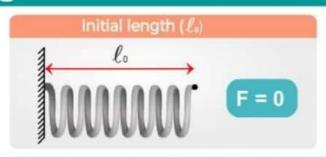


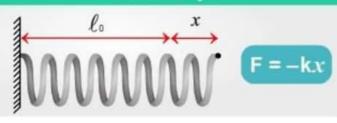
SPRING FORCE WWW.

0

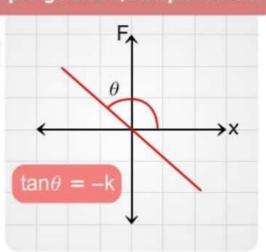
STRETCHED SPRING



Stretched by x



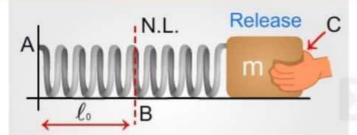
Spring Force v/s Displacement



2

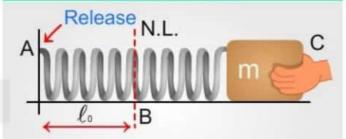
SPRING ATTACHED TO A BLOCK

Released at C



When the block is released at point C then spring force doesn't change instantaneously because of friction at mass m.

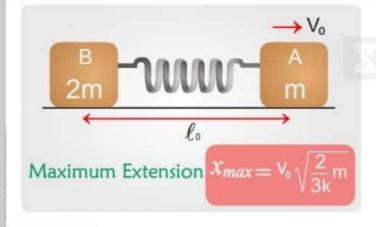
Released at A

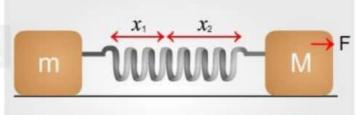


When point A is released then the spring force changes instantaneously to become zero.

3

SPRING BLOCK SYSTEM





$$X_{\text{max}} \equiv X_1 + X_2 \equiv \frac{2\text{mF}}{\text{k(m + M)}}$$

IMPULSE AND MOMENTUM

IMPULSE

Impulse of a force 'F' acting on a body for a time interval $t = t_1$ to $t = t_2$ is defined as

$$\overrightarrow{I} = \int_{1}^{1} \overrightarrow{F} dt$$

$$\overrightarrow{I}_{Re} = \int_{1}^{1} \overrightarrow{F}_{Res} dt = \Delta \overrightarrow{P}$$

(Impulse - Momentum Theorem)

COEFFICIENT OF RESTITUTION (e)

The coefficient of restitution is defined as the ratio of the impulses of reformation and deformation of either body.

$$e = \frac{\text{Impulse of reformation}}{\text{Impulse of deformation}} = \frac{\int F_r dt}{\int F_d dt} \qquad e = \frac{\text{Velocity of separation of point of contact}}{\text{Velocity of approach of point of contact}}$$

LINEAR MOMENTUM

Linear momentum is a vector quantity defined as the product of an object's mass m, and its velocity v. Linear momentum is denoted by the letter p and is called "momentum" in short:

Note that a body's momentum is always in the same direction as its velocity vector. The units of momentum are ka.m/s.

CONSERVATION OF LINEAR MOMENTUM

acting on the body is zero. Then,

$$\vec{p}$$
 = constant or \vec{v} = constant
(if mass = constant)

For a single mass or single body, If net force I If net external force acting on a system of particles or system of rigid bodies is zero. Then.

$$\vec{P}_{CM}$$
 = constant or \vec{V}_{CM} = constant

COLLISION



Note :- In every type of collision, only linear momentum remains constant.

HEAD ON ELASTIC COLLISION



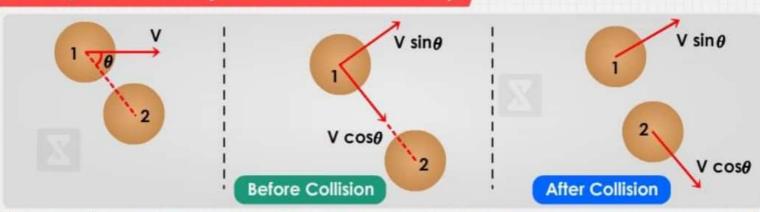
In this case, linear momentum and kinetic energy both are conserved. After solving two conservation equations. We get,

$$V'_1 = \left(\frac{m_1 - m_2}{m_1 + m_2}\right) V_1 + \left(\frac{2m_2}{m_1 + m_2}\right) V_2 \quad \text{and} \quad V'_2 = \left(\frac{m_2 - m_1}{m_1 + m_2}\right) V_2 + \left(\frac{2m_2}{m_1 + m_2}\right) V_1$$

HEAD ON INELASTIC COLLISION

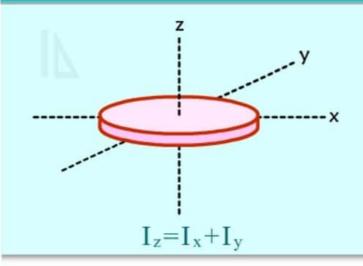
- In an inelastic collision, the colliding particles do not regain their shape and size completely after the collision.
- Some fraction of mechanical energy is retained by the colliding particles in the form of deformation potential energy. Thus, the kinetic energy of the particles no longer remains conserved.
- (Energy loss)_{Perfectly Inelastic} > (Energy loss)_{Partial Inelastic}
- 0 < e < 1 : e = coefficient of restitution</p>

OBLIQUE COLLISION (BOTH ELASTIC IN ELASTIC)

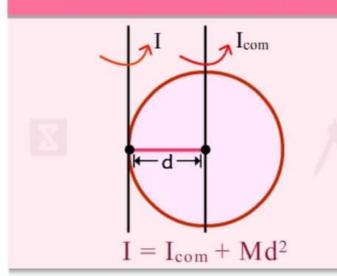


| BALL | COMPONENT ALONG COMMON TANGENT DIRECTION | | COMPONENT ALONG COMMON NORMAL DIRECTION | |
|------|--|-----------------|---|-----------------|
| | Before Collision | After Collision | Before Collision | After Collision |
| 1 | V sin <i>⊕</i> | V sin <i>θ</i> | V cosθ | 0 |
| 2 | 0 | 0 | 0 | V cosθ |

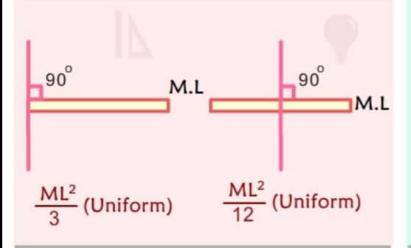
Perpendicular Axis Theorm



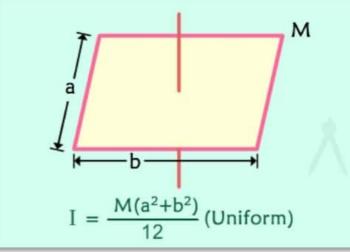
Parellel Axis Theorm



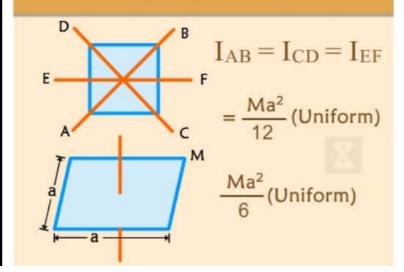
Rod



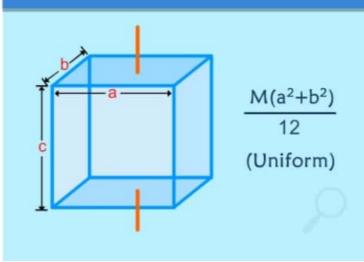
Rectangular Plate



Square Plate

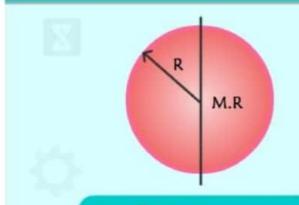


Cuboid



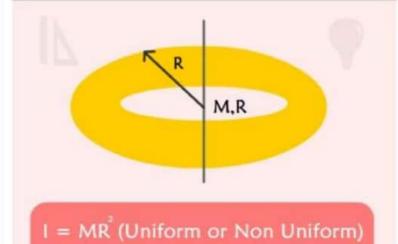
MOMENT OF INERTIA



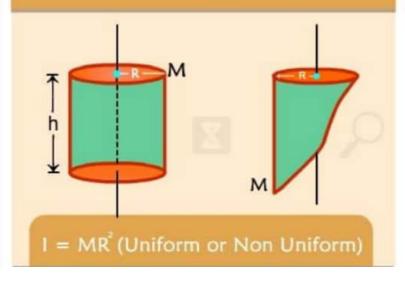


$$I = \frac{2}{5} MR^2 (Uniform)$$

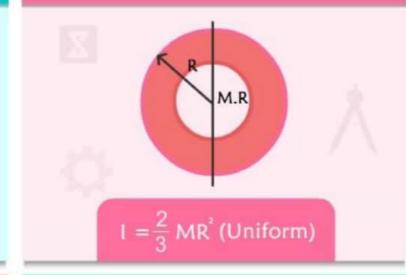
Ring



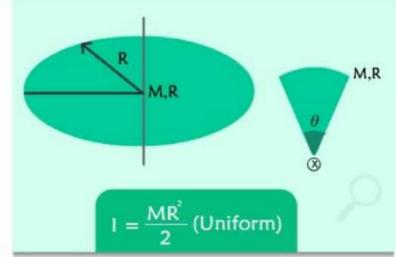
Hollow cylinder



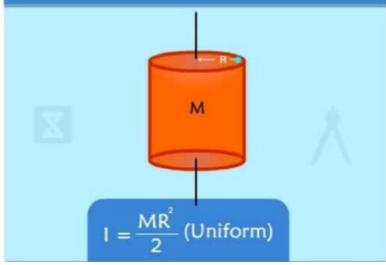
Hollow Sphere



Disc



Solid cylinder

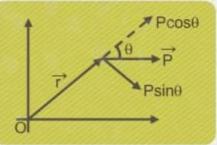


PARTI



1 ANGULAR MOMENTUM OF A PARTICLE ABOUT A POINT





2 ANGULAR MOMENTUM OF A RIGID BODY ROTATING ABOUT A FIXED AXIS

$$L = I_{\omega}$$

Here, I is the moment of inertia of the rigid body about axis.

CONSERVATION OF ANGULAR MOMENTUM

The law of conservation of angular momentum states that when no external torque acts on an object, no change of angular momentum will occur.

Since
$$\tau_{net} = \frac{d}{d}$$

$$\overrightarrow{\tau}_{net} = 0,$$

$$\frac{\overrightarrow{dL}}{dt} = 0,$$

 $=\frac{d\vec{L}}{dt}$. Now if, $\vec{\tau}_{net} = 0$, then $\frac{d\vec{L}}{dt} = 0$, so that $\vec{L} = \text{constant}$.

4 ANGULAR IMPULSE

The angular impulse of a torque in a given time interval is defined as

$$\int_{t_1}^{t_2} \vec{\tau} \, dt$$

$$\vec{\tau} = \frac{d\vec{L}}{dt}$$

UNIFORM PURE ROLLING

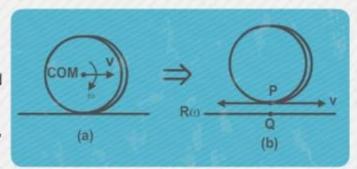
Pure rolling means no relative motion (or no slipping at point of contact between two bodies.)

$$V - R\omega = 0$$

If $V_P > V_Q$ or $V > R_{\omega}$, the motion is said to be forward slipping and if

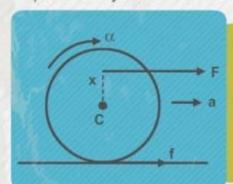
VP < Vo < Ro , the motion is said to be backward slipping.

The condition of pure rolling on a stationary ground is, $a = R_0$



1 PURE ROLLING WHEN FORCE F ACT ON A BODY

Suppose a force F is applied at a distance x above the centre of a rigid body of radius R, mass M and moment of inertia CMR^2 about an axis passing through the centre of mass. Applied force F can produces by itself a linear acceleration a and an angular acceleration α .



 $\alpha = liner$ acceleration . $\alpha = angular$ acceleration from linear motion

$$F + f = Ma$$

From rotational motion: Fx - fR = I a

$$a = \frac{F(R + X)}{MR(C + 1)}$$
, $f = \frac{F(x - RC)}{R(C + 1)}$

2 PURE ROLLING ON A INCLINED PLANS

A rigid body of radius R, and mass m is released at rest from height h on the incline whose inclination with horizontal is θ and assume that friciton is sufficient for pure rolling then,

$$a = \alpha R$$
 and $v = R\omega$

ω = Angular Velocity

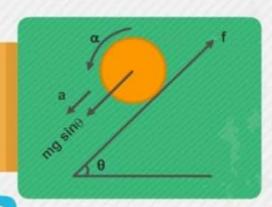
 α = Angular Acceleration

Linear Acceleration,

$$a = \frac{g \sin \theta}{1 + C}$$

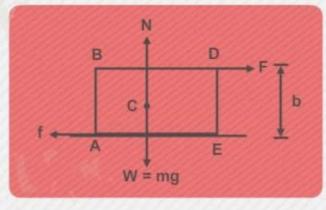
C = Center of Mass

So, body which have low value of C have greater acceleration.



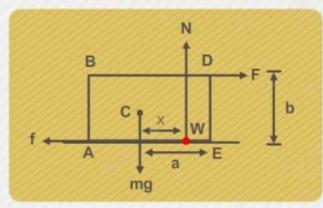
TOPPLING

Torque about E



Balancing Torque at E

Torque about W



Balancing Torque at W

$$Fb + N (a - x) = mg a$$

if
$$x = a$$

$$F_{\text{max}} b = \text{mga}$$
 \Longrightarrow $F_{\text{max}} = \frac{\text{mga}}{b}$