of XY it's downward weight = upward magnetic force *i.e.* $mg = \frac{\mu_0}{4\pi} \cdot \frac{2i_l i_2}{h} \cdot l$

Case 3 : Current carrying spring : If current is passed through a spring, then it will contract because current will flow through all the turns in the same direction.



If current makes to flow through If switch is closed then current start spring, then spring will contract flowing, spring will execute Fig. 21.44

Case **4** : Tension less strings : In the following figure the value and direction of current through the conductor *XY* so that strings becomes tensionless?

Strings becomes tensionless if weight of conductor XY



Fig. 21.45

Hence direction of current is from $X \rightarrow Y$ and in balanced

condition $F_m = mg \implies Bil = mg \implies i = \frac{mg}{Bl}$

Case 5 : Sliding of conducting rod on inclined rails : When a

conducting rod slides on conducting rails.





Fig. 21.48

Behaviour of Current Loop in a Magnetic Field

(1) **Torque** : Consider a rectangular current carrying coil *PQRS* having *N* turns and area *A*, placed in a uniform field \vec{B} , in such a way that the normal (\hat{n}) to the coil makes an angle θ with the direction of \vec{B} . the coil experiences a torque given by $\tau = NBiA \sin \theta$. Vectorially $\vec{\tau} = \vec{M} \times \vec{B}$



In the following situation conducting rod (X, Y) slides at constant velocity if

$$F\cos\theta = mg\sin\theta \implies Bil\cos\theta = mg\sin\theta \implies B = \frac{mg}{il}\tan\theta$$

Current Loop as a Magnetic Dipole

A current carrying circular coil behaves as a bar magnet whose magnetic moment is M = NiA; *Where* N = Number of turns in the coil, *i* = Current through the coil and A = Area of the coil

Magnetic moment of a current carrying coil is a vector and it's direction is given by right hand thumb rule



(1) For a given perimeter circular shape have maximum area. Hence maximum magnetic moment.

(2) For a any loop or coil \vec{B} at centre due to current in loop, and \vec{M} are always parallel.



(i) τ is zero when θ = 0, *i.e.*, when the plane of the coil is perpendicular to the field.

(ii) τ is maximum when $\theta = 90^{\,o}$, *i.e.*, the plane of the coil is parallel to the field $\tau_{\rm max} = NBiA$

(2) **Workdone** : If coil is rotated through an angle θ from it's equilibrium position then required work. $W = MB(1 - \cos \theta)$. It is maximum when $\theta = 180^{\circ} \Rightarrow W_{max} = 2 MB$

(3) Potential energy: $U = -MB \cos \theta \Rightarrow U = -\vec{M}.\vec{B}$

Moving Coil Galvanometer



In a moving coil galvanometer the coil is suspended between the pole pieces of a strong horse-shoe magnet. The pole pieces are made cylindrical and a soft iron cylindrical core is placed within the coil without touching it. This makes the field radial. In such a field the plane of the coil always remains parallel to the field. Therefore $\theta = 90^{\circ}$ and the deflecting torque always has the maximum value.

$$\tau_{\rm def} = NBiA$$
(i)

Coil deflects, a restoring torque is set up in the suspension fibre. If α is the angle of twist, the restoring torque is

 $\tau_{\rm rest} = C\alpha$ (ii)

where C is the torsional constant of the fibre.

When the coil is in equilibrium *NBiA* = $C\alpha \Rightarrow i = K\alpha$,

where $K = \frac{C}{NBA}$ is the galvanometer constant. This linear relationship between *i* and α makes the moving coil galvanometer useful for current measurement and detection.

Current sensitivity (*S*) : The current sensitivity of a galvanometer is defined as the deflection produced in the galvanometer per unit current flowing through it.

$$S_i = \frac{\alpha}{i} = \frac{NBA}{C}$$

Voltage sensitivity (S_{ν}) : Voltage sensitivity of a galvanometer is defined as the deflection produced in the galvanometer per unit voltage applied to it.

$$S_V = \frac{\alpha}{V} = \frac{\alpha}{iR} = \frac{S_i}{R} = \frac{NBA}{RC}$$



The device whose working principle based on Halmholtz coils and in which uniform magnetic field is used called as "Halmholtz galvanometer".

The value of magnetic field induction at a point, on the centre of separation of two linear parallel conductors carrying equal currents in the same direction is zero.

 \mathscr{A} If a current carrying circular loop (n = 1) is turned into a coil having n identical turns then magnetic field at the centre

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of the coil becomes n^2 times the previous field *i.e.* $B_{(n \text{ turn})} = n^2$ $B_{(single \text{ turn})}$

∠ When a current carrying coil is suspended freely in earth's magnetic field, it's plane stays in **East-West** direction.

 $\begin{array}{l} \swarrow \qquad \text{Magnetic field } (\vec{B}) \text{ produced by a moving charge } q \text{ is} \\ \text{given by } \vec{B} = \frac{\mu_0}{4\pi} \frac{q(\vec{v} \times \vec{r}\,)}{r^3} = \frac{\mu_0}{4\pi} \frac{q(\vec{v} \times \hat{r})}{r^2} \text{ ; where } \nu \text{ = velocity of} \\ \text{charge and } \nu << c \text{ (speed of light).} \end{array}$



 \cancel{e} If an electron is revolving in a circular path of radius *r* with speed *v* then magnetic field produced at the centre of circular path $B = \frac{\mu_0}{4\pi} \cdot \frac{ev}{r^2} \Rightarrow r \propto \sqrt{\frac{v}{B}}$

\checkmark The line integral of magnetising field (\vec{H}) for any closed path called magnetomotive force (MMF). It's S.I. unit is amp.

✓ The positive ions are produced in the gap between the two dees by the ionisation of the gas. To produce proton, hydrogen gas is used; while for producing alpha-particles, helium gas is used.

 Cyclotron frequency is also known as magnetic resonance frequency.

The energy of a charged particle moving in a uniform magnetic field does not change because it experiences a force in a direction, perpendicular to it's direction of motion. Due to which the speed of charged particle remains unchanged and hence it's K.E. remains same.

∠ Magnetic force does no work when the charged particle

is displaced while electric force does work in displacing the charged particle.

Magnetic force is velocity dependent, while electric force is independent of the state of rest or motion of the charged particle.

If a particle enters a magnetic field normally to the magnetic field, then it starts moving in a circular orbit. The point at which it enters the magnetic field lies on the circumference. (Most of us confuse it with the centre of the orbit)

Deviation in terms of time t; $\theta = \omega t = \left(\frac{Bq}{m}\right)t$

Deviation in terms of length of the magnetic field; $\theta = \sin^{-1}\left(\frac{x}{r}\right)$. This relation can be used only when $x \le r$.

For $x \ge r$, the deviation will be 180° as shown in the following figure $x \xrightarrow{\times} x$ $x \xrightarrow{\times} x$ $q, m \xrightarrow{\times} v \xrightarrow{\times} x$ $x \xrightarrow{\times} B$

If no nagnetic field is present, the oop will still open into a circle as in it's ediacent parts curren will be in opposite direction and opposite currents repel each other.



E In the following case if wire *XY* is slightly displaced from its equilibrium position, it executes SHM and it's time period is given by $T = 2\pi \sqrt{\frac{h}{g}}$.

✓ In the previous case if direction of current in movable wire is reversed then it's instantaneous acceleration produced is 2g ↓.

Electric force is an absolute concept while magnetic force is a relative concept for an observer.

 \swarrow The nature of force between two parallel charge beams decided by electric force, as it is dominator. The nature of force between two parallel current carrying wires decided by

magnetic prce. $f_{p} = F_{m} \text{ only}$ $F_{e} \rightarrow \text{repulsion}$ $F_{m} \rightarrow \text{ attraction}$ $F_{net} \rightarrow \text{repulsion (Due to)}$

If a straight current carrying wire is placed along the axis of a current carrying coil then it will not experience magnetic force because magnetic field produced by the coil is parallel to the wire.

 \swarrow The force acting on a curved wire joining points *a* and *b* as shown in the figure is the same as that on a straight wire joining these points. It is given by the expression $\vec{F} = i \vec{L} \times \vec{B}$

 \mathscr{B} If a current carrying conductor AB is placed transverse to

a long current carrying conductor as hown then force.

Experienced by wire
$$AB$$

 $F = \frac{\mu_0 i_1 i_2}{2\pi} \log_e \left(\frac{x+l}{x} \right)$