
Sample Question Paper 04
Class -IX Mathematics
Summative Assessment – II

Time: 3 Hours

Max. Marks: 90

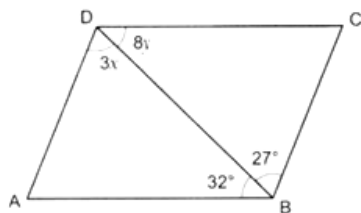
General Instructions:

- (i) All questions are compulsory.
 - (ii) The question paper consists of **31** question divided into five **section A, B, C, D and E**. Section-A comprises of **4** question of **1 mark** each, **Section-B** comprises of **6** question of **2 marks** each, **Section-C** comprises of **8** question of **3 marks** each and **Section-D** comprises of **10** questions of **4 marks** each. **Section E** comprises of **two questions of 3 marks each** and **1 question of 4 marks from Open Text theme**.
 - (iii) There is no overall choice.
 - (iv) Use of calculator is not permitted.
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SECTION-A

Question number **1** to **4** carry **one** mark each.

- 1. Find the total surface area of a cone whose radius is $\frac{r}{2}$ and slant height 2l.
- 2. Find the median of the numbers: 4, 4, 5, 7, 6, 7, 7, 12, 3.
- 3. In a single throw of two dice, what is the probability of getting a sum of 9.
- 4. In the given figure, ABCD is a \parallel^{gm} . Find x and y



SECTION-B

Question number **5** to **10** carry **two** marks each.

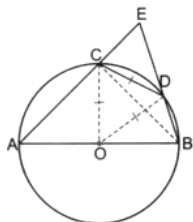
- 5. Find the co-ordinate where the linear equation $4x - \frac{2}{3}y = 7$ meets at y -axis.
 - 6. Write the linear equation represented by line AB and PQ. Also find the co-ordinate of intersection of line AB and PQ.
 - 7. Prove that $\angle CAD = \angle CBD$, if ABC and ADC are two right triangle with common hypotenuse AC.
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8. Show that $\text{ar (quad. ABCD)} = \frac{1}{2} BD (AM + CN)$ BD is one of the diagonals of a quadrilateral ABCD, AM and CN are the \perp from A and C
9. Determine the point on the graph of the linear equation $x + y = 6$, whose ordinates is 2 times its abscissa.
10. The points scored by a basketball team in a series of matches are as follows: 17, 2, 7, 27, 25, 5, 14, 18, 10, 24, 48, 10, 8, 7, 10, 28. Find the median and mode for the data.

SECTION-C

Question numbers **11** to **18** carry **three** marks each.

11. Write four solutions for equations: $2x + y = 7$
12. The temperature of a liquid can be measured in Kelvin units as x K or in Fahrenheit unit as $y^\circ\text{F}$. The relation between the two system of measurement of temperature is given by the linear equation $y = \frac{9}{5}(x - 273) + 32$.
- (i) Find the temperature of the liquid in Fahrenheit if the temperature of the body is 313K.
- (ii) If the temperature is 158°F , then find the temperature in Kelvin.
13. In given figure, AB is a diameter of the circle, CD is a chord equal to the radius of the circle. AC and BD when extended intersect at point E. Prove that $\angle AEB = 60^\circ$.



14. The diameter of the moon is approximately one-fourth of the diameter of the earth. What fraction of the volume of the earth is the volume of the moon?
15. A hemispherical tank is made up of an iron sheet 1 cm thick. If the inner radius is 1 m, then find the volume of the iron used to make the tank.
16. The radius of a spherical balloon increases from 7 cm to 14 cm as air is being pumped into it. Find the ratio of surface areas of the balloon in two cases.
17. The sum of the deviations of a set of n values x_1, x_2, \dots, x_n measured from 50 is -10 and the sum of deviation of the values from 46 is 70. Find the values of n and the mean.
18. Over the past 200 working days, the number of defective parts produced by a machine is given in the following table:

Number of defective parts	0	1	2	3	4	5	6	7	8	9	10	11	12	13
Days	50	32	22	18	12	12	10	10	10	8	6	6	2	2

Determine the probability that tomorrow output will have

- (i) no defective part,

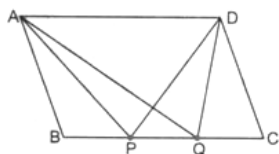
- (ii) at least one defective part,
(iii) not more than 5 defective parts.

SECTION-D

Question numbers **19** to 28 carry **four** marks each.

19. Construct an angle of 90° at the initial point of a given ray and give the justification.
20. Construct a triangle ABC, in which $\angle B = 60^\circ$, $\angle C = 45^\circ$ and $AB + BC + CA = 11\text{cm}$
21. The bisector of $\angle B$ of an isosceles triangle ABC with $AB = AC$ meets the circum circle of $\triangle ABC$ at P if AP and BC produced meet at Q, prove that $CQ = CA$
22. Shanti sweets stall was placing an order for making cardboard boxes for packing their sweets two sizes of boxes were required. The bigger of dimensions $25\text{cm} \times 20\text{cm} \times 5\text{cm}$ and the smaller of dimensions $15\text{cm} \times 12\text{cm} \times 5\text{cm}$ for all the overlaps, 5% of the total surface area is required extra. If the cost of cardboard is Rs 4 for 1000cm^2 . Find the cost of cardboard required for supplying 250 boxes of each kind.
23. Draw the graph of linear equation $x = 4$ and $y = 5$. Find the area formed by the two graph and the axes.
24. A hollow spherical shell is made of a metal of density $9.6\text{g}/\text{cm}^3$. The external diameter of the shell is 10cm and its internal diameter is 9 cm. Find
 - (i) Volume of the metal contained in the shell
 - (ii) Weight of the shell.
 - (iii) Outer surface area of the shell.
25. Prove that parallelograms on the same base and between the same parallels have the same area.
26. In given figure, ABCD is a parallelogram. Points P and Q on BC trisects BC. Prove that

$$ar(\triangle APQ) = ar(\triangle DPQ) = \frac{1}{6} ar(\text{||}^{gm} ABCD)$$



27. Find the unknown entries (a, b, c, d, e, f) from the following frequency distribution of heights of 50 students in a class.

Class intervals (heights in cm)	frequency	cumulative frequency
150-155	12	a
155-160	b	25
160-165	10	c
165-170	d	43
170-175	e	48
175-180	2	f

28. An organization selected 2400 families at random and surveyed them to determine a relationship between income level and the number of vehicles in a family. The information gathered is listed in the table below:

Monthly income (in Rs.)	Vehicles per family			
	0	1	2	Above 2
Less than 7000	10	160	25	0
7000 – 10000	0	305	27	2
10000 – 13000	1	535	29	1
13000 – 16000	2	469	59	25
16000 or more	1	579	82	88

Suppose a family is chosen. Find the probability that the family chosen is:

- (i) Earning Rs. 10000 – 13000 per month and owning exactly 2 vehicles.
- (ii) Earning Rs. 16000 or more per month and owning exactly 1 vehicle.
- (iii) Earning less than Rs. 7000 per month and does not own any vehicle.
- (iv) Earning Rs. 13000 – 16000 per month and owning more than 2 vehicles.
- (v) not more than 1 vehicle.

SECTION-E (10 Marks)

(Open Text from Chapter-8 Quadrilaterals)

(*Please ensure that open text of the given theme is supplied with this question paper.)

29. OTBA Question

30. OTBA Question

31. OTBA Question

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Solution

SECTION-A

Question number **1** to **4** carry **one** mark each.

1. Total surface area of the cone $= \left(\frac{r}{2}\right)\left(2l + \frac{r}{2}\right) = \left(l + \frac{r}{4}\right)$
2. Arranging the data in ascending order, we get
3, 4, 4, 5, 6, 7, 7, 7, 12
Here, $n = 9$
Median $= \frac{(9+1)th}{2}$ observation
 $= 5th \text{ observation} = 6.$
3. Outcomes with sum of 9 $= \{(3, 6), (4, 5), (5, 4), (6, 3)\}$
 $P(\text{getting a sum of 9}) = \frac{4}{36} = \frac{1}{9}$
4. $AB \parallel DC$ (Opposite sides of a parallelogram)
 $\therefore 8y = 32^\circ$ and $9x = 27^\circ$ (Alternate angles)
 $\Rightarrow y = 4^\circ$ and $x = 3^\circ$

SECTION-B

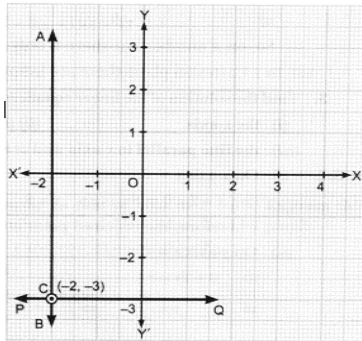
Question number **5** to **10** carry **two** marks each.

5. The point where the given linear equation in two variables meets at y – axis, the x co – ordinates will be 0.
 $\therefore 4x - \frac{2}{3}y = 7$
 $4(0) - \frac{2}{3}y = 7$
 $-\frac{2}{3}y = 7$
 $y = \frac{-21}{2}$
Hence, co-ordinate is $\left(0, \frac{-21}{2}\right)$
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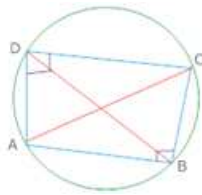
6. $AB \Rightarrow x = -2$

$PQ \Rightarrow y = -3$

\therefore point of intersection of AB and PQ is C (- 2, - 3).



7.



$\angle ADC = \angle ABC = 90^\circ$ [AC is the common hypotenuse of Δs ADC and ABC]

$$\angle ADC + \angle ABC = 180^\circ$$

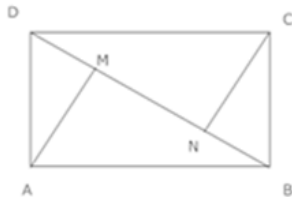
\Rightarrow Quadrilateral ABCD is cyclic

Now, chord CD subtends $\angle CAD$ and $\angle CBD$

$$\angle CAD = \angle CBD$$

[Angle in the same segment]

8.



$$\text{ar (quad. ABCD)} = \text{ar}(\Delta ABD) + \text{ar}(\Delta BCD)$$

$$= \frac{1}{2}(BD \times AM) + \frac{1}{2}(BD \times CN)$$

$$= \frac{1}{2}BD(AM + CN)$$

9. Given $y = 2x$, putting $y = 2x$ in the equation $x + y = 6$, we get

$$x + 2x = 6 \Rightarrow 3x = 6$$

$$\Rightarrow x = \frac{6}{3}$$

$$\Rightarrow x = 2$$

Putting $x = 2$ in the equation $y = 2x$ we get, $y = 2 \times 2 = 4$

\therefore the required point is (2, 4)

10. Arranging the data in ascending order, we get

2, 5, 7, 7, 8, 10, 10, 10, 14, 17, 18, 24, 25, 27, 28, 48

Since number of observations (n) = 16, which is even.

Therefore, median is the mean of $\left(\frac{n}{2}\right)^{th}$ and $\left(\frac{n}{2}+1\right)^{th}$ observation, i.e., 8th and 9th observation.

Here, 8th observation = 10

9th observation = 14

$$\text{Median} = \frac{10+14}{2} = 12$$

As 10 occurs most frequently, i.e., three times. So, the mode is 10

SECTION-C

Question numbers **11** to **18** carry **three** marks each.

11. $2x + y = 7$

We know that any linear equation has infinitely many solutions.

Let us put $x = 0$ in the linear equation $2x + y = 7$, to get

$$2(0) + y = 7$$

$$y = 7$$

Thus, we get first pair of solution as $(0, 7)$.

Let us put $x = 2$ in the linear equation $2x + y = 7$, to get

$$2(2) + y = 7 \quad \Rightarrow y + 4 = 7$$

$$y = 3$$

Thus, we get second pair of solution as $(2, 3)$.

Let us put $x = 4$ in the linear equation $2x + y = 7$, to get

$$2(4) + y = 7 \quad \Rightarrow y + 8 = 7$$

$$y = -1$$

Thus, we get third pair of solution as $(4, -1)$.

Let us put $x = 6$ in the linear equation $2x + y = 7$, to get

$$2(6) + y = 7 \quad \Rightarrow y + 12 = 7$$

$$y = -5$$

Thus, we get fourth pair of solution as $(6, -5)$.

Therefore, we can conclude that four solutions for the linear equation $2x + y = 7$ are $(0, 7)$, $(2, 3)$, $(4, -1)$ and $(6, -5)$.

12. (i) When $x = 313K$,

$$y = \frac{9}{5}(313 - 273) + 32$$

$$= \frac{9}{5}(40) + 32$$

$$= 72 + 32 = 104^\circ F$$

(ii) When $y = 158^\circ F$, then

$$158 = \frac{9}{5}(x - 273) + 32$$

$$158 - 32 = \frac{9}{5}(x - 273)$$

$$126 = \frac{9}{5}(x - 273)$$

$$126 \times \frac{5}{9} = (x - 273)$$

$$70 = x - 273$$

$$x = 70 + 273 = 343 \text{ K}$$

13. Join OC, OD and BC In $\triangle OCD$, we have

OC = OD = CD (Each equal to radius)

$\triangle ODC$ is an equilateral triangle.

$$\angle COD = 60^\circ$$

Also, $\angle COD = 2\angle CBD$

$$60^\circ = 2\angle CBD$$

$$\angle CBD = 30^\circ$$

Since $\angle ACB$ is angle in a semi-circle.

$$\angle ACB = 90^\circ$$

$$\angle BCE = 180^\circ - \angle ACB$$

$$180^\circ - 90^\circ = 90^\circ$$

Thus, in $\triangle BCE$, we have

$$\angle BCE = 90^\circ \text{ and } \angle CBE = 30^\circ$$

$$\angle BCE + \angle CEB + \angle CBE = 180^\circ$$

$$90^\circ + \angle CBE + 30^\circ = 180^\circ$$

$$\angle CEB = 60^\circ$$

Hence, $\angle AEB = \angle CEB = 60^\circ$

14. Let, the diameter of the moon = $2R_E$

Diameter of the earth = $2R_E$

$$\text{According to statement } R_M = \frac{1}{4}(2R_E)$$

$$R_E = 4R_M$$

$$\frac{\text{Volume of Moon}(V_M)}{\text{Volume of Earth}(V_E)} = \frac{\frac{4}{3}\pi R_M^3}{\frac{4}{3}\pi R_E^3}$$

$$= \frac{\frac{4}{3}\pi R_M^3}{\frac{4}{3}\pi (4R_M)^3} = \frac{1}{64} \frac{R_M^3}{R_M^3}$$

$$\frac{V_M}{V_E} = \frac{1}{64}$$

$$\Rightarrow V_M = \frac{1}{64} V_E$$

i.e., volume of moon is $\frac{1}{64}$ of the volume of earth.

15. Inner radius of the hemispherical tank (r) = 1 m

Outer radius of the hemispherical tank (R) = 1 + 0.01 = 1.01 m

Volume of iron used to make the hemispherical tank = $\frac{2}{3}\pi R^3 - \frac{2}{3}\pi r^3$

$$= \frac{2}{3}\pi(R^3 - r^3) = \frac{2}{3} \times \frac{22}{7} [(1.01)^3 - 1^3]$$

$$= \frac{44}{21} (1.0303 - 1) = \frac{44}{21} \times 0.0303 = 0.06349 m^3$$

16. Radius of the spherical balloon = $r_1 = 7$ cm

Surface area S_1 of the balloon = $4\pi r_1^2$

$$= 4 \times \frac{22}{7} \times 7^2 = 616 cm^2$$

Radius of the spherical balloon when air is pumped into it = $r_2 = 14$ cm

Surface area S_2 of the balloon = $4\pi r_2^2 = 4 \times \frac{22}{7} \times 14^2$

$$\frac{S_1}{S_2} = \frac{4 \times \frac{22}{7} \times 7^2}{4 \times \frac{22}{7} \times 14^2} = \frac{1}{4}$$

$$\therefore S_1 : S_2 = 1 : 4$$

17. We have

$$\sum_{i=1}^n (x_i - 50) = -10 \text{ and } \sum_{i=1}^n (x_i - 46) = 70$$

$$\sum_{i=1}^n x_i - 50 = 10 \quad \dots\dots\dots \text{(i)}$$

$$\text{and } \sum_{i=1}^n x_i - 46n = 70 \quad \dots\dots\dots \text{(ii)}$$

subtracting (ii) from (i), we get $-4n = -80$

n = 20

putting $n = 20$ in (i), we get

$$\sum_{i=1}^n (x_i - 50 \times 20) = -10$$

$$\sum_{i=1}^n x_i = 990$$

Therefore, mean = $\frac{1}{n} \left[\sum_{i=1}^n x_i \right] = \frac{990}{20}$

$$=49.5$$

Hence, $n = 20$ and mean = 49.5

18. (i) $P(\text{no defective part}) = \frac{50}{200} = 0.25$

(ii) $P(\text{at least one defective part}) = 1 - P(\text{no defective part}) = 1 - 0.25 = 0.75$

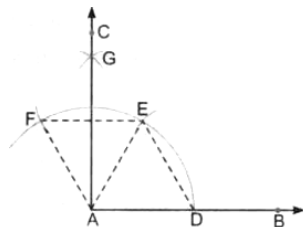
(iii) $P(\text{not more than 5 defective parts}) = P(\text{no defective part}) + P(1 \text{ defective part}) + P(2 \text{ defective parts}) + P(3 \text{ defective parts}) + P(4 \text{ defective parts}) + P(5 \text{ defective parts})$

$$= \frac{50}{200} + \frac{32}{200} + \frac{22}{200} + \frac{18}{200} + \frac{12}{200} + \frac{12}{200}$$
$$= \frac{146}{200} = 0.73$$

SECTION-D

Question numbers **19** to 28 carry **four** marks each.

19.



Steps of Construction

(i) Draw a ray AB.

(ii) Taking A as centre and some convenient radius draw an arc which intersect AB, say at point D.

(iii) Taking D as centre and with the same radius as before draw an arc intersecting the previously drawn arc, say at point E.

(iv) Taking E as centre and with the same radius draw an arc intersecting the drawn arc, say at point F.

(v) With E and F as centers, and some convenient radius (more than $\frac{1}{2}EF$), draw two arcs intersecting each other at G.

(vi) Draw ray AC passing through G. Then $\angle CAB$ is the required angle of 90° .

Justification

By construction $AD = DE = EA$

$\triangle EAD$ is an equilateral triangle. So $\angle EAD = 60^\circ$

Again $AE = EF = FA$.

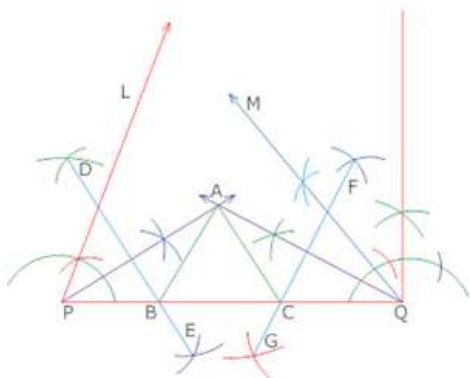
$\therefore \triangle FAE$ is an equilateral triangle. So $\angle FAE = 60^\circ$

As AG bisects $\angle FAE$, So $\angle GAE = 30^\circ$

Now, $\angle CAB = \angle GAE + \angle EAD$

$= 30^\circ + 60^\circ = 90^\circ$

20.



Steps of construction

(1) Draw a line segment $PQ = 11\text{cm} (= AB + BC + CA)$

(2) At P construct an angle of 60° and at Q an angle of 45°

(3) Bisects these angles let bisectors of these intersect at point A

(4) Draw perpendicular bisectors DE of AP to intersect PQ at B and FG of AQ to intersect PQ at C.

(5) Join AB and AC Then ABC is required triangle.

21. Join P and C

$$= (1522.5 + 661.5) \text{ cm}^2 = 2184 \text{ cm}^2$$

Cardboard used for making 250 boxes = $250 \times 2184 = 546000 \text{ cm}^2$

$$\text{Cost of cardboard} = \frac{4}{1000} \times 546000 = \text{Rs. } 2184$$

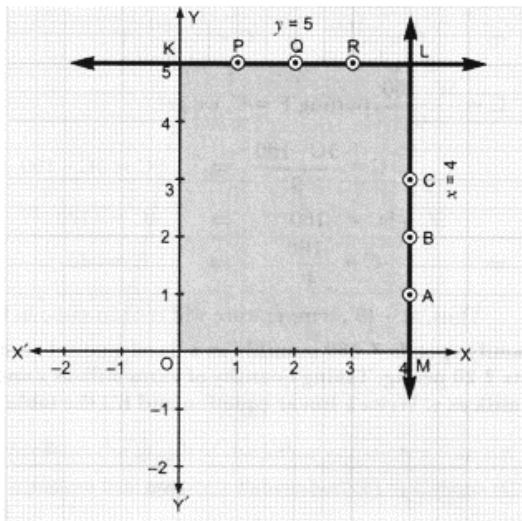
23. $x = 4$ and $y = 5$

$x = 4$ in two variables is $x + 0y = 4$

x	4	4	4
y	1	2	3
	A	B	C

$y = 5$ in two variables in $0x + y = 5$

x	1	2	3
y	5	5	5
	P	Q	R



\therefore Required area is OKLM with $x = 4$, $y = 5$ and both the axes.

The enclosed figure, i.e., OKLM is rectangle having length OM = 4 units and breadth OK = 5 units.

\therefore Area of rectangle/enclosed figure will be = $L \times B = 4 \times 5 = 20$ sq. units

24. External diameter of the spherical shell = 10cm

\therefore External radius $R = 5 \text{ cm}$

Internal diameter = 9cm

$$\text{Internal radius} = \frac{9}{2} \text{ cm}$$

$$r = \frac{9}{2} \text{ cm}$$

$$(i) \text{ Volume of the metal} = \frac{4}{3} \pi [R^3 - r^3] \text{ cm}^3$$

$$\begin{aligned}
&= \frac{4}{3} \pi \left[5^3 - \left(\frac{9}{2} \right)^3 \right] \text{cm}^3 \\
&= \frac{4}{3} \times \frac{22}{7} \left[125 - \frac{729}{8} \right] \text{cm}^3 \\
&= \frac{88}{21} \times \frac{271}{8} \text{cm}^3 = 141.95 \text{cm}^3
\end{aligned}$$

(ii) Weight of the shell = Volume \times density

$$= 141.95 \text{cm}^3 \times 9.6 \text{gm} / \text{cm}^3$$

$$= 1363 \text{gm}$$

$$= 1.363 \text{kg}$$

(iii) Outer surface area = $4\pi r^2$

$$= 4\pi (5)^2$$

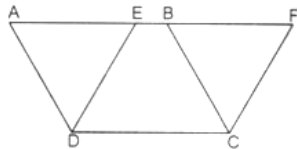
$$= 4 \times \frac{22}{7} \times 25$$

$$= \frac{2200}{7} = 314.389 \text{cm}^2$$

25. **Given:** Two parallelograms ABCD and EFCD on the same base DC and between the same parallel lines AF and DC.

To prove: $ar(\parallel^{gm} ABCD) = ar(\parallel^{gm} EFCD)$

Proof: In $\triangle ADE$ and $\triangle BCF$



$\angle DAE = \angle CBF$ (Corresponding angles from $AD \parallel BC$ and transversal AF)

$\angle AED = \angle BFC$ (Corresponding angles from $ED \parallel FC$ and transversal AF)

Therefore, $\angle ADE = \angle BCF$

Also, $AD = BC$ (Opposite sides of the parallelogram ABCD)

So, $\triangle ADE \cong \triangle BCF$ (By ASA congruence criterion)

As congruent triangles have equal areas

$$ar(\triangle ADE) = ar(\triangle BCF) \quad \dots (i)$$

Now, $ar(\parallel^{gm} ABCD) = ar(\triangle ADE) + ar(\text{quad.EDCB})$

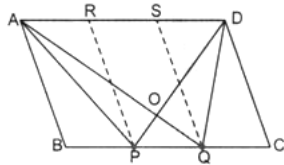
$$ar(\triangle BCF) + ar(\text{quad.EDCB}) \quad [\text{using (i)}]$$

$$= ar(\parallel^{gm} EFCD)$$

So, parallelograms ABCD and EFCD are equal in area.

26. Through P and Q, draw PR and QS parallel to AB. Now, PQSR is a parallelogram and its base

$$PQ = \frac{1}{3} BC.$$



Since $\triangle APQ$ and $\triangle DPQ$ are on the same base PQ, and between the same parallels AD and BC.

$$ar(\triangle APQ) = ar(\triangle DPQ) \quad \dots\dots\dots (i)$$

Since $\triangle APQ$ and parallelogram PQRS are on the same base PQ, and between the same parallels PQ and AC.

$$\therefore ar(\triangle APQ) = \frac{1}{2} (||^{gm} PQRS) \quad \dots\dots\dots (ii)$$

$$\text{Now, } \frac{(||^{gm} ABCD)}{(||^{gm} PQRS)} = \frac{BC \times height}{PQ \times height}$$

$$= \frac{3PQ}{PQ} \quad (\because \text{height of the two parallelogram is same})$$

$$ar(||^{gm} PQRS) = \frac{1}{3} ar(||^{gm} ABCD)$$

Using equation (ii) and (iii), we have

$$ar(\triangle APQ) = \frac{1}{2} ar(||^{gm} PQRS) = \frac{1}{2} \times \frac{1}{3} ar(||^{gm} ABCD)$$

$$\text{Hence, } ar(\triangle APQ) = ar(\triangle DPQ) = \frac{1}{6} ar(||^{gm} ABCD) \quad [\text{Using (i)}]$$

27. Since the given frequency distribution is the frequency distribution of 50 students. Therefore,

$$g = 50$$

From the table, we have

$$a = 12,$$

$$b + 12 = 25,$$

$$12 + b + 10 = c,$$

$$12 + b + 10 + d = 43,$$

$$12 + b + 10 + d + e = 48$$

$$\text{and } 12 + b + 10 + d + e + g = f$$

$$\text{Now, } b + 12 = 25$$

$$b = 13$$

$$12 + b + 10 = c \Rightarrow 12 + 13 + 10 = c \quad [\because b = 13]$$

$$c = 35$$

$$12 + b + 10 + d = 43 \Rightarrow 12 + 13 + 10 + d = 43 \quad [\because b = 13]$$

$$d = 8$$

$$12 + b + 10 + d + e = 48 \Rightarrow 12 + 13 + 10 + 8 + e = 48 \quad [\because b=13, d=8]$$

$$e = 5$$

$$\text{and } 12 + b + 10 + d + e + 2 = f$$

$$12 + 13 + 10 + 8 + 5 + 2 = f$$

$$f = 50$$

$$\text{Hence, } a = 12, b = 13, c = 35, d = 8, e = 5, f = 50$$

$$28. (i) P(\text{earning Rs. } 10000 - 13000 \text{ per month and owning exactly 2 vehicles}) = \frac{29}{2400}$$

$$(ii) P(\text{earning Rs. } 16000 \text{ or more per month and owning exactly 1 vehicles}) = \frac{579}{2400}$$

$$(iii) P(\text{earning Rs. } 7000 \text{ per month and does not own any vehicles}) = \frac{10}{2400} = \frac{1}{240}$$

$$(iv) P(\text{earning Rs. } 13000 - 16000 \text{ per month and owning more than 2 vehicles}) = \frac{25}{2400} = \frac{1}{96}$$

$$(v) P(\text{owning not more than 1 vehicle}) = \frac{2062}{2400} = \frac{1031}{1200}$$
