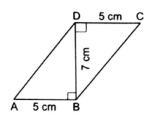
# 10. Area

# **Exercise 10A**

# 1. Question

In the adjoining figure, show that ABCD is a parallelogram.

Calculate the area of Igm ABCD.



# Answer

In the given figure consider  $\triangle$ ABD and  $\triangle$ BCD

Area of  $\triangle ABD = \frac{1}{2} \times base \times height = \frac{1}{2} \times AB \times BD$   $= \frac{1}{2} \times 5 \times 7 = \frac{35}{2} - \dots - 1$ Area of  $\triangle BCD = \frac{1}{2} \times base \times height = \frac{1}{2} \times DC \times DB$  $= \frac{1}{2} \times 5 \times 7 = \frac{35}{2} - \dots - 2$ 

From 1 and 2 we can tell that area of two triangle that is ∆ABD and ∆BCD are equal

Since the diagonal BD divides ABCD into two triangles of equal area and opp sides AB = DC

```
.ABCD is a parallelogram
```

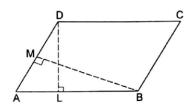
: Area of parallelogram ABCD = Area of  $\triangle$ ABD + Area of  $\triangle$ BCD

$$=\left(\frac{35}{2}+\frac{35}{2}\right)=\frac{70}{2}$$
 cm<sup>2</sup> = 35 cm<sup>2</sup>

 $\therefore$  Area of parallelogram ABCD = 35cm<sup>2</sup>

# 2. Question

In a parallelogram ABCD, it is being given that AB = 10 cm and the altitudes corresponding to the sides AB and AD are DL = 6 cm and BM = 8 cm, respectively. Find AD.



Given

AB = 10 cm

DL = 6 cm

BM = 8 cm

AD = ? (To find)

Here, Area of parallelogram = base x height

In the given figure if we consider AB as base Area =  $AB \times DL$ 

If we consider DM as base Area =  $AD \times BM$ 

∴ Area = AB x DL = AD x BM

 $\Rightarrow$  10 x 6 = AD x 8

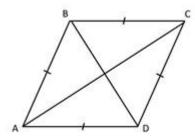
 $\Rightarrow$  60 = 8 x AD

$$\Rightarrow AD = \frac{60}{8} = 7.5 \ cm$$

### 3. Question

Find the area of a rhombus, the lengths of whose diagonals are 16 cm and 24 cm respectively.

#### Answer



Here, Let ABCD be Rhombus with diagonals AC and BD

Here let AC = 24 and BD = 16

We know that, in a Rhombus, diagonals are perpendicular bisectors to each other

∴ if we consider <u>ABC</u> AC is base and OB is height

Similarly, in <u>∧</u>ADC AC is base and OD is height

Now, Area of Rhombus = Area of  $\triangle ABC$  + Area of  $\triangle ADC$ 

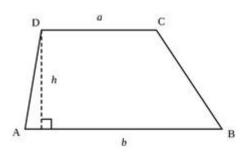
$$= \frac{1}{2} \times AC \times OB + \frac{1}{2} \times AC \times OD$$
  
=  $\frac{1}{2} \times 24 \times \frac{BD}{2} + \frac{1}{2} \times 24 \times \frac{BD}{2}$  (Since AC and BC are perpendicular bisectors  $\therefore OB = OD = \frac{BD}{2}$ )  
=  $\frac{1}{2} \times 24 \times \frac{16}{2} + \frac{1}{2} \times 24 \times \frac{16}{2} = 96 + 96 = 192 \text{ cm}^2$ 

. Area of Rhombus ABCD is 192cm<sup>2</sup>

# 4. Question

Find the area of a trapezium whose parallel sides are 9 cm and 6 cm respectively and the distance between these sides is 8 cm.

# Answer



Given

AB = a = 9 cm

DC = b = 6 cm

Height (h) = 8 cm

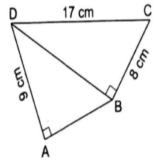
We know that area of trapezium is  $\frac{1}{2}$  x (sum of parallel sides) x height

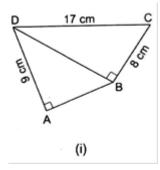
Therefore, Area of trapezium ABCD =  $\frac{1}{2}$  x (AB + DC) x h =  $\frac{1}{2}$  x (9 + 6) x 8 = 60 cm<sup>2</sup>

: Area of Trapezium ABCD =  $60 \text{ cm}^2$ 

# 5A. Question

Calculate the area of quad. ABCD, given in Fig. (i).





Given

AD = 9 cm

BC = 8 cm

DC = 17 cm

Here Area of Quad ABCD = Area of  $\triangle ABD$  + Area of  $\triangle BCD$ 

$$= \frac{1}{2} \times AB \times AD + \frac{1}{2} \times BC \times BD$$

By Pythagoras theorem in  $\triangle BCD$ 

 $DC^2 = BD^2 + BC^2$ 

 $17^2 = BD^2 + 8^2$ 

 $\mathsf{BD}^2 = 17^2 - 8^2 = 289 - 64 = 225$ 

Similarly in ∆ABD using Pythagoras theorem

 $\mathsf{B}\mathsf{D}^2 = \mathsf{A}\mathsf{D}^2 + \mathsf{A}\mathsf{B}^2$ 

 $15^2 = 9^2 + AB^2$ 

 $AB^2 = 15^2 - 9^2 = 225 - 81 = 144$ 

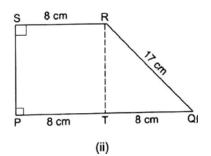
Now, Area of Quad ABCD = Area of  $\triangle ABD$  + Area of  $\triangle BCD$ 

$$= \frac{1}{2} \times AB \times AD + \frac{1}{2} \times BC \times BD$$
$$= \frac{1}{2} \times 12 \times 9 + \frac{1}{2} \times 8 \times 15 = 54 + 60 = 114 \text{ cm}^2$$

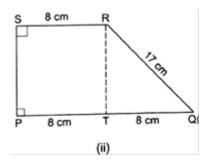
 $\therefore$  Area of Quadrilateral ABCD = 114 cm<sup>2</sup>

#### **5B.** Question

Calculate the area of trap. PQRS, given in Fig. (ii).



#### Answer



- Given :- Right trapezium
- RS = 8 cm
- PT = 8cm
- TQ = 8 cm
- RQ = 17 cm

Here PQ = PT + TQ = 8 + 8 = 16

We know that area of trapezium is  $\frac{1}{2}$  x (sum of parallel sides) x height

That is 
$$\frac{1}{2}$$
 x (AB + DC) x RT

Consider <u>∧</u>TQR

By Pythagoras theorem

$$RQ^{2} = TQ^{2} + RT^{2}$$
  

$$17^{2} = 8^{2} + RT^{2}$$
  

$$RT^{2} = 17^{2} - 8^{2} = 289 - 64 = 225$$
  

$$\therefore RT = 15 \text{ cm}$$
  

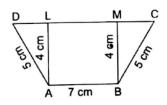
$$\therefore \text{ Area of trapezium} = \frac{1}{2} \times (RS + PQ) \times RT$$
  

$$= \frac{1}{2} \times (8 + 16) \times 15 = 180 \text{ cm}^{2}$$

 $\therefore$  Area of trapezium PQRS = 180 cm<sup>2</sup>

# 6. Question

In the adjoining figure, ABCD is a trapezium in which AB  $\parallel$  DC; AB = 7 cm; AD = BC = 5 cm and the distance between AB and DC is 4 cm. Find the length of DC and hence, find the area of trap. ABCD.



#### Answer

Given

AB = 7 cm

AD = BC 5 cm

AL = BM = 4cm (height)

DC = ?

Here in the given figure AB = LM

∴ LM = 7 cm -----1

Now Consider ∆ALD

By Pythagoras theorem

 $AD^2 = AL^2 + DL^2$ 

 $5^2 = 4^2 + DL^2$ 

 $\mathsf{DL}^2 = 5^2 - 4^2 = 25 - 16 = 9$ 

.. DL = 3 cm -----2

Similarly in ∆BMC

By Pythagoras theorem

 $BC^2 = BM^2 + MC^2$ 

 $5^2 = 4^2 + MC^2$ 

 $MC^2 = 5^2 - 4^2 = 25 - 16 = 9$ 

: MC = 3 cm --3

. from 1 2 and 3

DC = DL + LM + MC = 3 + 7 + 3 = 13 cm

We know that area of trapezium is  $\frac{1}{2}$  x (sum of parallel sides) x height

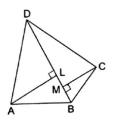
$$\therefore \text{ Area of trapezium} = \frac{1}{2} \times (\text{AB} + \text{DC}) \times \text{Al}$$

$$=\frac{1}{2} \times (7 + 13) \times 4 = 40 \text{ cm}^2$$

 $\therefore$  Area of trapezium ABCD = 180 cm<sup>2</sup>

# 7. Question

BD is one of the diagonals of a quad. ABCD. If AL  $\perp$  BD and CM  $\perp$  BD, show that ar(quad. ABCD) =  $\frac{1}{2}$  x BD x (AL + CM).



#### Answer

Given :

AL  $\perp$  BD and CM  $\perp$  BD

To prove : ar (quad. ABCD) =  $\frac{1}{2}$  x BD x (AL + CM)

Proof:

Area of 
$$\triangle ABD = \frac{1}{2} \times BD \times AM$$
  
Area of  $\triangle ABD = \frac{1}{2} \times BD \times CM$ 

Now area of Quad ABCD = Area of  $\triangle ABD$  + Area of  $\triangle BCD$ 

$$= \frac{1}{2} \times BD \times AL + \frac{1}{2} \times BD \times CM$$
$$= \frac{1}{2} \times BD \times (AL + CM)$$

Hence proved

### 8. Question

In the adjoining figure, ABCD is a quadrilateral in which diag. BD = 14 cm. If  $AL \perp BD$  and  $CM \perp BD$  such that AL = 8 cm and CM = 6 cm, find the area of quad. ABCD.

D

Given

AL  $\perp$  BD and CM  $\perp$  BD

BD = 14 cm

AL = 8 cm

CM = 6 cm

Here,

Area of  $\triangle ABD = \frac{1}{2} \times BD \times AM$ 

Area of  $\triangle ABD = \frac{1}{2} \times BD \times CM$ 

Now area of Quad ABCD = Area of  $\triangle ABD$  + Area of  $\triangle BCD$ 

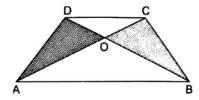
$$= \frac{1}{2} \times BD \times AL + \frac{1}{2} \times BD \times CM$$
$$= \frac{1}{2} \times BD \times (AL + CM)$$

: Area of quad ABCD =  $\frac{1}{2}$  x BD x (AL + CM) =  $\frac{1}{2}$  x 14 x (8 + 6) = 98cm<sup>2</sup>

: Area of quad ABCD =  $98 \text{cm}^2$ 

### 9. Question

In the adjoining figure, ABCD is a trapezium in which AB  $\parallel$  DC and its diagonals AC and BD intersect at O. Prove that ar( $\Delta$ AOD) = ar( $\Delta$ BOC).





Given

# AB II DC

To prove that: area( $\Delta AOD$ ) = area( $\Delta BOC$ )

Here in the given figure Consider  $\triangle ABD$  and  $\triangle ABC$ ,

we find that they have same base AB and lie between two parallel lines AB and CD

According to the theorem: triangles on the same base and between same parallel lines have equal areas.

 $\therefore$  Area of  $\triangle$ ABD = Area of  $\triangle$ BCA

Now,

```
Area of \triangle AOD = Area of \triangle ABD - Area of \triangle AOB ---1
```

```
Area of \triangle COB = Area of \triangle BCA - Area of \triangle AOB ---2
```

. From 1 and 2

```
We can conclude that area(\triangle AOD) = area(\triangle BOC) (Since Area of \triangle AOB is common)
```

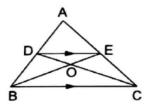
Hence proved

### **10. Question**

In the adjoining figure, DE || BC. Prove that

(i)  $ar(\Delta ACD) = ar(\Delta ABE)$ ,

(ii)  $ar(\Delta OCE) = ar(\Delta OBD)$ .



#### Answer

Given

AB II DC

```
To prove that : (i) area(\DeltaACD) = area(\DeltaABE)
```

```
(ii) area(\triangle OCE) = area(\triangle OBD)
```

(i)

Here in the given figure Consider  $\triangle$ BDE and  $\triangle$ ECD,

we find that they have same base DE and lie between two parallel lines BC and DE

According to the theorem: triangles on the same base and between same parallel lines have equal

areas.

∴ Area of  $\triangle$ BDE = Area of  $\triangle$ ECD Now, Area of  $\triangle$ ACD = Area of  $\triangle$ ECD + Area of  $\triangle$ ADE ---1 Area of  $\triangle$ ABE = Area of  $\triangle$ BDE + Area of  $\triangle$ ADE ---2 ∴ From 1 and 2 We can conclude that area( $\triangle$ AOD) = area( $\triangle$ BOC) (Since Area of  $\triangle$ ADE is common) Hence proved (ii) Here in the given figure Consider  $\triangle$ BCD and  $\triangle$ BCE, we find that they have same base BC and lie between two parallel lines BC and DE According to the theorem : triangles on the same base and between same parallel lines have equal areas.

 $\therefore$  Area of  $\triangle$ BCD = Area of  $\triangle$ BCE

Now,

Area of  $\triangle OBD =$  Area of  $\triangle BCD -$  Area of  $\triangle BOC ---1$ 

Area of  $\triangle OCE =$  Area of  $\triangle BCE -$  Area of  $\triangle BOC ---2$ 

. From 1 and 2

We can conclude that area( $\triangle OCE$ ) = area( $\triangle OBD$ ) (Since Area of  $\triangle BOC$  is common)

Hence proved

### 11. Question

In the adjoining figure, D and E are points on the sides AB and AC of  $\triangle$ ABC such that ar( $\triangle$ BCE) = ar( $\triangle$ BCD).

Show that DE || BC.

Answer

Given

A triangle ABC in which points D and E lie on AB and AC of  $\triangle$ ABC such that ar( $\triangle$ BCE) = ar( $\triangle$ BCD).

To prove: DE II BC

Proof:

Here, from the figure we know that  $\triangle$ BCE and  $\triangle$ BCD lie on same base BC and

It is given that area( $\Delta BCE$ ) = area( $\Delta BCD$ )

Since two triangle have same base and same area they should equal altitude(height)

That means they lie between two parallel lines

That is DE II BC

∴ DE 🛛 BC

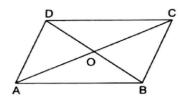
Hence proved

# 12. Question

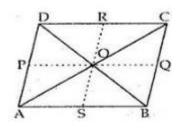
In the adjoining figure, O is any point inside a parallelogram ABCD. Prove that

(i) 
$$ar(\Delta OAB) + ar(\Delta OCD) = \frac{1}{2}ar( \|gm \ ABCD),$$

(ii)ar(
$$\Delta OAD$$
) + ar( $\Delta OBC$ ) =  $\frac{1}{2}$ ar( $\|$ gm ABCD).



Answer



Given : A parallelogram ABCD with a point 'O' inside it.

To prove : (i) area( $\Delta OAB$ ) + area( $\Delta OCD$ ) =  $\frac{1}{2}$  area( $\|gm|ABCD$ ),

(ii)area( $\Delta OAD$ ) + area( $\Delta OBC$ ) =  $\frac{1}{2}$  area(Igm ABCD).

Construction : Draw PQ || AB and RS || AD

Proof:

(i)

ΔAOB and parallelogram ABQP have same base AB and lie between parallel lines AB and PQ. According to theorem: If a triangle and parallelogram are on the same base and between the same parallel lines, then the area of the triangle is equal to half of the area of the parallelogram.

$$\therefore$$
 area( $\triangle$ AOB) =  $\frac{1}{2}$  area( $\|$ gm ABQP) ---1

Similarly, we can prove that area( $\Delta COD$ ) =  $\frac{1}{2}$  area(Igm PQCD) ---2

∴ Adding -1 and -2 we get,

area(
$$\Delta AOB$$
) + area( $\Delta COD$ ) =  $\frac{1}{2}$  area( $\|gm \ ABQP$ ) +  $\frac{1}{2}$  area( $\|gm \ PQCD$ )  
area( $\Delta AOB$ ) + area( $\Delta COD$ ) =  $\frac{1}{2}$  [area( $\|gm \ ABQP$ ) + area( $\|gm \ PQCD$ )] =  $\frac{1}{2}$  area( $\|gm \ ABCD$ )  
 $\therefore$  area( $\Delta AOB$ ) + area( $\Delta COD$ ) =  $\frac{1}{2}$  area( $\|gm \ ABCD$ )

Hence proved

(ii)

 $\Delta OAD$  and parallelogram ASRD have same base AD and lie between parallel lines AD and RS.

According to theorem: If a triangle and parallelogram are on the same base and between the same parallel lines, then the area of the triangle is equal to half of the area of the parallelogram.

$$\therefore$$
 area( $\Delta$ OAD) =  $\frac{1}{2}$  area(Igm ASRD) ---1

Similarly, we can prove that area( $\Delta OBC$ ) =  $\frac{1}{2}$  area( $\|gm BCRS$ ) ---2

. Adding -1 and -2 we get,

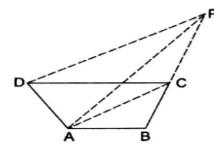
area(
$$\Delta OAD$$
) + area( $\Delta OBC$ ) =  $\frac{1}{2}$  area( $\|gm \ ASRD$ ) +  $\frac{1}{2}$  area( $\|gm \ BCRS$ )  
area( $\Delta OAD$ ) + area( $\Delta OBC$ ) =  $\frac{1}{2}$  [area( $\|gm \ ASRD$ ) + area( $\|gm \ BCRS$ )] =  $\frac{1}{2}$  area( $\|gm \ ABCD$ )  
 $\therefore$  area( $\Delta OAD$ ) + area( $\Delta OBC$ ) =  $\frac{1}{2}$  area( $\|gm \ ABCD$ )

Hence proved

# 13. Question

In the adjoining figure, ABCD is a quadrilateral. A line through D, parallel to AC, meets BC produced in P.

Prove that  $ar(\Delta ABP) = (quad.ABCD)$ .



### Answer

Given : ABCD is a quadrilateral in which a line through D drawn parallel to AC which meets BC produced in P.

To prove: area of  $(\Delta ABP)$  = area of (quad ABCD)

Proof:

Here, in the given figure

 $\Delta$ ACD and  $\Delta$ ACP have same base and lie between same parallel line AC and DP.

According to the theorem : triangles on the same base and between same parallel lines have equal

areas.

 $\therefore$  area of ( $\triangle$ ACD) = area of ( $\triangle$ ACP) -----1

Now, add area of ( $\Delta ABC$ ) on both side of (1)

: area of ( $\Delta$ ACD) + ( $\Delta$ ABC) = area of ( $\Delta$ ACP) + ( $\Delta$ ABC)

Area of (quad ABCD) = area of ( $\Delta$ ABP)

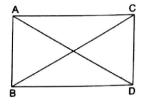
 $\therefore$  area of ( $\triangle$ ABP) = Area of (quad ABCD)

Hence proved

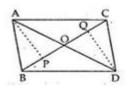
### 14. Question

In the adjoining figure,  $\triangle ABC$  and  $\triangle DBC$  are on the same base BC with A and D on opposite sides of BC such that  $ar(\triangle ABC) = ar(\triangle DBC)$ .

Show that BC bisects AD.







Given :  $\triangle ABC$  and  $\triangle DBC$  having same base BC and area( $\triangle ABC$ ) = area( $\triangle DBC$ ).

 $\triangle AOP \cong \triangle QOD [AAS]$ 

Thus By corresponding parts of congruent triangles law [C.P.C.T]

: OA = OD [C.P.C.T]

Hence BC bisects AD

Hence proved

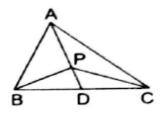
# 15. Question

In the adjoining figure, AD is one of the medians of a  $\Delta ABC$  and P is a point on AD.

Prove that

(i)  $ar(\Delta BDP) = ar(\Delta CDP)$ 

(ii)  $ar(\Delta ABP) = ar(\Delta ACP)$ 



Given : A  $\triangle$ ABC in which AD is the median and P is a point on AD

To prove: (i)  $ar(\Delta BDP) = ar(\Delta CDP)$ ,

```
(ii) ar(\Delta ABP) = ar(\Delta ACP).
```

(i)

```
In \DeltaBPC, PD is the median. Since median of a triangle divides the triangles into two equal areas
```

```
So, area(\DeltaBDP) = area(\DeltaCDP)----1
```

Hence proved

(ii)

In  $\triangle ABC AD$  is the median

So, area( $\triangle$ ABD) = area( $\triangle$ ADC) ----2 and

area( $\Delta$ BDP) = area( $\Delta$ CDP) [from 1]

Now subtracting area( $\Delta$ BDP) from ---2 , we have

area( $\Delta$ ABD) - area( $\Delta$ BDP) = area( $\Delta$ ADC) - area( $\Delta$ BDP)

```
area(\DeltaABD) - area(\DeltaBDP) = area(\DeltaADC) - area(\DeltaCDP) [since area(\DeltaBDP) = area(\DeltaCDP) from -1]
```

```
\therefore area(\triangleABP) = area(\triangleACP)
```

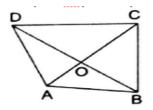
Hence proved.

### 16. Question

In the adjoining figure, the diagonals AC and BD of a quadrilateral ABCD intersect at O.

If BO = OD, prove that

 $Ar(\Delta ABC) = ar(\Delta ADC).$ 



#### Answer

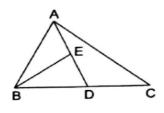
Given : A quadrilateral ABCD with diagonals AC and BD and BO = OD

To prove: Area of ( $\triangle ABC$ ) = area of ( $\triangle ADC$ ) Proof : BO = OD [given] Here AO is the median of  $\triangle ABD$   $\therefore$  Area of ( $\triangle AOD$ ) = Area of ( $\triangle AOB$ ) ------ 1 And OC is the median of  $\triangle BCD$   $\therefore$  Area of ( $\triangle COD$ ) = Area of ( $\triangle BOC$ ) ----- 2 Now by adding -1 and -2 we get Area of ( $\triangle AOD$ ) + Area of ( $\triangle COD$ ) = Area of ( $\triangle AOB$ ) + Area of ( $\triangle BOC$ )  $\therefore$  Area of ( $\triangle ABC$ ) = Area of ( $\square \# \times 2206; ADC$ )

Hence proved

# 17. Question

ABC is a triangle in which D is the midpoint of BC and E is the midpoint of AD. Prove that  $ar(\Delta BED) = \frac{1}{4}ar(\Delta ABC)$ .



#### Answer

Given : A  $\triangle$ ABC in which AD is the median and E is the midpoint on line AD

To prove: area( $\Delta$ BED) =  $\frac{1}{4}$  area( $\Delta$ ABC)

Proof : here in  $\triangle ABC AD$  is the midpoint

 $\therefore$  Area of ( $\triangle$ ABD) = Area of ( $\triangle$ ADE)

Hence Area of ( $\Delta ABD$ ) =  $\frac{1}{2}$  [Area of ( $\Delta ABC$ )] ------ 1

No in  $\Delta ABD$  E is the midpoint of AD and BE is the median

 $\therefore$  Area of ( $\triangle$ BDE) = Area of ( $\triangle$ ABE)

Hence Area of (
$$\Delta$$
BED) =  $\frac{1}{2}$  [Area of ( $\Delta$ ABD)] ------ 2

Substituting (1) in (2), we get

Hence Area of  $(\Delta BED) = \frac{1}{2} [\frac{1}{2} \text{ Area of } (\Delta ABC)]$  $\therefore \operatorname{area}(\Delta BED) = \frac{1}{4} \operatorname{area}(\Delta ABC)$ 

Hence proved

# **18. Question**

The vertex A of  $\triangle$ ABC is joined to a point D on the side BC. The midpoint of AD is E. Prove that

ar(
$$\Delta$$
BEC) =  $\frac{1}{2}$  ar( $\Delta$ ABC).

#### Answer

Given : A  $\triangle$ ABC in which AD is a line where D is a point on BC and E is the midpoint of AD

To prove:  $ar(\Delta BEC) = \frac{1}{2} ar(\Delta ABC)$ 

Proof: In  $\triangle ABD E$  is the midpoint of side AD

 $\therefore$  Area of ( $\triangle$ BDE) = Area of ( $\triangle$ ABE)

Hence Area of ( $\Delta$ BDE) =  $\frac{1}{2}$  [Area of ( $\Delta$ ABD)] -1

Now, consider  $\triangle$ ACD in which E is the midpoint of side AD

 $\therefore$  Area of ( $\Delta$ ECD) = Area of ( $\Delta$ AEC)

Hence Area of ( $\Delta$ ECD) =  $\frac{1}{2}$  [Area of ( $\Delta$ ACD)] -2

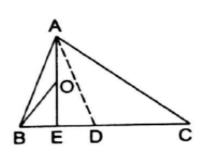
Now, adding -1 and -2, we get

Area of 
$$(\Delta BDE)$$
 + Area of  $(\Delta ECD) = \frac{1}{2}$  [Area of  $(\Delta ABD)$ ] +  $\frac{1}{2}$  [Area of  $(\Delta ACD)$ ]  
 $\therefore$  area $(\Delta BEC) = \frac{1}{2}$  [area $(\Delta ABD)$  + area $(\Delta ACD)$ ]  
 $\therefore$  Area $(\Delta BEC) = \frac{1}{2}$  Area $(\Delta ABC)$ 

Hence proved

### **19.** Question

D is the midpoint of side BC of  $\triangle$ ABC and E is the midpoint of BD. If O is the midpoint of AE, prove that ar( $\triangle$ BOE) =  $\frac{1}{8}$  ar( $\triangle$ ABC).



#### Answer

Given : D is the midpoint of side BC of  $\triangle$ ABC and E is the midpoint of BD and O is the midpoint of AE

To prove :  $ar(\Delta BOE) = \frac{1}{8}ar(\Delta ABC)$ 

Proof : Consider  $\triangle ABC$  here D is the midpoint of BC

 $\therefore$  Area of ( $\triangle$ ABD) = Area of ( $\triangle$ ACD)

$$\therefore \text{Area}(\Delta \text{ABD}) = \frac{1}{2} \text{Area}(\Delta \text{ABC}) - 1$$

Now, consider  $\triangle ABD$  here E is the midpoint of BD

 $\therefore$  Area of ( $\triangle$ ABE) = Area of ( $\triangle$ AED)

$$\therefore \text{Area}(\Delta \text{ABE}) = \frac{1}{2} \text{Area}(\Delta \text{ABD}) - 2$$

Substituting -1 in -2 , we get

$$\therefore \text{Area}(\Delta \text{ABE}) = \frac{1}{2} \left( \frac{1}{2} \text{ Area}(\Delta \text{ABC}) \right)$$

Area(
$$\Delta ABE$$
) =  $\frac{1}{4}$  Area( $\Delta ABC$ )—3

Now consider  $\triangle ABE$  here O is the midpoint of AE

 $\therefore$  Area of ( $\triangle$ BOE) = Area of ( $\triangle$ AOB)

$$\therefore \text{Area}(\Delta \text{BOE}) = \frac{1}{2} \text{Area}(\Delta \text{ABE}) - 4$$

Now, substitute -3 in -4 , we get

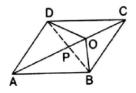
Area(
$$\Delta BOE$$
) =  $\frac{1}{2}(\frac{1}{4} \text{ Area}(\Delta ABC))$   
 $\therefore \text{ area}(\Delta BOE) = \frac{1}{8} \text{ area}(\Delta ABC)$ 

Hence proved

# 20. Question

In the adjoining figure, ABCD is a parallelogram and O is any point on the diagonal AC.

Show that  $ar(\Delta AOB) = ar(\Delta AOD)$ .



### Answer

Given : A parallelogram ABCD in which AC is the diagonal and O is some point on the diagonal AC

To prove: area( $\Delta AOB$ ) = area( $\Delta AOD$ )

Construction : Draw a diagonal BD and mark the intersection as P

Proof:

We know that in a parallelogram diagonals bisect each other, hence P is the midpoint of  $\Delta ABD$ 

: Area of ( $\Delta$ APB) = Area of ( $\Delta$ APD)-1

Now consider  $\triangle$ BOD here OP is the median, since P is the midpoint of BD

: Area of ( $\triangle OPB$ ) = Area of ( $\triangle OPD$ )-2

Adding -1 and -2 we get

Area of ( $\Delta$ APB) + Area of ( $\Delta$ OPB) = Area of ( $\Delta$ APD) + Area of ( $\Delta$ OPD)

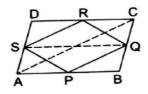
 $\therefore$  Area of ( $\triangle$ AOB) = Area of ( $\triangle$ AOD)

Hence proved

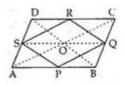
### 21. Question

P.Q.R.S are respectively the midpoints of the sides AB, BC, CD and DA of  $\parallel$  gm ABCD. Show that PQRS is a parallelogram and also show that

Ar( $\|gm PQRS$ ) =  $\frac{1}{2} \times ar(\|gm ABCD)$ .



Answer



Given : ABCD is a parallelogram and P,Q,R,S are the midpoints of AB,BC,CD,AD respectively To prove: (i) PQRS is a parallelogram

(ii) Area( $\|$ gm PQRS) =  $\frac{1}{2}$  x area( $\|$ gm ABCD) Construction : Join AC ,BD,SQ Proof: (i) As S and R are midpoints of AD and CD respectively, in  $\triangle$ ACD SR || AC [By midpoint theorem] ------ (1) Similarly in  $\triangle ABC$ , P and Q are midpoints of AB and BC respectively PQ || AC [By midpoint theorem] ------ (2) From (1) and (2) SR || AC || PQ ∴ SR || PQ ----- (3) Again in  $\triangle$ ACD as S and P are midpoints of AD and CB respectively SP || BD [By midpoint theorem] ------ (4) Similarly in  $\triangle ABC$ , R and Q are midpoints of CD and BC respectively RQ || BD [By midpoint theorem] ------ (5) From (4) and (5) SP || BD || RQ ... SP || RQ ----- (6) From (3) and (6) We can say that opposite sides are Parallel in PQRS Hence we can conclude that PQRS is a parallelogram. (ii) Here ABCD is a parallelogram

S and Q are midpoints of AD and BC respectively

∴ SQ || AB

...SQAB is a parallelogram

Now, area( $\Delta$ SQP) =  $\frac{1}{2}$  x area of (SQAB) ----- 1

[Since  $\Delta$ SQP and ||gm SQAB have same base and lie between same parallel lines] Similarly

S and Q are midpoints of AD and BC respectively

∴ SQ || CD

...SQCD is a parallelogram

Now, area( $\Delta$ SQR) =  $\frac{1}{2}$  x area of (SQCD) ----- 2

[Since  $\Delta$ SQR and ||<sup>gm</sup> SQCD have same base and lie between same parallel lines]

Adding (1) and (2) we get

area(
$$\Delta$$
SQP) + area( $\Delta$ SQR) =  $\frac{1}{2}$  x area of (SQAB) +  $\frac{1}{2}$  x area of (SQCD)

$$\therefore$$
area(PQRS) =  $\frac{1}{2}$  (area of (SQAB) + area of (SQCD))

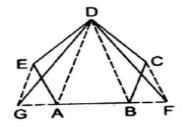
$$\therefore \text{ Area(IIgm PQRS)} = \frac{1}{2} \times \text{ area(IIgm ABCD)}$$

Hence proved

# 22. Question

The given figure shows a pentagon ABCDE, EG, drawn parallel to DA, meets BA produced at G, and CF, drawn parallel to DB, meets AB produced at F.

Show that  $ar(pentagon ABCDE) = ar(\Delta DGF)$ .



### Answer

Given : ABCDE is a pentagon EG is drawn parallel to DA which meets BA produced at G and CF is drawn parallel to DB which meets AB produced at F

To prove: area(pentagon ABCDE) = area( $\Delta$ DGF)

Proof:

Consider quadrilateral ADEG. Here,

 $area(\Delta AED) = area(\Delta ADG) -----(1)$ 

[since two triangles are on same base AD and lie between parallel line i.e, AD||EG]

Similarly now, Consider quadrilateral BDCF. Here,

 $area(\Delta BCD) = area(\Delta BDF)$  -----(2)

[since two triangles are on same base AD and lie between parallel line i.e, AD||EG]

Adding Eq (1) and (2) we get

 $area(\Delta AED) + area(\Delta BCD) = area(\Delta ADG) + area(\Delta BDF)$  ------(3)

Now add area( $\triangle ABD$ ) on both sides of Eq (3), we get

```
\therefore area(\DeltaAED) + area(\DeltaBCD) + area(\DeltaABD) = area(\DeltaADG) + area(\DeltaBDF) + area(\DeltaABD)
```

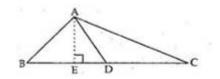
```
\therefore area(pentagon ABCDE) = area(\DeltaDGF)
```

Hence proved

# 23. Question

Prove that a median divides a triangle into two triangles of equal area.

# Answer



Given : A  $\triangle$ ABC with D as median

To prove : Median D divides a triangle into two triangles of equal areas.

Constructions: Drop a perpendicular AE onto BC

Proof: Consider  $\triangle ABD$ 

area(
$$\triangle$$
ABD) =  $\frac{1}{2}$  x BD x AE

Now , Consider  $\triangle$ ACD

area(
$$\Delta$$
ACD) =  $\frac{1}{2}$  x CD x AE

since D is the median

BD = CD

$$\therefore \frac{1}{2} \times BD \times AE = \frac{1}{2} \times CD \times AE$$

Hence , area( $\Delta ABD$ ) = area( $\Delta ACD$ )

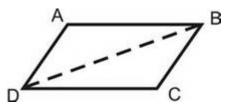
... we can say that Median D divides a triangle into two triangles of equal areas.

Hence proved

# 24. Question

Show that a diagonal divides a parallelogram into two triangles of equal area.

### Answer



Given: A parallelogram ABCD with a diagonal BD

To prove: area( $\Delta$ ABD) = area( $\Delta$ BCD)

Proof:

We know that in a parallelogram opposite sides are equal, that is

AD = BC and AB = CD

Now, consider  $\triangle ABD$  and  $\triangle BCD$ 

Here AD = BC

AB = CD

BD = BD (common)

Hence by SSS congruency

 $\triangle ABD \cong \triangle BCD$ 

By this we can conclude that both the triangles are equal

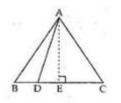
```
\therefore area(\triangleABD) = area(\triangleBCD)
```

Hence proved

# 25. Question

The base BC of  $\triangle$ ABC is divided at D such BD =  $\frac{1}{2}$  DC. Prove that ar( $\triangle$ ABD) =  $\frac{1}{3}$  x ar( $\triangle$ ABC).

# Answer



Given: A  $\triangle$ ABC with a point D on BC such that BD =  $\frac{1}{2}$ DC

To prove: area( $\triangle$ ABD) =  $\frac{1}{3}$  x area( $\triangle$ ABC)

Construction: Drop a perpendicular onto BC

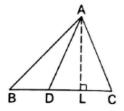
Proof: area( $\triangle ABC$ ) =  $\frac{1}{2} \times BC \times AE$  ------(1) and, area( $\triangle ABD$ ) =  $\frac{1}{2} \times BD \times AE$  -------(2) given that  $BD = \frac{1}{2}DC$  -------(3) so, BC = BD + DC = BD + 2BD = 3BD [from 2]  $\therefore BD = \frac{1}{3}(BC)$ Sub BD in (1), we get area( $\triangle ABD$ ) =  $\frac{1}{2} \times (\frac{1}{3}(BC) \times AE)$ area( $\triangle ABD$ ) =  $\frac{1}{3} \times (\frac{1}{2}BC \times AE)$  $\therefore area(\triangle ABD) = \frac{1}{3} \times (\frac{1}{2}BC \times AE)$  $\therefore area(\triangle ABD) = \frac{1}{3} \times area(\triangle ABC)$  [from 1]

Hence proved

### 26. Question

In the adjoining figure, the points D divides the

Side BC of  $\triangle$ ABC in the ratio m:n. prove that area( $\triangle$ ABD): area( $\triangle$ ABC) = m:n



Given : A  $\triangle$ ABC in which a point D divides the Side BC in the ratio m:n.

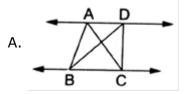
To prove: area( $\Delta ABD$ ): area( $\Delta ABC$ ) = m:n Construction : Drop a perpendicular AL on BC Proof: area( $\triangle ABD$ ) =  $\frac{1}{2}$  x BD x AL ----- (1) and, area( $\Delta$ ADC) =  $\frac{1}{2}$  x DC x AL ------ (2) BD:DC = m:n $\frac{BD}{DC} = \frac{m}{n}$  $\therefore BD = \frac{m}{n} \times DC - (3)$ sub Eq (3) in eq (1)area( $\Delta ABD$ ) =  $\frac{1}{2} \times (\frac{m}{n} \times DC) \times AL$ area( $\triangle ABD$ ) =  $\frac{m}{n} \times (\frac{1}{2} \times DC \times AL)$ area( $\triangle ABD$ ) =  $\frac{m}{n} \times area(\triangle ADC)$  $\therefore \frac{\text{area}(\Delta ABD)}{\text{area}(\Delta ADC)} = \frac{m}{n}$ : Area( $\Delta$ ABD): Area( $\Delta$ ABC) = m:n

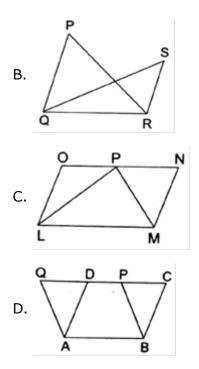
Hence proved

# **CCE** Questions

### 1. Question

Out of the following given figures which are on the same base but not between the same parallels?



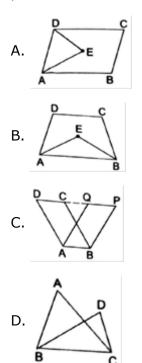


Here,  $\Delta$ PQR and  $\Delta$ SQR are on the same base QR but there is no parallel line to QR.

 $\therefore$  Here, Figure in option B is on the same base but not between the same parallels.

### 2. Question

In which of the following figures, you find polynomials on the same base and between the same parallels?



#### Answer

Here parallelogram ABCD and parallelogram ABQP lie on the same base AB and lie between the parallel line AB and DP.

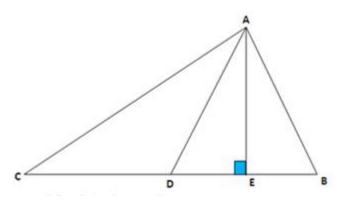
 $\therefore$  Here, Figure in option C is on the same base and between the same parallels.

# 3. Question

The median of a triangle divides it into two

- A. Triangles of equal area
- B. Congruent triangles
- C. Isosceles triangles
- D. Right triangles

# Answer



In  $\Delta ABC, \, AD$  is the median

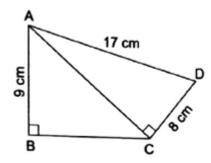
Hence BD = DCDraw AE  $\perp$  BC

Area of  $\triangle ABD = Area of \triangle ADC$ 

Thus median of a triangle divides it into two triangles of equal area.

# 4. Question

The area of quadrilateral ABCD in the given figure is



- A. 57cm<sup>2</sup>
- B. 108cm<sup>2</sup>
- C. 114cm<sup>2</sup>
- D. 195cm<sup>2</sup>

# Answer

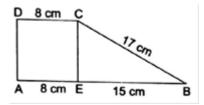
Given:

 $\angle ABC = 90^{\circ}$  $\angle ACD = 90^{\circ}$ CD = 8cmAB = 9cmAD = 17cmConsider ∆ACD Here, By Pythagoras theorem :  $AD^2 = CD^2 + AC^2$  $17^2 = 8^2 + AC^2$  $\Rightarrow AC^2 = 17^2 - 8^2$  $\Rightarrow AC^2 = 289 - 64 = 225$  $\Rightarrow AC = 15$ Now, Consider ΔABC Here, By Pythagoras theorem :  $AC^2 = AB^2 + BC^2$  $15^2 = 9^2 + AC^2$  $\Rightarrow BC^2 = 15^2 - 9^2$  $\Rightarrow BC^2 = 225 - 81 = 144$  $\Rightarrow$  BC = 12 Here, Area (quad.ABCD) = Area ( $\Delta$ ABC) + Area ( $\Delta$ ACD) Area (quad.ABCD) =  $1/2 \times AB \times BC + 1/2 \times AC \times CD$ Area (quad.ABCD) =  $1/2 \times 9 \times 12 + 1/2 \times 15 \times 8 = 54 + 60 = 104$  cm<sup>2</sup>

# $\therefore$ Area (quad.ABCD) = 114cm<sup>2</sup>

# 5. Question

The area of trapezium ABCD in the given figure is





B. 93cm<sup>2</sup>

C. 124cm<sup>2</sup>

D. 155cm<sup>2</sup>

#### Answer

Given:

∠BEC = 90°

∠DAE = 90°

CD = AE = 8cm

BE = 15cm

BC = 17cm

Consider ∆CEB

Here, By Pythagoras theorem

 $BC^2 = CE^2 + EB^2$ 

 $17^2 = CE^2 + 15^2$ 

 $CE^2 = 17^2 - 15^2$ 

 $CE^2 = 289 - 225 = 64$ 

CE = 8

Here,

∠AEC = 90°

CD = CE = 8cm

 $\therefore$  AECD is a Square.

 $\therefore$  Area (Trap. ABCD) = Area (Sq. AECD) + Area ( $\Delta$ CEB)

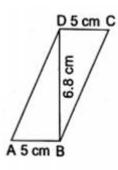
Area (Trap. ABCD) =  $AE \times EC + 1/2 \times CE \times EB$ 

Area (Trap. ABCD) =  $8 \times 8 + 1/2 \times 8 \times 15 = 64 + 60 = 104 \text{cm}^2$ 

 $\therefore$  Area (Trap. ABCD) = 124cm<sup>2</sup>

## 6. Question

In the given figure, ABCD is a lgm in which AB = CD = 5cm and  $BD\perp DC$  such that BD = 6.8cm. Then, the area of lgm ABCD = ?



A. 17cm<sup>2</sup>

B. 25cm<sup>2</sup>

C. 34cm<sup>2</sup>

D. 68cm<sup>2</sup>

# Answer

Given:

AB = CD = 5cm

BD⊥DC

BD = 6.8cm

Now, consider the parallelogram ABCD

Here, let DC be the base of the parallelogram then BD becomes its altitude (height).

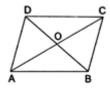
Area of the parallelogram is given by: Base  $\times$  Height

 $\therefore$  area of  $\|$ gm ABCD = CD×BD = 5×6.8 = 34cm<sup>2</sup>

 $\therefore$ area of  $\|$ gm ABCD = 34cm<sup>2</sup>.

# 7. Question

In the given figure, ABCD is a lgm in which diagonals AC and BD intersect at O. If ar(lgm ABCD) is  $52cm^2$ , then the ar( $\Delta OAB$ ) = ?



A. 26cm<sup>2</sup>

B. 18.5cm<sup>2</sup>

C. 39cm<sup>2</sup>

D. 13cm<sup>2</sup>

Given: ABCD is a lgm in which diagonals AC and BD intersect at O and ar(lgm ABCD) is 52cm<sup>2</sup>.

Here,

Ar ( $\triangle ABD$ ) = ar( $\triangle ABC$ )

(:  $\Delta ABD$  and  $\Delta ABC$  on same base AB and between same parallel lines AB and CD)

Here,

 $ar(\Delta ABD) = ar(\Delta ABC) = 1/2 \times ar(||gm ABCD)$ 

(:  $\Delta ABD$  and  $\Delta ABC$  on same base AB and between same parallel lines AB and CD are half the area of the parallelogram)

 $\therefore$  ar( $\triangle$ ABD) = ar( $\triangle$ ABC) = 1/2 × 52 = 26cm<sup>2</sup>

Now, consider  $\triangle ABC$ 

Here OB is the median of AC

(: diagonals bisect each other in parallelogram)

 $\therefore$  ar( $\triangle$ AOB) = ar( $\triangle$ BOC)

(:median of a triangle divides it into two triangles of equal area)

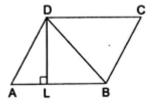
 $ar(\Delta AOB) = 1/2 \times ar(\Delta ABC)$ 

 $ar(\Delta AOB) = 1/2 \times 26 = 13 cm^2$ 

 $\therefore ar(\Delta AOB) = 13 cm^2$ 

### 8. Question

In the given figure, ABCD is a  $\|gm \|$  in which  $DL \perp AB$ . If AB = 10cm and DL = 4cm, then the ar( $\|gm ABCD$ ) = ?



- A. 40cm<sup>2</sup>
- B. 80cm<sup>2</sup>

C. 20cm<sup>2</sup>

D. 196cm<sup>2</sup>

### Answer

Area of parallelogram is: base × height

Here,

Base = AB = 10cm

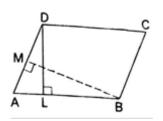
Height = DL = 4cm

 $\therefore$  ar(lgm ABCD) = AB  $\times$ DL = 10 $\times$ 4 = 40cm<sup>2</sup>

 $\therefore$  ar(Igm ABCD) = 40cm<sup>2</sup>

### 9. Question

In  $\|$ gm ABCD, it is given that AB = 10cm, DL  $\perp$  AB and BM  $\perp$  AD such that DL = 6cm and BM = 8cm. Then, AD = ?



- A. 7.5cm
- B. 8cm
- C. 12cm
- D. 14cm

#### Answer

Given:

AB = 10cm

 $\mathsf{DL}\perp\mathsf{AB}$ 

 $\mathsf{BM}\perp\mathsf{AD}$ 

DL = 6cm

BM = 8cm

Now, consider the parallelogram ABCD

Here, let AB be the base of the parallelogram then DL becomes its altitude (height).

Area of the parallelogram is given by: Base × Height

 $\therefore$  area of lgm ABCD = AB×DL = 10×6 = 60cm<sup>2</sup>

#### Now,

Consider AD as base of the parallelogram then BM becomes its altitude (height)

 $\therefore$  area of  $\|$ gm ABCD = AD  $\times$  BM = 60cm<sup>2</sup>

 $AD \times 8 = 60 \text{cm}^2$ 

AD = 60/8 = 7.5 cm

 $\therefore$ length of AD = 7.5cm.

# **10.** Question

The lengths of the diagonals of a rhombus are 12cm and 16cm. The area of the rhombus is

A. 192cm<sup>2</sup>

B. 96cm<sup>2</sup>

C. 64cm<sup>2</sup>

D. 80cm<sup>2</sup>

# Answer

Given:

Length of diagonals of rhombus: 12cm and 16cm.

Area of the rhombus is given by:  $\frac{\text{product of diagonals}}{2}$ 

 $\therefore$  Area of the rhombus =  $\frac{12 \times 16}{2}$  = 96cm<sup>2</sup>

# 11. Question

Two parallel sides of a trapezium are 12cm and 8cm long and the distance between them

6.5cm. The area of the trapezium is

A. 74cm<sup>2</sup>

B. 32.5cm<sup>2</sup>

C. 65cm<sup>2</sup>

D. 130cm<sup>2</sup>

# Answer

Given:

Lengths of parallel sides of trapezium: 12cm and 8cm

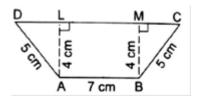
Distance between two parallel lines (height): 6.5cm

Area of the trapezium is given by:  $\frac{(\text{sum of parallel sides}) \times \text{height}}{2}$ 

 $\therefore \text{ Area of the trapezium} = \frac{(12 + 8) \times 6.5}{2} = 65 \text{ cm}^2$ 

# 12. Question

In the given figure ABCD is a trapezium such that  $AL \perp DC$  and  $BM \perp DC$ . If AB = 7cm, BC = AD = 5cm and AL = BM = 4cm, then ar(trap. ABCD) = ?



A. 24cm<sup>2</sup>

B. 40cm<sup>2</sup>

C. 55cm<sup>2</sup>

D. 27.5cm<sup>2</sup>

#### Answer

Given:

 $\mathsf{AL}\perp\mathsf{DC}$ 

 $\mathsf{BM}\perp\mathsf{DC}$ 

AB = 7cm

BC = AD = 5cm

AL = BM = 4cm

Here,

MC = DL and AB = LM = 7 cm

Consider the  $\Delta BMC$ 

Here, by Pythagoras theorem

 $BC^2 = BM^2 + MC^2$ 

 $5^2 = 4^2 + MC^2$ 

 $MC^2 = 25 - 16$ 

 $MC^{2} = 9$ 

MC = 3cm

 $\therefore$  MC = DL = 3cm

CD = DL + LM + MC = 3 + 7 + 3 = 13cm

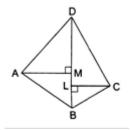
Now,

Area of the trapezium is given by: (sum of parallel sides)×height

 $\therefore$  Area of the rhombus =  $\frac{(13 + 7) \times 4}{2} = 40 \text{ cm}^2$ 

## 13. Question

In a quadrilateral ABCD, it is given that BD = 16cm. If  $AL \perp BD$  and  $CM \perp BD$  such that AL = 9cm and CM = 7cm, then ar(quad.ABCD) = ?



A. 256cm<sup>2</sup>

B. 128cm<sup>2</sup>

C. 64cm<sup>2</sup>

D. 96cm<sup>2</sup>

### Answer

Given:

BD = 16cm

 $AL \perp BD$ 

 $\mathsf{CM}\perp\mathsf{BD}$ 

AL = 9cm

CM = 7cm

Here,

Area of quadrilateral ABCD = area( $\Delta$ ABD) + area( $\Delta$ BCD)

Area of triangle =  $1/2 \times base \times height$ 

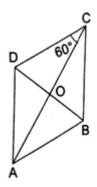
area( $\Delta ABD$ ) = 1/2 × base × height = 1/2 × BD × CM = 1/2 × 16 × 7 = 56cm<sup>2</sup>

area( $\Delta$ BCD) = 1/2 × base × height = 1/2 × BD × AL = 1/2 × 16 × 9 = 64cm<sup>2</sup>

 $\therefore$  Area of quadrilateral ABCD = area( $\triangle$ ABD) + area( $\triangle$ BCD) = 56 + 64 = 120cm<sup>2</sup>

## 14. Question

ABCD is a rhombus in which  $\angle C = 60^{\circ}$ . Then, AC : BD = ?



- A. 3:1
- B. 3:2
- C. 3:1
- D. 3:2

Given:∠DCB = 60°

Let the length of the side be x

Here, consider  $\triangle BCD$ 

BC = DC (all sides of rhombus are equal)

 $\therefore \angle CDB = \angle CBD$  (angles opposite to equal sides are equal)

Now, by angle sum property

 $\angle CDB + \angle CBD + \angle BCD = 180^{\circ}$ 

2× ∠CBD = 180° -60°

 $2 \times \angle CBD = 180^{\circ} - 60^{\circ}$ 

 $\therefore 2 \times \angle CBD = 120^{\circ}$ 

$$\angle \text{ CBD} = \frac{120}{2} = 60^{\circ}$$

- $\therefore \angle CDB = \angle CBD = 60^{\circ}$
- $\mathrel{\scriptstyle \mathrel{.\, }} \Delta$  ADC is equilateral triangle
- $\therefore$  BC = CD = BD = x cm

In Rhombus diagonals bisect each other.

Consider  $\Delta$  COD

By Pythagoras theorem

 $CD^2 = OD^2 + OC^2$  $x^2 = \begin{bmatrix} x \\ -2 \end{bmatrix}^2 + OC^2$ 

$$x^2 = \left[\frac{x}{2}\right]^2 + OC^2$$

$$OC^{2} = x^{2} - \left[\frac{x}{2}\right]^{2}$$

$$OC = \left[\frac{\sqrt{4x^{2} - x^{2}}}{2}\right]$$

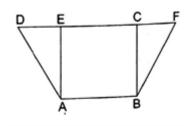
$$OC = \frac{\sqrt{3} \times x}{2} \text{ cm}$$

$$\therefore AC = 2 \times OC = 2 \times \frac{\sqrt{3} \times x}{2} = \sqrt{3} \times AC: BD = \sqrt{3} \times 1 \times 1$$

$$\therefore AC: BD = \sqrt{3} \times 1 \times 1$$

#### 15. Question

In the given figure ABCD and ABFE are parallelograms such that ar(quad. EABC) =  $17 \text{cm}^2$  and ar(Igm ABCD) =  $25 \text{cm}^2$ . Than, ar( $\Delta$ BCF) = ?



A. 4cm<sup>2</sup>

B.4.8cm<sup>2</sup>

C. 6cm<sup>2</sup>

D. 8cm<sup>2</sup>

#### Answer

Given:  $ar(quad. EABC) = 17 cm^2$  and  $ar(\|gm ABCD) = 25 cm^2$ 

We know that any two or parallelogram having the same base and lying between the same parallel lines are equal in area.

 $\therefore$  Area (Igm ABCD) = Area (||gm ABFE) = 25cm<sup>2</sup>

Here,

Area (||gm ABFE) = Area (quad. EABC) + Area ( $\Delta$ BCF)

 $25 \text{cm}^2 = 17 \text{cm}^2 + \text{Area} (\Delta \text{BCF})$ 

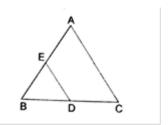
Area ( $\Delta$ BCF) = 25 - 17 = 8cm<sup>2</sup>

 $\therefore$  Area ( $\Delta$ BCF) = 8cm<sup>2</sup>

## 16. Question

 $\Delta$ ABC and  $\Delta$ BDE are two equilateral triangles such that D is the midpoint of BC. Then,

ar( $\Delta$ BDE): ar( $\Delta$ ABC) = ?



- A. 1:2
- B. 1:4

C. 3:2

D. 3:4

## Answer

Given:  $\triangle ABC$  and  $\triangle BDE$  are two equilateral triangles, D is the midpoint of BC.

Consider **ABC** 

Here, let AB = BC = AC = x cm (equilateral triangle)

Now, consider  $\triangle BED$ 

Here,

BD = 1/2 BC

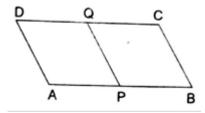
 $\therefore$  BD = ED = EB = 1/2 BC = x/2 (equilateral triangle)

Area of the equilateral triangle is given by:  $\frac{\sqrt{3}}{4}a^2$  (a is side length)

: ar( $\Delta$ BDE): ar( $\Delta$ ABC) =  $\frac{\sqrt{3}}{4} \times (\frac{x}{2})^2$ :  $\frac{\sqrt{3}}{4}x^2 = \frac{1}{4}$ : 1 = 1:4

## 17. Question

In a lgm ABCD, if Point P and Q are midpoints of AB and CD respectively and ar(lgm ABCD) =  $16cm^2$ , then ar(lgmAPQD) = ?



A. 8cm<sup>2</sup>

B. 12cm<sup>2</sup>

C. 6cm<sup>2</sup>

D. 9cm<sup>2</sup>

## Answer

Given:

P and Q are midpoints of AB and CD respectively

ar(Igm ABCD) = 16cm<sup>2</sup>

Now, consider the (Igm ABCD)

Here,

Q is the midpoint of DC and P is the midpoint of AB.

 $\therefore$  By joining P and Q (Igm ABCD) is divided into two equal parallelograms.

That is, ar(Igm ABCD) = ar(IgmAPQD) + ar(IgmPQCB)

ar(Igm ABCD) = 2×ar(IgmAPQD) (:ar(IgmAPQD) = ar(IgmPQCB))

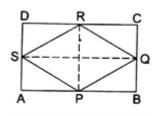
 $2 \times ar(\|gmAPQD) = 16cm^2$  ( $::ar(\|gmABCD) = 16cm^2$ )

 $ar(IIgmAPQD) = 16/2 = 8cm^2$ 

 $\therefore$  ar( $\|gmAPQD$ ) =  $8cm^2$ 

## 18. Question

The figure formed by joining the midpoints of the adjacent sides of a rectangle of sides 8cm and 6cm is a



A. Rectangle of area 24cm<sup>2</sup>

- B. Square of area 24cm<sup>2</sup>
- C. Trapezium of area 24cm<sup>2</sup>
- D. Rhombus of area 24cm<sup>2</sup>

## Answer

Given: A rectangle with sides 8cm and 6cm.

Consider the Rectangle ABCD

Here DR = RD = AP = PB = 8/2 = 4cm (: P and R are the midpoints of DC and AB respectively)

and AS = SD = BQ = QC = 6/2 = 3cm(:: S and Q are the midpoints of AD and BC respectively)Now, consider the  $\Delta RSD$ By Pythagoras theorem  $SR^2 = SD^2 + DR^2$   $SR^2 = 3^2 + 4^2$   $SR^2 = 9 + 16$   $SR^2 = 25$  SR = 5 cmSimilarly using Pythagoras theorem in  $\Delta QRC$ ,  $\Delta PBQ$  and  $\Delta APS$ We get RQ = QP = PS = 5cm:: SR = RQ = QP = PS = 5cm

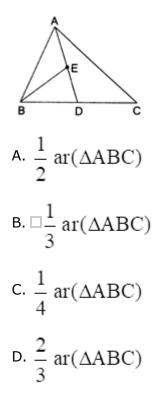
 $\therefore$  PQSR is Rhombus of side length 5cm

Area of the rhombus is given by:  $\frac{\text{product of diagonals}}{2}$ 

- : Area of the rhombus =  $\frac{PR \times SQ}{2} = \frac{8 \times 6}{2} = 24 \text{ cm}^2$
- $\therefore$  Area(PQRS) = 24cm<sup>2</sup>

## **19. Question**

In  $\triangle ABC$ , if D is the midpoint of BC and E is the midpoint of AD, then ar( $\triangle BED$ ) = ?



#### Answer

Given: D is the midpoint of BC and E is the midpoint of AD

Here,

D is the midpoint of BC and AD is the median of  $\Delta ABC$ 

Area ( $\Delta$  ABD) = Area ( $\Delta$  ADC) (: median divides the triangle into two triangles of equal areas)

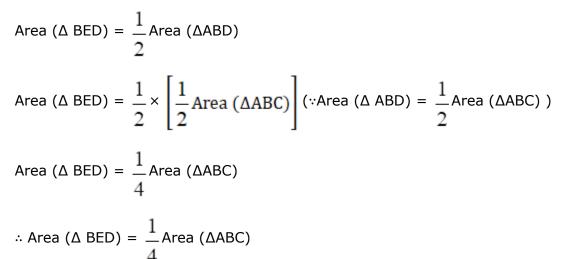
: Area (
$$\triangle$$
 ABD) = Area ( $\triangle$  ADC) =  $\frac{1}{2}$  Area ( $\triangle$ ABC)

Now, consider  $\Delta$  ABD

Here, BE is the median

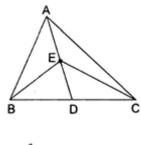
Area ( $\Delta$  ABE) = Area ( $\Delta$  BED)

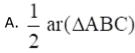
.: Area (Δ ABE) = Area (Δ BED) = 
$$\frac{1}{2}$$
 Area (ΔABD)



## 20. Question

The vertex A of  $\triangle ABC$  is joined to a point D on BC. If E is the midpoint of AD, then  $ar(\triangle BEC) = ?$ 





B. 
$$\frac{1}{3} \operatorname{ar}(\Delta ABC)$$
  
C.  $\frac{1}{4} \operatorname{ar}(\Delta ABC)$   
D.  $\frac{1}{6} \operatorname{ar}(\Delta ABC)$ 

#### Answer

Given:

Here,

D is the midpoint of BC and AD is the median of  $\Delta ABC$ 

Area ( $\Delta$  ABD) = Area ( $\Delta$  ADC) (: median divides the triangle into two triangles of equal areas)

∴ Area (Δ ABD) = Area (Δ ADC) = 
$$\frac{1}{2}$$
 Area (ΔABC)

Now, consider  $\Delta$  ABD

Here, BE is the median

Area ( $\triangle$  ABE) = Area ( $\triangle$  BED)

∴ Area (Δ ABE) = Area (Δ BED) = 
$$\frac{1}{2}$$
 Area (ΔABD)

Area (
$$\Delta$$
 BED) =  $\frac{1}{2}$  Area ( $\Delta$ ABD)  
Area ( $\Delta$  BED) =  $\frac{1}{2} \times \left[\frac{1}{2}$  Area ( $\Delta$ ABC)\right] (::Area ( $\Delta$  ABD) =  $\frac{1}{2}$  Area ( $\Delta$ ABC) ) -1

Area (
$$\Delta$$
 BED) =  $\frac{1}{4}$  Area ( $\Delta$ ABC)

Similarly,

Area (
$$\Delta$$
 EDC) =  $\frac{1}{4}$  Area ( $\Delta$ ABC) -2

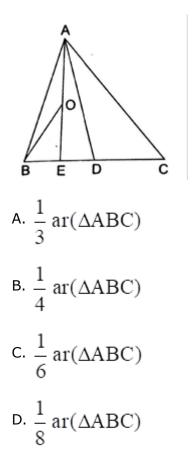
Add -1 and -2

Area ( $\Delta$  BED) + Area ( $\Delta$  EDC) =  $\frac{1}{4}$ Area ( $\Delta$ ABC) +  $\frac{1}{4}$ Area ( $\Delta$ ABC) =  $\frac{1}{2}$ Area ( $\Delta$ ABC)

 $\therefore$  Area (Δ BEC) =  $\frac{1}{2}$  Area (ΔABC)

#### 21. Question

In  $\triangle$ ABC, it given that D is the midpoint of BC; E is the midpoint of BD and O is the midpoint of AE. Then ar( $\triangle$ BOE) = ?



#### Answer

Given: D is the midpoint of BC; E is the midpoint of BD and O is the midpoint of AE.

Here,

D is the midpoint of BC and AD is the median of  $\Delta ABC$ 

Area ( $\Delta$  ABD) = Area ( $\Delta$  ADC) (: median divides the triangle into two triangles of equal areas)

: Area (Δ ABD) = Area (Δ ADC) = 
$$\frac{1}{2}$$
 Area (ΔABC)

Now, consider  $\Delta$  ABD

Here, AE is the median

Area ( $\Delta$  ABE) = Area ( $\Delta$  BED)

$$\therefore \operatorname{Area} (\Delta \operatorname{ABE}) = \operatorname{Area} (\Delta \operatorname{BED}) = \frac{1}{2} \operatorname{Area} (\Delta \operatorname{ABD})$$

$$\operatorname{Area} (\Delta \operatorname{ABE}) = \frac{1}{2} \operatorname{Area} (\Delta \operatorname{ABD})$$

$$\operatorname{Area} (\Delta \operatorname{ABE}) = \frac{1}{2} \times \left[ \frac{1}{2} \operatorname{Area} (\Delta \operatorname{ABC}) \right] (\because \operatorname{Area} (\Delta \operatorname{ABD}) = \frac{1}{2} \operatorname{Area} (\Delta \operatorname{ABC}) ) -1$$

$$\operatorname{Area} (\Delta \operatorname{ABE}) = \frac{1}{4} \operatorname{Area} (\Delta \operatorname{ABC})$$

$$\operatorname{Consider} \Delta \operatorname{ABE}$$

$$\operatorname{Here, BO is the median}$$

$$\operatorname{Area} (\Delta \operatorname{BOE}) = \operatorname{Area} (\Delta \operatorname{BOA})$$

$$\therefore \operatorname{Area} (\Delta \operatorname{BOE}) = \operatorname{Area} (\Delta \operatorname{BOA}) = \frac{1}{2} \operatorname{Area} (\Delta \operatorname{ABE})$$

Area (
$$\Delta$$
 BOE) =  $\frac{1}{2} \times \left[\frac{1}{4} \operatorname{Area} (\Delta ABC)\right]$  ("Area ( $\Delta$  ABE) =  $\frac{1}{4}$  Area ( $\Delta$  ABC) )  
Area ( $\Delta$  BOE) =  $\frac{1}{8}$  Area ( $\Delta$  ABC)  
... Area ( $\Delta$  BOE) =  $\frac{1}{8}$  Area ( $\Delta$  ABC)

#### 22. Question

If a triangle and a parallelogram are on the same base and between the same parallels, then the ratio of the area of the triangle to the parallelogram is

A. 1:2

- B. 1:3
- C. 1:4
- D. 3:4

#### Answer

Given:

We know that when a parallelogram and a triangle lie on same base and between same parallel lines then, area of the triangle is half the area of the parallelogram.

Area ( $\Delta ABF$ ) = 1/2 Area(||gm ABCD) -1

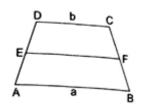
Area ( $\Delta ABF$ ) : Area (||gm ABCD) = 1/2 Area(||gm ABCD) : Area(||gm ABCD) (from -1)

Area ( $\Delta ABF$ ) : Area (||gm ABCD) = 1/2 : 1 = 1:2

 $\therefore$  Area ( $\triangle$ ABF) : Area (||gm ABCD) = 1:2

## 23. Question

In the given figure ABCD is a trapezium in which  $AB\|DC$  such that AB = a cm and DC = b cm. If E and F are the midpoints of AD and BC respectively. Then, ar (ABFE) : ar(EFCD) = ?



#### A. A:b

- B. (a + 3b):(3a + b)
- C. (3a + b):(a + 3b)
- D. (2a + b):(3a + b)

## Answer

Given: ABCD is a trapezium, ABIDC, AB = a cm and DC = b cm, E and F are the midpoints of AD and BC.

Since E and F are midpoints of AD and BC, EF will be parallel to both AB and CD.

 $EF = \frac{a+b}{2}$ 

Height between EF and DC and height between EF and AB are equal, because E and F are midpoints OF AD and BC and EF||AB||DC.

Let height between EF and DC and height between EF and AB be h cm.

Area of trapezium =  $1/2 \times (\text{sum of parallel lines}) \times \text{height}$ 

Now,

Area (Trap.ABFE) = 
$$1/2 \times (a + \frac{a+b}{2}) \times h$$
.

and

Area (Trap.ABFE) = 
$$1/2 \times (b + \frac{a+b}{2}) \times h$$
.

Area (Trap.ABFE) : Area (Trap.ABFE) =  $1/2 \times (a + \frac{a+b}{2}) \times h : 1/2 \times (b + \frac{a+b}{2}) \times h$ 

Area (Trap.ABFE) : Area (Trap.ABFE) =  $\frac{2a+a+b}{2}$  :  $\frac{2b+a+b}{2}$  = 3a + b : a + 3b

∴ Area (Trap.ABFE) : Area (Trap.ABFE) = 3a + b : a + 3b

## 24. Question

ABCD is a quadrilateral whose diagonal AC divides it into two parts, equal in area, then ABCD is

A. a rectangle

- B. allgm
- C. a rhombus
- D. all of these

## Answer

Given: a quadrilateral whose diagonal AC divides it into two parts, equal in area.

Here,

A quadrilateral is any shape having four sides, it is given that diagonal AC of the quadrilateral

divides it into two equal parts.

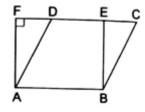
We know that the rectangle, parallelogram and rhombus are all quadrilaterals, in these

quadrilaterals if a diagonal is drawn say AC it divides it into equal areas.

 $\cdot$  This diagonal divide the quadrilateral into two equal or congruent triangles.

## 25. Question

In the given figure, a Igm ABCD and a rectangle ABEF are of equal area. Then,



A. Perimeter of ABCD = perimeter of ABEF

B. Perimeter of ABCD < perimeter of ABEF

C. Perimeter of ABCD > perimeter of ABEF

D. Perimeter of ABCD =  $\frac{1}{2}$  (perimeter of ABEF)

## Answer

Given: Area (Igm ABCD) = Area (rectangle ABEF)

Consider ∆AFD

Clearly AD is the hypotenuse

 $\therefore AD > AF$ 

Perimeter of Rectangle ABEF =  $2 \times (AB + AF) - 1$ 

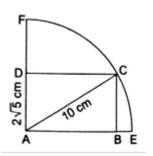
Perimeter of Parallelogram ABCD =  $2 \times (AB + AD) - 2$ 

On comparing -1 and -2, we can see that

Perimeter of ABCD > perimeter of ABEF (::AD > AF)

## 26. Question

In the given figure, ABCD is a rectangle inscribed in a quadrant of a circle of radius 10cm. If AD = 25cm, then area of the rectangle is



- A. 32cm<sup>2</sup>
- B. 40cm<sup>2</sup>
- C. 44cm<sup>2</sup>
- D. 48cm<sup>2</sup>

## Answer

Given: ABCD is a rectangle inscribed in a quadrant of a circle of radius 10cm and AD = 25cm

Consider  $\Delta$  ADC

By Pythagoras theorem

 $AC^2 = AD^2 + DC^2$ 

 $10^2 = (25)^2 + AC^2$ 

 $AC^2 = 10^2 - (25)^2$ 

 $AC^2 = 100 - 20 = 80$ 

Area of rectangle = length  $\times$  breadth = DC  $\times$  AD

Area of rectangle =  $45 \times 25 = 40 \text{ cm}^2$ 

 $\therefore$  Area of rectangle = 40cm<sup>2</sup>

## 27. Question

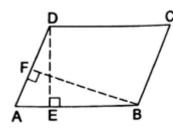
Look at the statements given below:

(I) A parallelogram and a rectangle on the same base and between the same parallels are equal in area.

(II) In a  $\|$ gm ABCD, it is given that AB = 10cm. The altitudes DE on AB and BF on AD being 6cm and 8cm respectively, then AD = 7.5 cm.

(III) Area of a  $\|gm = \frac{1}{2}x$  base x altitude.

Which is true?



A. I only

B. II only

C. I and II

D. II and III

#### Answer

Consider Statement (I) :

Two or more parallelograms on the same base and between the same parallels are equal in area. Rectangle is also a parallelogram.

 $\therefore$  It is true.

Consider Statement (II) :

Here, let AB be the base of the parallelogram then DE becomes its altitude (height).

Area of the parallelogram is given by: Base × Height

 $\therefore$  Area of  $\|$ gm ABCD = AB $\times$ DE = 10 $\times$ 6 = 60cm<sup>2</sup>

Now,

Consider AD as base of the parallelogram then BF becomes its altitude (height)

 $\therefore$  area of lgm ABCD = AD  $\times$  BF = 60cm<sup>2</sup>

 $AD \times 8 = 60 \text{cm}^2$ 

$$AD = \frac{60}{8} = 7.5 cm$$

 $\therefore$ length of AD = 7.5cm.

∴ Statement (II) is correct.

Consider Statement (III)

Area of parallelogram is base× height

- : Statement (III) is false
- $\therefore$  Statement (I) and (II) are true and statement (III) is false

## 28. Question

The question consists of two statements, namely, Assertion (A) and Reason (R). Choose the correct answer.

Assertion (A)	Reason (R)
In a trapezium ABCD we have AB    DC and the diagonals AC and BD intersect at O.	Triangles on the same base and between the same parallels are equal in areas.
Then, $ar(\Delta AOD) = ar(\Delta BOC)$	
A B	

A. Both Assertion (A) and Reason (R) are true and Reason (R) is a correct explanation of Assertion (A).

B. Both Assertion (A) but Reason (R) are true and Reason (R) is not a correct explanation of Assertion (A).

C. Assertion (A) is true and Reason (R) is false.

D. Assertion (A) is false and Reason (R) is true.

## Answer

Assertion:

Here, Area ( $\Delta ABD$ ) = Area( $\Delta ABC$ ) (: Triangles on same base and between same parallel lines) -1

Subtract Area ( $\Delta$  AOB) on both sides of -1

Area ( $\Delta ABD$ ) – Area ( $\Delta AOB$ ) = Area ( $\Delta ABC$ ) – Area ( $\Delta AOB$ )

Area ( $\triangle AOD$ ) = Area ( $\triangle BOC$ )

 $\therefore$  Both Assertion and Reason are true and Reason is a correct explanation of Assertion.

## 29. Question

The question consists of two statements, namely, Assertion (A) and Reason (R). Choose the correct answer.

Assertion (A)	Reason (R)
If ABCD is a rhombus whose one angle is 60°, then the ratio of the lengths of its diagonals is 3:1.	Median of a triangle divides it into two triangles of equal area.

A. Both Assertion (A) and Reason (R) are true and Reason (R) is a correct explanation of Assertion (A).

B. Both Assertion (A) but Reason (R) are true and Reason (R) is not a correct explanation of Assertion (A).

C. Assertion (A) is true and Reason (R) is false.

D. Assertion (A) is false and Reason (R) is true.

## Answer

Given: ∠DCB = 60°

Let the length of the side be x

Here, consider  $\triangle BCD$ 

BC = DC (all sides of rhombus are equal)

 $\therefore \angle CDB = \angle CBD$  (angles opposite to equal sides are equal)

Now, by angle sum property

 $\angle CDB + \angle CBD + \angle BCD = 180^{\circ}$ 

 $2 \times \angle CBD = 180^{\circ} - 60^{\circ}$ 

 $2 \times \angle CBD = 180^{\circ} - 60^{\circ}$ 

 $\therefore 2 \times \angle CBD = 120^{\circ}$ 

$$\angle \text{CBD} = \frac{120}{2} = 60^{\circ}$$

 $\therefore \angle CDB = \angle CBD = 60^{\circ}$ 

 $\therefore$   $\Delta$  ADC is equilateral triangle

 $\therefore$  BC = CD = BD = x cm

In Rhombus diagonals bisect each other.

Consider  $\Delta$  COD

By Pythagoras theorem

$CD^2 = OD^2 + OC^2$
$x^2 = \left[\frac{x}{2}\right]^2 + OC^2$
$OC^2 = x^2 - \left[\frac{x}{2}\right]^2$
$OC = \left[\frac{\sqrt{4x^2 - x^2}}{2}\right]$
$OC = \frac{\sqrt{3} \times x}{2} cm$
$\therefore AC = 2 \times OC = 2 \times \frac{\sqrt{3} \times x}{2} = \sqrt{3} \times x$
AC: BD = $\sqrt{3}x : x = \sqrt{3} : 1$
$\therefore$ AC: BD = $\sqrt{3}$ : 1

 $\therefore$  Both Assertion but Reason are true and Reason is not a correct explanation of Assertion.

## **30.** Question

The question consists of two statements, namely, Assertion (A) and Reason (R). Choose the correct answer.

Assertion (A)	Reason (R)
The diagonals of a∥gm	A diagonal of a ∥ gm divides
divide it into four	it into two triangles of equal
triangles of equal area.	area.

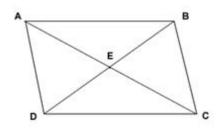
A. Both Assertion (A) and Reason (R) are true and Reason (R) is a correct explanation of Assertion (A).

B. Both Assertion (A) but Reason (R) are true and Reason (R) is not a correct explanation of Assertion (A).

C. Assertion (A) is true and Reason (R) is false.

D. Assertion (A) is false and Reason (R) is true.

# Answer



Consider  $\Delta$  ABD

We know that diagonals in a parallelogram bisect each other

 $\therefore$  E is the midpoint of BD, AE is median of  $\Delta$  ABD

: Area ( $\Delta$  ADE) = Area ( $\Delta$  AEB) (: Median divides the triangle into two triangles of equal areas)

Similarly we can prove

Area ( $\Delta$  ADE) = Area ( $\Delta$  DEC)

Area ( $\Delta$  DEC) = Area ( $\Delta$  CEB)

Area ( $\Delta$  CEB) = Area ( $\Delta$  AEB)

 $\therefore$  Diagonals of a  ${\rm I\hspace{-.1em I}}$  gm divide into four triangles of equal area.

 $\therefore$  Both Assertion and Reason are true and Reason is a correct explanation of Assertion.

# 31. Question

The question consists of two statements, namely, Assertion (A) and Reason (R). Choose the correct answer.

Assertion (A)	Reason (R)
The area of a trapezium whose parallel sides measure 25cm and 15cm respectively and the distance between them is 6cm, is 120cm <sup>2</sup> .	The area of an equilateral triangle of side 8cm is 163cm <sup>2</sup> .

A. Both Assertion (A) and Reason (R) are true and Reason (R) is a correct explanation of Assertion (A).

B. Both Assertion (A) but Reason (R) are true and Reason (R) is not a correct explanation of Assertion (A).

C. Assertion (A) is true and Reason (R) is false.

D. Assertion (A) is false and Reason (R) is true.

## Answer

Area of trapezium =  $1/2 \times (\text{sum of parallel sides}) \times \text{height} = 1/2 \times (25 + 15) \times 6 = 120 \text{cm}^2$ 

 $\therefore$  Area of trapezium = 120cm<sup>2</sup>

 $\therefore$  Assertion is correct.

Area of an equilateral triangle is given by:  $\frac{\sqrt{3}}{4} \times a^2$  (here 'a' is length of the side)

: Area of an equilateral triangle with side length 8 cm =  $\frac{\sqrt{3}}{4} \times 8^2 = 16\sqrt{3}$ 

∴ Reason is correct

 $\therefore$  Both Assertion but Reason are true and Reason is not a correct explanation of Assertion.

## 32. Question

The question consists of two statements, namely, Assertion (A) and Reason (R). Choose the correct answer.

Assertion (A)	Reason (R)
In the given figure, ABCD is a $\parallel$ gm in which DE $\perp$ AB and BF $\perp$ AD. If AB = 16cm, DE = 8cm and BF = 10cm, then AD is 12cm.	Area of a ∥gm = base x height.

A. Both Assertion (A) and Reason (R) are true and Reason (R) is a correct explanation of Assertion (A).

B. Both Assertion (A) but Reason (R) are true and Reason (R) is not a correct explanation of Assertion (A).

C. Assertion (A) is true and Reason (R) is false.

D. Assertion (A) is false and Reason (R) is true.

## Answer

Here, let AB be the base of the parallelogram then DE becomes its altitude (height).

Area of the parallelogram is given by: Base × Height

 $\therefore$  Area of Igm ABCD = AB×DE =  $16 \times 8 = 128$ cm<sup>2</sup>

Now,

Consider AD as base of the parallelogram then BF becomes its altitude (height)

 $\therefore$  area of lgm ABCD = AD  $\times$  BF = 128cm<sup>2</sup>

 $AD \times 10 = 128 cm^2$ 

$$AD = \frac{128}{10} = 12.8 cm$$

 $\therefore$ length of AD = 12.8cm

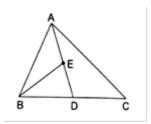
 ${\scriptstyle \rm ...} Assertion$  is false and Reason is true

## 33. Question

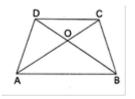
Which of the following is a false statement?

- (A) A median of a triangle divides it into two triangles of equal areas.
- (B) The diagonals of a Igm divide it into four triangles of equal areas.

(C) In a  $\triangle ABC$ , if E is the midpoint of median AD, then  $ar(\triangle BED) = \frac{1}{4}ar(\triangle ABC)$ .



(D) In a trap. ABCD, it is given that ABIDC and the diagonals AC and BD intersect at O. Then,  $ar(\Delta AOB) = ar(\Delta COD)$ .



#### Answer

The correct answer is Option (D)

 $\Delta$  ABC and  $\Delta$  BCD does not lie between parallel lines and also  $\Delta$  AOB and  $\Delta$  COD are not congruent.

## 34. Question

Which of the following is a false statement?

A) If the diagonals of a rhombus are 18cm and 14cm, then its area is  $126 \text{ cm}^2$ .

B) Area of a  $\|gm = \frac{1}{2}x$  base x corresponding height.

C) A parallelogram and a rectangle on the same base and between the same parallels are equal in area.

D) If the area of a  $\parallel$  gm with one side 24cm and corresponding height h cm is 192cm<sup>2</sup>, then h = 8cm.

## Answer

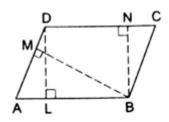
The correct answer is Option (B)

Area of parallelogram = base × corresponding height.

# Formative Assessment (Unit Test)

## 1. Question

The area of I gm ABCD is



- A. AB X BM
- B. BC X BN

C. DC X DL

D. AD X DL

## Answer

Area of the ||gm is Base×Height

Here, height is distance between the Base and its corresponding parallel side.

 $\therefore$  Area (||gm ABCD) = Base  $\times$  Height = DC  $\times$  DL

(: Here DC is taken as length and DL is the distance between DC and its corresponding parallel side AB).

## 2. Question

Two parallelograms are on equal bases and between the same parallels. The ratio of their areas is

A. 1:2

B. 1:1

C. 2:1

D. 3:1

#### Answer

We know that any two or parallelogram having the same base and lying between the same parallel lines are equal in area.

Consider two ||gms ABCD and PQRS which are on same base and lie between same parallel lines.

 $\therefore$  ar(||gm ABCD) = ar(||gm PQRS) -1

 $\therefore$  ar(||gm ABCD ) : ar(||gm PQRS) = 1:1 ( $\because$  eq -1)

## 3. Question

ABCD is a quadrilateral whose diagonal AC divides it into two parts, equal in area. Then, ABCD

A. Is a rectangle

B. is a rhombus

C. is a parallelogram

D. need not be any of (A), (B), (C)

#### Answer

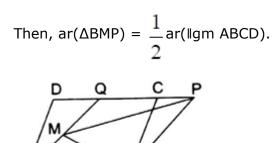
Quadrilateral is any closed figure which has four sides.

Rhombus, Rectangle, Parallelograms are few Quadrilaterals.

When a Diagonal AC of a quadrilateral divides it into two parts of equal areas, it is not necessary for the figure to be a Rhombus or a Rectangle or a Parallelogram, it can be any Quadrilateral.

# 4. Question

In the given figure, ABCD and ABPQ are two parallelograms and M is a point on AQ and BMP is a triangle.





B. False

## Answer

We know that any two or parallelogram having the same base and lying between the same parallel lines are equal in area.

 $\therefore$  ar(||gm ABCD) = ar(||gm ABPQ) -1

We also know that when a parallelogram and a triangle lie on same base and between same parallel lines then, area of the triangle is half the area of the parallelogram.

$$\therefore \operatorname{ar}(\Delta \mathsf{BMP}) = \frac{1}{2} \operatorname{ar}(\operatorname{Igm} \mathsf{ABPQ})$$

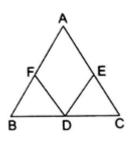
But, from -1

ar(||gm ABCD) = ar(||gm ABPQ)

$$\therefore \operatorname{ar}(\Delta \mathsf{BMP}) = \frac{1}{2} \operatorname{ar}(\operatorname{Igm} \mathsf{ABCD})$$

## 5. Question

The midpoints of the sides of a triangle along with any of the vertices as the fourth point makes a parallelogram of area equal to



- A. 1/2 (ar ΔABC)
- B. 1/3 (ar∆ABC)
- C. 1/4 (ar∆ABC)
- D. ar ( $\Delta ABC$ )

## Answer

Join EF

Here Area (
$$\Delta AEF$$
) = Area ( $\Delta BDF$ ) = Area ( $\Delta DEF$ ) = Area ( $\Delta DEC$ ) =  $\frac{1}{4}$  Area ( $\Delta ABC$ ) - 1

Consider any vertex of the triangle.

Let us consider Vertex B

Here, BDEF form a parallelogram.

Area (||gm BDEF) = Area ( $\Delta$ BDF) + Area ( $\Delta$ DEF)

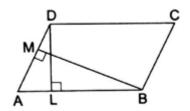
Area (||gm BDEF) =  $\frac{1}{4}$  Area ( $\Delta$ ABC) +  $\frac{1}{4}$  Area ( $\Delta$ ABC) =  $\frac{1}{2}$  Area ( $\Delta$ ABC) (from -1)

: Area (||gm BDEF) =  $\frac{1}{2}$  Area ( $\Delta$ ABC)

Similarly, we can prove for other vertices.

## 6. Question

Let ABCD be a  $\parallel$  gm in which DL  $\perp$  AB and BM  $\perp$  AD such that AD = 6 cm, BM = 10 and DL = 8 cm. Find AB.



## Answer

Given:

AD = 6cm

DL ⊥AB

 $\mathsf{BM}\perp\mathsf{AD}$ 

DL = 8cm

BM = 10cm

Now, consider the parallelogram ABCD

Here, let AD be the base of the parallelogram then BM becomes its altitude (height).

Area of the parallelogram is given by: Base × Height

 $\therefore$  area of lgm ABCD = AD×BM = 6×10 = 60cm<sup>2</sup>

#### Now,

Consider AB as base of the parallelogram then DL becomes its altitude (height)

```
\therefore area of lgm ABCD = AB \times DL = 60cm<sup>2</sup>
```

 $AB \times 8 = 60 \text{ cm}^2$ 

$$AB = \frac{60}{8} = 7.5 cm$$

 $\therefore$ length of AB = 7.5cm.

#### 7. Question

Find the area of the trapezium whose parallel sides are 14 cm and 10 cm and whose height is 6 cm.

#### Answer

Given: Length of parallel sides 14 cm and 10 cm, height is 6cm

We know that area of trapezium is given by: 1/2 (sum of parallel sides)×height

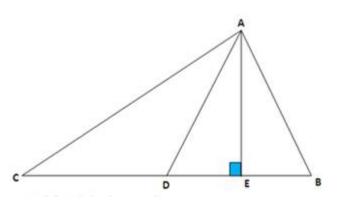
: Area of trapezium =  $1/2 (14 + 10) \times 6 = 72 \text{ cm}^2$ 

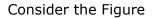
 $\therefore$  Area of trapezium = 72cm<sup>2</sup>

#### 8. Question

Show that the median of a triangle divides it into two triangles of equal area.

#### Answer





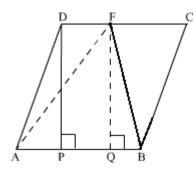
Here,

In  $\triangle$ ABC, AD is the medianHence BD = DCDraw AE  $\perp$  BCArea of  $\triangle$ ABD = Area of  $\triangle$ ADCThus median of a triangle divides it into two triangles of equal area.

## 9. Question

Prove that area of a triangle =  $\frac{1}{2}$  X base X altitude.

## Answer



We know that when a parallelogram and a triangle lie on same base and between same parallel lines then, area of the triangle is half the area of the parallelogram.

Consider the figure,

Here,

```
Area(\Delta ABF) = 1/2 Area(||gm ABCD) (From above statement) -1
```

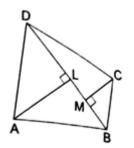
```
Area(||gm ABCD) = Base × Height -2
```

Sub -2 in -1

Area( $\Delta ABF$ ) = 1/2 × Base× Height

## **10. Question**

In the adjoining figure, ABCD is a quadrilateral in which diagonal BD = 14cm. If AL  $\perp$  BD and CM  $\perp$  BD such that AL = 8 cm and CM = 6 cm, find the area of quad. ABCD.



#### Answer

Given: BD = 14cm, AL = 8 cm, CM = 6 cm and also, AL  $\perp$  BD and CM  $\perp$  BD.

Here,

Area (Quad.ABCD) = Area ( $\Delta$ ABD) + Area ( $\Delta$ ABC)

Area ( $\Delta ABD$ ) = 1/2 base × height = 1/2 × BD×AL = 1/2 × 14 × 8 = 56 cm<sup>2</sup>

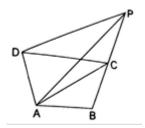
Area ( $\triangle ABC$ ) = 1/2 base × height = 1/2 × BD×CM = 1/2 × 14 × 6 = 42cm<sup>2</sup>

 $\therefore$  Area (Quad.ABCD) = Area ( $\triangle$ ABD) + Area ( $\triangle$ ABC) = 56 + 42 = 98 cm<sup>2</sup>

 $\therefore$  Area (Quad.ABCD) = 98 cm<sup>2</sup>

## 11. Question

In the adjoining figure, ABCD is a quadrilateral. A line through D, parallel to AC, meets BC produced in P. Prove that  $ar(\Delta ABP) = ar(quad. ABCD)$ .



Answer

Given: AC ||DP

We know that any two or Triangles having the same base and lying between the same parallel lines are equal in area.

 $\therefore$  Area ( $\triangle$  ACD) = Area ( $\triangle$  ACP) -1

Add Area ( $\Delta$  ABC) on both sides of eq -1

We get,

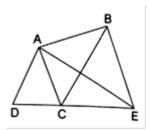
Area ( $\Delta$  ACD) + Area ( $\Delta$  ABC) = Area ( $\Delta$  ACP) + Area ( $\Delta$  ABC)

That is,

Area (quad.ABCD) = Area ( $\Delta$  ABP)

#### 12. Question

In the given figure, ABCD is a quadrilateral and BE  $\parallel$  AC and also BE meets DC produced at E. Show that the area of  $\Delta$ ADE is equal to the area of quad. ABCD.



**Answer** Given: BE ||AC We know that any two or more Triangles having the same base and lying between the same parallel lines are equal in area.

```
\therefore Area (\triangle ACE) = Area (\triangle ACB) -1
```

```
Add Area (\Delta ADC) on both sides of eq -1
```

We get,

Area ( $\Delta$  ACE) + Area ( $\Delta$  ADC) = Area ( $\Delta$  ACB) + Area ( $\Delta$  ADC)

That is,

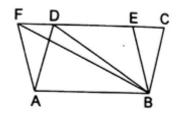
Area ( $\Delta$  ADE) = Area (quad. ABCD)

# 13. Question

In the given figure, area of  $\parallel$  gm ABCD is 80 cm<sup>2</sup>.

Find (i) ar(Igm ABEF)

(ii)  $ar(\Delta ABD)$  and (iii)  $ar(\Delta BEF)$ .



## Answer

Given: area of I gm ABCD is 80 cm<sup>2</sup>

We know that any two or parallelogram having the same base and lying between the same parallel lines are equal in area.

 $\therefore$  ar(||gm ABCD) = ar(||gm ABEF) -1

We also know that when a parallelogram and a triangle lie on same base and between same parallel lines then, area of the triangle is half the area of the parallelogram.

 $\therefore$  ar( $\triangle$ ABD) = 1/2  $\times$  ar(||gm ABCD) and,

```
ar(\Delta BEF) = 1/2 \times ar(||gm ABEF)
```

(i)

ar(||gm ABCD) = ar(||gm ABEF)

 $\therefore \operatorname{ar}(||\operatorname{gm} ABEF) = 80 \operatorname{cm}^2(\operatorname{car}(||\operatorname{gm} ABCD) = 80 \operatorname{cm}^2)$ 

(ii)

 $ar(\Delta ABD) = 1/2 \times ar(||gm ABCD)$ 

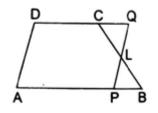
 $ar(\Delta ABD) = 1/2 \times 80 = 40 cm^2 (::ar(||gm ABCD) = 80 cm^2)$ 

```
\therefore \operatorname{ar}(\Delta ABD) = 40 \operatorname{cm}^2
(iii)
\operatorname{ar}(\Delta BEF) = 1/2 \times \operatorname{ar}(||\operatorname{gm} ABEF)
\operatorname{ar}(\Delta BEF) = 1/2 \times 80 = 40 \operatorname{cm}^2 (\operatorname{var}(||\operatorname{gm} ABEF) = 80 \operatorname{cm}^2)
\therefore \operatorname{ar}(\Delta BEF) = 40 \operatorname{cm}^2
```

## 14. Question

In trapezium ABCD, ABIDC and L is the midpoint of BC. Through L, a line PQ II AD has been drawn which meets AB in Point P and DC produced in Q.

Prove that ar(trap. ABCD) = ar(Igm APQD).



#### Answer

Given: ABIDC and L is the midpoint of BC, PQ I AD

Construction: Drop a perpendicular DM from D onto AP

Consider  $\triangle PBL$  and  $\triangle CQL$ 

Here,

```
\angleLPB = \angleLQC (Alternate interior angles, AB|| DQ)
```

BL = LC (L is midpoint of BC)

 $\angle$ PLB =  $\angle$ QLC (vertically opposite angles)

 $\therefore$  By AAS congruency

```
\Delta PBL \cong \Delta CQL
```

 $\therefore PB = CQ (C.P.C.T)$ 

Area (||gm APQD) = base × height = AP × DM -1

Area (Trap.ABCD) =  $1/2 \times (\text{sum of parallel sides}) \times \text{height} = 1/2 \times (AB + DC) \times DM$ 

Area (Trap.ABCD) =  $1/2 \times (AB + DC) \times DM = 1/2 \times (AP + PB + DC) \times DM$  (: AB = AP + PB)

Area (Trap.ABCD) =  $1/2 \times (AP + CQ + DC) \times DM$  (: PB = CQ)

Area (Trap.ABCD) =  $1/2 \times (AP + DQ) \times DM$  (: DC + CQ = DQ)

Area (Trap.ABCD) =  $1/2 \times (2 \times AP) \times DM$  (: AP = DQ)

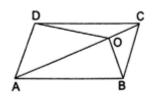
Area (Trap.ABCD) =  $AP \times DM - 2$ 

From -1 and -2

Area (Trap.ABCD) = Area (||gm APQD)

## 15. Question

In the adjoining figure, ABCD is a  $\parallel$  gm and O is a point on the diagonal AC. Prove that ar( $\Delta$ AOB) = ar( $\Delta$ AOD).



#### Answer

Given: ABCD is a I gm and O is a point on the diagonal AC.

Construction: Drop perpendiculars DM and BN onto diagonal AC.

Here,

DM = BN (perpendiculars drawn from opposite vertices of a ||gm to the diagonal are equal)

Now,

Area ( $\Delta AOB$ ) = 1/2 × base × height = 1/2 × AO × BN -1

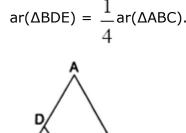
Area ( $\Delta AOD$ ) = 1/2 × base × height = 1/2 × AO × DM -2

From -1 and -2

Area ( $\triangle AOB$ ) = Area ( $\triangle AOD$ ) ( $\because BN = DM$ )

## 16. Question

 $\Delta$  ABC and  $\Delta$ BDE are two equilateral triangles such that D(E) is the midpoint of BC. Then, prove that



# B E

## Answer

Given:  $\triangle$  ABC and  $\triangle$  BDE are two equilateral triangles, D is the midpoint of BC.

Consider ∆ABC

Here, let AB = BC = AC = x cm (equilateral triangle)

Now, consider  $\triangle BED$ 

Here,

BD = 1/2 BC

 $\therefore$  BD = ED = EB = 1/2 BC = x/2 (equilateral triangle)

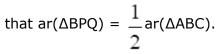
Area of the equilateral triangle is given by:  $\frac{\sqrt{3}}{4}a^2$  (a is side length)

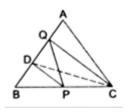
 $\therefore \operatorname{ar}(\Delta \text{BDE}): \operatorname{ar}(\Delta \text{ABC}) = \frac{\sqrt{3}}{4} \times \left(\frac{x}{2}\right)^2: \frac{\sqrt{3}}{4}x^2 = \frac{1}{4}: 1 = 1:4$ That is  $\frac{\operatorname{ar}(\Delta \text{BDE})}{\operatorname{ar}(\Delta \text{ABC})} = \frac{1}{4}$  $\therefore \operatorname{ar}(\Delta \text{BDE}) = \frac{1}{4}\operatorname{ar}(\Delta \text{ABC})$ 

Hence Proved

## 17. Question

In ∆ABC, D is the midpoint of AB and P Point is any point on BC. If CQ II PD meets AB in Q, then prove





#### Answer

Given: D is the midpoint of AB and P Point is any point on BC, CQI PD

In Quadrilateral DPQC

Area ( $\Delta$  DPQ) = Area ( $\Delta$  DPC)

Add Area ( $\Delta$  BDP) on both sides

We get,

Area ( $\Delta$  DPQ) + Area ( $\Delta$  BDP) = Area ( $\Delta$  DPC) + Area ( $\Delta$  BDP)

Area ( $\Delta$  BPQ) = Area ( $\Delta$  BCD) -1

D is the midpoint BC, and CD is the median

 $\therefore$  Area ( $\triangle$  BCD) = Area ( $\triangle$  ACD) = 1/2  $\times$  Area ( $\triangle$  ABC) -2

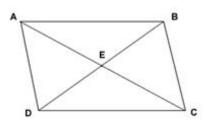
Sub -2 in -1

Area ( $\Delta$  BPQ) = 1/2 × Area ( $\Delta$  ABC) ( $\because$ Area ( $\Delta$  BCD) = 1/2 × Area ( $\Delta$  ABC))

## **18. Question**

Show that the diagonals of a I gm divide into four triangles of equal area.

## Answer



Consider  $\Delta$  ABD

We know that diagonals in a parallelogram bisect each other

 $\therefore$  E is the midpoint of BD, AE is median of  $\Delta$  ABD

: Area ( $\Delta$  ADE) = Area ( $\Delta$  AEB) (: Median divides the triangle into two triangles of equal areas)

Similarly we can prove

Area ( $\Delta$  ADE) = Area ( $\Delta$  DEC)

Area ( $\Delta$  DEC) = Area ( $\Delta$  CEB)

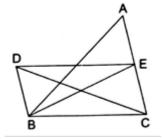
Area ( $\Delta$  CEB) = Area ( $\Delta$  AEB)

 $\therefore$  Diagonals of a  ${\tt I\hspace{-.1em}I}$  gm divide into four triangles of equal area.

## **19.** Question

In the given figure, BD || CA, E is the midpoint of CA and BD =  $\frac{1}{2}$  CA.

Prove that  $ar(\Delta ABC) = 2 \times ar(\Delta DBC)$ .



#### Answer

Given: BD || CA, E is the midpoint of CA and BD =  $\frac{1}{2}$ CA

Consider  $\Delta$  BCD and  $\Delta$  DEC

Here,

BD = EC (: E is the midpoint of AC that is CE = 
$$\frac{1}{2}$$
 CA, BD =  $\frac{1}{2}$  CA)

CD = CD (common)

 $\angle$ BDC =  $\angle$ ECD (alternate interior angles, DB||AC)

 $\therefore$  By SAS congruency

 $\Delta$  BCD  $\cong \Delta$  DEC

 $\therefore$  Area ( $\triangle$  BCD) = Area ( $\triangle$  DEC) -1

Here,

Area ( $\Delta$  BCE) = Area ( $\Delta$  DEC) (triangles on same base CE and between same parallel lines) -2

E is the midpoint of AC, BE is the median of  $\triangle$ ABC

 $\therefore$  Area ( $\triangle$  BCE) = Area ( $\triangle$  ABE) = 1/2 × Area ( $\triangle$  ABC)

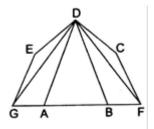
: Area ( $\Delta$  DEC) = 1/2 × Area ( $\Delta$  ABC) (: Area ( $\Delta$  BCE) = Area ( $\Delta$  DEC))

 $\therefore$  Area ( $\triangle$  BCD) = 1/2  $\times$  Area ( $\triangle$  ABC) ( $\because$ Area ( $\triangle$  DEC) = Area ( $\triangle$  BCD))

## 20. Question

The given figure shows a pentagon ABCDE in which EG, drawn parallel to DA, meets BA produced at G and CF drawn parallel to DB meets AB produced at F.

Show that ar(pentagon ABCDE) =  $ar(\Delta DGF)$ .



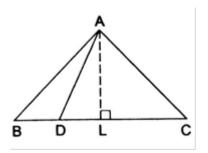
## Answer

Given: EG||DA, CF||DB Here, in Quadrilateral ADEG Area ( $\Delta$  AED) = Area ( $\Delta$  ADG) -1 In Quadrilateral CFBD Area ( $\Delta$  CBD) = Area ( $\Delta$  BCF) -2 Add -1 and -2 Area ( $\Delta$  AED) + Area ( $\Delta$  CBD) = Area ( $\Delta$  ADG) + Area ( $\Delta$  BCF) -3 Add Area ( $\Delta$  ABD) to -3 Area ( $\Delta$  AED) + Area ( $\Delta$  CBD) + Area ( $\Delta$  ABD) = Area ( $\Delta$  ADG) + Area ( $\Delta$  BCF) + Area ( $\Delta$  ABD)

Area (pentagon ABCDE) = Area ( $\Delta$ DGF)

## 21. Question

In the adjoining figure, the point D divides the side BC of  $\triangle$ ABC in the ratio m:n. Prove that ar( $\triangle$ ABD): ar( $\triangle$ ADC) = m:n.



#### Answer

Given: D divides the side BC of  $\triangle$ ABC in the ratio m:n

Area ( $\Delta$  ABD) = 1/2 × BD × AL

Area ( $\Delta$  ADC) = 1/2 × CD × AL

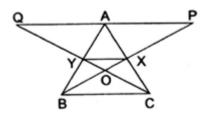
Area ( $\triangle ABD$ ): Area ( $\triangle ADC$ ) = 1/2 × BD × AL: 1/2 × CD × AL

Area ( $\triangle$ ABD): Area ( $\triangle$ ADC) = BD: CD

Area ( $\triangle$ ABD): Area ( $\triangle$ ADC) = m: n ( $\because$  BD:CD = m:n)

#### 22. Question

In the give figure, X and Y are the midpoints of AC and AB respectively, QP  $\parallel$  BC and CYQ and BXP are straight lines. Prove that ar( $\Delta$ ABP) = ar( $\Delta$ ACQ).



#### Answer

Given: X and Y are the midpoints of AC and AB respectively, QP II BC and CYQ and BXP are straight lines.

Construction: Join QB and PC

In Quadrilateral BCQP

Area ( $\Delta$  QBC) = Area ( $\Delta$  BCP) (Triangles on same base BC and between same parallel lines are equal in area) -1 and,

Area (||gm ACBQ) = Area (||gm ABCP) (parallelograms on same base BC and between same parallel lines are equal in area) -2

Subtract -1 from -2

Area (||gm ACBQ) – Area ( $\Delta$  QBC) = Area (||gm ABCP) – Area ( $\Delta$  BCP)

Area ( $\Delta$ ACQ) = Area ( $\Delta$ ABP)

 $\therefore$  Area( $\triangle$ ABP) = Area( $\triangle$ ACQ)