CAPACITANCE

1. (i)
$$q \propto V \implies q = CV$$

 $q: Charge on positive plate of the capacitor
 $C: Capacitance of capacitor.$
 $V: Potential difference between positive and negative plates.$
(ii) Representation of capacitor : $-||-, -||(-)|$
(iii) Energy stored in the capacitor : $U = \frac{1}{2}CV^2 = \frac{Q^2}{2C} = \frac{QV}{2}$
(iv) Energy density $= \frac{1}{2} \varepsilon_0 \varepsilon_r E^2 = \frac{1}{2} \varepsilon_0 K E^2$
 $\varepsilon_r = Relative permittivity of the medium.$
 $K = \varepsilon_r: Dielectric Constant$
For vacuum, energy density $= \frac{1}{2} \varepsilon_0 E^2$
(v) Types of Capacitors :
(a) Parallel plate capacitor
 $C = \frac{\varepsilon_0 \varepsilon_r A}{d} = K \frac{\varepsilon_0 A}{d}$
 $A: Area of plates$
 $d: distance between the plates(<< size of plate)$
(b) Spherical Capacitor :
• Capacitance of an isolated spherical Conductor (hollow or solid)
 $C = 4 \pi \varepsilon_0 \varepsilon_r R$
 $R = Radius of the spherical conductor
• Capacitance of spherical capacitor$$

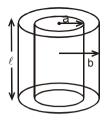
<mark>⋥</mark>[₭])₭₂)₭₃

$$C=4\pi\varepsilon_0\frac{ab}{(b-a)}$$

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$$C = \frac{4\pi\varepsilon_0 K_2 ab}{(b-a)}$$

(c) Cylindrical Capacitor : $\ell >> \{a,b\}$

Capacitance per unit length = $\frac{2\pi\epsilon_0}{\ell n(b/a)}$ F/m



- (vi) Capacitance of capacitor depends on
 - (a) Area of plates
 - (b) Distance between the plates
 - (c) Dielectric medium between the plates.
- (vii) Electric field intensity between the plates of capacitor

$$\mathsf{E} = \frac{\sigma}{\varepsilon_0} = \frac{\mathsf{V}}{\mathsf{d}}$$

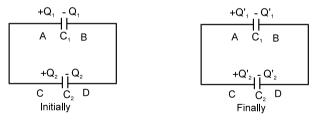
 σ : Surface change density

(viii) Force experienced by any plate of capacitor :

$F = \frac{q^2}{2A\varepsilon_0}$

2. DISTRIBUTION OF CHARGES ON CONNECTING TWO CHARGED CAPACITORS:

When two capacitors are C₁ and C₂ are connected as shown in figure



(a) Common potential :

$$\Rightarrow \qquad V = \frac{C_1 V_1 + C_2 V_2}{C_1 + C_2} = \frac{\text{Total charge}}{\text{Total capacitance}}$$

(b)
$$Q_1' = C_1 V = \frac{C_1}{C_1 + C_2} (Q_1 + Q_2)$$

$$Q_{2}' = C_{2} V = \frac{C_{2}}{C_{1} + C_{2}} (Q_{1} + Q_{2})$$

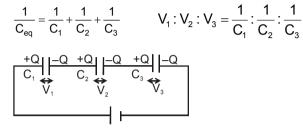
(c) Heat loss during redistribution :

$$\Delta H = U_i - U_f = \frac{1}{2} \frac{C_1 C_2}{C_1 + C_2} (V_1 - V_2)^2$$

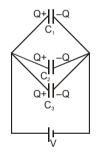
The loss of energy is in the form of Joule heating in the wire.

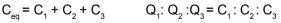
3. Combination of capacitor :

(i) Series Combination



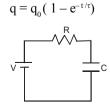
(ii) Parallel Combination :



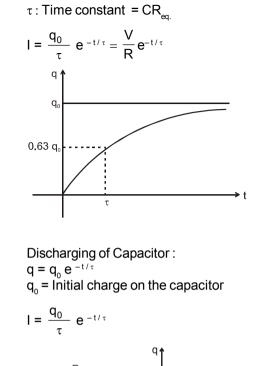


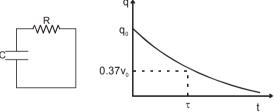
4. Charging and Discharging of a capacitor :

(i) Charging of Capacitor (Capacitor initially uncharged):



 q_0 = Charge on the capacitor at steady state q_0 = CV





5. Capacitor with dielectric :

(ii)

(i) Capacitance in the presence of dielectric :

 C_0 = Capacitance in the absence of dielectric.

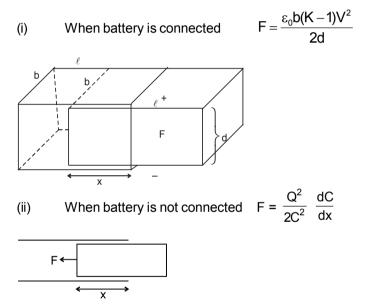
(ii)
$$E_{in} = E - E_{ind} = \frac{\sigma}{\epsilon_0} - \frac{\sigma_b}{\epsilon_0} = \frac{\sigma}{K\epsilon_0} = \frac{V}{d}$$

 $E: \frac{\sigma}{\epsilon_0} \quad \text{Electric field in the absence of dielectric}$

E_{ind} : Induced (bound) charge density.

(iii)
$$\sigma_{\rm b} = \sigma(1 - \frac{1}{K}).$$

6. Force on dielectric



* Force on the dielectric will be zero when the dielectric is fully inside.