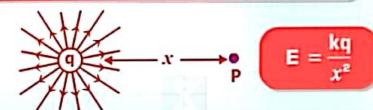


ELECTRIC FIELD

Electric Field due to Point Charge



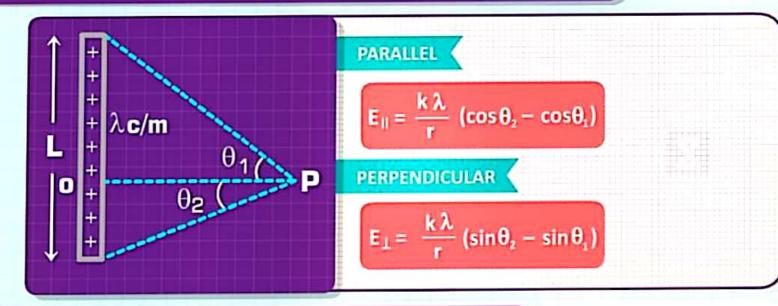
Vector Form
$$\vec{E} = \frac{kq}{x^3} \cdot \vec{x}$$

$$\mathbf{k} = \frac{1}{4\pi\varepsilon_0}$$

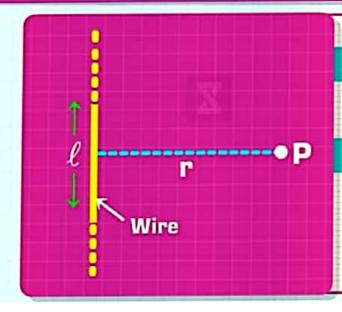
q = Charge ; x = Distance

If a charge qois placed at a point in electric field, it experiences a net force F on it, then electric field strength at that point can be $\vec{E} = \frac{F}{q_0}$

ELECTRIC FIELD DUE TO A UNIFORMLY CHARGED ROD



ELECTRIC FIELD DUE TO INFINITE WIRE (\$>>r)



Since
$$\ell >> r \implies \theta_1 = \theta_2 = 90^\circ$$

PERPENDICULAR

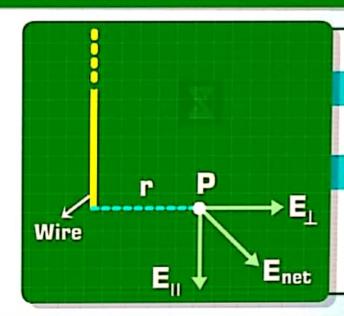
$$E_{\perp} = \frac{k\lambda}{r} \text{ (sin90°+ sin90°)} \Longrightarrow \left[E_{\perp} = \frac{2k\lambda}{r} \right]$$

PARALLEL

$$E_{II} = \frac{k\lambda}{r} (\cos 90^{\circ} - \cos 90^{\circ}) \Longrightarrow E_{II} = 0$$

At P,
$$E_{net} = E_{\perp} + E_{||}$$
 $E_{net} = \frac{2k\lambda}{r}$

ELECTRIC FIELD DUE TO SEMI INFINITE WIRE



$$\theta_1 = 90^\circ$$
 , $\theta_2 = 0^\circ$

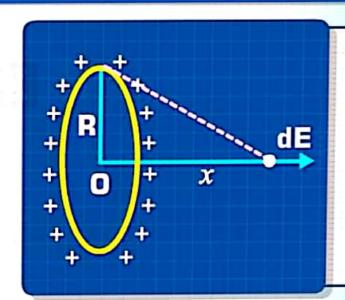
PERPENDICULAR

$$E_{\perp} = \frac{k\lambda}{r} (\sin 90^{\circ} + \sin 0^{\circ}) = \frac{k\lambda}{r}$$

PARALLEL

$$E_{\parallel} = \frac{k\lambda}{r} (\cos 0^{\circ} - \cos 90^{\circ}) = \frac{k\lambda}{r}$$

ELECTRIC FIELD DUE TO UNIFORMLY CHARGED RING

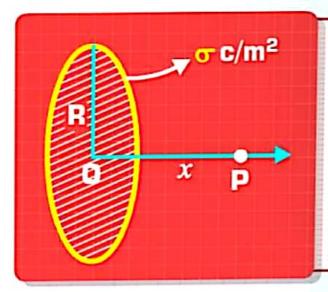


$$E = \frac{kQx}{(R^2 + x^2)^{3/2}}$$

For maxima,
$$x = \pm \frac{R}{\sqrt{2}}$$

$$E_{max} = \pm \frac{2}{3\sqrt{3}} \frac{kQ}{R^2}$$

ELECTRIC FIELD ON THE AXIS OF DISC



$$E = \frac{\sigma}{2\varepsilon_0} \left[1 - \frac{x}{\sqrt{x^2 + R^2}} \right]$$
 [along the axis]

If
$$x >> R$$

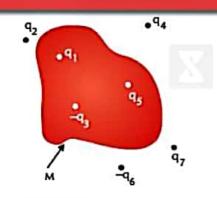
If
$$x << R$$

$$\mathbf{E} = \mathbf{0}$$

$$\mathbf{E} = \frac{\sigma}{2\epsilon_0} (1 - \mathbf{0}) = \frac{\sigma}{2\epsilon_0}$$

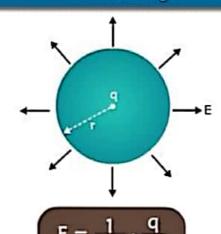
ELECTRIC FIELD STRENGTH

Gauss's Law

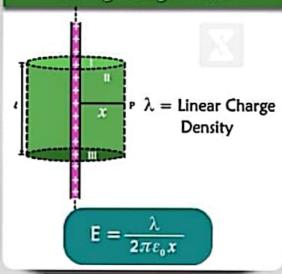


$$\oint \vec{E} \cdot d\vec{S} = \frac{q_1 + q_5 - q_3}{\epsilon_0}$$

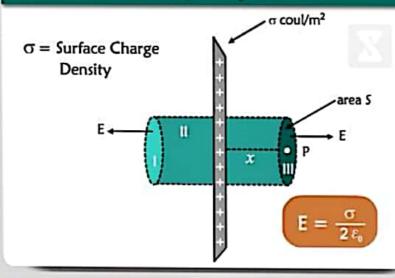
Electric Field due to a Point Charge



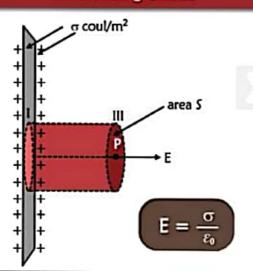
Electric Field Strength due to a Long Charged Wire



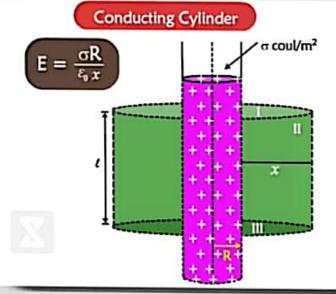
Electric Field Strength due to Non-Conducting Uniformly Charged Sheet



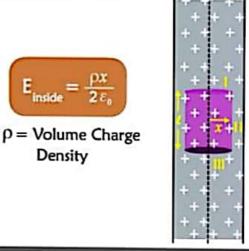
Electric Field Strength due to Charged Conducting Sheet



Electric Field Strength due to a Long Uniformly Charged Cylinder



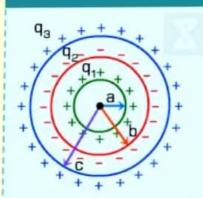
Uniformly Charged Non - Conducting Cylinder



Part IV GRAPH OF ELECTRIC FIELD DUE TO BINARY CHARGES 3 2 TE TE q **-**q **4**q (5) **(**1) †E ↑E q 4q **-q** 8 q -q

ELECTRIC POTENTIAL

POTENTIAL DUE TO CONCENTRIC SPHERES



At a point r > c

$$V = \frac{1}{4\pi\epsilon_0} \frac{q_1 - q_2 + q_3}{r}$$

At a point a < r < b

$$V = \frac{1}{4\pi\epsilon_0} \frac{q_1 - q_2 + q_3}{r} \qquad V = \frac{1}{4\pi\epsilon_0} \frac{q_1}{r} - \frac{1}{4\pi\epsilon_0} \frac{q_2}{b} + \frac{1}{4\pi\epsilon_0} \frac{q_3}{c}$$

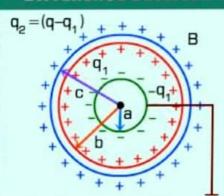
At a point b < r < c

$$V = \frac{1}{4\pi\varepsilon_0} \frac{q_1 - q_2}{r} + \frac{1}{4\pi\varepsilon_0} \frac{q_3}{c} \qquad V = \frac{1}{4\pi\varepsilon_0} \left[\frac{q_1}{a} - \frac{q_2}{b} + \frac{q_3}{c} \right]$$

At a point r < a

$$V = \frac{1}{4\pi\varepsilon_0} \left[\frac{q_1}{a} - \frac{q_2}{b} + \frac{q_3}{c} \right]$$

TWEEN TWO CONCENTRIC SPHERES WHEN ONE OF THEM IS EARTHED



$$V_{in} = \frac{1}{4\pi\epsilon_0} \left[-\frac{q_1}{a} + \frac{q_2}{b} \right]$$

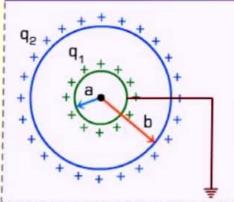
$$\frac{q_2}{c} = q_1 \left(\frac{1}{a} - \frac{1}{b} \right) \dots (i)$$
 $q_1 + q_2 = q \dots (ii)$

$$V_{in} = \frac{1}{4\pi\epsilon_0} \left[-\frac{q_1}{a} + \frac{q_2}{b} \right] \quad V_{out} = \frac{1}{4\pi\epsilon_0} \left[-\frac{q_1}{b} + \frac{q_2}{b} \right]$$

$$q_1 + q_2 = q(ii)$$

Solving (i) and (ii) we can get q1 and q2

ETWEEN TWO CONCENTRIC UNIFORMLY CHARGED METALLIC SPHERES

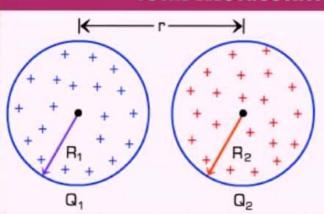


$$V_{in} = \frac{1}{4\pi\epsilon_0} \frac{q_1}{a} + \frac{1}{4\pi\epsilon_0} \frac{q_2}{b}$$

$$V_{in} = \frac{1}{4\pi\epsilon_0} \frac{q_1}{a} + \frac{1}{4\pi\epsilon_0} \frac{q_2}{b} \qquad V_{out} = \frac{1}{4\pi\epsilon_0} \frac{q_1}{b} + \frac{1}{4\pi\epsilon_0} \frac{q_2}{b}$$

$$\Delta V = V_{in} - V_{out} \implies \Delta V = \frac{q_1}{4\pi\epsilon_0} \left[\frac{1}{a} - \frac{1}{b} \right]$$

TOTAL ELECTROSTATIC ENERGY OF A SYSTEM OF CHARGES



$$U = \frac{3KQ_{1}^{2}}{5R_{1}} + \frac{3KQ_{2}^{2}}{5R_{2}} + \frac{KQ_{1}Q_{2}}{r}$$

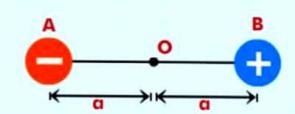
ELECTRIC DIPOLE

ELECTRIC DIPOLE

$$\vec{p} = q.2\vec{a}$$

SI unit: Coulomb - meter

It is a vector quantity



Direction of dipole moments (p) is from negative charge to positive charge

ELECTRIC FIELD ON AXIAL LINE OF AN ELECTRIC DIPOLE

$$E = \frac{1}{4\pi\varepsilon_0} \frac{2qa}{(r^2-a^2)^2}$$

For a<<r

$$\vec{E}_{axial} = \frac{1}{4\pi\epsilon_0} \frac{2\vec{p}}{r^3}$$

Eaxial is along the direction of dipole moment

ELECTRIC FIELD ON EQUATORIAL LINE OF AN ELECTRIC DIPOLE

$$E = -\frac{1}{4\pi\epsilon_0} \cdot \frac{q.2a}{(r^2-a^2)^{3/2}}$$

$$\vec{E}_{\text{equiatoral}} = -\frac{1}{4\pi\epsilon_0} \cdot \frac{\vec{p}}{r^3}$$

E_{equatorial} is along the opposite direction of dipole moment

DIPOLE IN A UNIFORM EXTERNAL ELECTRIC FIELD

VECTOR FORM

$$\vec{\tau} = \vec{p} \cdot \vec{E}$$

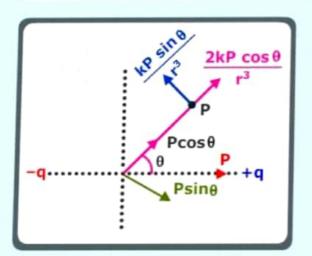
$$U = -pE \cos \theta$$

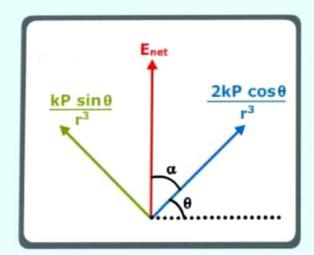
$$\theta = 0^{\circ}$$

$$U_{min}$$

$$U_{max}$$

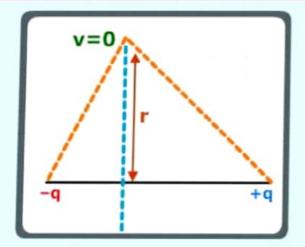
ELECTRIC FIELD AT A GENERAL POINT DUE TO A DIPOLE

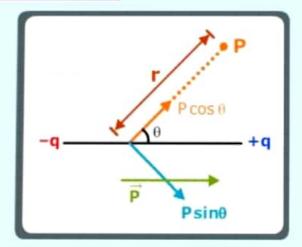




$$E_{net} = \frac{kP}{r^3} \, \sqrt{1 + 3 cos^2 \, \theta} \ , \ \tan \alpha = \frac{\tan \theta}{2} \quad ; \quad k = \frac{1}{4 \pi \epsilon_o}$$

ELECTRIC POTENTIAL DUE TO A DIPOLE





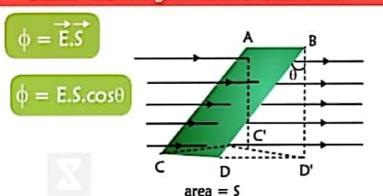
POTENTIAL AT 'P' DUE TO DIPOLE,
$$V_p = \frac{2kP \cos \theta}{r^2}$$

AT AN AXIAL POINT,
$$V_{net} = \frac{kp}{r^2}$$
 (As P = q.2a)

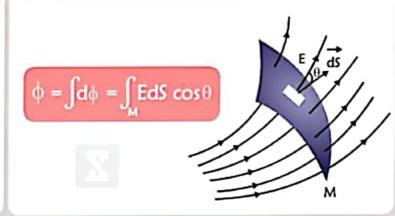
AT PERPENDICULAR BI-SECTOR, Vnet = 0

ELECTRIC FLUX

Electric Field Strength in terms of Electric Flux

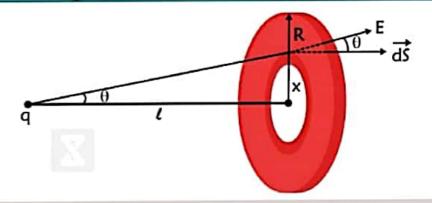


Electric Flux in Non-uniform Electric Field



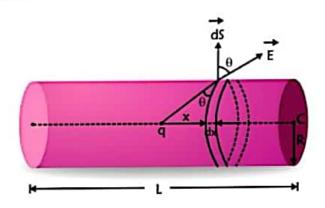
Electric Flux through a Circular Disc

$$\phi = \frac{q}{\epsilon_0} \left[1 - \frac{\ell}{\sqrt{R^2 + x^2}} \right]$$

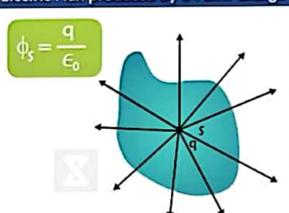


Electric Flux through the Lateral Surface of a Cylinder due to a Point Charge

$$\phi = \frac{q}{\epsilon_0} \cdot \frac{\ell}{\sqrt{R^2 + x^2}}$$



Electric Flux produced by a Point Charge



Flux Calculation in the Region of Varying Electric Field

