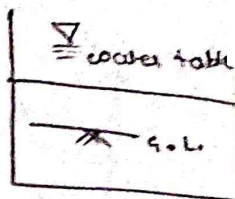


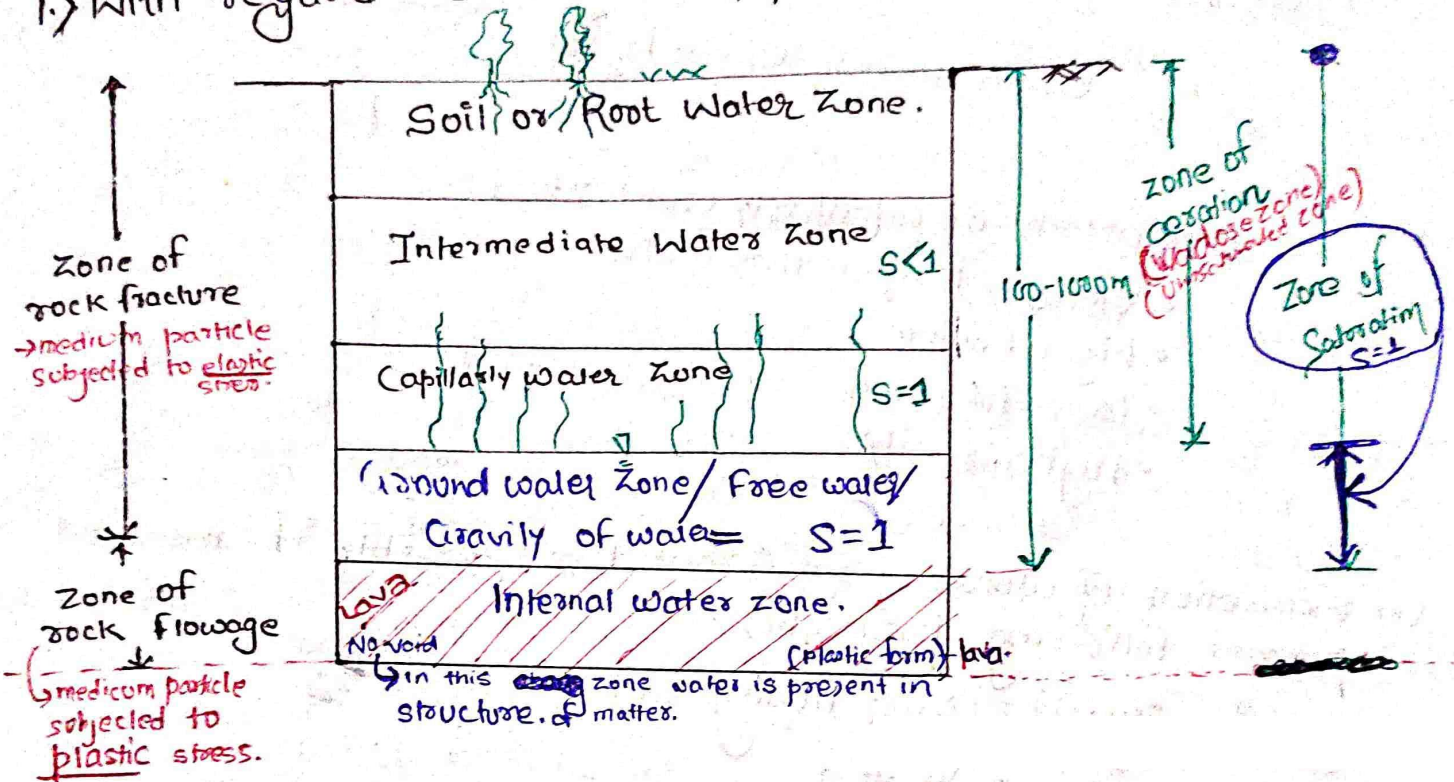
SOURCE OF WATER

marshy - ~~water~~ area

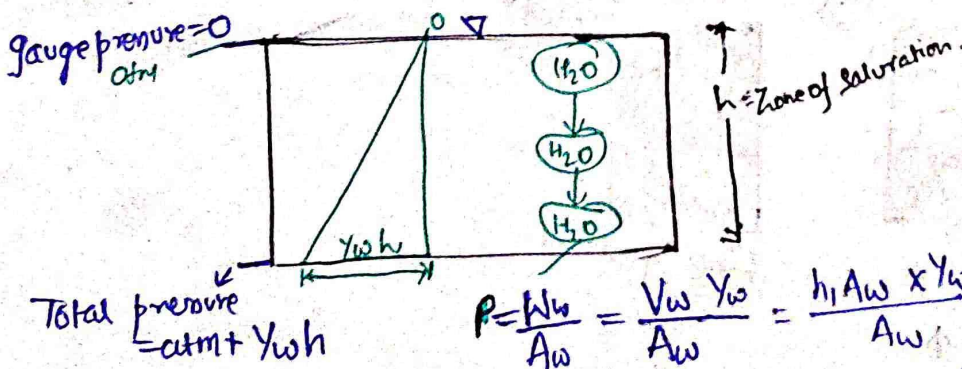


SOURCE $\rightarrow$ Surface
 $\rightarrow$ Subsurface (ground water) - soil
 $\rightarrow$ Rain/precipitation.

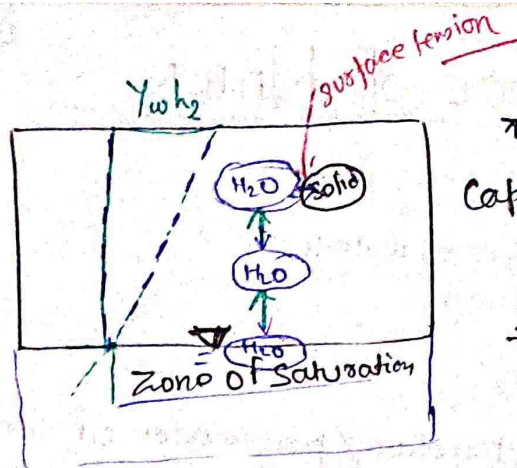
1. With regard to extraction/presence of water in ground.



* Soil transfer its weight through soil grains not water.



$\rightarrow$ hydrostatic pressure (compression)
 $\rightarrow$ Pressure head = h



-ve	+ve = tension
+ve	-ve = compression

$$\text{Surface tension} = w_w = h_2 \gamma_w$$

every property of capillary water :-

- Viscosity is higher than water
- higher boiling
- lower freezing
- higher density

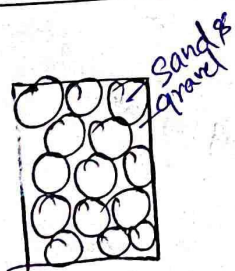
(ii) Extraction of water from Ground is possible if medium possess following properties:-

Porosity (η) = water holding capacity & voids.

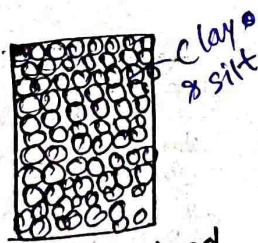
$$= \frac{V_v}{V} \times 100$$

$$\eta \propto V_v \propto \frac{1}{d}$$

d = size of particle.



Coarse



Fine grained

Size of voids $\rightarrow \uparrow$
Volume of void $\rightarrow \uparrow$
no. of voids $\rightarrow \downarrow$

$\downarrow$
 $\downarrow$
 $\uparrow$
 $\uparrow$

Total volume of void = $\eta \times V_v \rightarrow \downarrow$

Ground Water Development.

With regards to the existence of water below the Earth crust. It is divided into following zone.

(i) Zone of rock flowage:-

- It is the zone in which medium particles are being subjected to permanent deformation due to the application of plastic stress over them. NO VOIDS.
- Water in this zone is present only inside the structure of medium particles thereby it is termed as internal water zone. Structural water.
- Thickness of this zone extends upto several kms. below the earth crust.
- This zone is no. of egg use. as water can't be derived by it by any means.

(ii) Zone of Rock Fracture:-

- It is the zone in which medium particles are being subjected to elastic stresses hence water is available in the voids of this zone extraction of water which depends upon the properties of the medium.
- Thickness of this zone is the range of 100-1000m below the earth crust.
 - This zone is further divided into:-
- ### (a) Zone of saturation & zone of aeration.

Ground/free/gravity of water zone:-

Ground → because it found in ground.

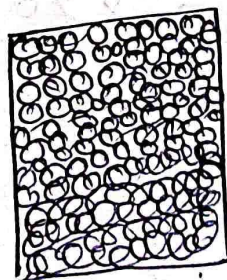
free → free to move.

gravity → only weight of water act.

Note:- (1)

(ii) If we have choice to extract water from capillary ground then our first choice would be ground water zone because in this water is free but in capillary zone water is held by soil so more energy is required to extract water from this zone.

(iv) Permeability/Hydraulic conductivity (K)
Permeability is the ability of the media to transmit water through its pores.

$$K = f(\text{friction}) \propto \frac{1}{f}$$


no. of particle

Total surface area = $n \cdot SA$

Permeability

* Water is only extracted from coarse site, fine sand.

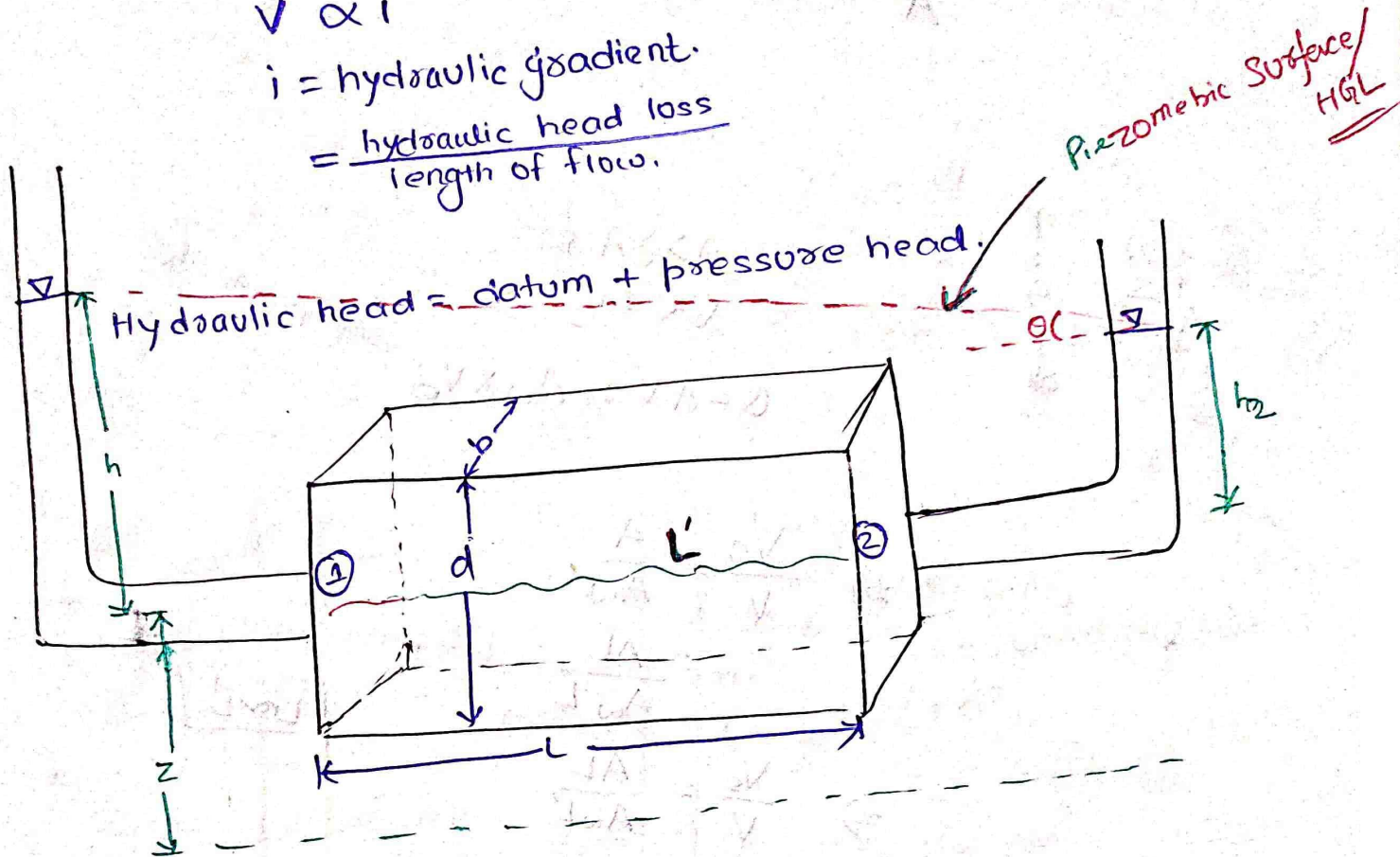
Darcy's law

Assumption: - $S=1$ and laminar flow.

$$V \propto i$$

i = hydraulic gradient.

$$= \frac{\text{hydraulic head loss}}{\text{length of flow.}}$$



$$i = \frac{(z+h_1) - (z+h_2)}{L'} = \frac{h_1 - h_2}{L'}$$

$(L' > L)$

Hydraulic gradient line,

$$\tan \theta = \frac{h_1}{L}$$

Assume $L' = L$

$$i = \frac{h_1}{L} \approx \frac{h_1}{L}$$

$$V = Ki$$

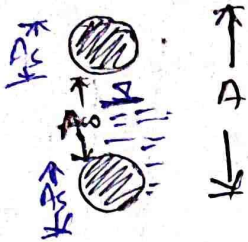
$$Q = VA$$

$$Q = KiA$$

$$\text{if } i=1$$

$$Q = KA$$

$$k = \frac{Q}{A} \text{ (m/sec)} = \frac{\text{m}^3}{\text{sec} \cdot \text{m}^2}$$



$$A \gg A_w$$

$$V \ll V_s$$

$$Q = AV = A_w \times V_s \quad \text{seepage velocity}$$

$$\Rightarrow \frac{V_s}{V} = \frac{A}{A_w}$$

$$= \frac{AL}{A_w L}$$

$$L \propto L'$$

$$\Rightarrow \frac{V_s}{V} = \frac{AL}{A_w L'}$$

$$\Rightarrow \frac{V_s}{V} = \frac{V}{V_w}$$

$$= \frac{V}{V_v} \cdot \frac{V_v}{V_w}$$

$$\frac{V_s}{V} = \left(\frac{V_v}{V} \right) \left(\frac{V_w}{V_v} \right)$$

$$V_s = \frac{V}{\eta_s}$$

$$\Rightarrow \text{if } s=1$$

$$V_s = \frac{V}{\eta}$$

$$0 < s \leq 1$$

$$0 < \eta < 1$$

$$\therefore V_s > V$$

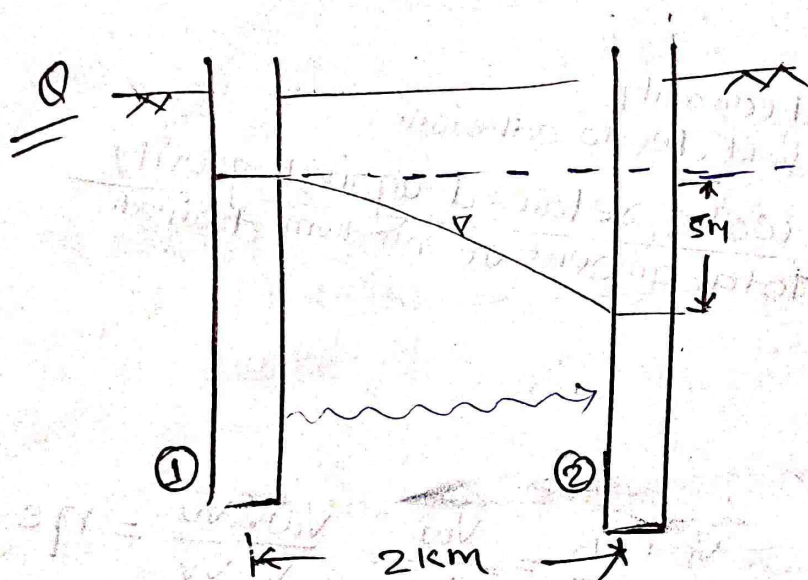
Transmissibility

→ Rate of flow through medium per unit width. $\Rightarrow$ under unit hydraulic gradient

$$T = \frac{Q}{b} = \underline{m^3/m/sec}$$

$$K = \frac{Q}{bd}$$

$$K = \frac{T}{d} \Rightarrow \boxed{T = Kd} = m^3/m/sec.$$



$$\begin{aligned} \eta &= 0.35 \\ K &= 300 \text{ m/day} \\ t &= ? \end{aligned}$$

$$\text{time of travel} = \frac{\text{distance} \approx 2 \text{ km}}{V_s}$$

$$= \frac{2000 \text{ m}}{\frac{V}{n}}$$

$$= \frac{2000 \times \eta}{V}$$

$$= \frac{2000 \times 0.35}{Ki}$$

$$= \frac{2000 \times 0.35}{300 \times \frac{5}{2000}}$$

$$= 933.3 \text{ days} \\ = 2.55 \text{ years.}$$

$$i = \frac{hL}{L} \approx 2000 \text{ m}$$

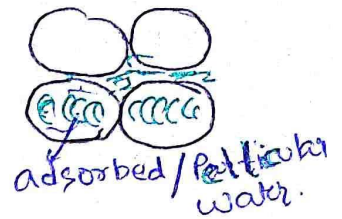
(specific - per unit quantity (m or v))

→ Even if the medium is porous and permeable, we can't withdraw all water. because certain amount of water will be retained over surface of ^{medium} particle. because of physical force of attraction between water molecule and particle. and this water retained inside the medium particle this water is called adsorbed water.

(iii) Specific Yield (Y_s)

$Y_s = \frac{\text{Amount of water drained by gravity}}{\text{Amount of medium drained.}}$

$$Y_s = \frac{V_w}{V} \times 100.$$



Specific Retention / field capacity.
→ The water retained in field due to adhesion.

$Y_R = \frac{\text{Amount of water retained against gravity}}{\text{Total amount of medium drained.}}$

$$= \frac{V_R}{V} \times 100.$$

$$Y_s + Y_R = \frac{V_D}{V} + \frac{V_R}{V} = \frac{V_D + V_R}{V} = \frac{V_w}{V} = \frac{V_w}{V} \cdot \frac{V_v}{V_v} = \eta_s$$

$$Y_s + Y_R = \eta_s$$

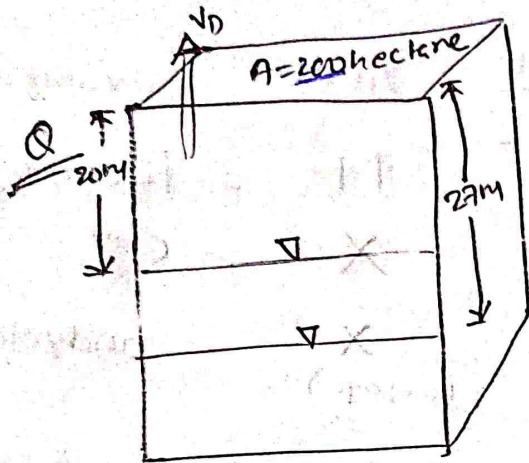
if $S = 1$

$$Y_s + Y_R = \eta$$

$$Y_s = f[d] \quad [d \uparrow \rightarrow SSA \downarrow \rightarrow f \downarrow \rightarrow Y_s \uparrow]$$

$$Y_R = f[d] \quad [d \uparrow \rightarrow SSA \downarrow \rightarrow Y_R \downarrow]$$

Clay, silt $\rightarrow$ retention $\uparrow$ Yield $\downarrow$
 Sand, gravel $\rightarrow$ retention $\downarrow$ Yield $\uparrow$



change in ground water storage due to pumping
 $\eta = 0.4$, $Y_R = 0.15$.

Nature of change = decreasing.

V_D

$$Y_s = \frac{V_D}{V}$$

$$V_D = Y_s V$$

$$V_D = (\eta - Y_R) \times V$$

$$= (0.4 - 0.15) \times 7 \times 200$$

$$= 350 \text{ hectare-meter.}$$

$$Y_s + Y_R = \eta$$

$$Y_s = (0.4 - Y_R)$$

~~350~~

$$\eta = 0.4$$

If due to rain 500 hectare-m

$$300 \text{ hac-m} \rightarrow 7 \text{ m} \uparrow$$

$$50 \text{ hac-m} \rightarrow 1 \text{ m} \uparrow$$

$$500 \text{ hac-m} \rightarrow 10 \text{ m} \uparrow$$

$$\text{New water table} = 27 - 10 = 17 \text{ m from top.}$$

$$\frac{350-7}{50-1}$$

$$\eta = 0.4 = \frac{V_D}{V} = \frac{V_w}{V}$$

$$= V_w = \eta \times V$$

$$= 0.4 \times 200 \times 7$$

$$= 560 \text{ hectare-m}$$

DIFFERENT TYPES OF GEOLOGICAL FORMATION

1) Aquifer: Aquifer are those geological formation which are highly porous and permeable. hence, they give high yield.
eg. fine sand, coarse sand.

	Porosity (n)	Permeability (k)	Yield	Example
1) AQUIFER	↑↑	↑↑	↑↑	fine sand, coarse silt.
2) AQUICLUDE	↑↑↑	↓↓↓	X	clay
3) AQUITARD	↑↑ ↑↑	↓↓	X (seepage)	sandy clay
4) AQUIFUSE	X (voids zero)	X	X	Granite stone

Types of Aquifer :-

- Unconfined Aquifer / Non-artesian / water table aquifer.
- Confined aquifer / Artesian.
- Perched aquifer.

② Aquiclude:- These are type of geological formation which are high porous but impermeable hence water can't be drained through it eg. clay.

③ Aquitard: These are type of formation which are porous (but less as compare to aquiclude) and less permeable hence water does not flow through them but instead it seeps. (seepage) eg. sandy clay.

④ Aquifuse:- These are formation which are neither porous nor permeable.
eg. granite rock.

Type of Aquifer:-

(i) Unconfined/Water Table Aquifer/Non-artesian.

- No confining pressure.
- No artificial pressure.
- Top zone of saturation is water table level.
- These are type of saturation aquifer in which G.W.T. marks the upper limit of saturation.
- Water in these aquifer is subjected to pressure not greater than hydrostatic pressure.

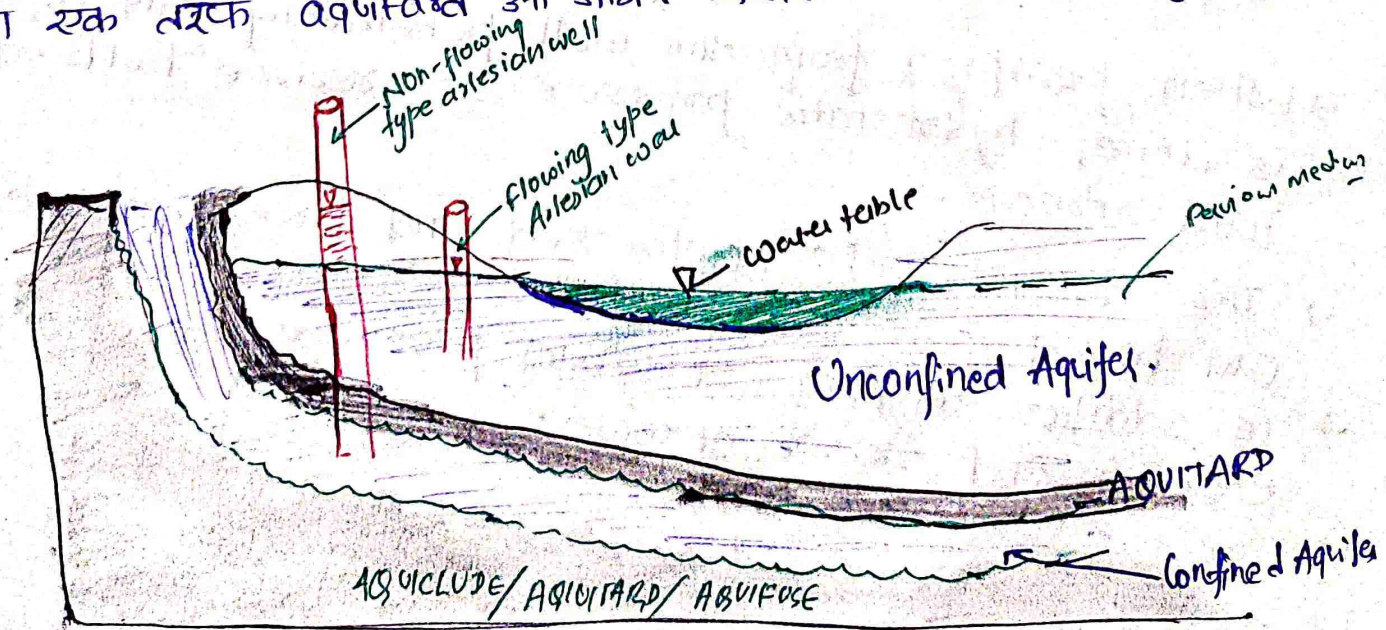
(ii) Confined Artesian Aquifer:

- Confining pressure.
- These are the type of aquifer which are formed when a pervious medium is found to exist in between two impermeable layer.
- Water in these aquifer are subjected to pressure greater than hydrostatic pressure.

(iii) Perched aquifer.

Sometimes an impermeable layer is found to exist in a pervious medium, above the G.W.T. carrying the saturated soil mass that can also be used as source of water and is termed as perched aquifer.

Semi-confined:- Confined aquifer. के दोनों तरफ ~~aquifer~~ या एक तरफ aquitard आ जाये. जिससे water leak हो जाता है।



Storativity / specific storage / co-efficient of storage (S)

~~S~~ $S = \frac{V_w}{V}$ (by any means)

$$S = \frac{\text{Volume of water drained from medium (By any means)}}{\text{Volume of medium drained (SA} \times \text{drop in water table / Potentiometric head)}}$$

$$\gamma_s = \frac{V_w}{V}$$

(i) For unconfined aquifer

$$\gamma_s = S$$

(ii) For confined aquifer.

$$\gamma_s \neq S$$

→ In case of confined aquifer water is drained because of = compression of aquifer + Expansion of water

→ In confined aquifer, the hydrostatic within the partially supports the overburden, while remaining is supported by the soil structure of aquifer.

→ When pumping from the well penetrating this aquifer is done, hydrostatic pressure is reduced but aquifer load increases.

→ The aquifer gets compressed and forces some water out from it.

→ In addition lowering of water pressure cause small expansion and release of water.

Hence in this case storage coefficient is defined as volume of water release from the aquifer from full aquifer height and unit cross-sectional area, when piezometric surface decline by unity.

Storage of coefficient for confined aquifer:-

$$S = \gamma_w H (\alpha + \eta \beta)$$

$$= \gamma_w H \left\{ \frac{1}{E_s} + \eta \frac{1}{E_w} \right\}$$

γ_w = unit weight of water

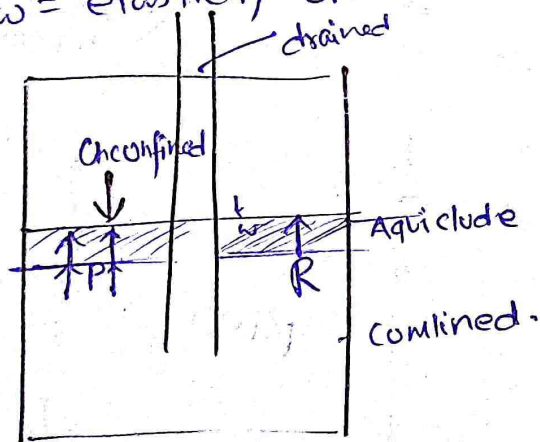
H = confined aquifer thickness m.

α = compressibility of the aquifer = $\frac{1}{E_s}$

E_s = Elasticity of aquifer.

β = compressibility of water = $\frac{1}{E_w}$

E_w = elasticity of water.



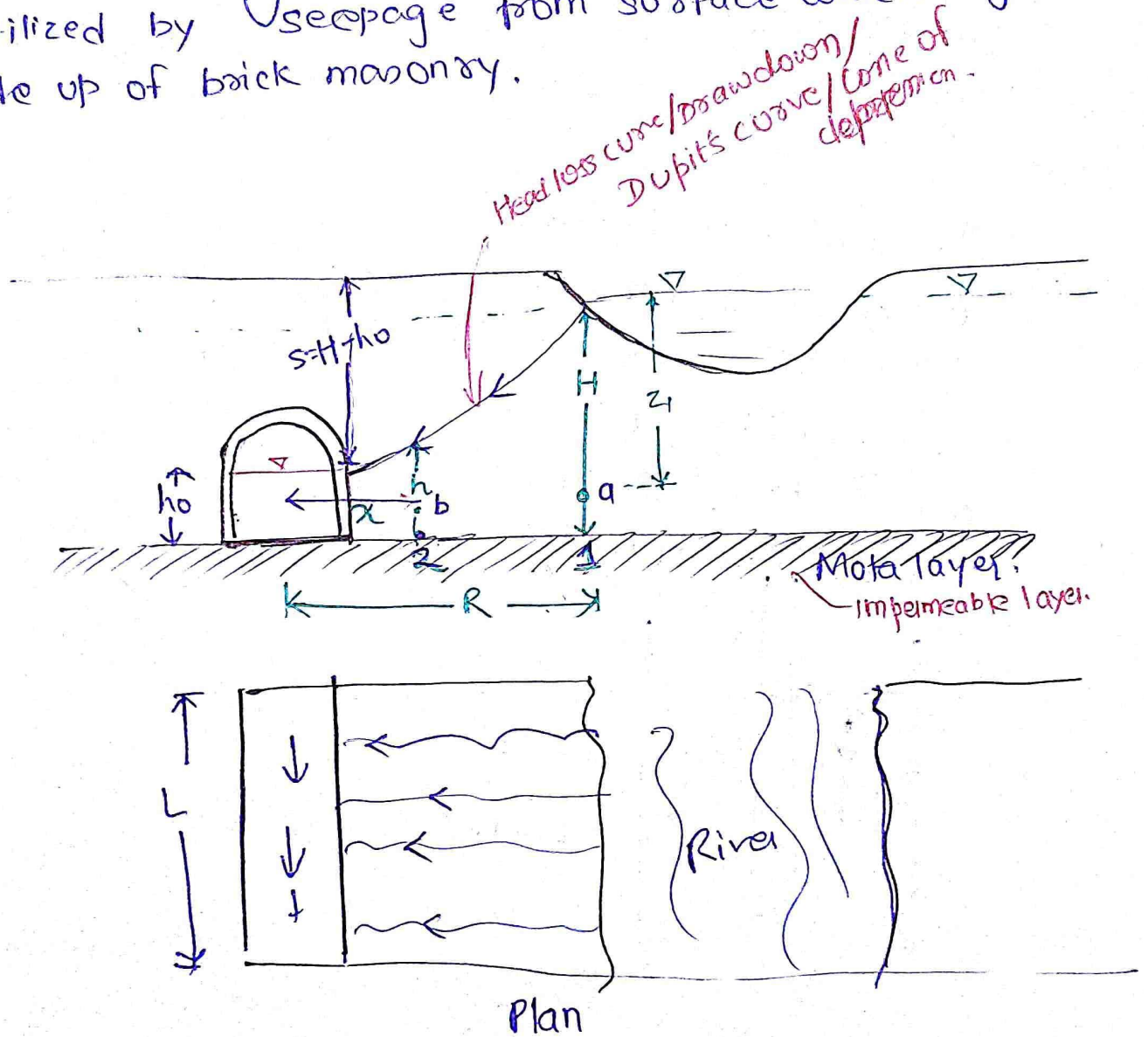
Different forms of extraction of Ground Water:

1) Infiltration Gallery

→ Infiltration Gallery

Infiltration gallery are generally horizontal tunnel constructed at shallow depth of 3-6m along the bank of the river in water bearing structure through which the water is utilized by seepage from surface which is generally made up of brick masonry.

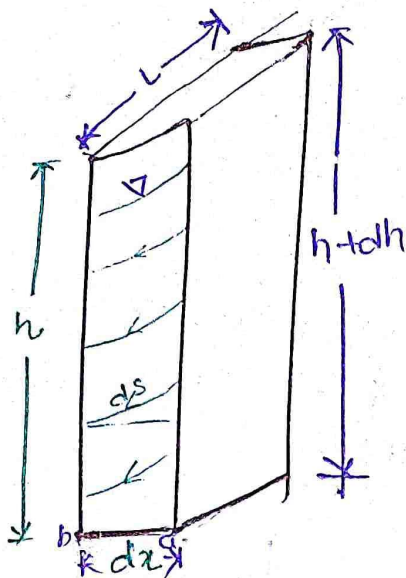
re/drawdown / Cone of depression



H = Height of the water in the river/
or high of original water table.

h_0 = height of water in ~~the~~ storage gallery

$R = \text{radius of influence} \approx 300\text{m.}$



$$q_x = q_x \times V_x$$

$$= (h \cdot L) \cdot K i_x$$

$$q_x = h L \cdot K \frac{dh}{ds}$$

$ds > dx$
if θ is small, $\sin \theta \approx \tan \theta$.

$$ds = dx$$

$$\therefore q_x = h L K \left(\frac{dh}{dx} \right)$$

Assume $dh = ds$
 $\sin \theta = \frac{dh}{ds}$, $\tan \theta = \frac{dh}{dx}$

$\tan \theta = \frac{1}{300}$
 $\theta = 0.19^\circ$

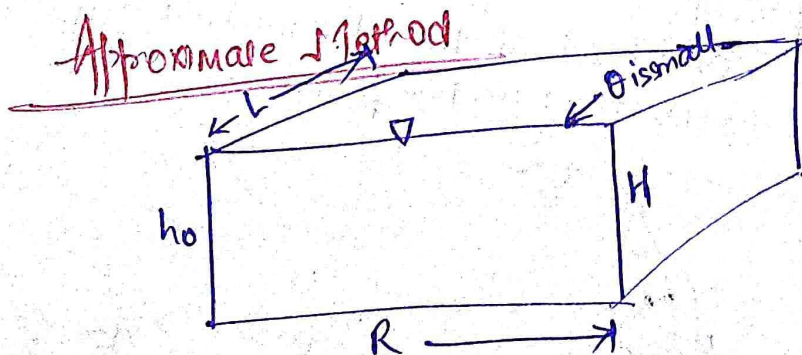
$$Q = \int q_x = \int h L K \frac{dh}{dx}$$

~~$$Q = \int_{x=0}^R q_x dx = \int_{x=0}^R h L K \frac{dh}{dx} dx$$~~

$$\int_{x=0}^R Q dx = \int_{h=h_0}^{h=H} h L K dh$$

$$Q[x]_0^R = L K \left[\frac{h^2}{2} \right]_0^H$$

$$Q = \frac{K L (H^2 - h_0^2)}{2R}$$



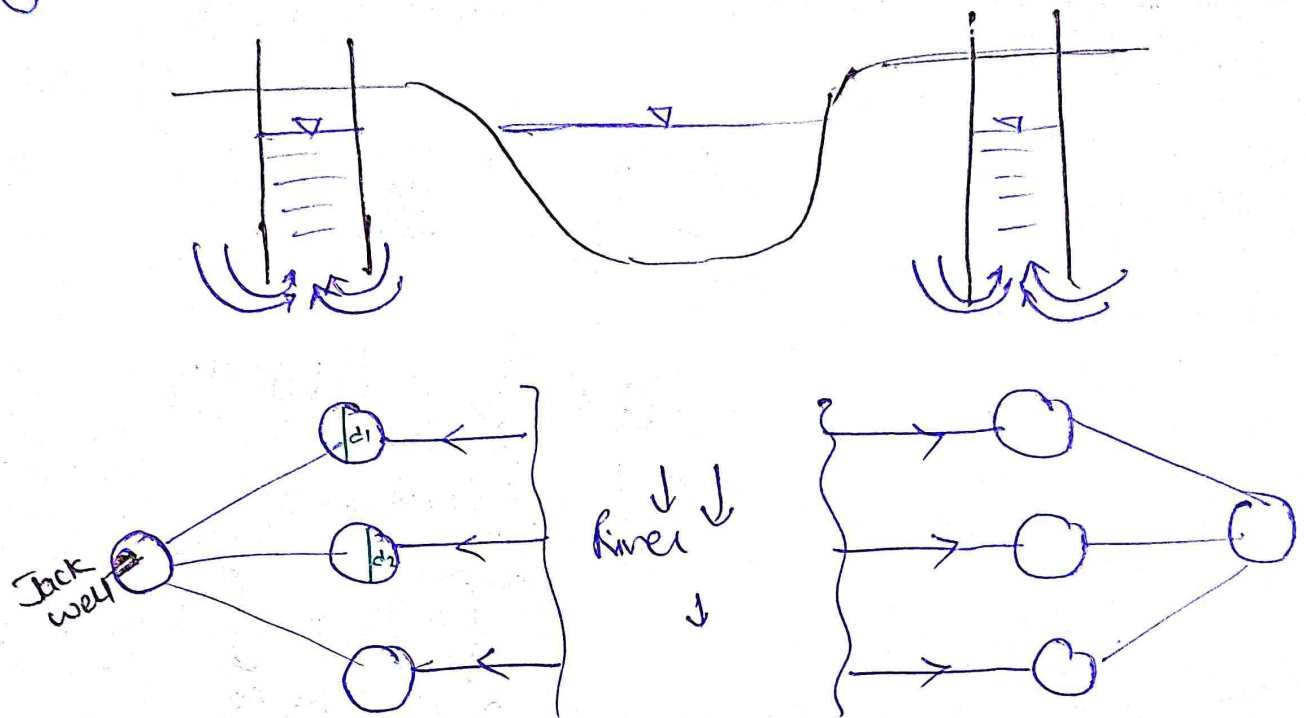
$$Q = A_{avg} \times V_{avg}^{ki}$$

$$= \left(\frac{H L + h_0 L}{2} \right) \frac{K (H - h_0)}{R} = \frac{K L (H^2 - h_0^2)}{2R}$$

② Infiltration well.

Infiltration wells are shallow discontinuous constructed along the bank of the river through which the water is utilised by seepage from bottom.

→ Several such infiltration wells are connected through a common well known as Jack well from where water being pumped into the treatment plant.

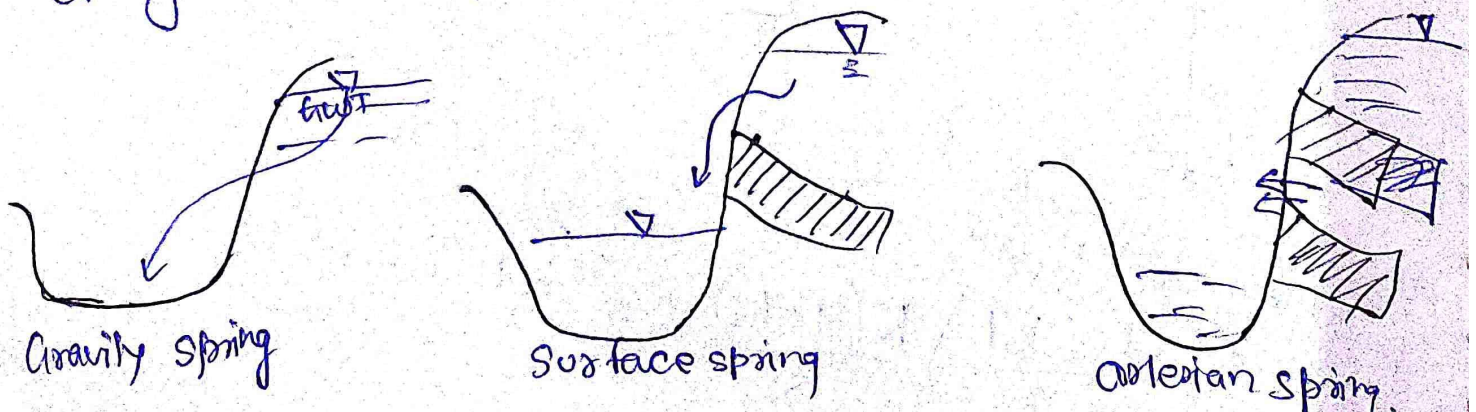


$$L = (d_1 + d_2 + d_3 + \dots + d_n)$$

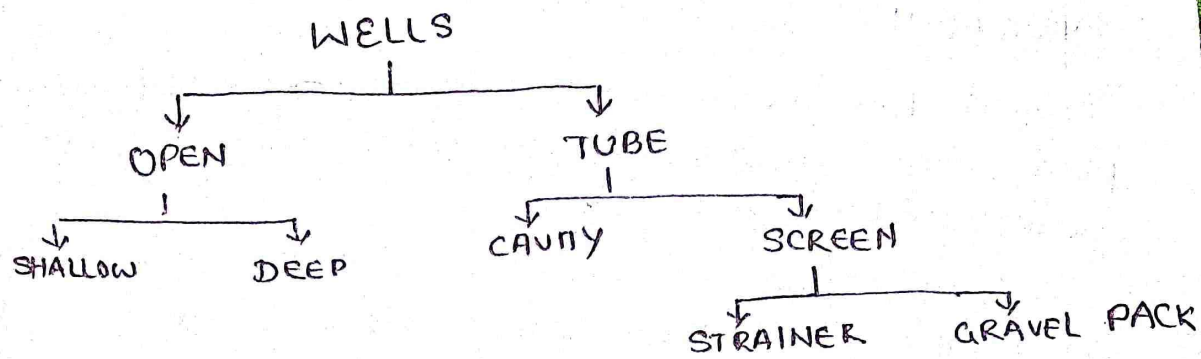
3) Springs.

Natural out of flow of ground water ~~at~~ over the ground surface is termed as spring.

→ only artesian spring are considered as the potential source of ground water { since water flow under pressure? }



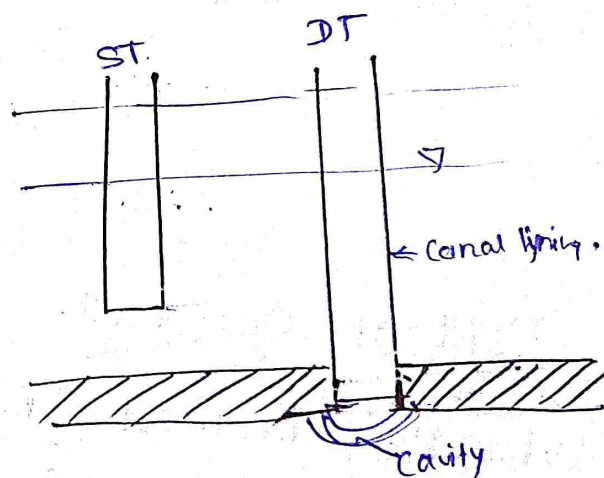
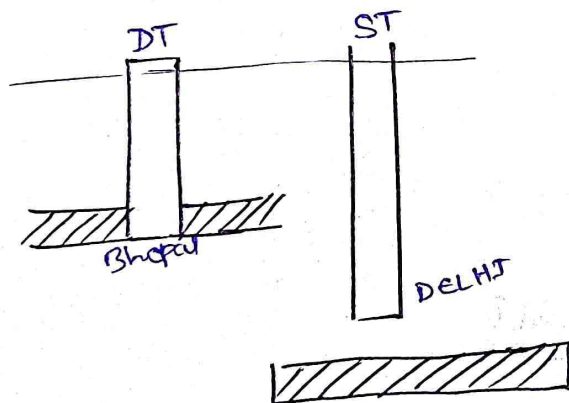
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	OW (2-5)m	TW (20cm)
Dia -	↑	↓
depth -	↓	↑
Discharge -	↓↓	↑↑↑

SHALLOW WELL :- are those which derive water from upper water bearing strata.

DEEP WELL :- derive water from lower water bearing strata.



	ST	DT
Quality	Poor	better.
Quantity	less	More.

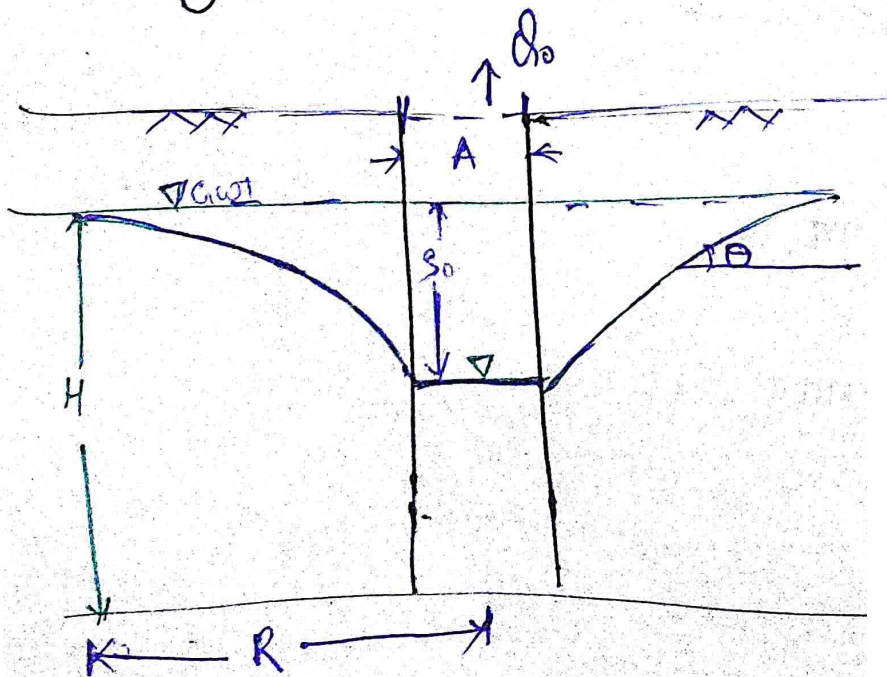
Open Well

Shallow type open wells are those which utilize water from upper water bearing strata. that is liable to be contaminated to higher extent.

- Discharge from the shallow well is also very limited as if the discharge through those wells is increased critical velocity & settling velocity of medium particle may also lead to the removal of medium particle along with the flowing water and if this process continuous it may also lead to the sinking of the well into the medium.
- However this process is not observed in deep type wells as they derive their support from the lower impermeable layer but cavity is formed at the bottom of these wells due to the removal of the medium particle along with following water.

Yield of Open well.

(1) Pumping method {field test}



$[V_0, t_0, S_0]$
 Volume time depression.

$v = \text{velocity}$

$$[S_0 = H - h_0]$$

$$Q_0 = \frac{V_0}{t_0} \quad \text{--- (i)}$$

$$Q_0 = A v$$

$$Q_0 = A K i$$

$$= A K \frac{S_0}{R}$$

$$Q_0 = \frac{K}{R} A S_0$$

$$\boxed{\frac{K}{R} = C \cong \text{constant}}$$

$$Q_0 = C A S_0$$

$$\boxed{C = \frac{Q_0}{A S_0}}$$

$C = \text{Specific capacity of open well (m}^3/\text{m}^2/\text{m/sec or sec}^{-1})$

$$Q = C A S$$

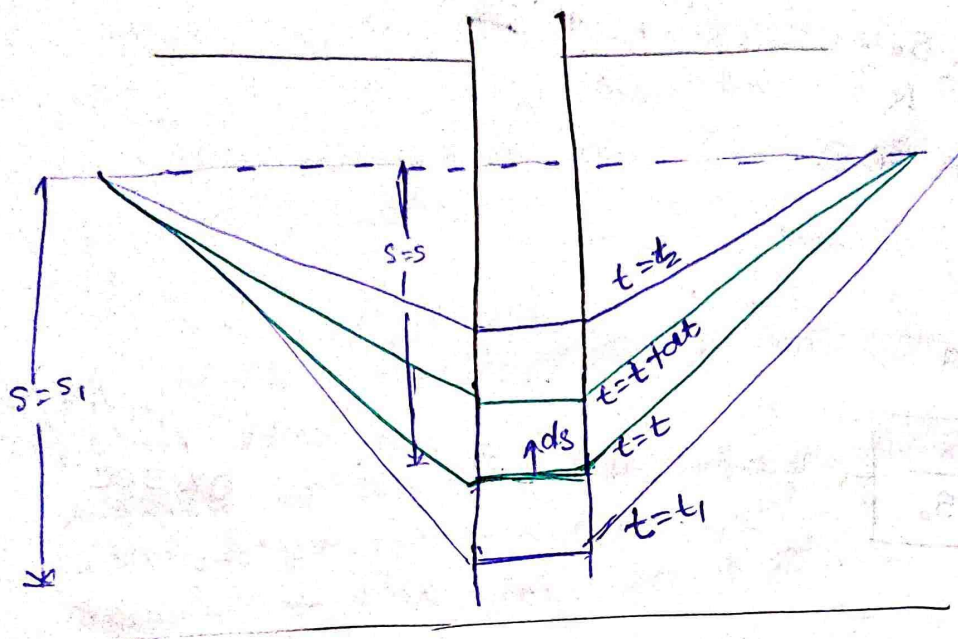
$$Q = \left(\frac{Q_0}{A S_0} \right) A S$$

Drawback: Not use for unsteady state.

$\rightarrow$ Discharge constant

(ii) RECUPERATION TEST

As it is difficult to maintain constant level (steady state) of water in well recuperation test is being performed in order to find the specific capacity of the well in which level of water recuperated in the well well in a given time is noted in order to find its yield.



Volume of water recuperated in well in time dt .

$$dv = -Q dt = +A ds \quad \begin{matrix} (+ \text{ increasing}) \\ (- \text{ decreasing}) \end{matrix}$$

$$-CAs dt = A ds$$

$$C dt = -\frac{ds}{s}$$

$$C \int_{t=t_1}^{t=t_2} dt = - \int_{s=s_1}^{s=s_2} \frac{ds}{s}$$

$$C [t]_{t_1}^{t_2} = \left| \ln s \right|_{s_2}^{s_1}$$

$$C (t_2 - t_1) = \ln(s_1/s_2)$$

$$C = \frac{\ln(s_1/s_2)}{t} = \frac{2.303 \log_{10}(s_1/s_2)}{t} \quad (m^3/m^2/m/sec)$$

As change in s

I	II
10	10
8	12
$\frac{10}{8}$	$\frac{12}{10}$

let $t_1 - t_2 = t$

$$1 \text{ liter} = 10^{-3} \text{ m}^3$$

$$Q' = C A S'$$

$$= \left(\frac{2.303 \log_{10} (s_1/s_2)}{t} \right) A S'$$

Q During a recuperation test water is pumped upto 3m and it recuperated by 1.1m in 90 minutes. find the size of well to yield 10 liters/second under depression head of 2.5m.

$$Q' = 10 \text{ liters/second}$$

$$= 10 \times 10^{-4} / \text{s} \text{ m}^3/\text{s}$$

$$s_1 = 3 \text{ m}$$

$$s_2 - s_1 = 1.1$$

$$s = 3 - 1.1 = 1.9$$

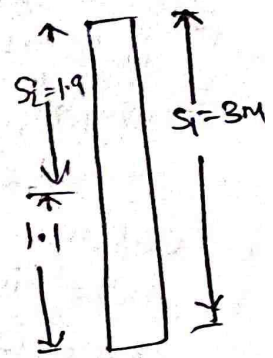
$$t = 90 \text{ min}$$

$$Q' = \left(\frac{2.303 \log_{10} (s_1/s_2)}{t} \right) A S'$$

$$10 \times 10^{-3} = \frac{2.303 \log_{10} \left(\frac{3}{3-1.1} \right)}{90 \times 60} \times \frac{\pi}{4} d^2 \times 2.5$$

$$d^2 = 60.20$$

$$d = 7.75$$



Q Water is pumped from a fine sand aquifer region at a rate of 12 lit/s find size of the well to give the required yield. at the draw down of 2m take $\frac{C'}{A} = 0.06 \text{ m}^3/\text{hr} \cdot \text{m}^2 \cdot \text{m}$.

$$Q = 12 \text{ lit/s} = 12 \times 10^{-3} \text{ m}^3/\text{s}$$

1% specific capacity
= C

$$Q' = C A S'$$

$$12 \times 10^{-3} = \frac{0.06}{60 \times 60} \times \frac{\pi d^2}{4} \times 2 \text{ m}$$

$$d = 21.4 \text{ m}$$

TUBE WELL

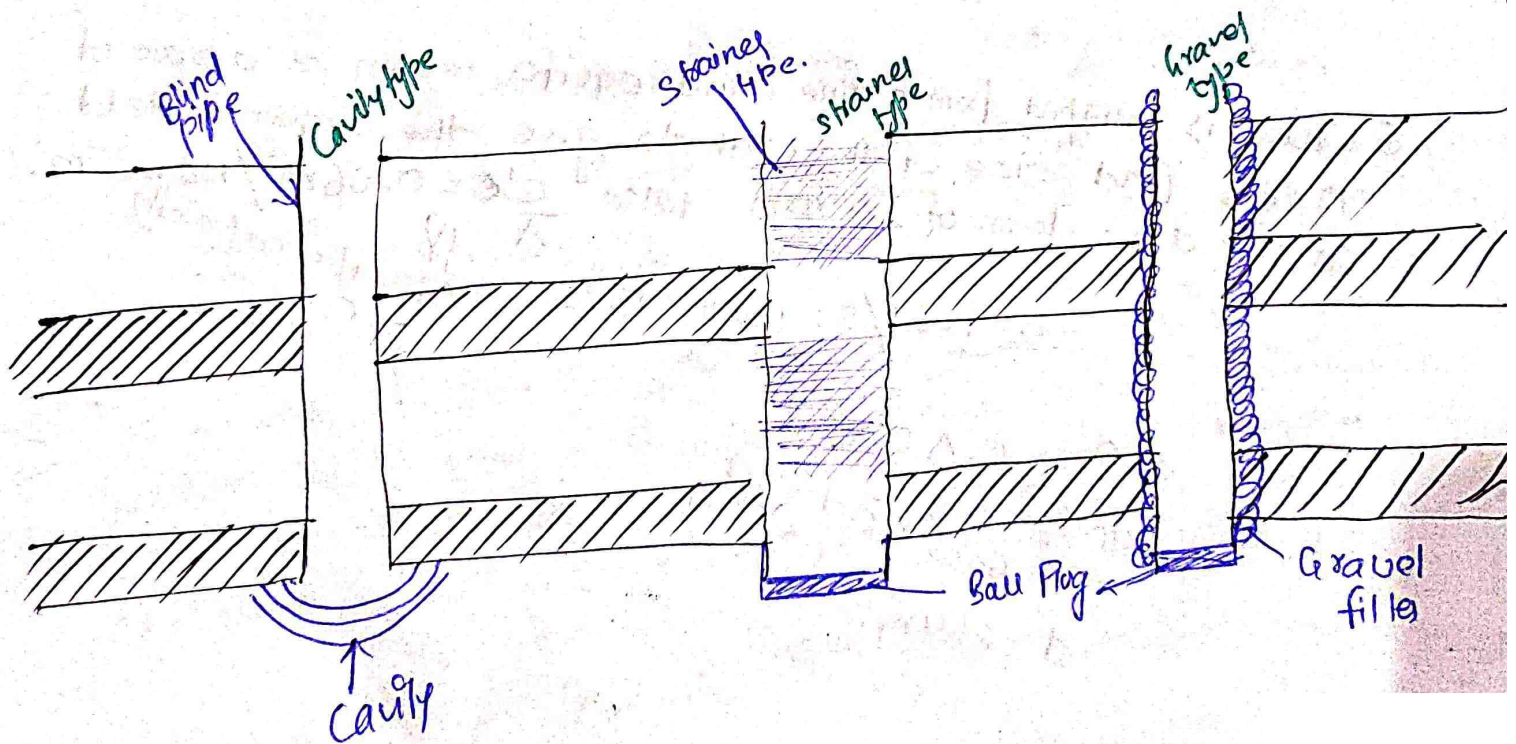
Discharge from the open well is limited in the range of 5-10 lit/sec whenever discharge from tubewell extends upto 200-220 lit/sec as they derive their water from depth or 70-300 m.

→ Gravity type tubewell are those tubewell which utilize the water from the bottom.

→ Whereas screen type tubewell are those which utilise water from the surface.

→ In order to prevent the entry of the medium particles into the well along with the flowing water screens are used & gravel pack type tubewell.

capacity of well will reduce if medium particles will inters into the screen type well not in cavity type since there is no option of sedimentary of particles in cavity type.



Q what is the strainer length required for a tube well giving a discharge of 8 l/s ? Assume permissible entrance velocity of ~~20~~ 2 m/s . It is desired to have the strainer of slot $20 \text{ mm} \times 0.2 \text{ mm}$ with no. of slots per cm of the strainer as 100.

$$Q = A_s \times V$$

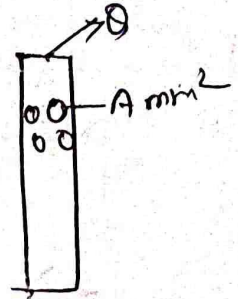
$$A_s = \frac{Q}{V} = \frac{8 \times 10^{-3}}{2 \times 10^{-2}}$$

$$A_s = 0.4 \text{ m}^2$$

$$A_s = n A_{s1}$$

$$0.4 = L \times 10^4 \times (20 \times 0.2) 10^{-6}$$

$$L = 10 \text{ m}$$



$$1 \text{ cm} = 100$$

$$1 \text{ m} = 100 \times 100$$

Yield of Tube Well

① DUPUIT'S theory

② Thiem's theory.

! Unconfined Aquifer:-

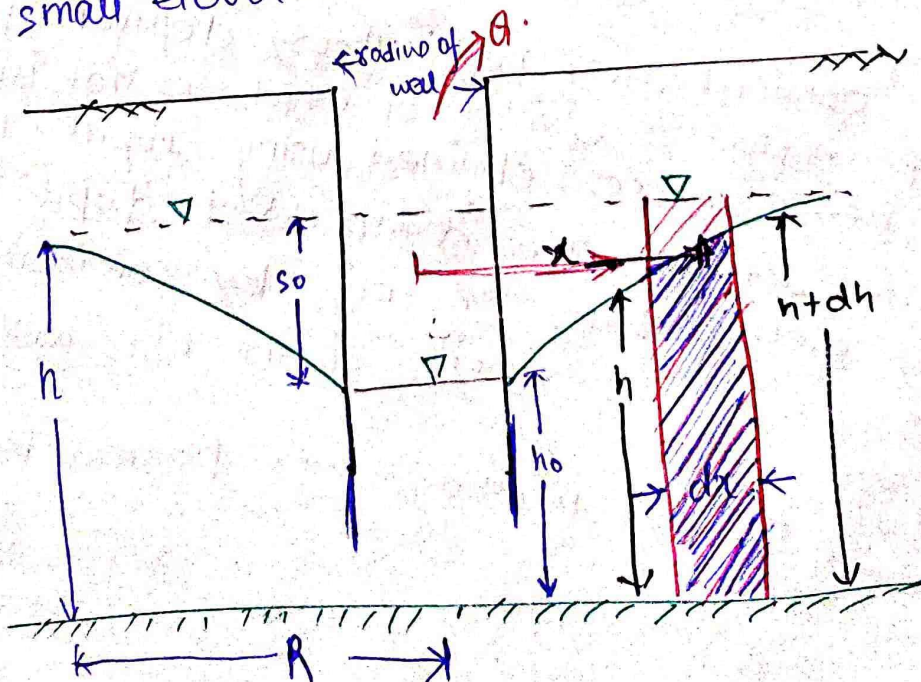
Dupuit's theory:-

Assumptions:-

(i) Medium is homogenous, isotropic, infinite.

(ii) Flow is radial, horizontal and laminar in the vicinity of the well.

(iii) for small elevation [water surface] $\sin \theta = \tan \theta$.



$$q_x = Q_x V_x \\ = (2\pi x h) K \frac{dh}{dx}$$

$$Q = \int q_x = \int 2\pi x h \frac{dh}{dx}$$

$$\Rightarrow Q \int_{x=r_w}^{x=R} \frac{dx}{x} = \int_{h=h_0}^{h=H} 2\pi h dh$$

$$\Rightarrow Q \left[\ln x \right]_{r_w}^R = 2\pi K \left[\frac{h^2}{2} \right]_{h_0}^H$$

$$\Rightarrow Q = \frac{2\pi K (H^2 - h_0^2)}{2.303 \log_{10} (R/r_w)}$$

$$\Rightarrow Q = \frac{\pi K (H^2 - h_0^2)}{2.303 \log_{10} (R/r_w)}$$

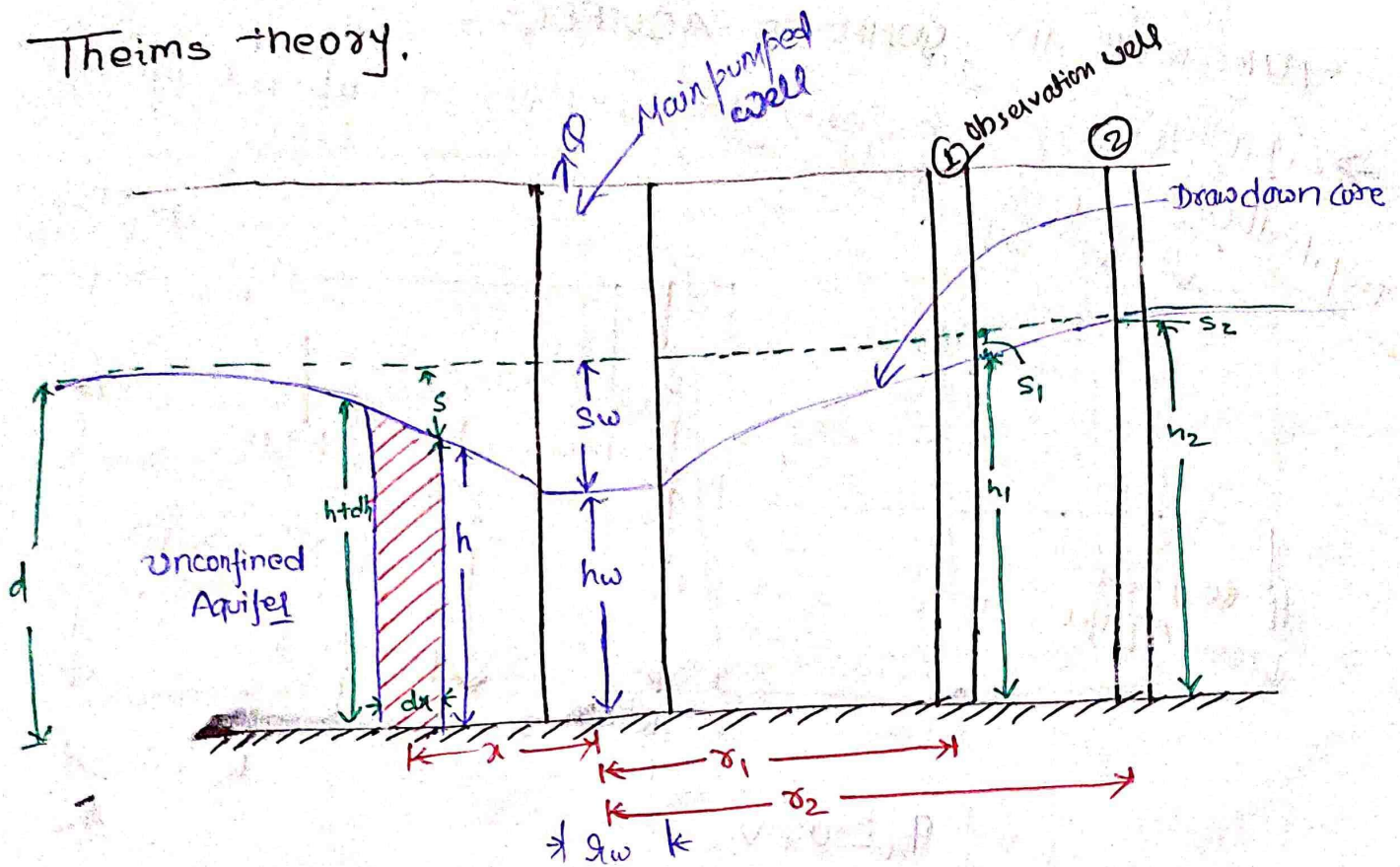
$$R = 150 - 300 \text{ m.}$$

$$\text{Schidout } e q^n = \frac{R}{(m)} = 3000 \frac{S \sqrt{K}}{(m)} \text{ m/sec.}$$

$S = \text{draw down due to correction to constant discharge.}$

Note:- Discharge obtained using Dupit's theory depend upon radius of influence value of which is not known precisely hence stresses obtained using Dupit's theory deviates from actual. This drawback of Dupit's theory was further eliminated by Thiem's by considering two observation well in the vicinity of the test well to the drawback. Corresponding a particle discharge being pumped from the test well.

Theims theory.



$$q_x = a_x \times v_x = (2\pi x h) K i_x$$

$$= (2\pi x h) K \cdot \frac{dh}{ds}$$

($\sin 0 = \tan 0$)
 $\frac{dh}{ds} = \frac{dn}{dx}$

$$\Rightarrow q_x = (2\pi x h) K \cdot \frac{dh}{dx}$$

$$\Rightarrow Q = \int q_x = \int 2\pi x h \frac{dh}{dx}$$

$$\Rightarrow \int_{r_w}^{r_1} \frac{dx}{x} = 2\pi K \int_{h_w}^{h_1} h dh$$

$$\Rightarrow Q \ln x \Big|_{r_w}^{r_1} = 2\pi K \left[\frac{h^2}{2} \right]_{h_w}^{h_1}$$

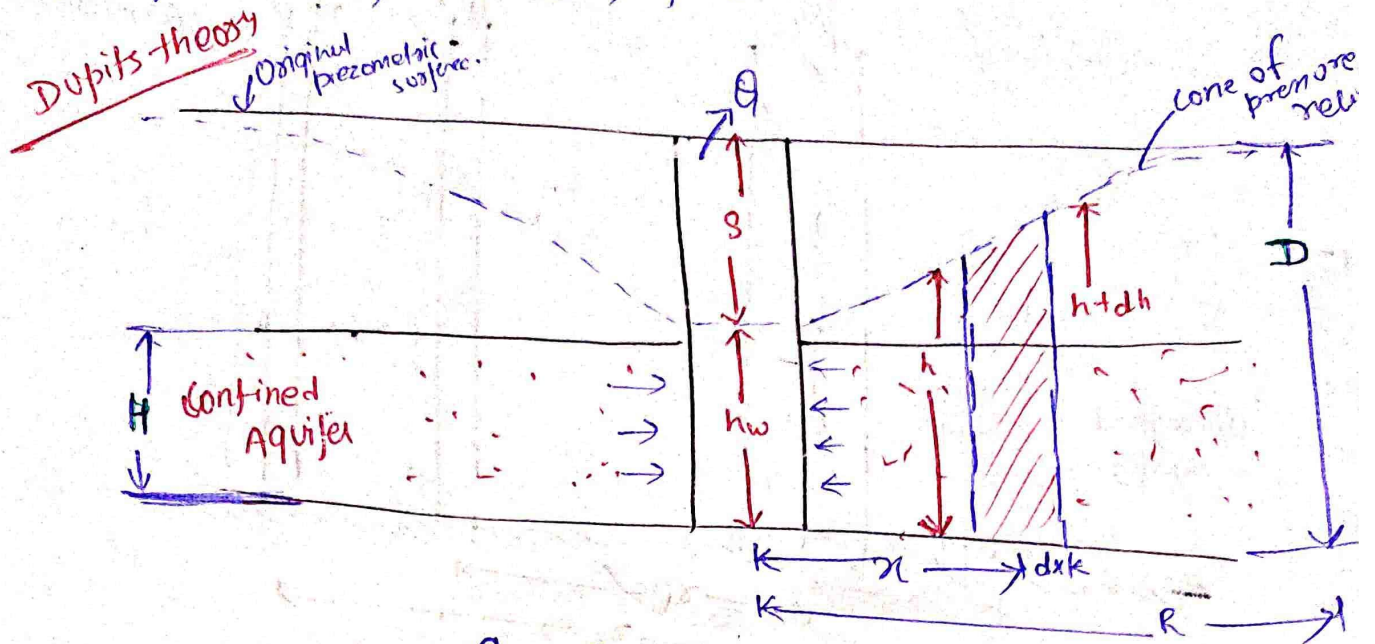
$$\Rightarrow Q = \frac{\pi K [h_1^2 - h_w^2]}{2.303 \log_{10} \left(\frac{r_1}{r_w} \right)}$$

$$\text{or, } Q = \frac{\pi K [h_2^2 - h_1^2]}{2.303 \log_{10} \left(\frac{r_2}{r_1} \right)}$$

$$\text{or } Q = \frac{\pi K [h_2^2 - h_1^2]}{2.303 \log_{10} \left(\frac{r_2}{r_1} \right)}$$

TUBE WELL IN CONFINED AQUIFER: -

→ Dupit's theory was only proposed for unconfined aquifer



$$Q_x = a_x V_x$$

$$= 2\pi x H k i$$

$$= 2\pi x H k \frac{dh}{dx}$$

$$Q = \int_{x=R} Q_x = \int_{x=R} 2\pi x H k \frac{dh}{dx}$$

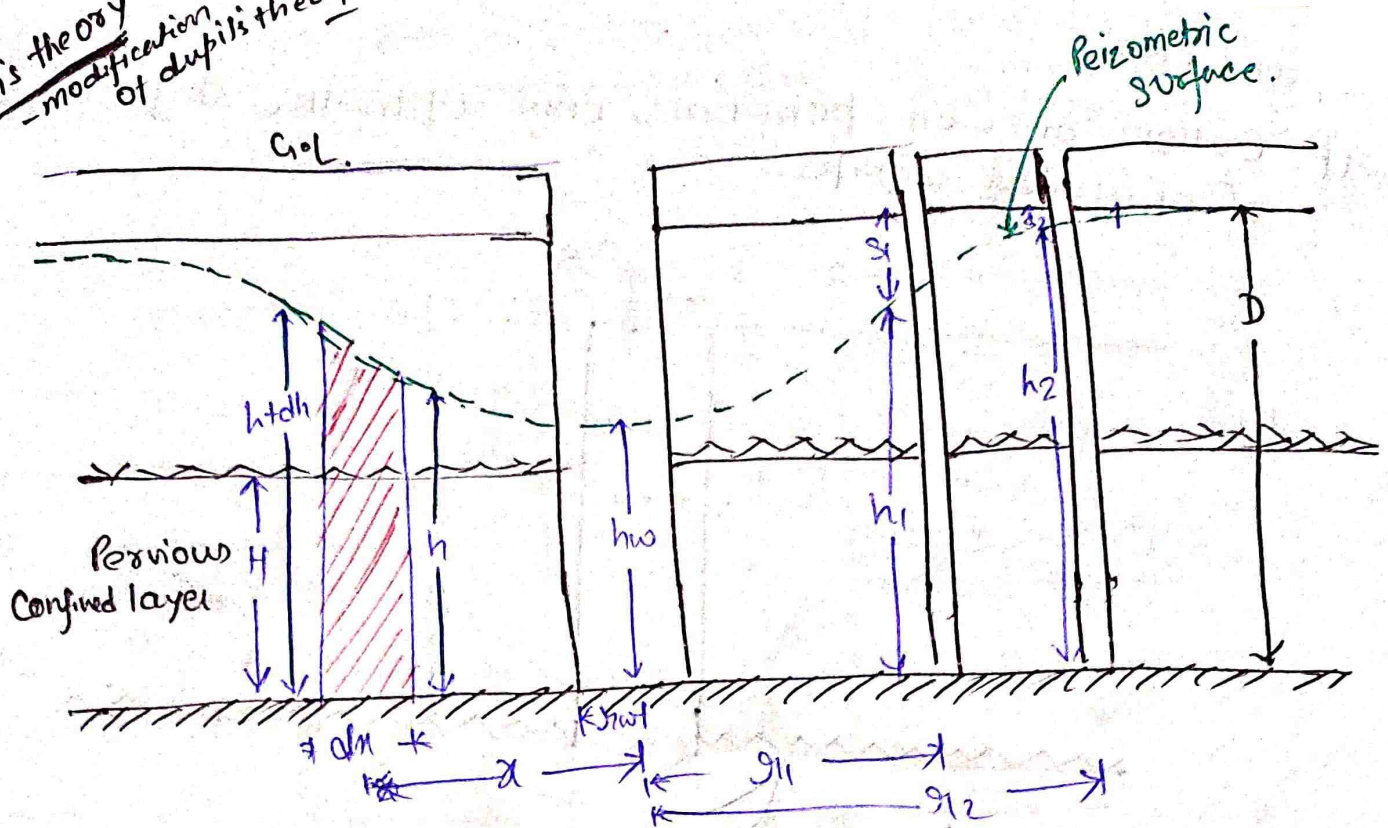
$$Q \int_{x=R} \frac{dx}{x} = \int_{h=h_w}^{h=D} 2\pi k H dh$$

$$Q |\ln x|_{x=R}^{x=r_w} = 2\pi k H [H]_{h_w}^D$$

$$Q = \frac{2\pi k H (D - h_w)}{2.303 \log_{10} \left(\frac{R}{r_w} \right)}$$

$kH = \text{transmissibility}$

Thiem's theory
- modification of Dupuit's theory.



$$q_r = q_r V_r$$

$$= (2\pi r H) K i_r$$

$$= (2\pi r H) K \frac{dh}{dr}$$

$$\Rightarrow Q = \int q_r = \int 2\pi r H K \frac{dh}{dr}$$

$$\Rightarrow Q \int \frac{dr}{r} = \int 2\pi H K dh$$

$r = r_w$ $h = h_w$

$$\Rightarrow Q \left[\ln r \right]_{r_w}^{r_1} = 2\pi H K [h]_{h_w}^{h_1}$$

$$\Rightarrow Q = \frac{2\pi H K [h_1 - h_w]}{2.303 \log_{10} \left(\frac{r_1}{r_w} \right)}$$

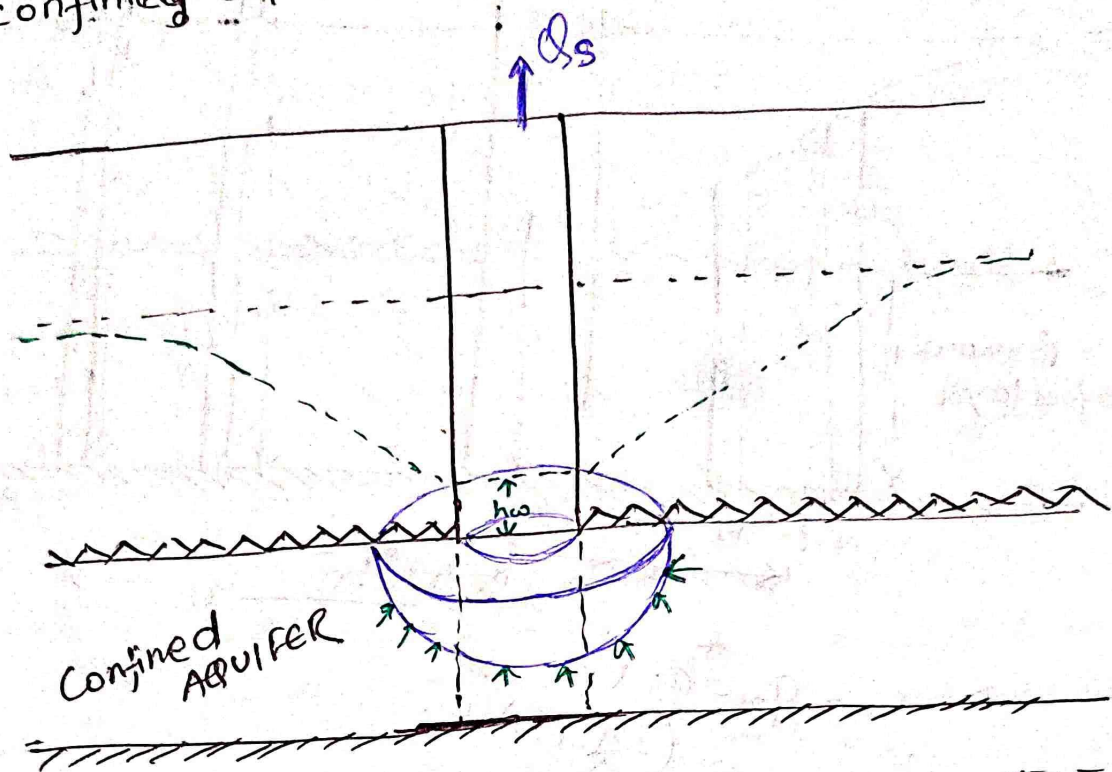
or,

$$Q = \frac{2\pi H K [h_2 - h_w]}{2.303 \log_{10} \left(\frac{r_2}{r_w} \right)}$$

$$Q = \frac{2\pi H K [h_2 - h_1]}{2.303 \log_{10} \left(\frac{r_2}{r_1} \right)}$$

Special case.

21f Bottom of well penetrates only upto the top surface of confined aquifer.



$$Q_s = A \cdot V$$

$$= (2\pi r_w^2) K i$$

$$= 2\pi r_w^2 \cdot K \cdot \frac{S_0}{r_w}$$

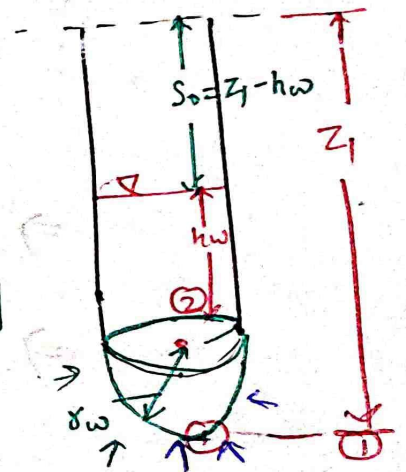
~~$$Q_s = 2\pi r_w K S_0$$~~

$$Q = 2\pi r_w K S_0$$

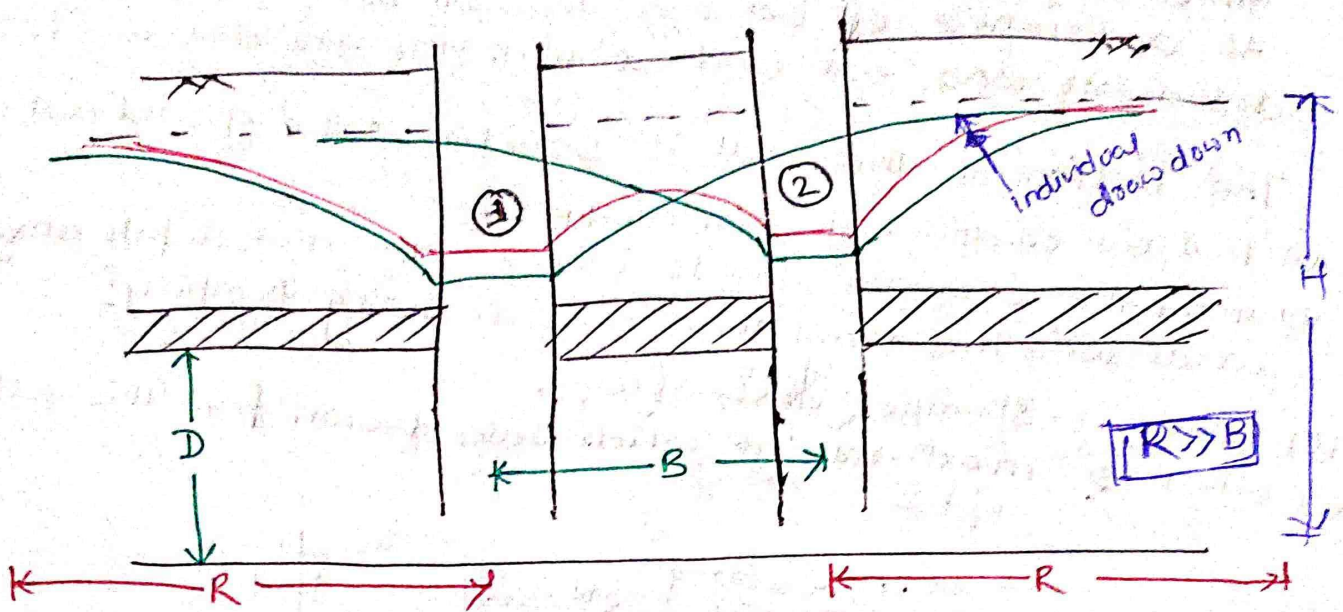
$$Q_R = \frac{2\pi K H (D - h_w)}{2.303 \log_{10} (R/r_w)}$$

$$Q_R = \frac{2\pi K H S_0}{2.303 \log_{10} (R/r_w)} \quad (i)$$

$$Q_s = \left(\frac{1}{20} \text{ to } \frac{1}{30} \right) Q_R$$



If two wells are situated nearby to each other such that their draw down interfere within the radius of influence.



$$Q_1 = Q_2 = Q_T = \frac{2\pi KD(H-h_w)}{2.303 \log_{10}(R/r_w)}$$

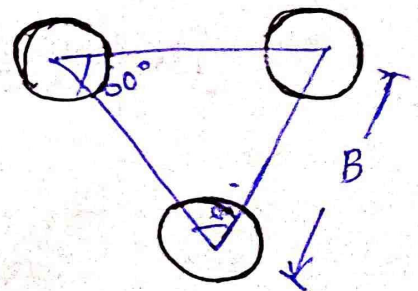
$$Q_1' = Q_2' = \frac{2\pi KD(H-h_w)}{2.303 \log_{10}\left(\frac{R^2}{r_w B}\right)} < Q_1 = Q_2$$

$$Q_T' = Q_1' + Q_2' > Q_T$$

③ $Q_1'' = Q_2'' = Q_3'' = \frac{2\pi KD(H-h_w)}{2.303 \log_{10}\left(\frac{R^3}{r_w B^2}\right)}$

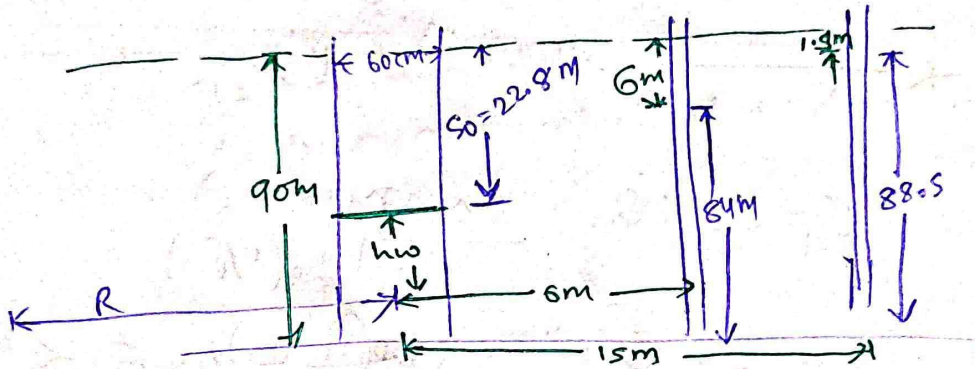
$$Q_1'' = Q_2'' = Q_3'' < Q_1' = Q_2' < Q_1 = Q_2$$

$$Q_T'' = Q_1'' + Q_2'' + Q_3'' > Q_T' > Q_T$$



Q A 60cm dia well is pumped at a rate of 1360 l/m. Measurement in a nearby test well are made at the time as follow:-
At a distance of 6m from the well being pumped, the drawdown was 6m and at 15m the drawdown was 1.5 m.
The bottom of the well is 90m below the ground water table.

- Find out coefficient of permeability.
- If all the observed points where one the dupils ~~care~~ ^{care}, what was the draw down in well, during pumping?
- What is specific ^{capacity} ~~gravity~~ of well.
- What is maxm rate at which water drawn from this well.



$$Q = 1360 \text{ l/min}$$
$$\frac{1360 \times 10^{-3} \text{ m}^3/\text{s}}{60}$$
$$= 0.0226 \text{ (1)}$$

$$Q = \frac{\pi K [h_2^2 - h_1^2]}{2.303 \log_{10} \left(\frac{g_2}{g_1} \right)}$$

$$\frac{1360 \times 10^{-3}}{60} = \frac{\pi K [88.5^2 - 84^2]}{2.303 \log_{10} \left(\frac{15}{6} \right)}$$

$$K = 8.51 \times 10^{-6} \text{ m/sec.}$$

$$91w = \frac{60}{2}$$
$$= 30 \text{ cm}$$
$$= 0.3$$

$$Q = \frac{\pi K [h_1^2 - h_w^2]}{2.303 \log_{10} \left[\frac{r_1}{r_w} \right]}$$

$$\frac{1360 \times 10^{-3}}{60} = \frac{\pi \times 8.51 \times 10^{-6} \times [84^2 - h_w^2]}{2.303 \times \log_{10} \left[\frac{6}{0.3} \right]}$$

$$8540326 = 84^2 - h^2$$

$$h_w = 67.198$$

drawdown = 22.80

W

for, $Q = Q_{sc} \Rightarrow S_0 = 1 \text{ m}$

$h_w = H - S_0 = 90 - 1 = 89 \text{ m}$

By Dupuit's theory.

$$Q = \frac{\pi K (H^2 - h_w^2)}{2.303 \log_{10} (R/r_w)}$$

$$\frac{1360 \times 10^{-3}}{60} = \frac{3.14 \times 8.51 \times 10^{-6} [90^2 - 67.22^2]}{2.303 \log_{10} (R/0.3)}$$

$R = 20.5 \text{ m}$

$$Q_{sc} = \frac{\pi K (H^2 - h_w^2)}{2.303 \log_{10} (R/r_w)}$$

$$= \frac{\pi \times 8.51 \times 10^{-6} (90^2 - 89^2)}{2.303 \log_{10} (20.5/0.3)}$$

$Q_{sc} = 1.13 \times 10^{-3} \text{ m}^3/\text{sec}$

or $Q_{sc} = \frac{Q}{S} = \frac{\frac{1360 \times 10^{-3}}{60}}{22.78} = 9.9 \times 10^{-4} \text{ m}^3/\text{sec}$

(50)

Non-Equilibrium flow [Unsteady flow]

Theis theory! → Gives the solution of this in terms of well function. $w(u)$

Well function → it is a complex integral which is used to find drawdown in well pumping.

$$w(u) = -0.5772 - \ln u + u + \text{higher } \rightarrow \text{neglected terms of } u$$

$$u = \frac{r^2 S}{4 T t}$$

S = storativity.

T = transmissibility.

t = time after which draw down is calculated in observation well.

$$s(t, r) = \frac{Q}{4 \pi T} \times \text{well function}$$

$$s(t, r) = \frac{Q}{4 \pi T} \times w(u)$$

As per Jacob's Modification,

$$w(u) = -0.5772 - \ln \left(\frac{r^2 S}{4 T t} \right)$$

$$w(u) = \ln \left(\frac{4 T t}{r^2 S} \right) - 0.5772$$

$$s(t, r) = \frac{Q}{4 \pi T} \left[\ln \left(\frac{4 T t}{r^2 S} \right) - 0.5772 \right]$$

Q Give the characteristic of different formation in which ground water exist. A fully penetrating artesian well is discharging at a rate of 25 l/s. The storage coefficient and transmissibility of the aquifer are 4.5×10^{-4} and $0.15 \text{ m}^2/\text{min}$ respectively. Find the drawdown at,

- A radius of 5m distance after 2 hours pumping.
- A radius 180m distance after 1 day pumping.

Using the following approximation well function,
 $w(u) = -0.5772 - \ln(u) + U$

$$U = \frac{\sigma^2 S}{4Tt}$$

① $s(5\text{m}, 2\text{hrs})$

$$U = \frac{5^2 \times 4.5 \times 10^{-4}}{4 \times 0.15 \times 2 \times 60} = 1.5625 \times 10^{-4}$$

$$\begin{aligned} w(u) &= -0.5772 - \ln(u) + U \\ &= -0.5772 - \ln(1.5625 \times 10^{-4}) + 1.5625 \times 10^{-4} \\ &= 8.187 \end{aligned}$$

$s(5\text{m}, 2\text{h})$

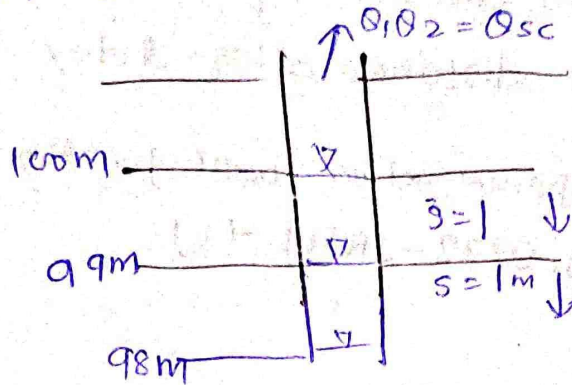
$$= \frac{Q}{4\pi T} w(u)$$

$$\begin{aligned} &= \frac{25 \times 10^{-3}}{4 \times \pi \times 0.15} \times 8.187 \\ &= 6.51 \text{ m} \end{aligned}$$

$$\textcircled{2} \quad s(\text{180m}, 24\text{hrs}) = 3.08$$

Specific Capacity of tube well.

- Rate of flow through the well per unit drawdown.
- It is calculated for initial 1st meter fall of height of water in well.
- And it is not same for all the unit drawdown.



Note:-

$$\begin{aligned}
 Q &= \frac{\pi K (H^2 - h_0^2)}{2.303 \log_{10} (R/r_w)} \\
 &= \frac{\pi K (H - h_0)(H + h_0)}{2.303 \log_{10} (R/r_w)} \\
 &= \frac{\pi K S_0 (H + h_0)}{2.303 \log_{10} (R/r_w)}
 \end{aligned}$$

$$\boxed{S_0 = C_1 Q} \quad \text{Aquifer loss.}$$

$$h_f = \frac{f l v^2}{2 g d} = \frac{f l Q^2}{2 g d A^2}$$

$$\boxed{S_w = C_2 Q^2} \quad \text{well loss.}$$

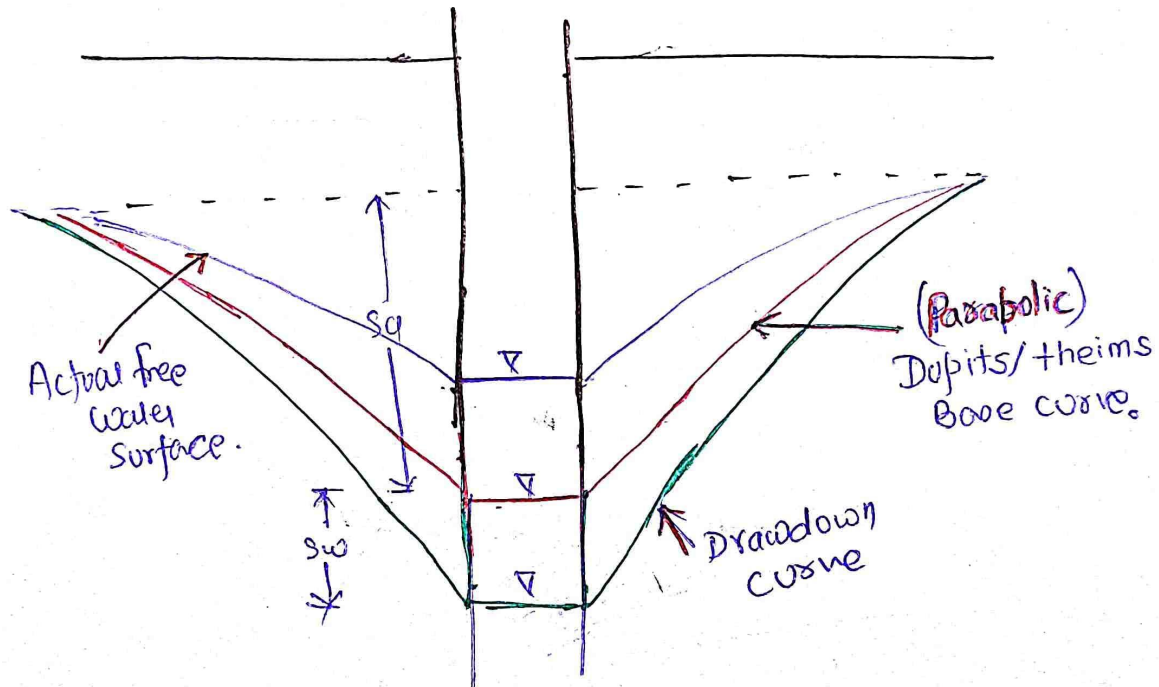
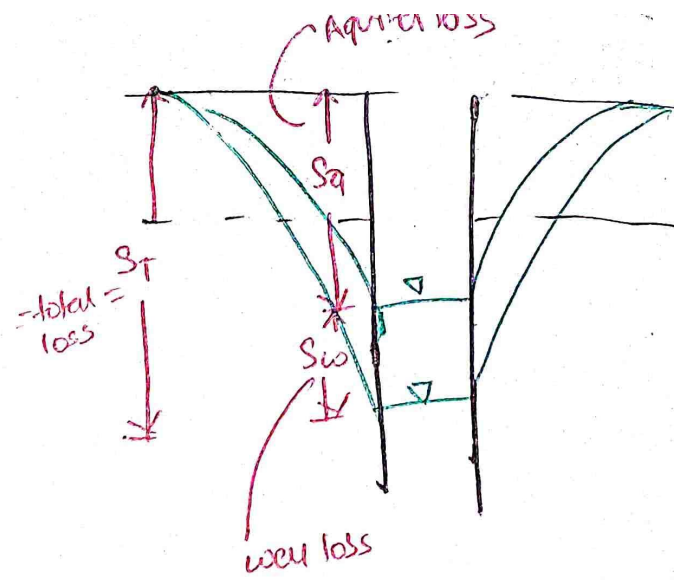
$$S_T = S_a + S_w = C_1 Q + C_2 Q^2$$

Specific capacity = $SC = \frac{Q}{S_T}$

$$= \frac{Q}{C_1 Q + C_2 Q^2}$$

$$SC = \frac{1}{C_1 + C_2 Q}$$

$$SC \propto \frac{1}{Q}$$



well development:- Quantity $\uparrow$, Quality $\uparrow$

