

Sl.No. 33314

S.S.L.C. EXAMINATION, MARCH - 2013
MATHEMATICS (English)

Time : 2½ Hours

Total Score : 80

Instructions :

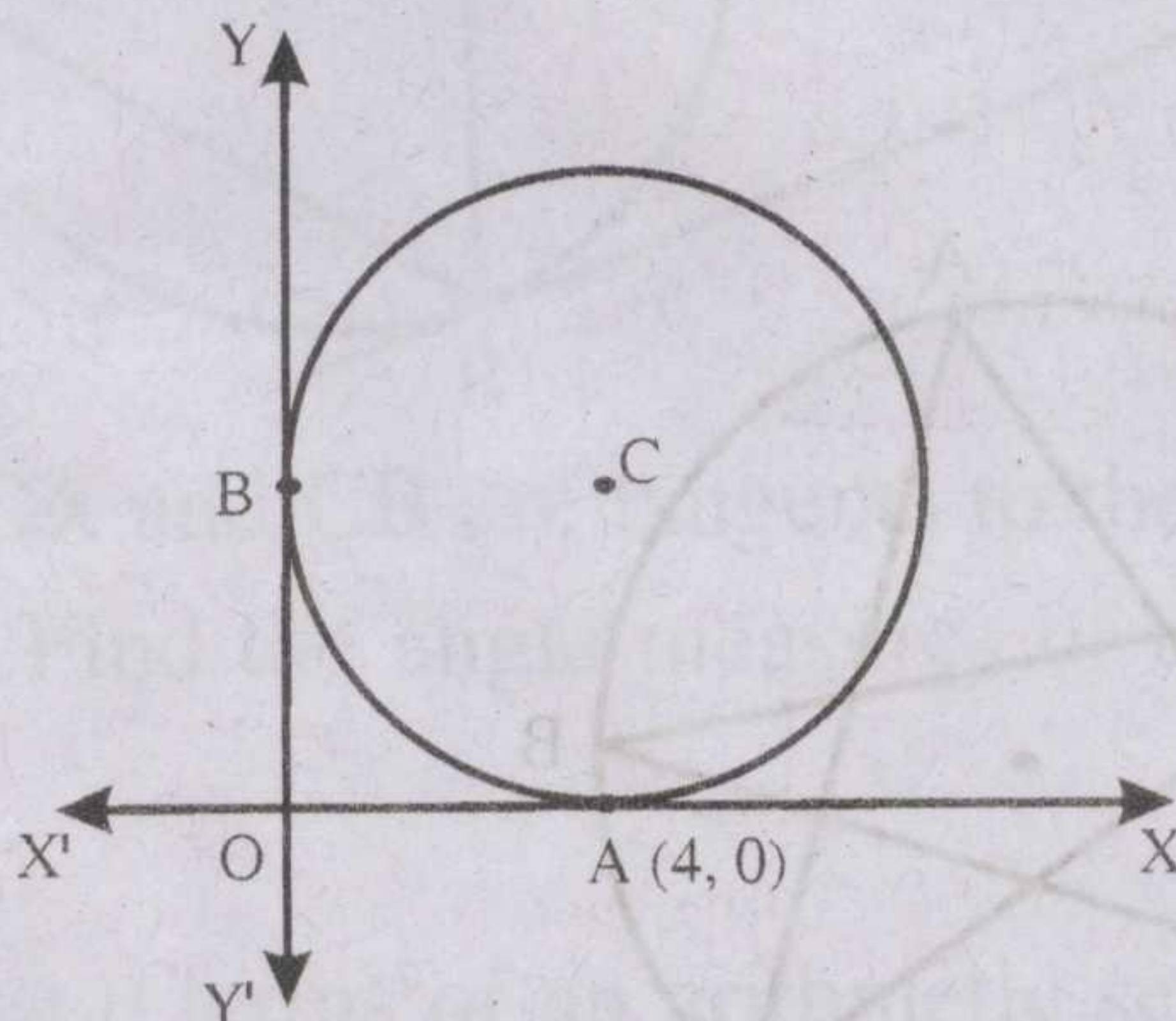
- 1) Read the questions carefully, understand each question and then answer the questions.
- 2) Give explanations wherever necessary.
- 3) If there is an OR between any two questions, you may answer only one among them.
- 4) 15 minutes will be given at the beginning as cool off time. This time may be utilised to read and understand the questions.
- 5) Simplification using irrationals like $\pi, \sqrt{2}$ etc. with their approximate values is not required if not specified in the question.

[SCORE]

Q1 Second and fourth terms of the following arithmetic sequence are missing. Find the numbers at these positions. [2]

11, —, 19, —,

Q2 If $(x - 2)$ is a factor of the polynomial $3x^3 - 2x^2 + kx - 6$, then what is the value of k ? [2]

Q3

In the figure, C is the centre of the circle. X and Y axes are tangents to the circle at the points A and B respectively. If the coordinates of A are (4, 0), find the coordinates of B and C. [2]



Q4) There are 18 beads in a box. Some of them are white and the remaining are black. The Probability of drawing a black bead from it is $\frac{1}{3}$. Then

[3]

- How many black beads are there in the box?
- How many white beads are there in the box?
- How many white beads should be added to it so that the probability of drawing a black bead becomes $\frac{1}{4}$?

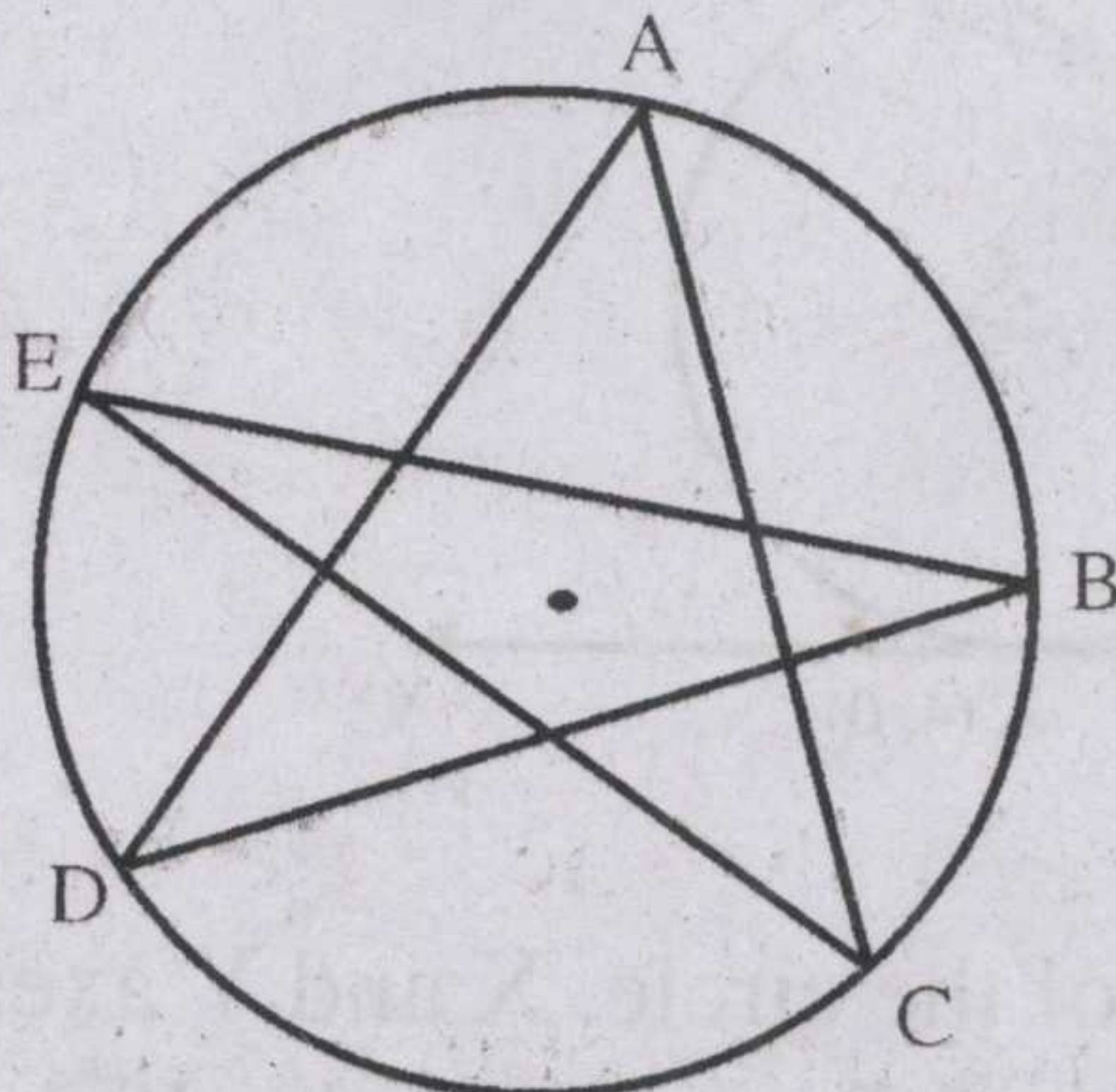
Q5) The table below shows the classification of people, participated in a medical camp, according to their weights.

[3]

Weight (in kilogram)	Number of people
20 – 30	16
30 – 40	21
40 – 50	28
50 – 60	24
60 – 70	11

Calculate the mean weight.

Q6)

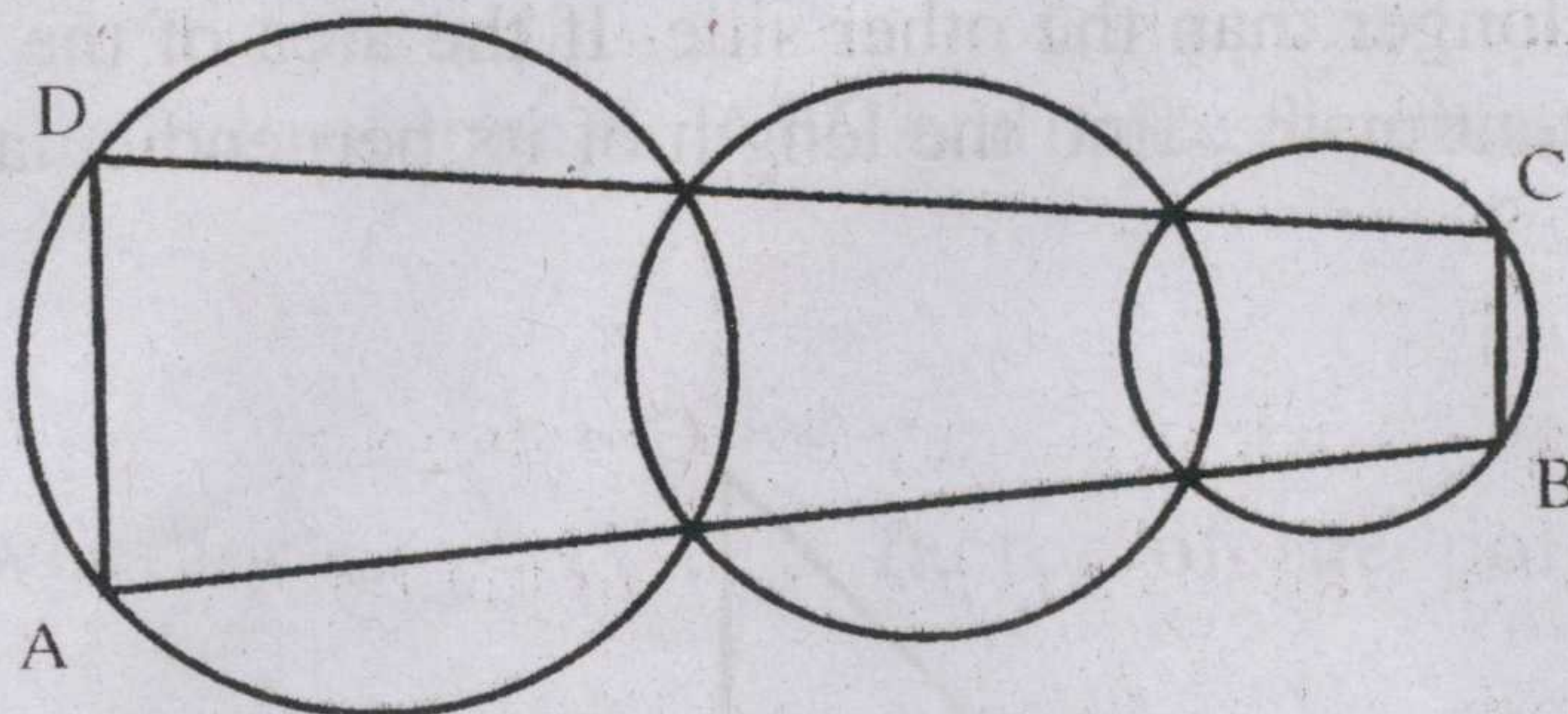


In the figure A, B, C, D and E are points on the circle. Prove that $\angle A + \angle B + \angle C + \angle D + \angle E = 180^\circ$.

[3]



OR

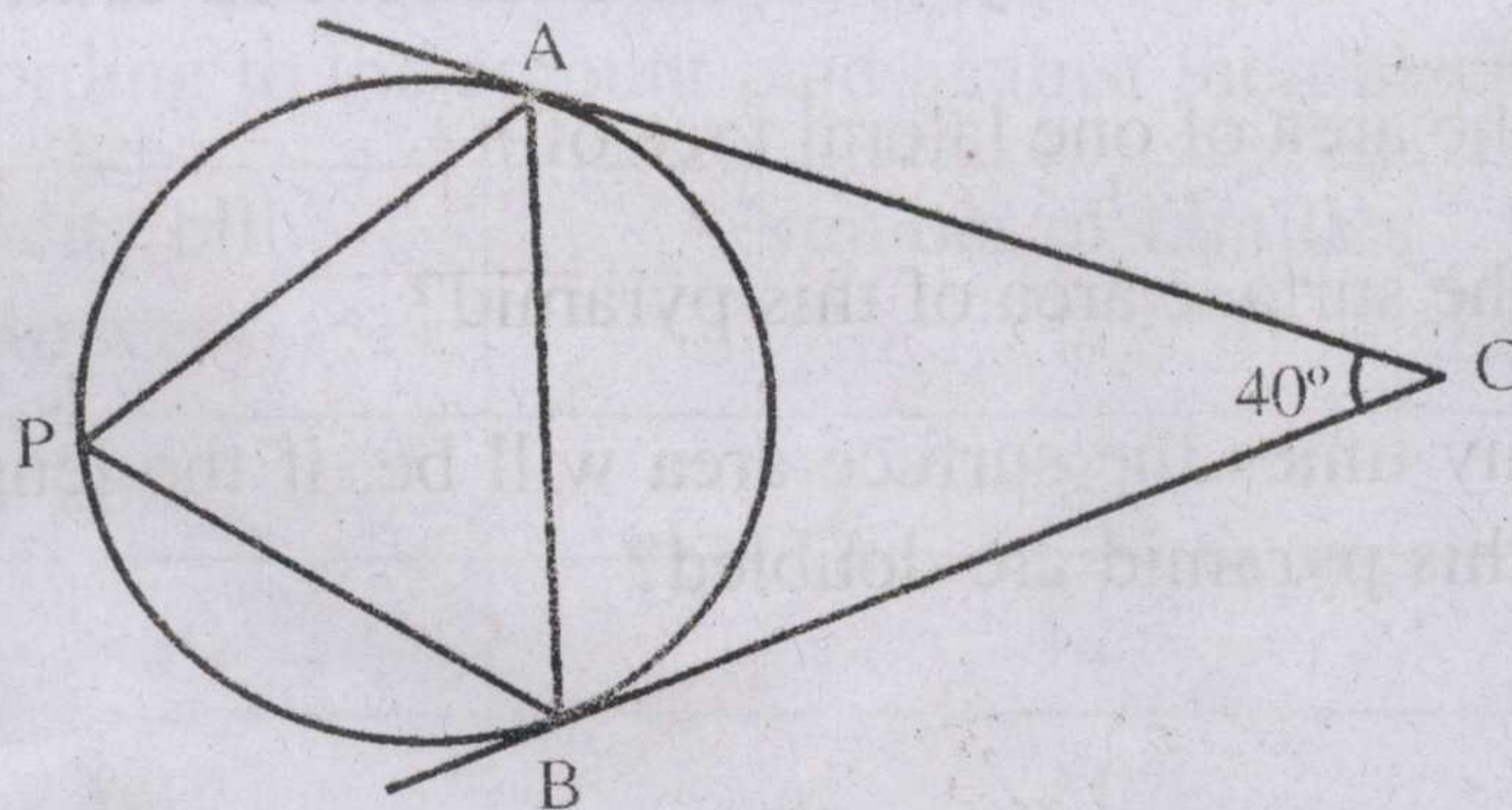


Prove that the quadrilateral ABCD shown in the figure is a cyclic quadrilateral.

- Q7) (a) Check whether the circle with centre at the point $(2, 4)$ and radius 5 units pass through the point $(2, 0)$.
- (b) Write the coordinates of the points at which this circle cuts the X axis.

[3]

Q8)



In the figure, CA and CB are tangents to the circle. Also $PA = PB$ and $\angle C = 40^\circ$. Find the angle measures of triangle PAB.

[3]

- Q9) The sum of first n terms of an arithmetic sequence is $5n^2 + 2n$.

[3]

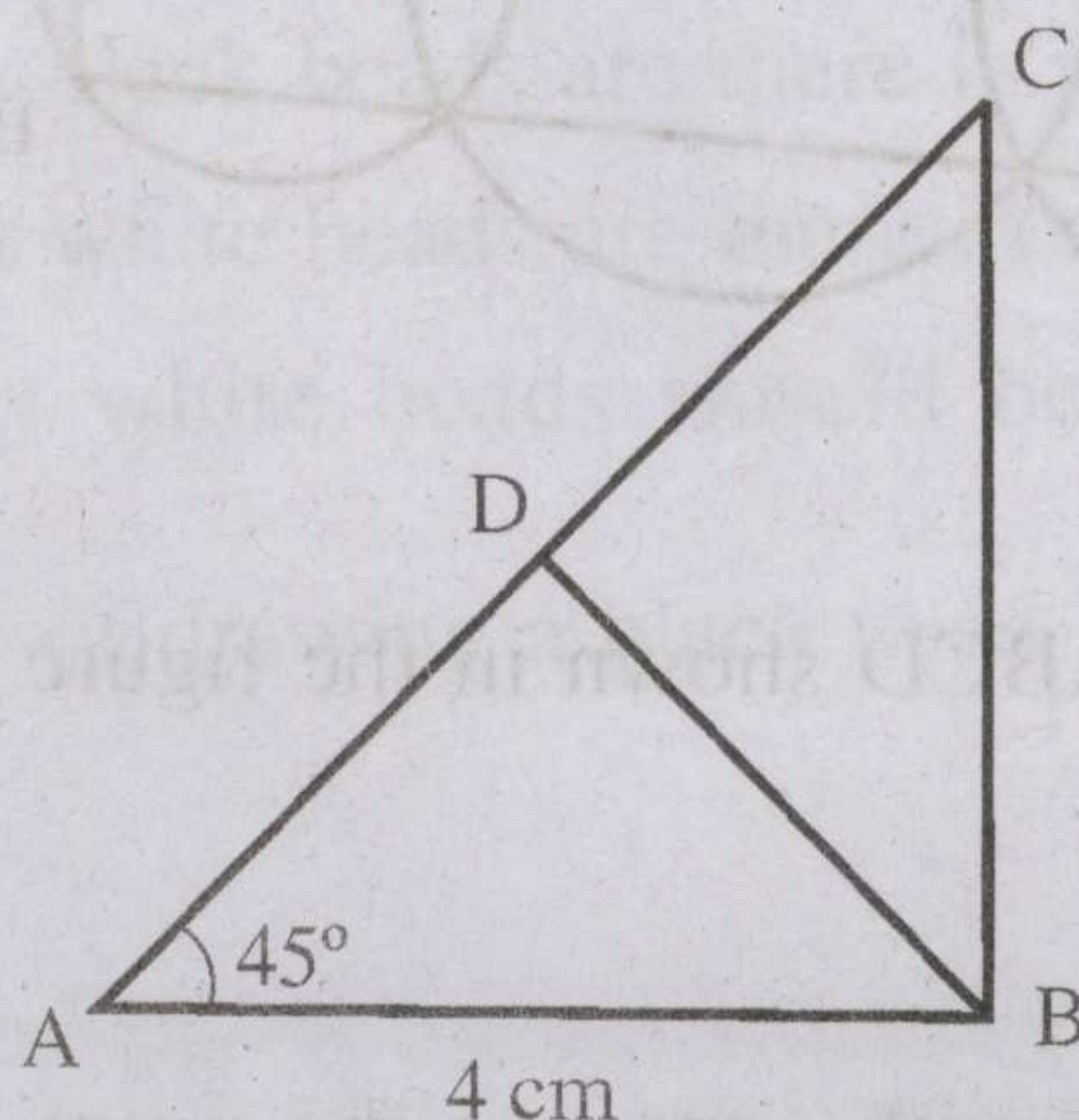
a) What is the sum of first two terms of this sequence?

- (b) Write the first two terms of this sequence.



- Q10)** In a right angled triangle, one of the perpendicular sides is 6 centimetre longer than the other side. If the area of the triangle is 36 square centimetre, find the length of its perpendicular sides. [3]

Q11)



In the figure, ABC is a right angled triangle. $AB = 4\text{cm}$, $\angle A = 45^\circ$ and D is the midpoint of AC. Then find the length of BC, AC and BD. [3]

- Q12)** All the edges of a square pyramid are of length 12 centimetre. [4]
- What is the area of one lateral face of it?
 - What is the surface area of this pyramid?
 - How many times the surface area will be, if the length of the sides of this pyramid are doubled?

- Q13)**
- Write the algebraic form of the arithmetic sequence 1, 4, 7, 10, [4]
 - Is 100 a term of this sequence? Why?
 - Prove that the square of any term of this sequence is also a term of it.



Good Mark

627

[SCORE]

- Q14)** a) Draw triangle ABC with $AB = 10$ cm, $\angle A = 50^\circ$ and $\angle B = 70^\circ$.
b) Draw the incircle of triangle ABC and write the measure of its radius.

[4]

- Q15)** a) Check whether $(x + 1)$ is a factor of the polynomial $p(x) = 6x^3 + 3x^2$.
b) What first degree polynomial added to $p(x)$ gives a polynomial for which $(x^2 - 1)$ is a factor?

[4]

OR

The remainder on dividing the polynomial $q(x)$ by $(x - a)$ is k and the remainder on dividing the polynomial $r(x)$ by $(x - a)$ is $-k$.

- a) Find $q(a)$.
b) Prove that $(x - a)$ is a factor of the polynomial $q(x) + r(x)$.

$q(x)$
 $q(a) = k$
 $r(a) = -k$

- Q16)** The table below shows the classification of 100 families in a locality, according to the amount paid against their electricity bill.

[4]

Electricity bill (in Rupees)	Number of families
0 – 200	8
200 – 400	12
400 – 600	21
600 – 800	30
800 – 1000	23
1000 – 1200	6

Find the median of the amount paid.



Q17) a) Draw a rectangle of sides 5 centimetre and 4 centimetre. Draw a square, equal in area to this rectangle.

b) Draw an isosceles triangle, equal in area to this square.

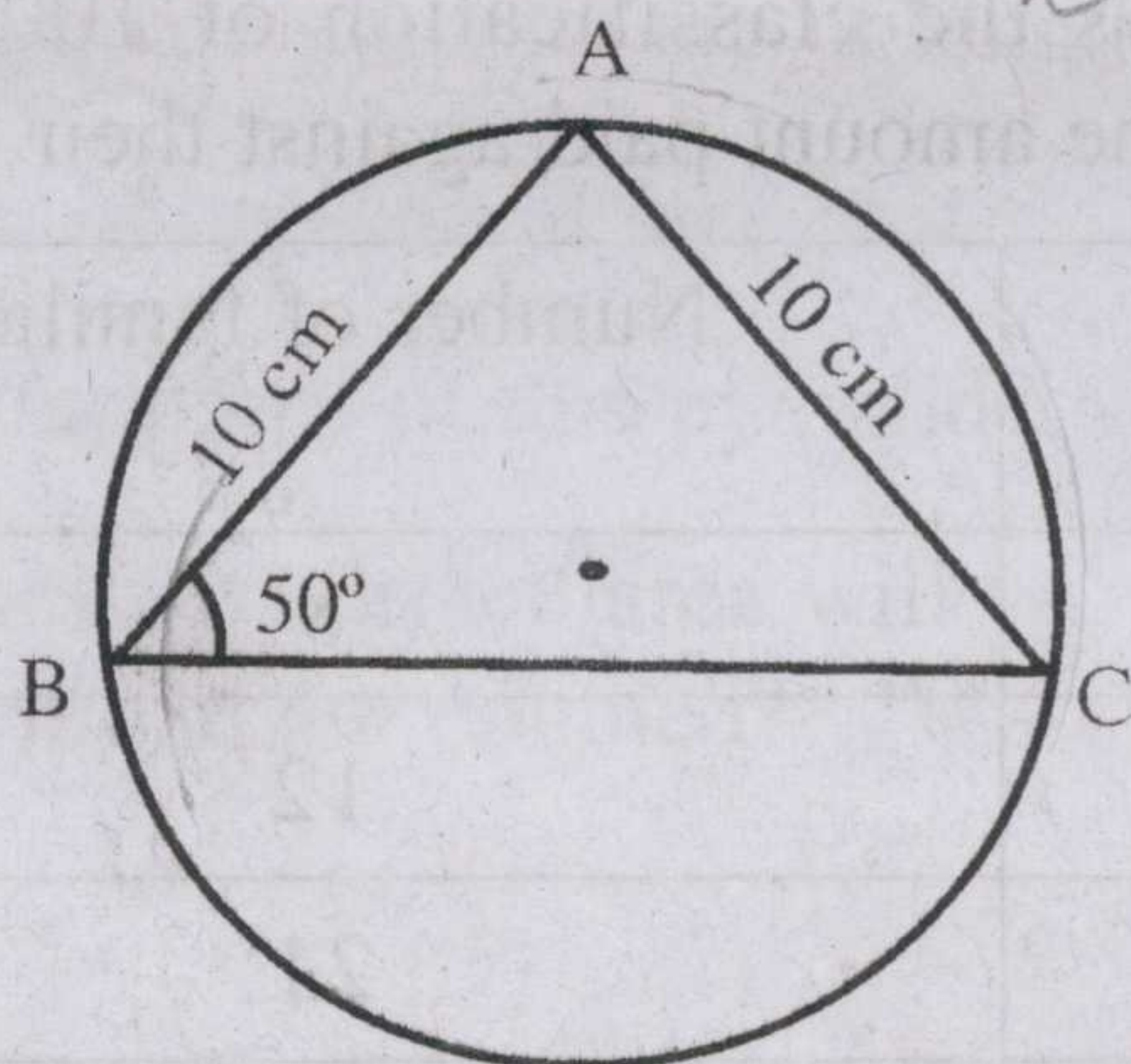
Q18) a) The sum of a number and its reciprocal is $\frac{25}{12}$. What is the number?

b) Prove that the sum of a positive number and its reciprocal is always greater than or equal to 2.

OR

To complete a job, Babu needs 6 more days than Abu. If both of them do the job together it takes 4 days to complete it. How many days each one needs, if they do the job separately?

Q19)



x
 $6+x$
 $x + (6+x) = 4$
 $2x = 4 - 6$
 $2x = -2$
 $x = -1$

In triangle ABC, $AB = AC = 10$ cm. $\angle ABC = 50^\circ$.

a) Find the length of BC.

b) Find the diameter of the circle.

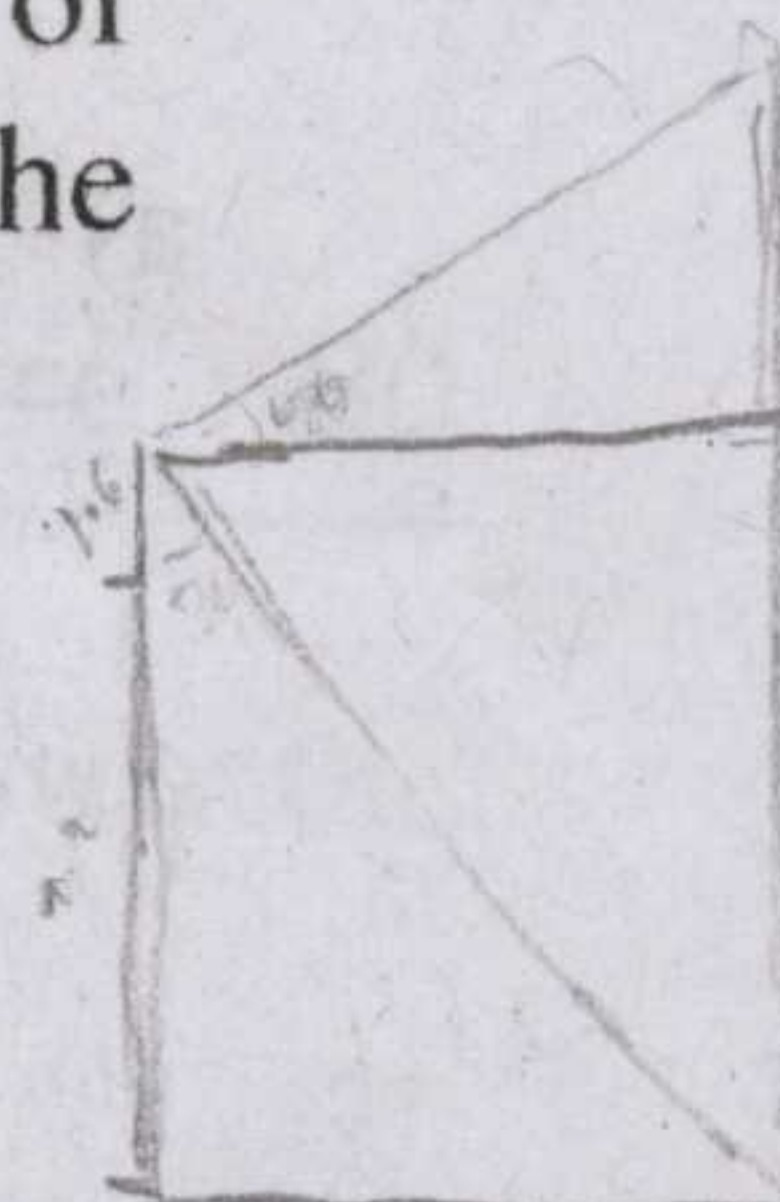
[$\sin 50^\circ = 0.77$, $\cos 50^\circ = 0.64$, $\tan 50^\circ = 1.19$]

OR



[SCORE]

Hari, standing on the top of a building, sees the top of a tower at an angle of elevation of 50° and the foot of the tower at an angle of depression of 20° . Height of Hari is 1.6 metre and height of the building on which he is standing is 9.2 metre.



- a) Draw a rough sketch according to the given information.
- b) How far is the tower from the building?
- c) Calculate the height of the tower.

$$\left[\begin{array}{l} \sin 20^\circ = 0.34, \cos 20^\circ = 0.94, \tan 20^\circ = 0.36 \\ \sin 50^\circ = 0.77, \cos 50^\circ = 0.64, \tan 50^\circ = 1.19 \end{array} \right]$$

Q20) a) The base diameter and slant height of a wooden cone is 10 centimetre each. What is the volume of this cone?

b) If this cone is carved in to a sphere of maximum size, find the volume of the sphere.

[5]

Q21) a) Draw X and Y axes and mark the points A(5, 8) and B(3, 2).

b) If we draw triangle ABC such that the side BC is parallel to the X axis, what will be its height?

c) Draw triangle ABC, such that the side BC is parallel to the X axis and area of the triangle is equal to 15 square units.

[5]



Q22) Consider the line $4x - 3y - 10 = 0$.

[5]

- Prove that $(4, 2)$ is a point on this line. Find another point on this line.
- Find the slope of this line.
- Write the equation of the line with the same slope and passing through the point $(3, 5)$.

$$4 \times 2$$

$$4, 2$$

$$8, 4$$

$$32 - 12$$

$$\begin{array}{r} 32 \\ 12 \\ \hline 20 \end{array}$$