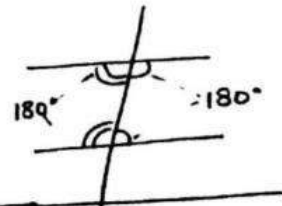
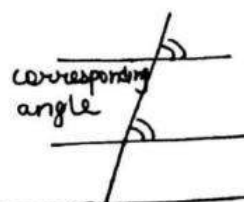
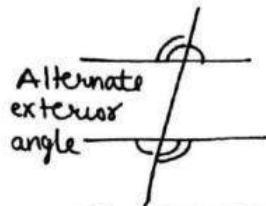
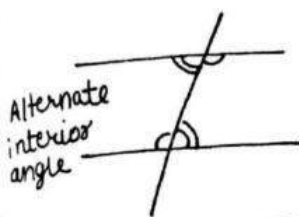
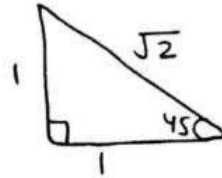
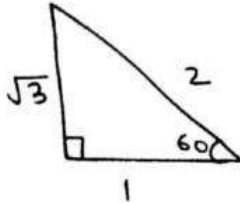
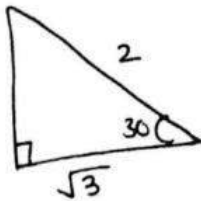


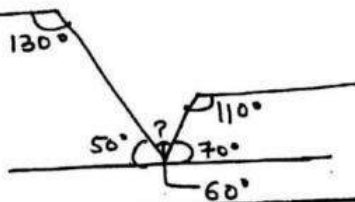
CLASS
48

GEOMETRY

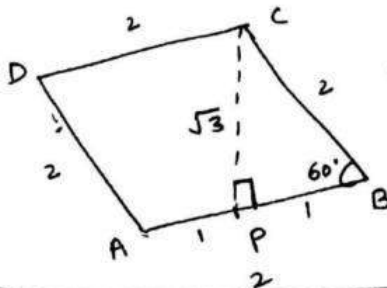
⑧



①

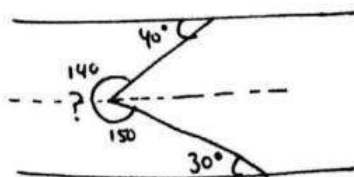


- ② A, B, C, D are the vertex of a Rhombus and P, Q, R, S are the mid points of AB, BC, CD & DA. find the largest angle of the rhombus? & $CP \perp AB$



$$\angle DAB = 180 - 60^\circ = 120^\circ$$

③



$$140 + 150 = 290^\circ$$

Rak... ..

03 | Advance Maths (Volume-2)

④

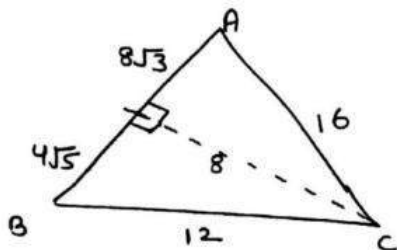
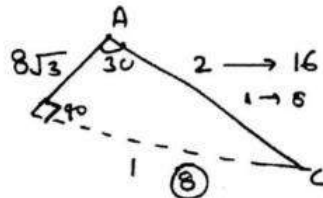
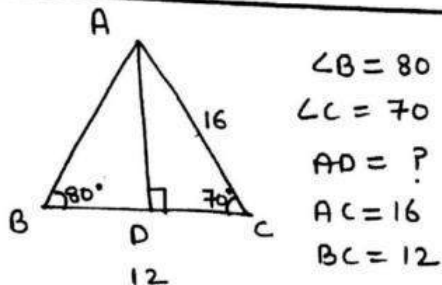


$$x + y + z = ?$$

$$180 - x + 180 - y = z$$

$$x + y + z = 360^\circ$$

⑤

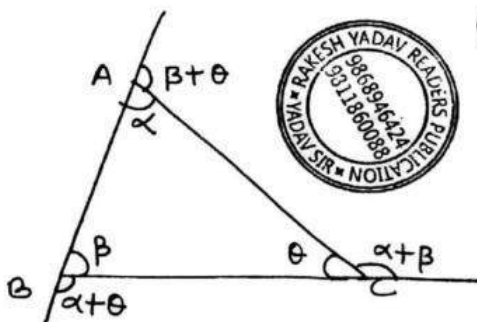


Area ($\triangle ABC$)

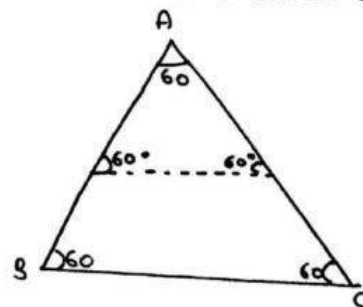
$$\frac{1}{2} (8\sqrt{3} + 4\sqrt{3}) \times 8 = \frac{1}{2} \times 12 \times AD$$

$$AD = \frac{2}{3} (8\sqrt{3} + 4\sqrt{3})$$

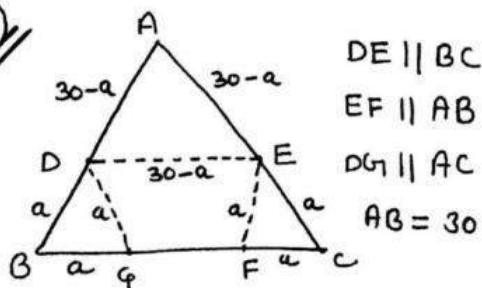
⑥



⑦



⑥



$$GD + DE + EF = 42$$

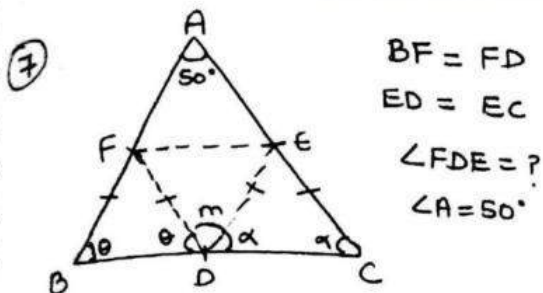
$$GF = ?$$

$$AB = BC = CA$$

$$30 - a + a = 42$$

$$a = 12$$

$$GF = 30 - 12 - 12 = 6 \text{ cm}$$



$BF = FE$
 $ED = EC$
 $\angle FDE = ?$
 $\angle A = 50^\circ$

$\angle A + \angle B + \angle C = 180^\circ$

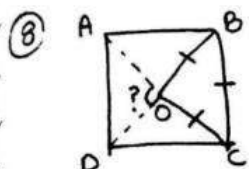
$50^\circ + \theta + \alpha = 180^\circ$

$\theta + \alpha = 130^\circ$

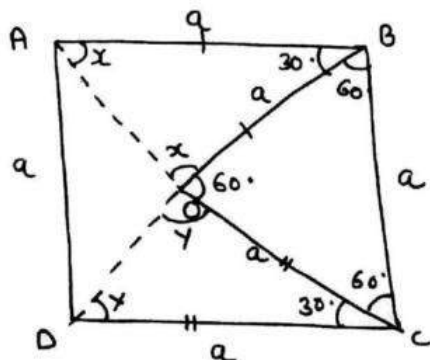
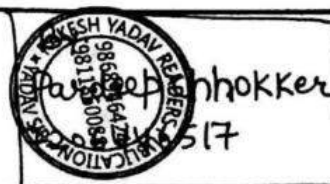
$\therefore \theta + \alpha + m = 180^\circ$

$130 + m = 180^\circ$

$m = 50^\circ$



$ABCD$ is a square.
 OBC is equilateral Δ
 find angle $\angle AOD$.



ΔABO

$x + x + 30^\circ = 180^\circ$

$x = 75^\circ$

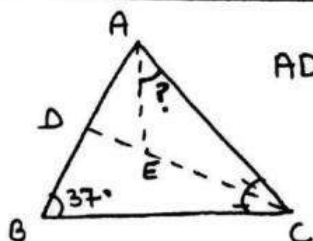
ΔCDO

$y = 75^\circ$

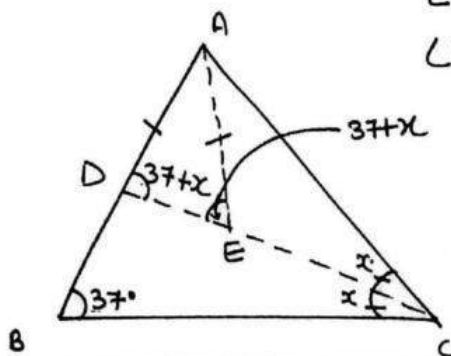
$\therefore \angle AOD = 75 + 75 + 60 + \angle AOD = 360$

$\angle AOD = 150^\circ$

⑨



$AD = AE$



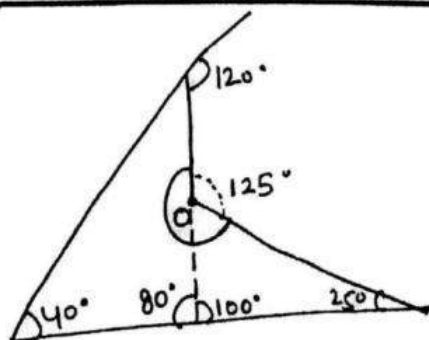
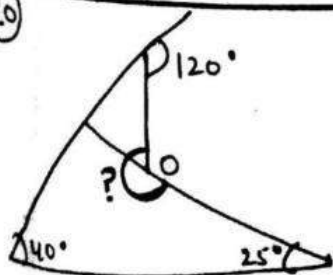
$\angle ADE = 37 + x$

$\angle AED = 37 + x$

$\downarrow$
 External angle
 of ΔACE

$\therefore \angle EAC = 37^\circ$

⑩

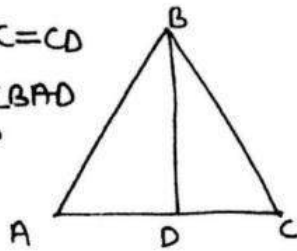


$360 - 125^\circ$
 $= 235^\circ$ Ans.

⑪ $BC = CD$

$\angle ABC - \angle BAD = 30^\circ$

$\angle ABD = ?$



$\angle B = \alpha, \angle A = \theta$

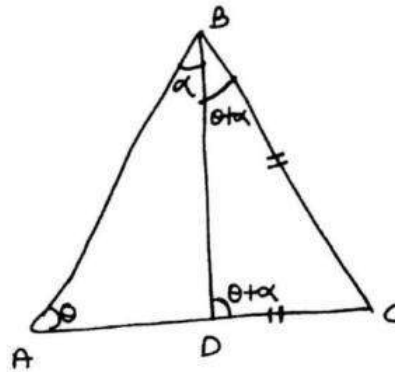
$\angle BDC = \theta + \alpha$

$\angle DBC = \theta + \alpha$

$\angle ABC - \angle BAD = 30^\circ$

$2\alpha + \theta - \theta = 30^\circ$

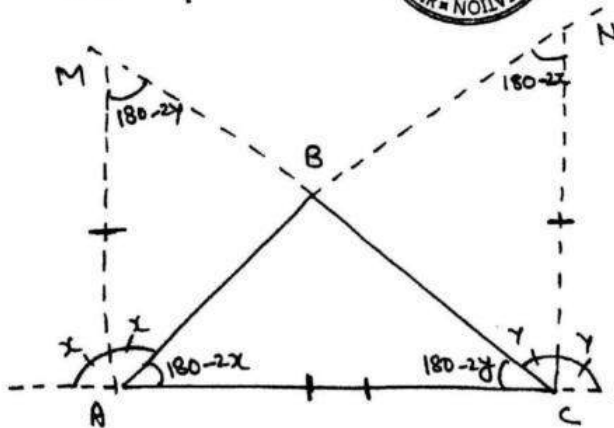
$\alpha = 15^\circ$



- ⑫ In an obtuse angle $\triangle ABC$ the external angle bisector of $\angle A$ intersect the extended part of line CB at M and the external angle bisector of $\angle C$ intersect the extended part of line AB at N.

$MA = AC = CN$

$\angle B = ?$



$x + 4y = 360^\circ$

$4x + y = 360^\circ$

$5(x + y) = 720^\circ$

$x + y = 144^\circ$

$\triangle MAC$

$180 - 2y + 180 - 2y + x + 180 - 2x = 180^\circ$

$x + 4y = 360^\circ$

$\triangle NAC$

$180 - 2x + 180 - 2x + 180 - 2y + y = 180^\circ$

$4x + y = 360^\circ$

$\triangle ABC$

$\angle B + 180 - 2x + 180 - 2y = 180^\circ$

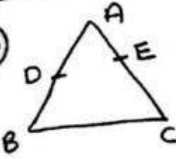
$B = 2(x + y) - 180^\circ$

$B = 288 - 180$

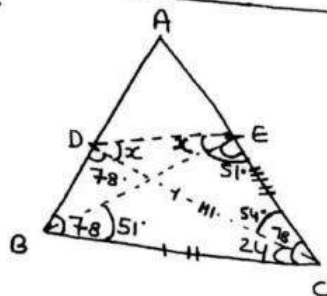
$B = 108^\circ$

CLASS 49

13

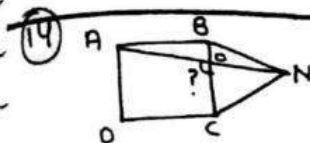


$\angle B = \angle C = 78^\circ$
 $\angle BCD = 24^\circ$
 $\angle EBC = 51^\circ$
 $\angle DEB = ?$

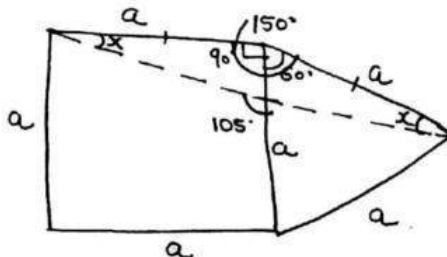


$DC = BC$
 $BC = EC$
 $\therefore DC = BC = EC$
 $m \triangle CDE$
 $x + x + 54 = 180^\circ$
 $x = 63^\circ$

$\angle DEB = 63^\circ - 51^\circ = 12^\circ$



$ABCD$ square
 BCN equilateral Δ .
 $\angle AOC = ?$



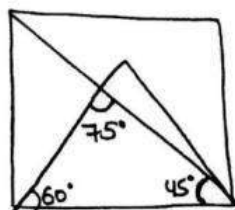
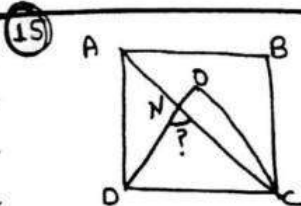
$x + x + 150 = 180^\circ$

$x = 15^\circ$

$\angle AOC = 90 + 15^\circ$

$= 105^\circ$

(external angle of $\triangle ABO$)

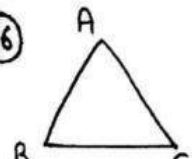


diagonal of the square is angle bisector

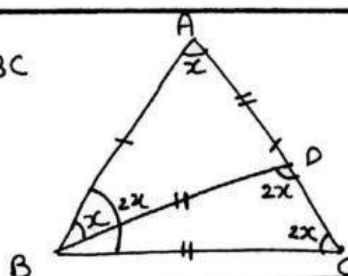
$ABCD$ - square
 AC - diagonal
 CD - equilateral Δ

$\angle DNC = ?$

16



$AD = DB = BC$
 $AB = AC$
 $\angle B = ?$



$\triangle ABC$

$2x + 2x + x = 180^\circ$

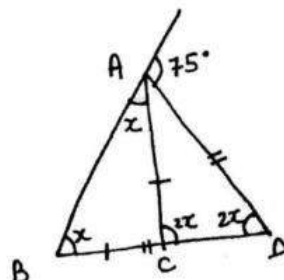
$x = 36^\circ$

$\angle B = 72^\circ$

17



$AC = BC = AD$
 $\angle D = ?$

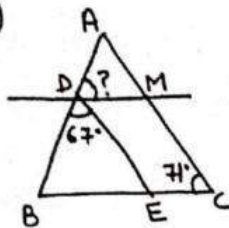


$2x + x = 75^\circ$

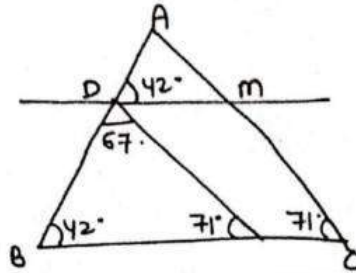
$x = 25^\circ$

$\angle D = 2 \times 25^\circ = 50^\circ$

18)



DE || AC
DM || BC
 $\angle ADM = ?$



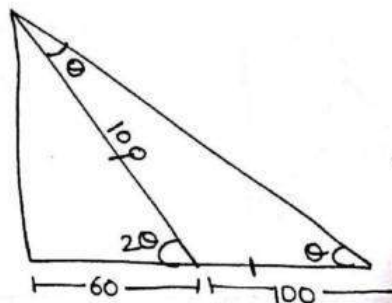
$$\angle ADM = 42^\circ$$

19)

The angle of elevation from a point on the base w/c is 160 m away is θ . After moving 100 m towards the tower the angle of elevation becomes double. find the height of the tower.

20) The angle of elevation from a point on the ground to a top of tower is 15° . After moving 100 m towards the tower the elevation becomes double. find the height of the tower.

19)



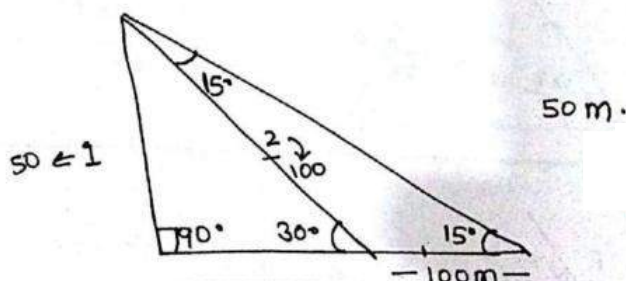
$$H = \sqrt{100^2 - 60^2}$$

$$= \sqrt{10000 - 3600}$$

$$= \sqrt{6400}$$

$$= 80 \text{ m.}$$

20)

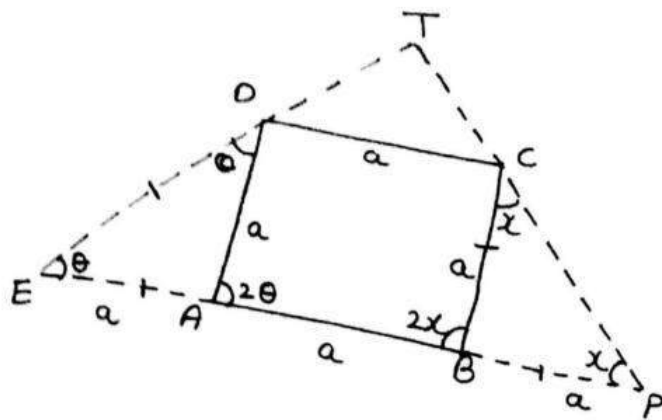


21) A, B, C, D are the vertex of a Rhombus, the ~~extended part~~ of line AB & BA is extended to point P & E. The extended part of line ED & PC meets at T. find $\angle T$. $EA = AB = BP$

Rakesh Yadav

98

Advance Maths (Volume)



$$2\theta + 2x = 180$$

$$\theta + x = 90^\circ$$

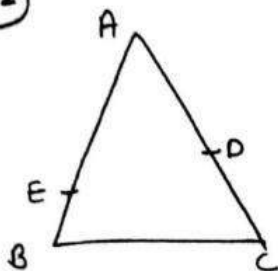
$\triangle TEP$

$$\angle T + \theta + x = 180^\circ$$

$$\angle T = 180 - 90$$

$$\boxed{\angle T = 90^\circ}$$

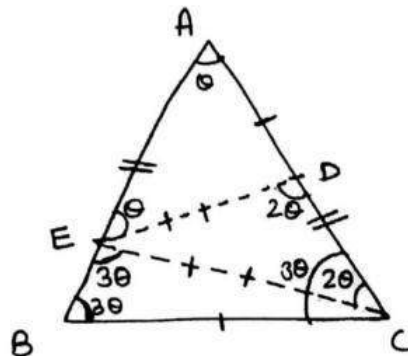
22



$$AD = DE = EC = BC$$

$$AB = AC$$

$$\angle A = ?$$



$\triangle ABC$

$$3\theta + 3\theta + \theta = 180^\circ$$

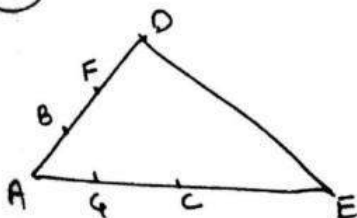
$$7\theta = 180$$

$$\theta = \frac{180}{7}$$

Important Triplets

3, 4, 5	18, 20, 30	9, 40, 41
6, 8, 10	5, 12, 13	8, 12, 15
9, 12, 15	10, 24, 26	
12, 16, 20	15, 36, 39	
15, 20, 25	7, 24, 25	

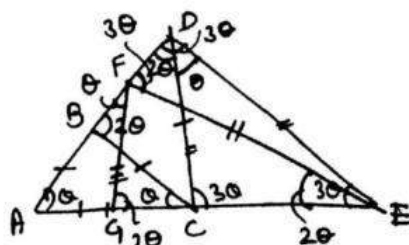
23



$$AB = BC = CD = DE =$$

$$EF = FG = GA$$

$$\angle CDE = ?$$



$\triangle ADE$

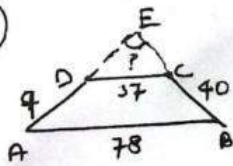
$$\theta + 3\theta + 3\theta = 180^\circ$$

$$7\theta = 180$$

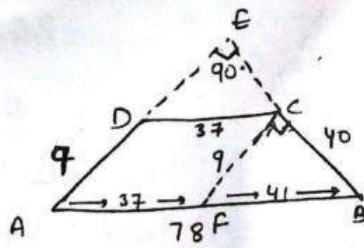
$$\theta = \frac{180}{7}$$

अगर figure ऐसे zig-zag हो, तो देखो कितनी side equal दे रखी है। यहाँ 7 sides equal दे रखी हैं तो angle होगा $\frac{180^\circ}{7}$

24



$\angle DEC = ?$



$\triangle BCF$ (right angle)

$\angle BCF = 90^\circ$

$AD \parallel FC$

BE transversal line

$\therefore \angle DEC = \angle BCF$

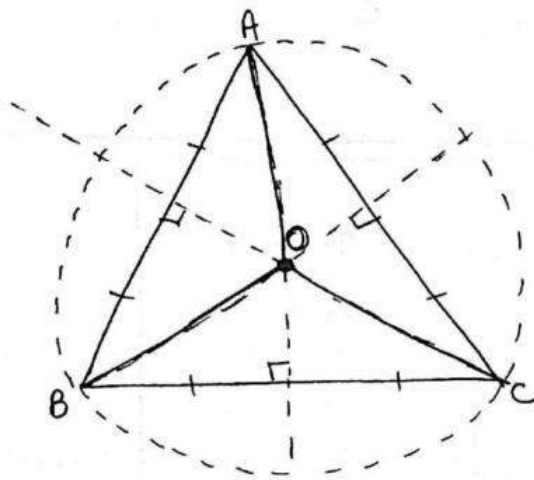
$\angle DEC = 90^\circ$

CENTERS

Circumcentre

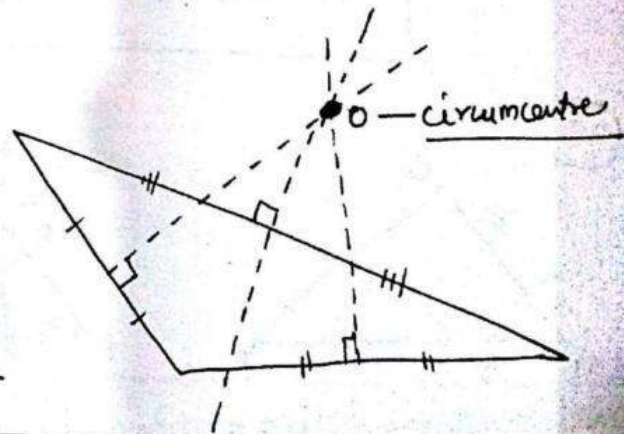
where perpendicular bisector of all sides meet.

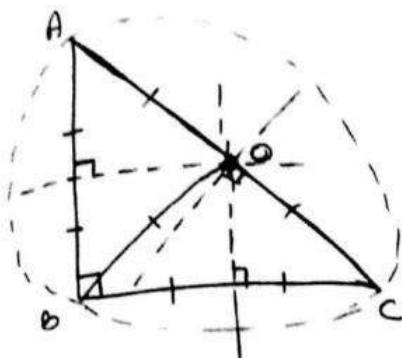
we can not calculate the length of perpendicular bisector because it has no end points.



$$OA = OB = OC = R \text{ (Circum-radius)}$$

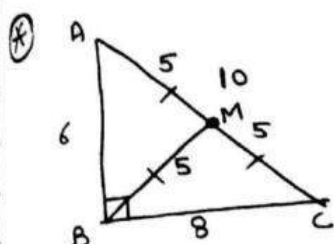
Circumcentre in obtuse angle $\Delta \rightarrow$





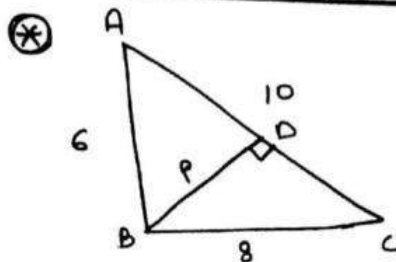
$$OA = OB = OC = R$$

By.
Pardeep Chokker
7206446517



M is the mid point of AC.

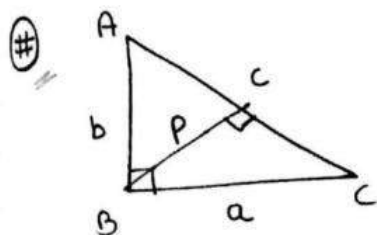
$$BM = AM = MC = R$$



$$\frac{1}{2} \times 6 \times 8 = \frac{1}{2} \times 10 \times P$$

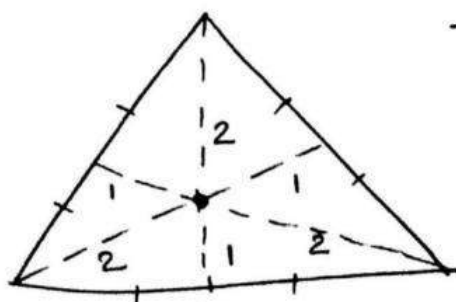
$$P = 4.8$$

$$\text{or } \frac{6 \times 8}{10} = 4.8$$



$$\begin{aligned} \frac{P}{1} &= \frac{ab}{c} \\ \frac{1}{p^2} &= \frac{c^2}{a^2b^2} \\ \frac{1}{p^2} &= \frac{a^2+b^2}{a^2b^2} \\ \frac{1}{p^2} &= \frac{1}{b^2} + \frac{1}{a^2} \end{aligned}$$

Centroid



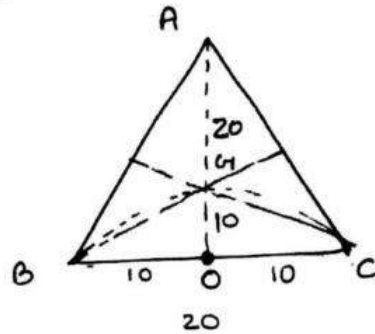
- where 3 medians intersect
- median divide the side in two equal parts.

$$\text{Vertex : Base} = 2 : 1$$

25) In a ΔABC , G is centroid

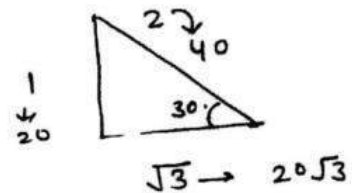
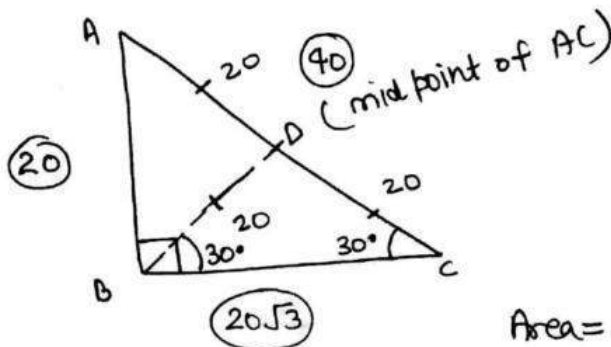
$$AG = GC$$

$$\angle BGC = ?$$



$O \rightarrow$ centre
draw a semicircle
 $\angle BGC = 90^\circ$
(angle in semi-circle)

26) find the area of a right angle Δ in w/c a median of length 20 cm intersect the right angle in the ratio 2:1

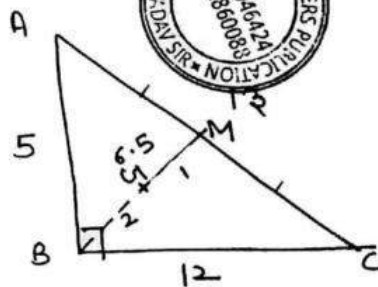


$$\text{Area} = \frac{1}{2} \times 20\sqrt{3} \times 20 = 200\sqrt{3} \text{ Ans}$$

27) In a ΔABC , G is centroid

$$AB = 5, BC = 12$$

$$CA = 13, BG = ?$$



$$AM = MC = BM$$

$$= 6.5$$

$$2 : 1$$

$$BG = \frac{13}{2} \times \frac{2}{3}$$

$$\frac{13}{3} \text{ Ans}$$

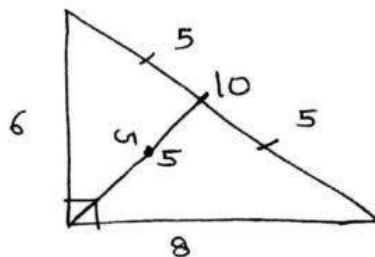
28) In a ΔABC , G is centroid

$$AB = 6$$

$$BC = 8$$

$$CA = 10$$

$$BG = ?$$



$$2 : 1$$

$$BG = 5 \times \frac{2}{3}$$

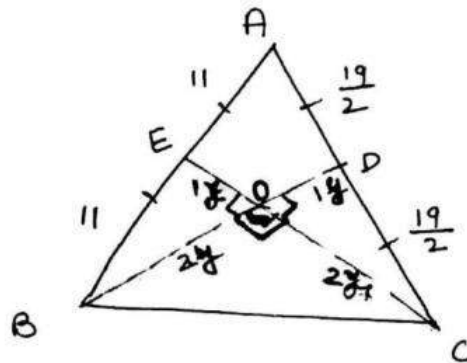
$$\frac{10}{3}$$

- 29) In a ΔABC , BD & CE are the two medians w/c intersect each other at right angle. Find

$$AB = 22$$

$$AC = 19$$

$$BC = ?$$



$$4x^2 + y^2 = \frac{361}{4} \quad (\Delta COO)$$

$$x^2 + 4y^2 = 121 \quad (\Delta BOE)$$

$$5(x^2 + y^2) = \frac{845}{4}$$

$$x^2 + y^2 = \frac{169}{4}$$

$$\therefore 4x^2 + 4y^2 = 169$$

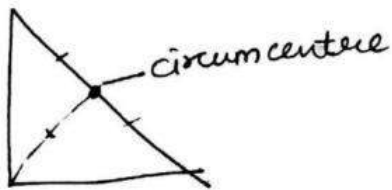
$$BC^2 = 4x^2 + 4y^2$$

$$BC^2 = 169$$

$$BC = 13$$

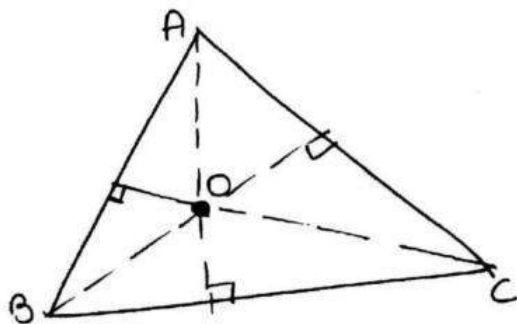
OR

$$BC = \sqrt{\frac{AB^2 + AC^2}{5}}$$

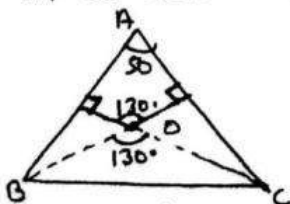


Orthocentre

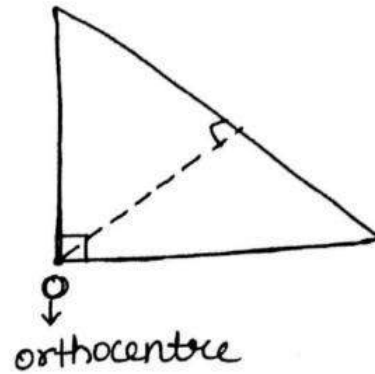
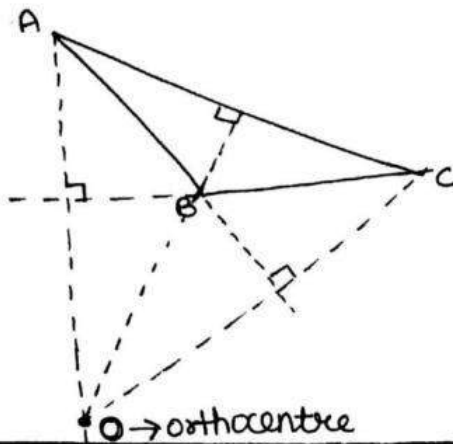
Meeting point of three altitudes



- 30) In a acute angle ΔABC , O is orthocentre. $\angle A = 50^\circ$, $\angle BOC = ?$

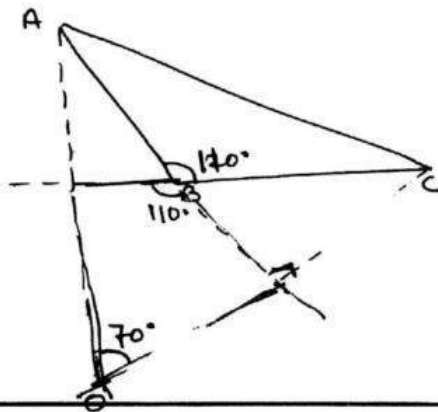


#

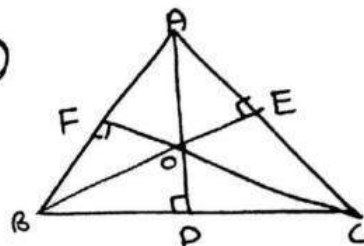


orthocentre

- 31) In obtuse angle Δ , obtuse angle is 110° . Find the angle made on its orthocentre-



#



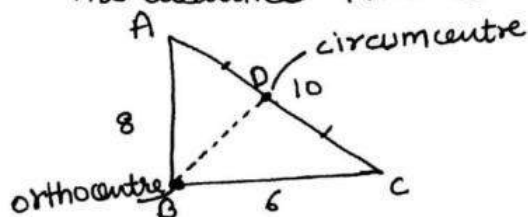
O $\rightarrow$ orthocentre

vertex E $\rightarrow$ is the orthocentre of ΔAOC

AOE, ABE, COE, BEE.

vertex B $\rightarrow$ orthocentre of ΔAOC

- 32) The length of the sides of a Δ are 6, 8, 10 cm. Find the distance from its orthocentre to circumcentre.



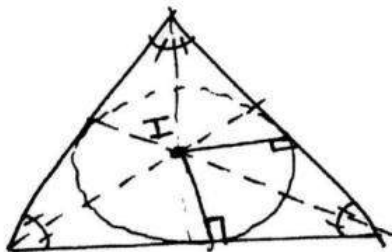
D $\rightarrow$ circumcentre

$$AD = DC = 5$$

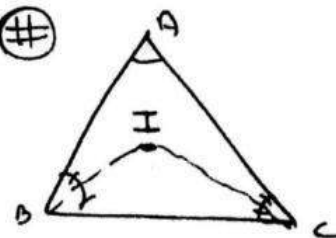
$$AD = DC = BD = R$$

$$\therefore BD = 5$$

Incentre meeting point of angle bisector



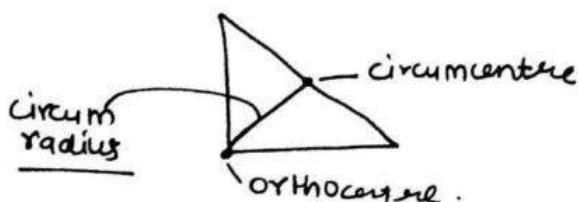
#



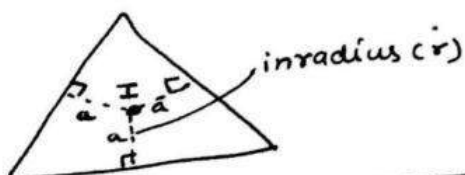
$$\angle I = 90 + \frac{1}{2} \angle A$$

⑧ The same line represents the median from the right angle vertex and the circumcircle radius in a right angle Δ .

⑨ In right angle Δ , the distance b/w orthocentre and circumcentre is equal to the circumradius of the Δ .

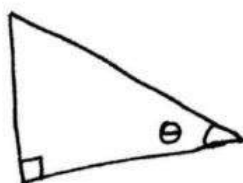
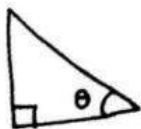


⑩ Incentre is the only centre w/c is equi perpendicular distance from all the sides of the Δ and circumcentre is the only centre w/c have equal distance from all the vertex.



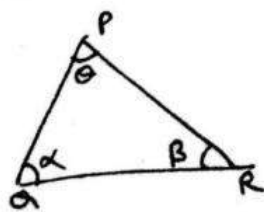
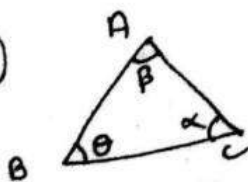
Similarity

①



if two angles are equal then Δ 's are similar.

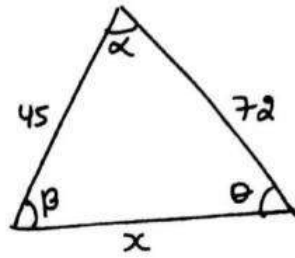
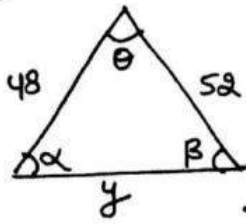
②



$$\frac{AC}{QR} = \frac{AB}{PR} = \frac{BC}{PQ} = \frac{P(\Delta ABC)}{P(\Delta PQR)} = \frac{\text{median of } \Delta ABC}{\text{median of } \Delta PQR}$$

$$= \frac{\text{Angle Bisector of } \Delta ABC}{\text{Angle Bisector of } \Delta PQR} = \frac{\text{Altitude of } \Delta ABC}{\text{Altitude of } \Delta PQR}$$

33



$$x+y = ?$$

$$\frac{y}{45} = \frac{48}{72} \cdot 2$$

$$y = 30$$

$$\frac{x}{52} = \frac{72}{48} \cdot 3$$

$$x = 78$$

$$x+y = 108$$

$$\frac{48}{72} = 2 : 3$$

$$2 \rightarrow 52$$

$$1 \rightarrow 26$$

$$3 \rightarrow 78 = x$$

Now

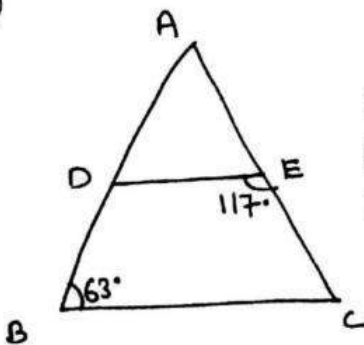
$$3 \rightarrow 45$$

$$1 \rightarrow 15$$

$$2 \rightarrow 30 = y$$

$$x+y = 108$$

34

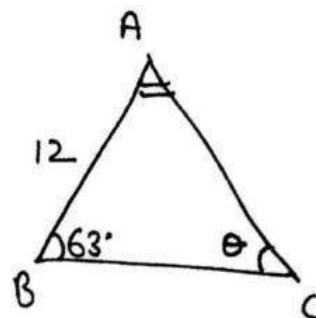
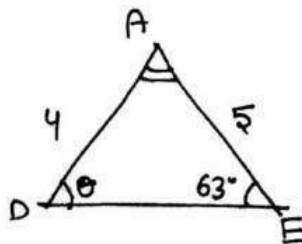
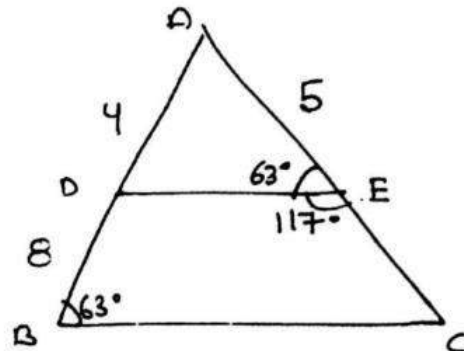


$$AD=4$$

$$AB=12$$

$$AE=5$$

$$EC=?$$



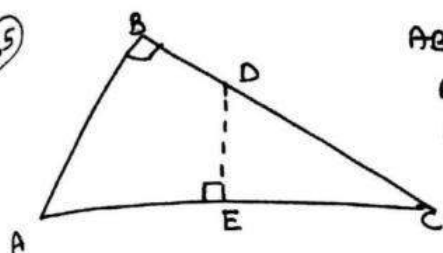
$$\frac{AC}{4} = \frac{12}{5}$$

$$AC = \frac{48}{5} = 9.6$$

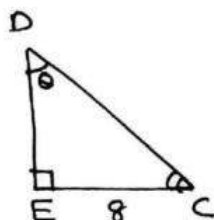
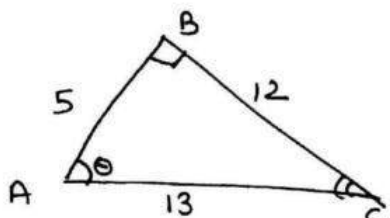
$$EC = 9.6 - 5 = 4.6$$

Ans

35



$$\begin{aligned} AB &= AE = 5 \\ BC &= 12 \\ DE &= ? \end{aligned}$$

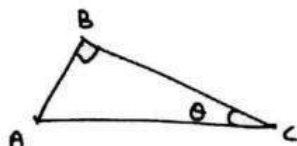
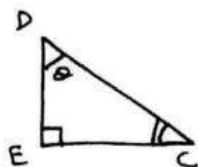


$$\begin{aligned} AE &= 5 \\ AC &= 13 \\ EC &= 8 \end{aligned}$$

$$\frac{DE}{5} = \frac{5^2}{12^2}$$

$$DE = \frac{10}{3}$$

OR



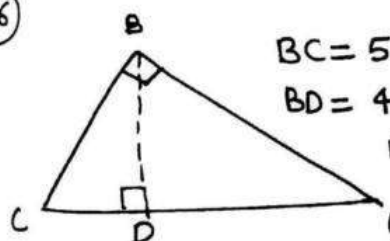
$$\frac{DE}{8} = \frac{5}{12}$$

$$\tan \theta = \frac{DE}{8}$$

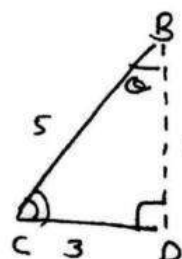
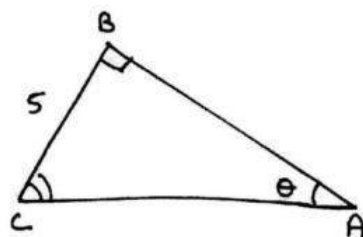
$$\tan \theta = \frac{5}{12}$$

$$DE = \frac{10}{3}$$

36



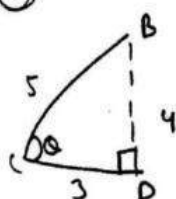
$$\begin{aligned} BC &= 5 \\ BD &= 4 \\ AB &= ? \\ AC &= ? \end{aligned}$$



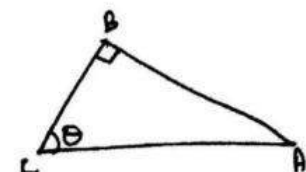
$$\frac{AB}{4} = \frac{5}{3}$$

$$AB = \frac{20}{3}$$

OR



$$\tan \theta = \frac{4}{3}$$



$$\tan \theta = \frac{AB}{5}$$

$$\frac{AC}{5} = \frac{5}{3}$$

$$AC = \frac{25}{3}$$

$$AB = \frac{20}{3}$$

37) In a right angle ΔABC , $AD \perp BC$. BC is the hypotenuse.

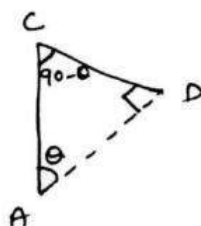
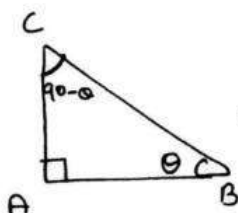
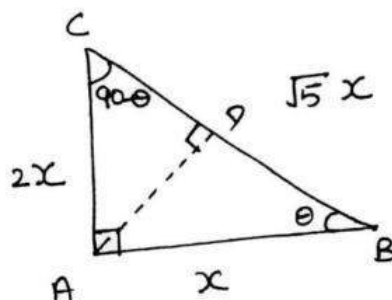
$$AC = 2AB, \quad BD = ?$$

A) $\frac{BC}{2}$

C) $\frac{BC}{4}$

B) $\frac{BC}{3}$

D) $\frac{BC}{5}$



$$\frac{AC}{CD} = \frac{BC}{AC} = \frac{AB}{AD}$$

$$AC^2 = BC \times CD$$

$$AB^2 = BD \times BC$$

Imp

$$AC^2 = BC \times CD$$

$$AB^2 = BD \times BC$$

$$AD^2 = CD \times DB$$

$$AB^2 = BD \times BC$$

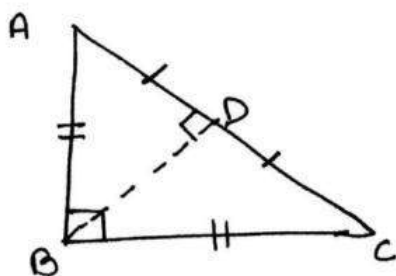
$$x^2 = BD \times \sqrt{5}x$$

$$BD = \frac{x}{\sqrt{5}}$$

$$= \frac{x}{\sqrt{5}} \times \frac{\sqrt{5}}{\sqrt{5}} = \frac{\sqrt{5}x}{5} = \frac{BC}{5}$$

$$BD = \frac{BC}{5}$$

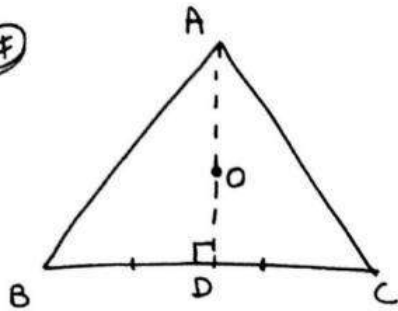
Right angle isosceles Δ



BD is
 Median
 Altitude
 $\perp$ bisector
 Angle bisector

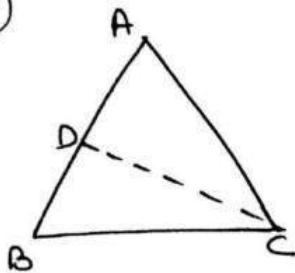
BD = line formed by joining orthocentre & circumcentre

37



In $\triangle ABC$
 Any median (AD) is
 median
 $\perp$ bisector
 Altitude
 Angle bisector
 and all centres lie on the same place
 Circumcentre
 orthocentre
 centroid
 incentre.

38



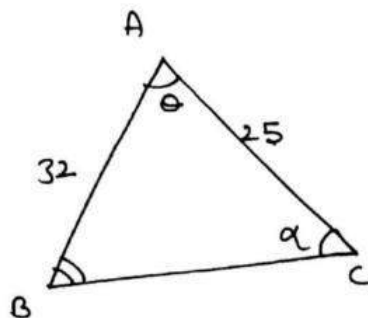
$$\angle BAC = \angle BCD$$

$$AD = 14$$

$$BD = 18$$

$$AC = 25$$

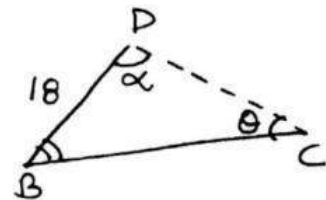
$$BC = ?$$



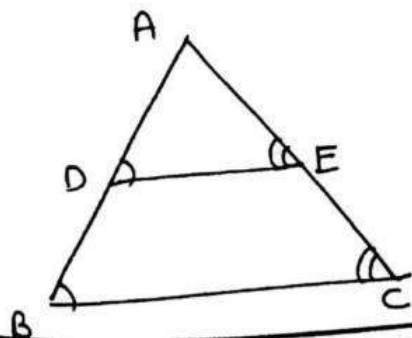
$$\frac{BC}{18} = \frac{32}{BC}$$

$$BC^2 = 576$$

$$BC = 24$$



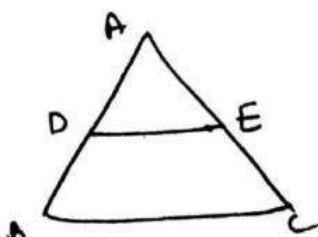
39



$$\frac{AD}{AB} = \frac{AE}{AC} = \frac{DE}{BC}$$

$$\frac{AD}{DB} = \frac{AE}{EC}$$

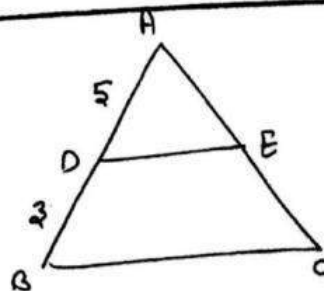
39



$$\frac{AD}{DB} = \frac{5}{3}$$

$$BC = 72$$

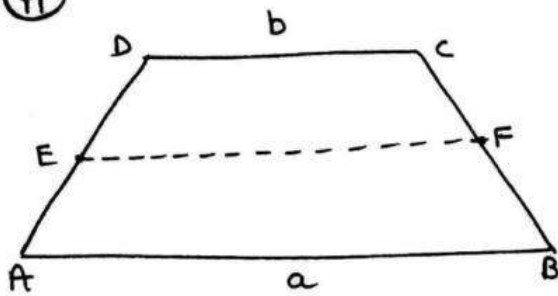
$$DE = ?$$



$$\frac{5}{3} = \frac{DE}{72}$$

$$DE = 45$$

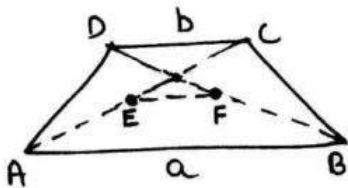
#



$$\frac{DE}{EA} = \frac{CF}{FB}$$

If E & F are mid points

$$EF = \frac{a+b}{2}$$

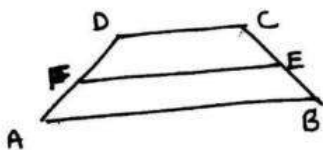


E & F are mid points of diagonals

$$EF = \frac{a-b}{2}$$

CLASS
SI

40



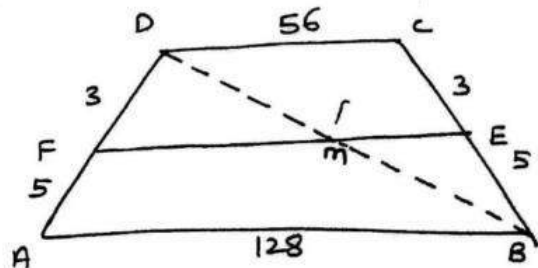
$AB \parallel DC \parallel FE$

$$\frac{DF}{FA} = \frac{3}{5}$$

$$AB = 128$$

$$DC = 56$$

$$FE = ?$$



$\triangle ADB \sim \triangle DFM$

$$\frac{3}{8} = \frac{FM}{128}$$

$$FM = 48$$

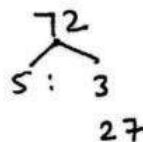
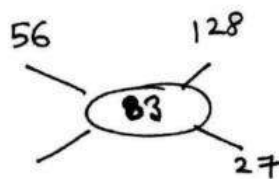
$\triangle BCD \sim \triangle BEM$

$$\frac{5}{8} = \frac{ME}{56} \Rightarrow ME = 35$$

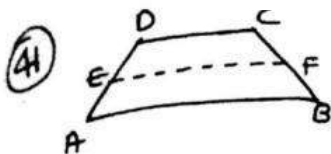
$$FE = 48 + 35 = 83$$

Ans.

OR



$$5 : 3$$



$$DC = 45$$

$$AB = 125$$

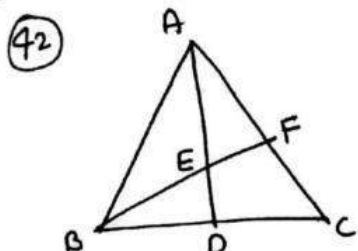
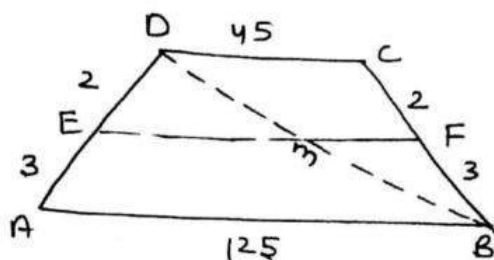
$$EF = ?$$

$$\frac{DE}{EA} = \frac{2}{3}$$

$$\Rightarrow \frac{2}{5} = \frac{EM}{125 - 25} \quad \boxed{EM = 50}$$

$$\Rightarrow \frac{3}{5} = \frac{MF}{45 - 9} \quad \boxed{MF = 27}$$

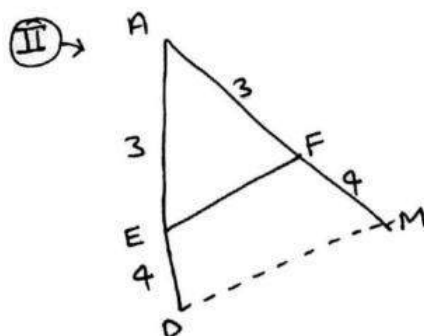
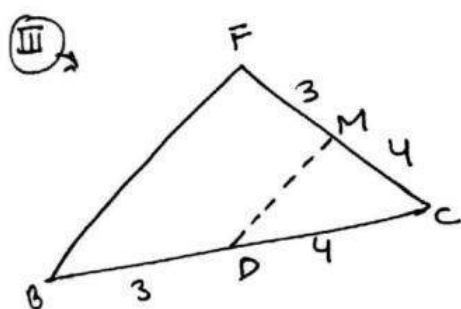
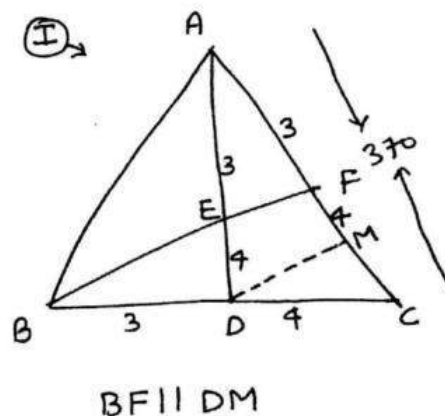
$$\boxed{EF = 50 + 27 = 77} \quad \underline{\text{Ans}}$$



$$AE:ED = BD:DC = 3:4$$

$$AC = 370 \text{ cm}$$

$$AF = ?$$



$$AF:FM = 3:4$$

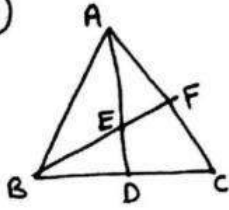
$$\begin{array}{r} AF : FM : MC \\ 3 : 4 : 4 \\ 3 : 3 : 4 \\ \hline 9x \quad 12x \quad 16x \end{array}$$

$$37x = 370$$

$$\boxed{x = 10}$$

$$\boxed{\begin{array}{l} AF = 90 \\ FM = 120 \\ MC = 160 \end{array}}$$

43



E is mid point of AD

D is mid point of BC

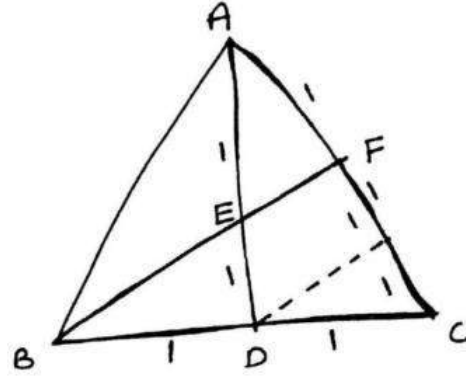
AC = 30 cm

AF = ?

3 → 30

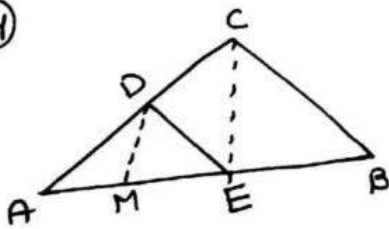
1 → 10

AF = 10



$$\begin{array}{ccc} AE : FM : MC & & \\ 1 : 1 & & 1 \\ 1 & : & 1 \\ \hline 1 : 1 : 1 \end{array}$$

44



BC || DE

CE || DM

AE : EB = 2 : 3

AM : MB = ?

$$\begin{array}{ccc} AE = 2+3 = 5 & \rightarrow & 20 \\ 1 & \rightarrow & 4 \end{array}$$

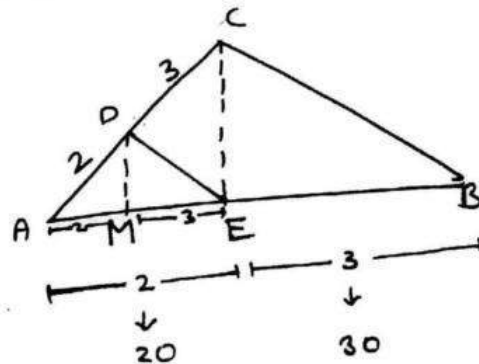
AM = 8 , ME = 12 , EB = 30

AM : MB

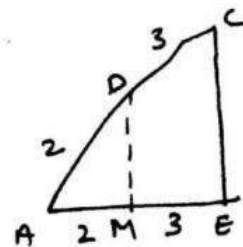
8 : 42

4 : 21

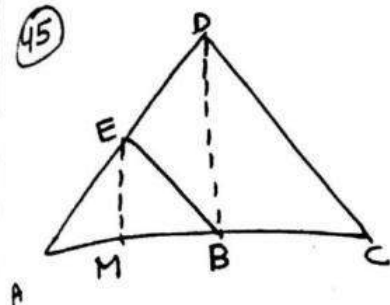
Any



AE = 20
EB = 30

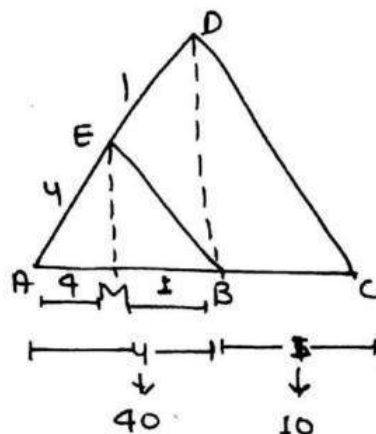


45



$$AB:BC = 4:1$$

$$MB:BC = ?$$



$$AM = 32$$

$$MB = 8$$

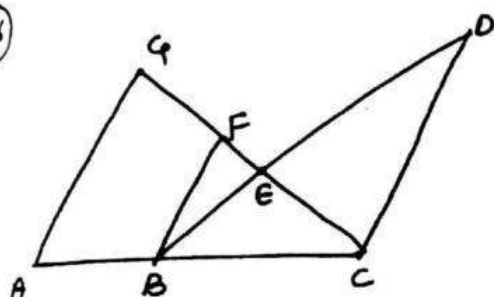
$$BC = 10$$

$$MB : BC$$

$$8 : 10$$

$$4 : 5$$

46



$$FE = 5$$

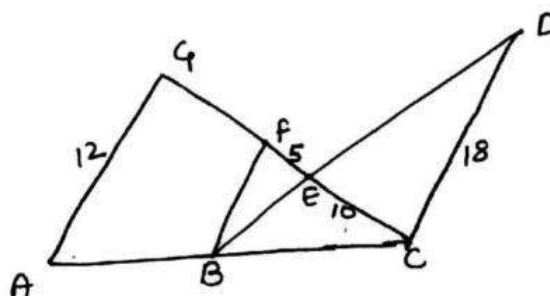
$$EC = 10$$

$$DC = 18$$

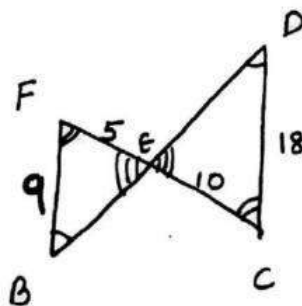
$$AG = 12$$

$$GC = ?$$

$$AG \parallel BF \parallel CD$$



(I)



$$FB \parallel CD$$

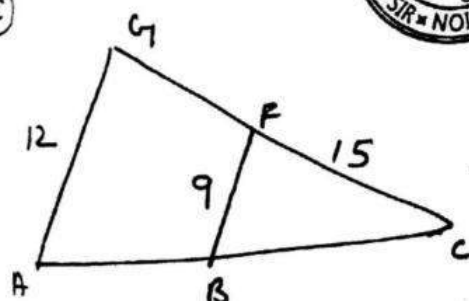
$$BD \text{ \& } FC$$

$$\text{Transversal}$$

$$\frac{FB}{18} = \frac{5}{10}$$

$$FB = 9$$

(II)

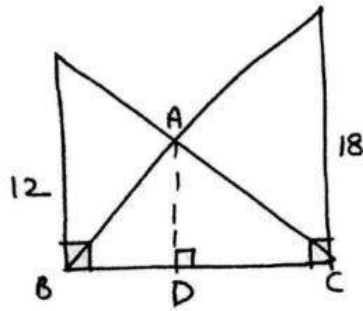


$$\frac{15}{GC} = \frac{9}{12}$$

$$GC = 20$$

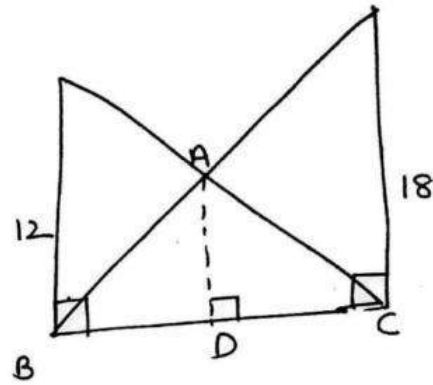


47



Area of $\triangle ABC = ?$

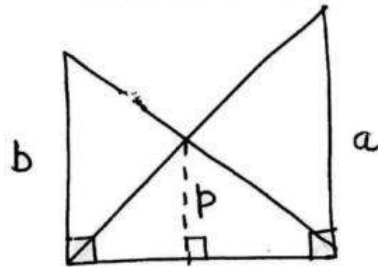
$$BC = 6$$



$$AD = \frac{12 \times 18}{30} = \frac{36}{5}$$

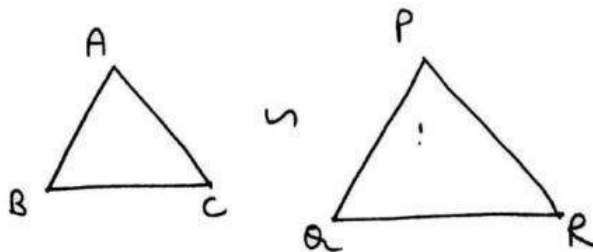
$$\text{Area } \triangle ABC = \frac{1}{2} \times 6 \times \frac{36}{5} = \frac{108}{5}$$

#



$$p = \frac{ab}{a+b}$$

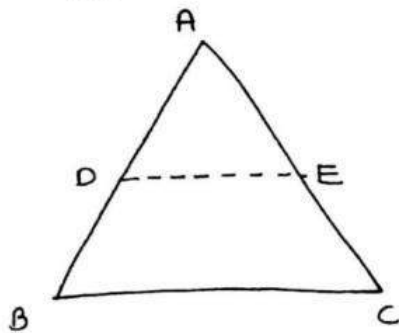
#



$$\frac{\text{Area}(\triangle ABC)}{\text{Area}(\triangle PQR)} = \left(\frac{AB}{PQ}\right)^2 = \left(\frac{BC}{QR}\right)^2 = \left(\frac{AC}{PR}\right)^2 = \left(\frac{\text{P.of } \triangle ABC}{\text{P.of } \triangle PQR}\right)^2 =$$

$$\left(\frac{\text{Median / Angle bisector / Altitude of } \triangle ABC}{\text{Median / Angle bisector / Altitude of } \triangle PQR}\right)^2$$

- 48) In a $\triangle ABC$ a line DE is drawn parallel to BC in such a way that it divides the $\triangle$ in two equal areas find $\frac{AD}{DB}$



	Small $\triangle$ ($\triangle ADE$)	Larger $\triangle$ ($\triangle ABC$)
Area	1	2
Side	1	$\sqrt{2}$

$$AD = 1$$

$$AB = \sqrt{2}$$

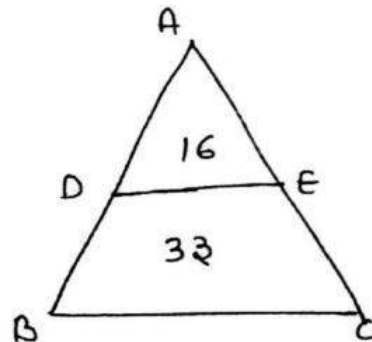
$$DB = \sqrt{2} - 1$$

$$\frac{AD}{DB} = \frac{1}{\sqrt{2} - 1}$$

- 49) In $\triangle ABC$ a line DE is drawn parallel to BC in such a way that

$$\text{Area } \triangle ADE : \text{Area } \square BCED = 16 : 33$$

$$\frac{AD}{DB} = ?$$

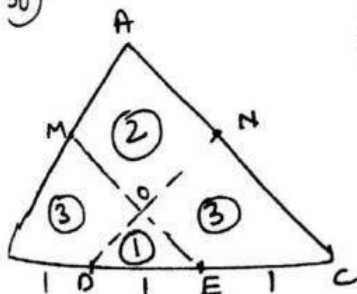


	$\triangle ADE$	$\triangle ABC$
Area	16	49
Side	4	7
	$\downarrow$ AD	$\downarrow$ AB

$$DB = 7 - 4 = 3$$

$$\frac{AD}{DB} = \frac{4}{3}$$

50)



- in $\triangle ABC$, D & E are two points on BC such that they trisect the line BC

$$DN \parallel AB$$

$$EM \parallel AC$$

$$\frac{\text{Area } \triangle DDE + \text{Area } \square AMON}{\text{Area } \triangle ABC} =$$

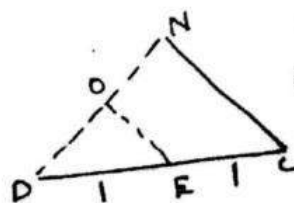
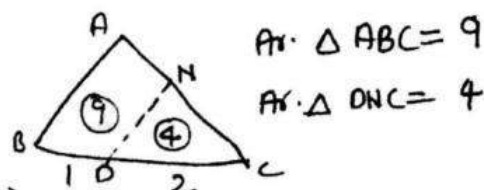
$$\text{Ar } \triangle DNC = 4$$

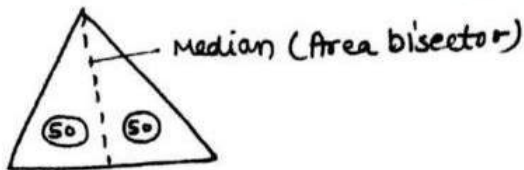
$$\text{Ar } \triangle DOE = 1$$

$$\text{Ar } \triangle EMB = 4$$

$$\frac{1+2}{9} = \frac{1}{3}$$

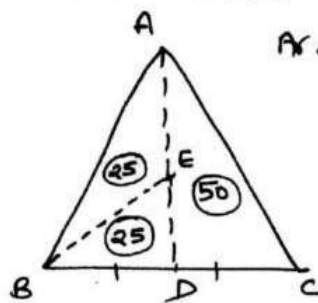
$$\text{Ans}$$





(51) in $\triangle ABC$, D is the mid point of BC. And E is the mid point of line ~~AB~~ AD.

Ar. $\triangle ABE$: Ar $\triangle ABC$ = ?

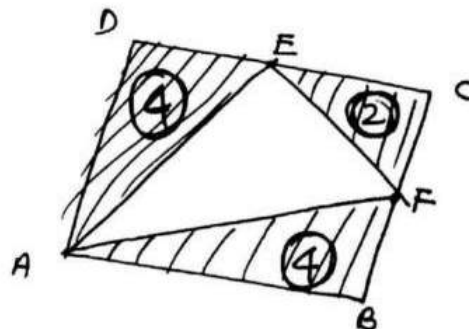
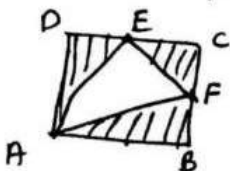


Ar $\triangle ABC$ = 100 (let)

$$\frac{\text{Ar. } \triangle ABE}{\text{Ar } \triangle ABC} = \frac{25}{100} = \frac{1}{4}$$

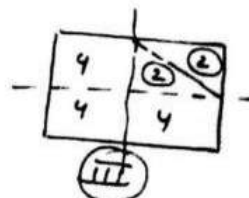
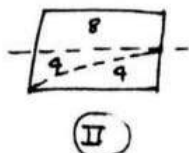
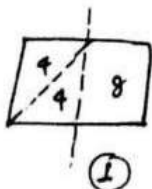
(52) ABCD is a $\square$. E & F are mid point of DC & BC.

find the ratio of area of shaded portion to the area of unshaded portion.



16 इसलिए लेते हैं क्योंकि बार-बार half करना पड़ रहा है, so fraction ना बने।

Let area of $\square ABCD$ = 16

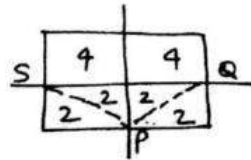
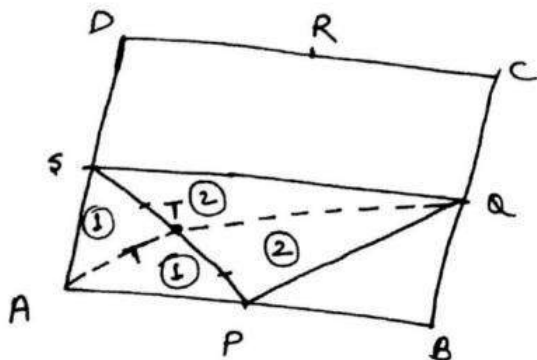


$$\frac{\text{Area shaded}}{\text{unshaded}} = \frac{10}{6} = \frac{5}{3} \quad \text{Ans.}$$

- 53) A, B, C, D are the vertex of a ||gm. P, Q, R, S are the mid point of AB, BC, CD & DA. T is the mid point of line PS.

Area ΔATS : Area ΔPTQ

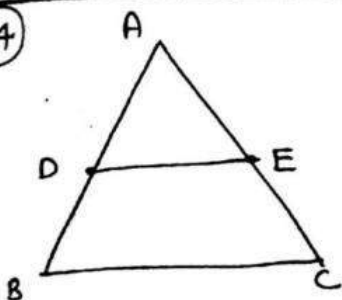
Let area $\square ABCD = 16$



Ar $\Delta SPQ = 4$

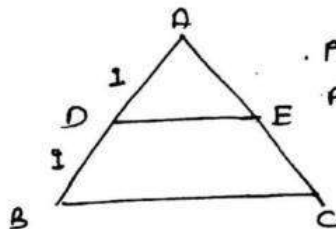
$$\frac{\text{Ar. } \Delta ATS}{\text{Ar. } \Delta PTQ} = \frac{1}{2} \quad \underline{\text{Ans}}$$

54)



D & E are mid points.

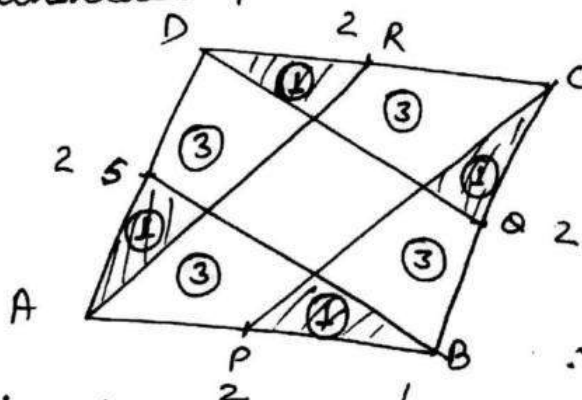
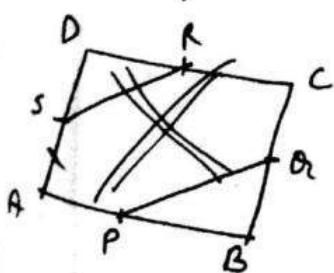
find area ΔADE : Area ΔABC



$$\frac{\text{Ar. } \Delta ADE}{\text{Ar. } \Delta ABC} = \frac{(1)^2}{(2)^2} = \frac{1}{4}$$

55)

A, B, C, D are the vertex of a ||gm. P, Q, R, S are the mid points of AB, BC, CD, DA. find the area of shaded portion : unshaded portion.

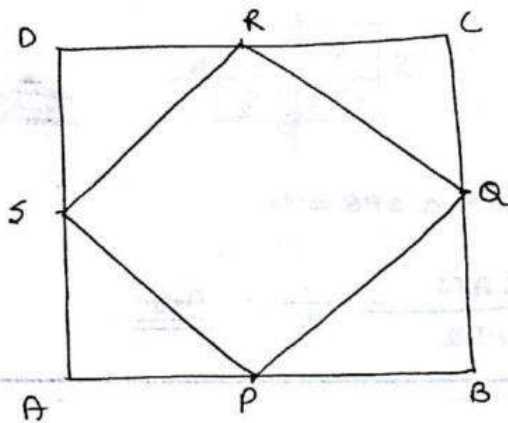


$\therefore \text{Ar. } ABCD = 20$

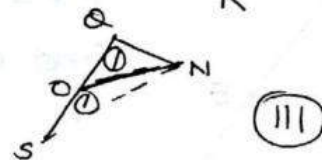
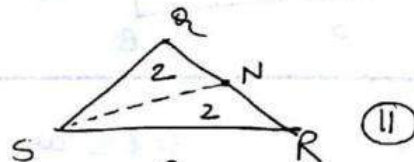
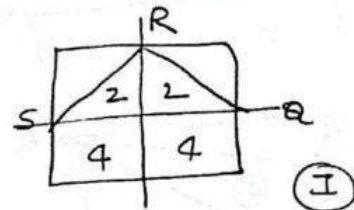
$$\frac{\text{Shaded}}{\text{Unshaded}} = \frac{4}{16} = 1:4$$

- 56) A, B, C, D are the vertex of a $\square$ ABCD. P, Q, R, S are the mid points of line AB, BC, CD & DA. M, N, O, E are the mid points of PQ, QR, RS & SP.

Area of $\triangle SON$: Area of $\square$ ABCD

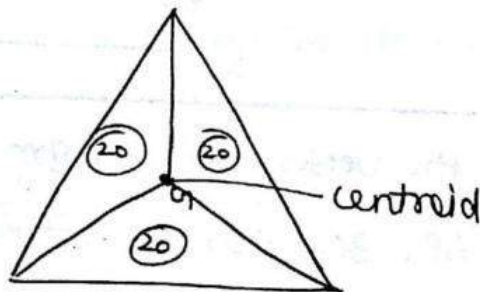
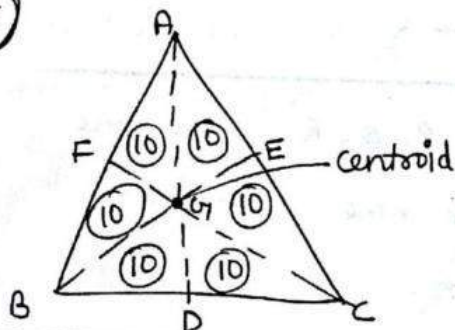


Area $\square$ ABCD = 16 (let)



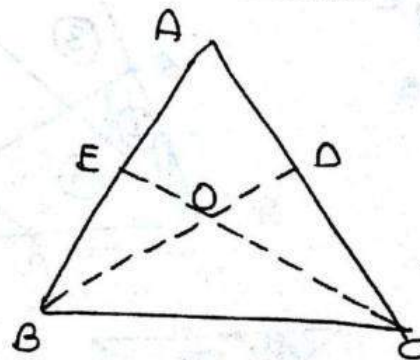
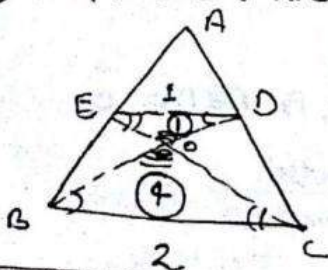
$$\frac{\text{Ar } \triangle SON}{\text{Ar } \square ABCD} = \frac{1}{16}$$

#



- 57) In a $\triangle$ ABC BD & CE are two medians, cut each other at point O.

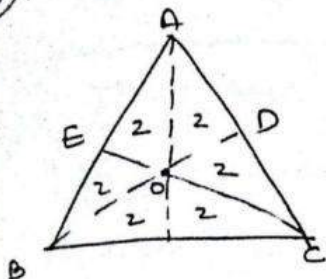
(A) Area $\triangle DOE$: Area $\triangle BOC$



Rakesh Yadav

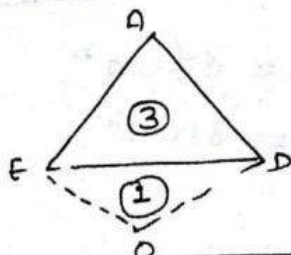
$$\frac{\text{Area } \triangle DOE}{\text{Area } \triangle ABC} = \frac{1}{4+4+4} = \frac{1}{12}$$

(B) Area $\triangle DOE$: Area of $\triangle DOC$



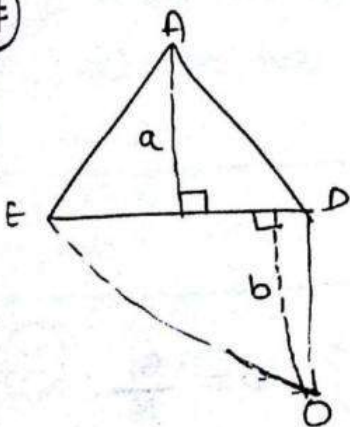
1:2

(C) Area $\triangle DOE$: Area of $\triangle ADE$.



$$\frac{\text{Area } \triangle DOE}{\text{Area } \triangle ADE} = \frac{1}{3}$$

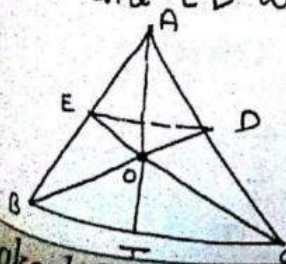
(#)



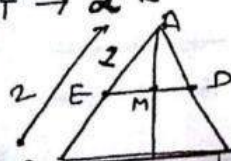
$$\frac{\text{Ar. } \triangle AED}{\text{Ar. } \triangle EOD} = \frac{\frac{1}{2} \times ED \times a}{\frac{1}{2} \times ED \times b} = \boxed{\frac{a}{b}}$$

The ratio of area of two Δ 's w/c are based on the same base is equal to the ratio of length of their altitudes drawn on the same base.

(58) In a $\triangle ABC$, BD & CE are two medians w/c intersect each other on O. The line AO intersect the line ED at M. $AM : MO = ?$



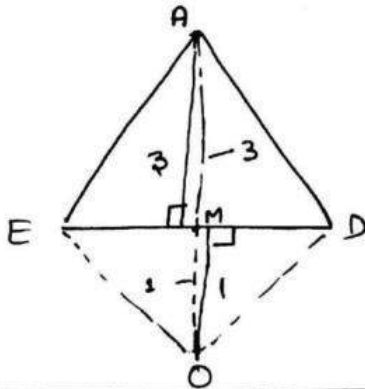
$AO \rightarrow 4$ $OT \rightarrow 2$ $\therefore AO : OT = 2 : 1$



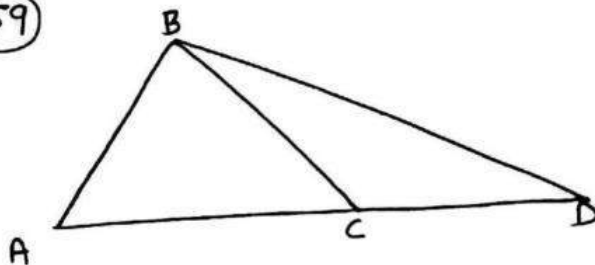
$AT \rightarrow 6$ $\frac{AM}{MO} = \frac{3}{1}$ $\underline{\underline{AM}}$

$AM = 3$
आप दो Δ similar है तो उनकी sides के ratio के बराबर

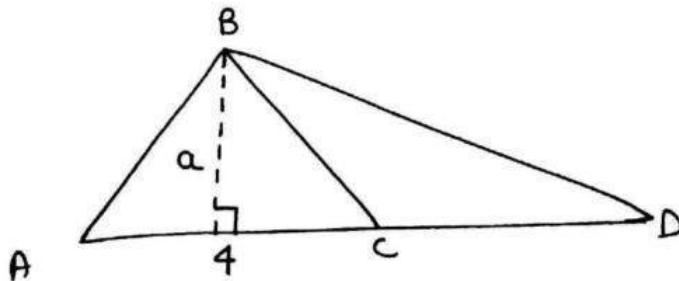
$$\therefore \frac{\text{Area } \triangle AED}{\text{Area } \triangle EOD} = \frac{3}{1}$$



(59)

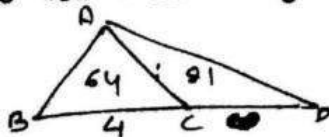


$$\begin{aligned} \text{Area } \triangle ACB &= 64 \text{ cm}^2 \\ \text{Area } \triangle BCD &= 81 \text{ cm}^2 \\ AC &= 4 \\ CD &= ? \end{aligned}$$



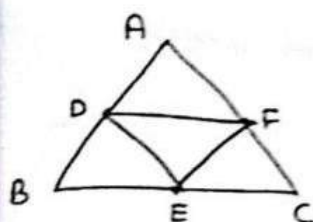
$$\begin{aligned} \text{Ar } \triangle ABC &= \frac{1}{2} \times AC \times h \\ \text{Ar } \triangle BCD &= \frac{1}{2} \times CD \times h \end{aligned} \Rightarrow \frac{64}{81} = \frac{4}{CD} \quad CD = \frac{81}{16}$$

⊗ If two $\triangle$'s have a common vertex and are based on a same straight line, have the area in the ratio as the length of their bases.



4 → 64	64 → 4
16 → 81	1 → 16
	81 → 16

#



Ar. $\triangle DEF$: Ar. $\triangle ABC$

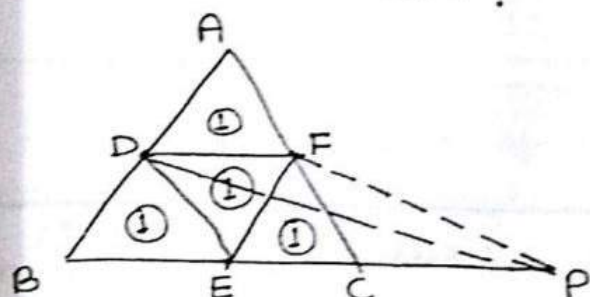
1 : 4

D, E, F are mid points.

60 In $\triangle ABC$, the length BC extended to point P.

D, F are the mid points of line AB & AC.

Ar $\triangle DFP$: Ar $\triangle ABC$ = ?



1 : 4

Ar $\triangle DFE$ = Ar $\triangle DFP$

$\therefore$ Ar $\triangle DFP$ = 1

Ar $\triangle ABC$ = 4

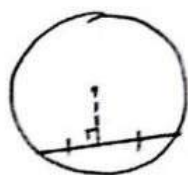
$\therefore$ Ar $\triangle DFP$: Ar $\triangle ABC$ = 1 : 4

When two $\triangle$'s have the same base and are present between two parallel lines, then their area will be same.

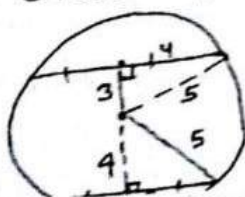
CLASS
53

CIRCLE

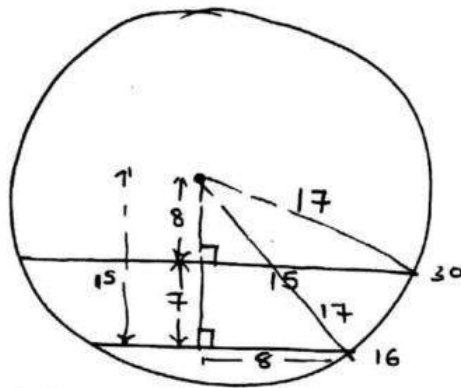
#



61 find the $\perp$ distance b/w two parallel chords of length 6 cm and 8 cm w/c are on the opposite direction on the centre of circle of radius 5 cm.



- 62) Find the $\perp$ distance b/w two $\parallel$ chords of length 16 cm and 30 cm w/e are on the same side of the centre of the circle of radius 17 cm.



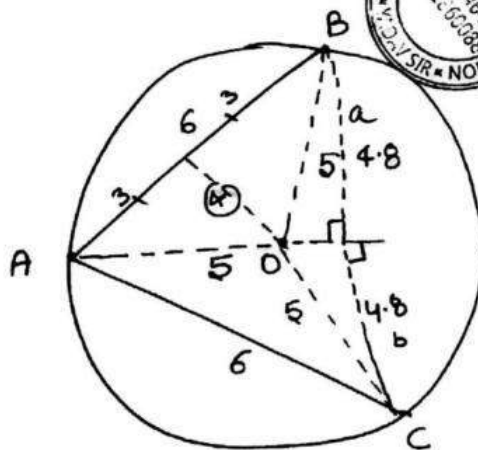
7 cm Ans

- 3) AB and AC are two chords of a circle of radius 5 cm

$$AB = AC = 6 \text{ cm}$$

$$r = 5 \text{ cm}$$

$$BC = ?$$



$$BC = 4.8 + 4.8 = 9.6$$

$\Delta AOB = \text{obtuse isosceles } \Delta$

$\Delta AOB =$

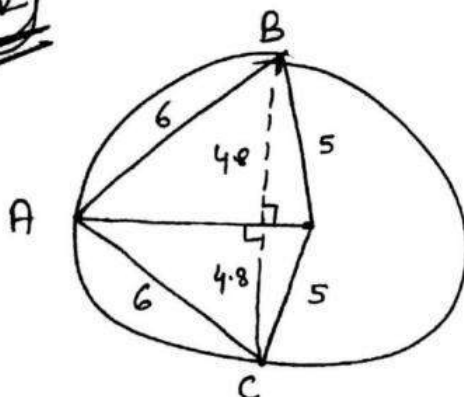
$$\frac{1}{2} \times 6 \times 4 = \frac{1}{2} \times 5 \times a$$

$$a = 4.8$$

$$\text{similarly } b = 4.8$$

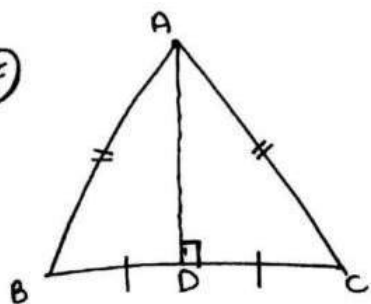
$$BC = a + b = 9.6$$

102



Δ obtuse या acute
कैसी भी बन सकती है

#



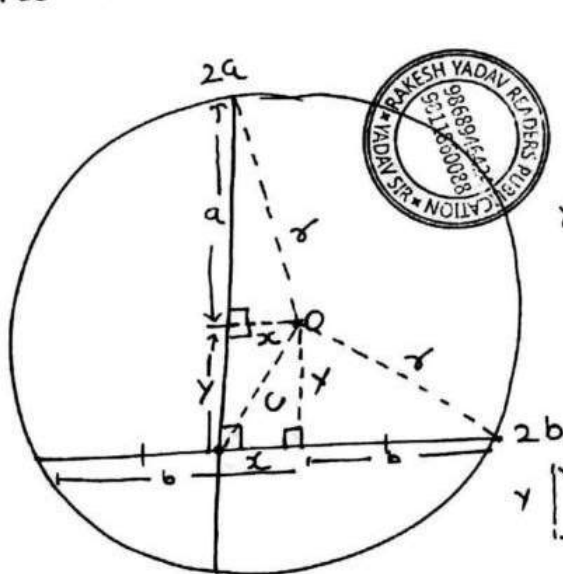
In an isosceles Δ , if a $\perp$ is drawn from the common vertex of two equal sides on the opposite side, then it will bisect the opposite side.

$AB = AC$ (common vertex = A)

$AD \perp BC$

$\therefore \boxed{BD = DC}$

- 64) $2a, 2b$ are the length of two chords w/c intersect each other at right angle. find the radius of the circle and the distance from their intersecting point to the centre of circle is c , $c < \text{radius}$.



$$a^2 + x^2 = r^2 \rightarrow x^2 = r^2 - a^2$$

$$y^2 + b^2 = r^2 \rightarrow y^2 = r^2 - b^2$$

$$y^2 = r^2 - (r^2 - a^2)$$

$$\boxed{y^2 = a^2 - r^2 + b^2}$$

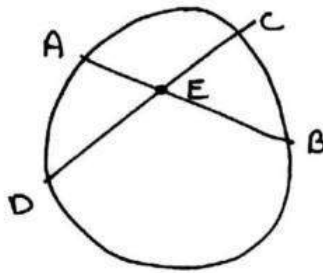
$$r^2 = y^2 + b^2$$

$$r^2 = a^2 - r^2 + b^2 + b^2$$

$$r^2 = \frac{a^2 + b^2 + c^2}{2}$$

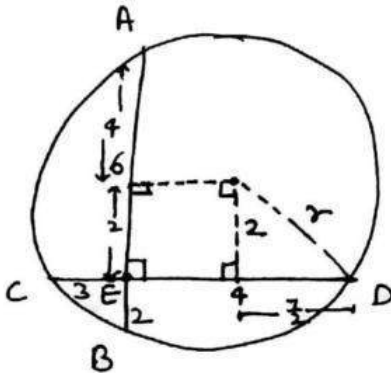
$$r = \sqrt{\frac{a^2 + b^2 + c^2}{2}}$$

#



$$AE \times EB = CE \times ED$$

- (65) AB and CD are two chords of a circle w/c intersects each other at right angle at E
 $AE = 6$, $EB = 2$, $CE = 3$, $r = ?$



$$6 \times 2 = 3 \times ED$$

$$ED = 4$$

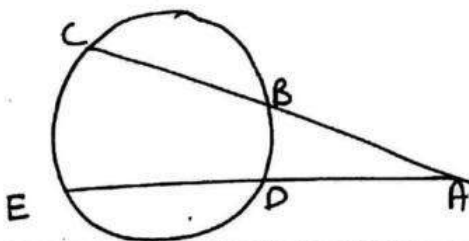
$$r^2 = 4 + \frac{49}{4}$$

$$r^2 = \frac{16 + 49}{4}$$

$$r^2 = \frac{65}{4}$$

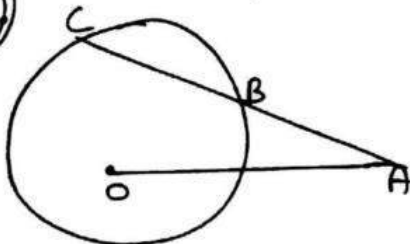
$$r = \frac{\sqrt{65}}{2}$$

#



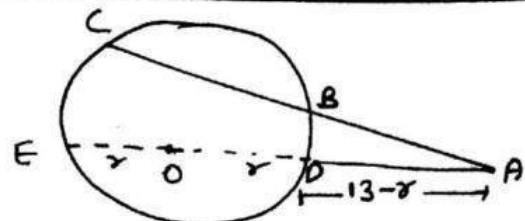
$$AB \times AC = AD \times AE$$

(66)



$$AB = 9, BC = 7$$

$$AO = 13, r = ?$$



$$AD = 13 - r$$

$$AE = 13 + r$$

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124

Advance Maths (Volume-2)

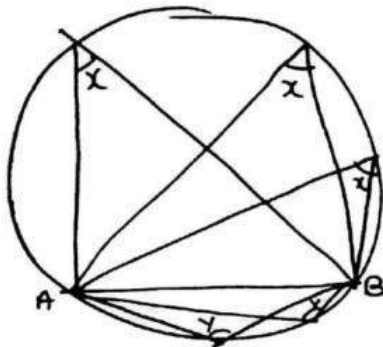
$$9 \times 16 = (13-x)(13+x)$$

$$144 = 169 - x^2$$

$$25 = x^2$$

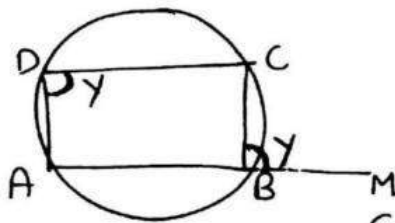
$$x = 5$$

#



angle made by the ^{same} chord on the same side of the circle are equal.

#



cyclic quadrilateral

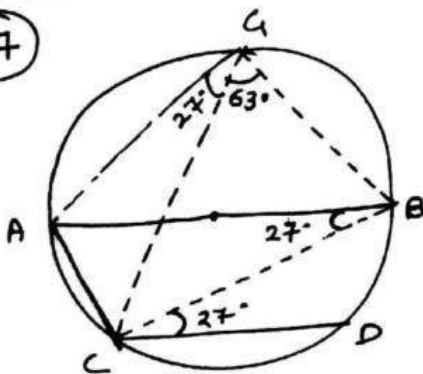
$$A + C = 180$$

$$B + D = 180$$

External angle is equal to opposite internal angle.

$$\angle CBM = \angle CDA = y$$

67



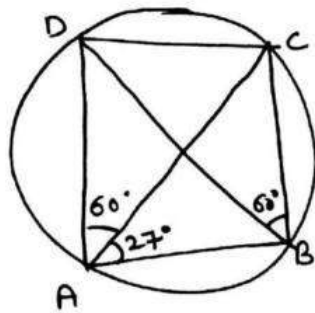
$AB \parallel CD$
 $\angle BCD = ?$

$AB \rightarrow$ diameter
angle made by
diameter = 90°
 $90 - 63^\circ = 27^\circ$

angle made by same chord AC
 $\therefore \angle ABC = 27^\circ$

$AB \parallel CD$
 $\therefore \angle BCD = 27^\circ$

68) $\angle BCD = ?$



$$\angle DBC = \angle DAC = 60^\circ$$

(angle made by same chord DC)

$$A + C = 180^\circ$$

$$67 + C = 180^\circ$$

$$C = 93^\circ$$

69) In a ΔABC , the angle bisector of angle A, B & C intersect the circumcircle at D, E & F.

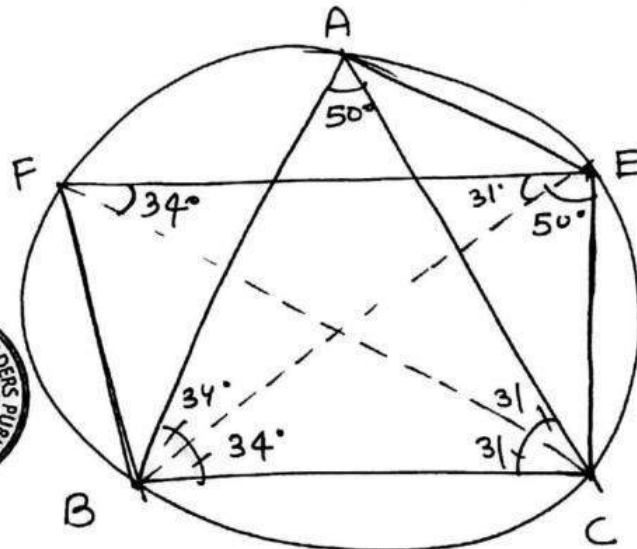
$$\angle A = 50^\circ$$

$$\angle EFC = 34^\circ$$

$$\angle FEB = ?$$

$$\angle FEC = ?$$

$$\angle AEC = ?$$



$$\angle EFC = \angle EBC = 34^\circ \text{ (Angle made by same chord EC)}$$

$$\angle B + \angle E = 180^\circ$$

$$68^\circ + \angle E = 180^\circ$$

$$\angle FEC = 112^\circ$$

$$\angle C = 62^\circ \quad (\because \angle A = 50^\circ, \angle B = 68^\circ)$$

$$\angle FEB = \angle FCB = 31^\circ \text{ (Angle made by same chord FB)}$$

$$\angle BAC = \angle BEC = 50^\circ \text{ (Angle made by same chord BC)}$$

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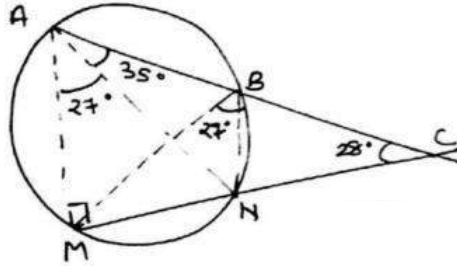
CLASS
54

70) ~~ABC and M~~ ABC & MNC are two secants of a circle cut at point C outside circle. AN is the diameter of the circle.

$$\angle C = 28^\circ$$

$$\angle NAB = 35^\circ$$

$$\angle MBN = ?$$



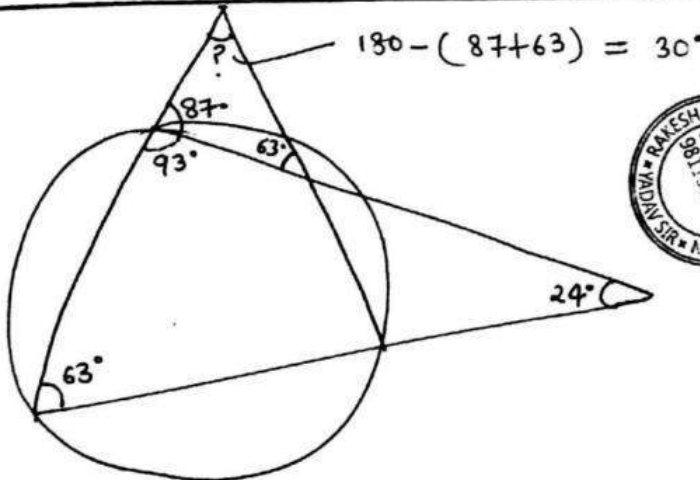
AN $\rightarrow$ diameter

$$\angle AMC = 90^\circ \text{ (angle in the half circle)}$$

$$\angle MAN = 180^\circ - (90^\circ + 28^\circ + 35^\circ) = 27^\circ$$

$$\angle MBN = 27^\circ \text{ (Angle made by the same chord MN).}$$

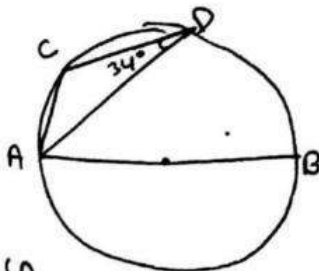
71



$$180 - (87 + 63) = 30^\circ$$

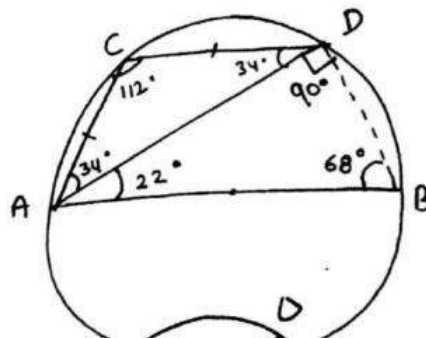


72



$$CA = CD$$

$$\angle OAB = ?$$



BC = OD
and intersecting
straight line
at a point
? $\angle BCD = 20^\circ$

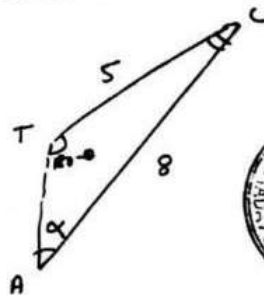
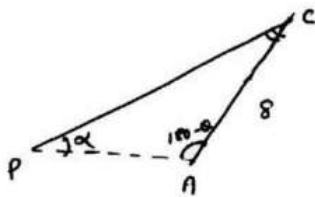
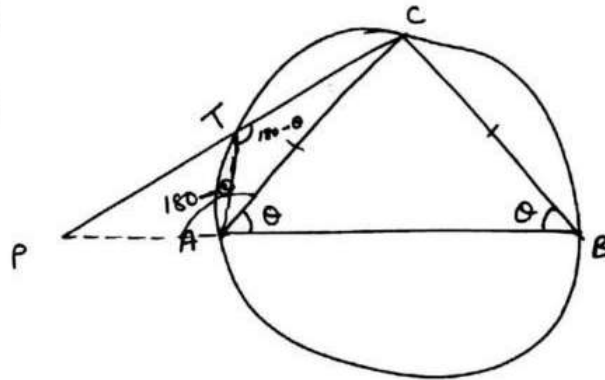
73) AC & BC are the length of two chords, the line BA is produced to any point P & when line CP is joined it cuts the circle at T .

$$AC = BC$$

$$CP = ?$$

$$CT = 5$$

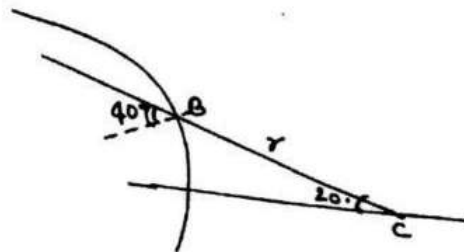
$$BC = 8$$



$$\frac{CP}{8}$$

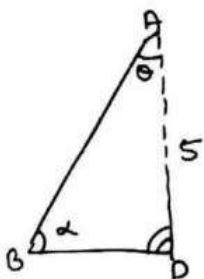
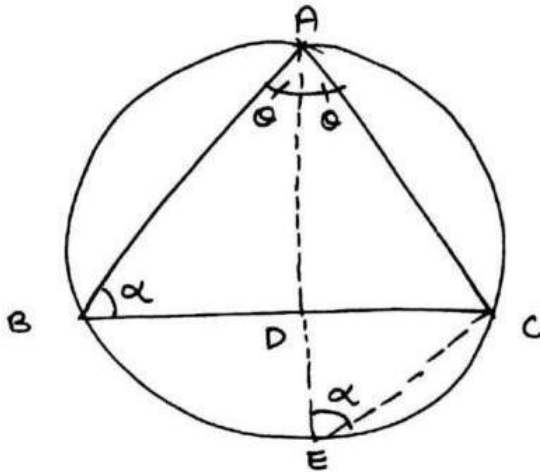
$$\therefore CP = \frac{64}{5} = 12.8$$

A circle of centre O . BOC is a $\angle$ from a point B on the circle producing at C .

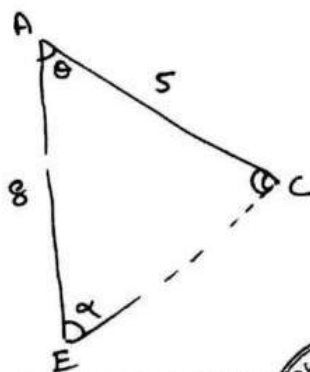


75) The bisector of angle $\angle A$ of a ΔABC cuts BC at D and the circumcircle of the Δ at E .

$DE = 3$
 $AC = 4$
 $AD = 5$
 $AB = ?$

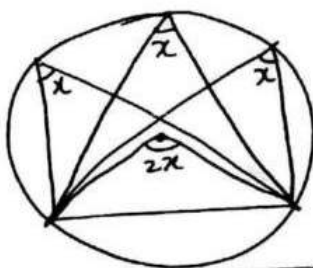


1155



$$\frac{AB}{8} = \frac{5}{4}$$

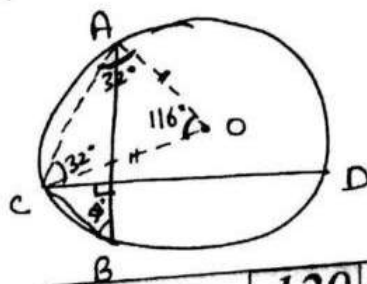
$$AB = 10$$



76) AB & CD are two chords of a circle w/c intersect each other at 90° . O is the centre of the circle.

$\angle CAO = 32^\circ$

$\angle BCD = ?$



$\angle CBA = 58^\circ$

(Half of the angle made by the same chord AC at centre)

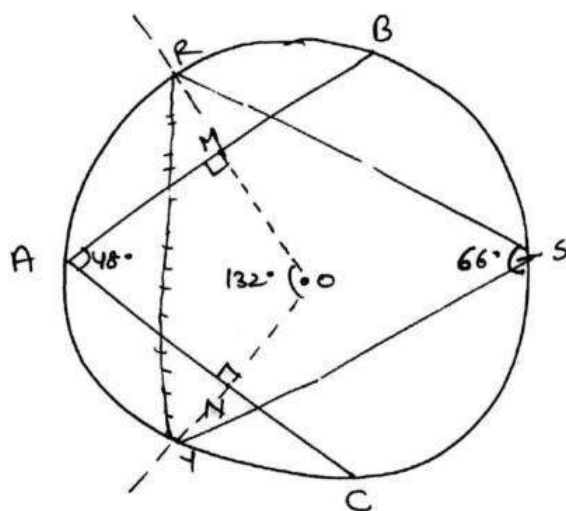
$\angle BCD = 180 - (90 + 58^\circ)$

Advance Maths (Volume-2)

- 77) AB & AC are two chords of a circle of centre O. M & N are their mid points. The line OM and ON are extended w/c intersects the circumcircle at R & Y. S is a point on major arc RY.

$$\angle A = 48^\circ$$

$$\angle RSY = ?$$



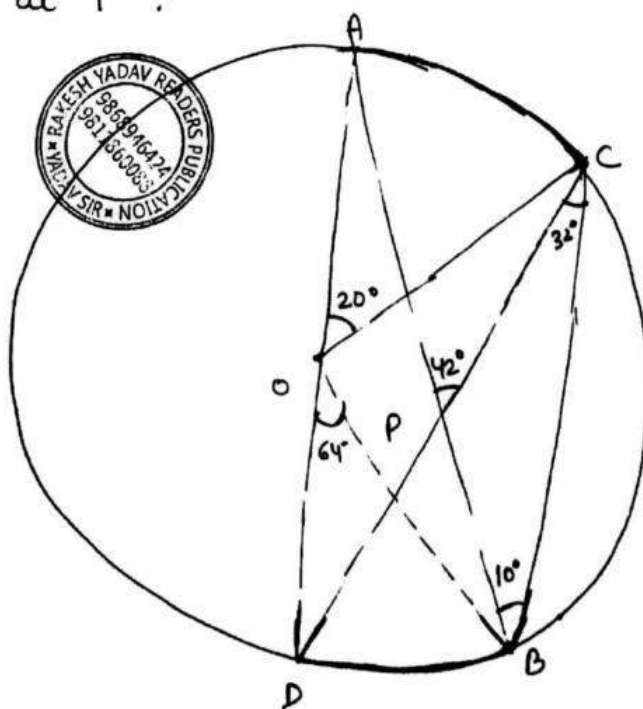
$$\angle RSY = 66^\circ$$

- 78) AB & CD are two chords of a circle w/c intersects each other at P.

$$\angle AOC = 20^\circ$$

$$\angle APC = 42^\circ$$

$$\angle BOD = ?$$



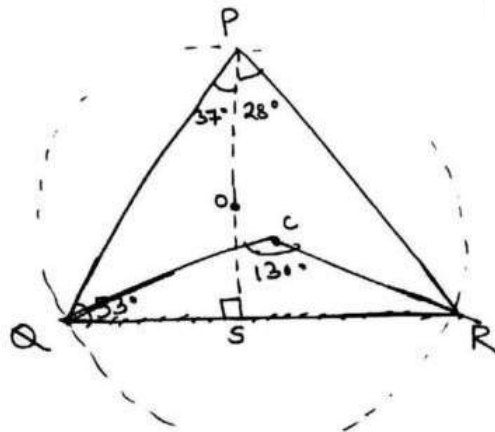
$$\angle BOD = 64^\circ$$

- 79) O and C are respectively orthocentre & circumcentre of an acute angle ΔPQR . The point P and O are joined and produced to meet the side QR at S

$$\angle QCR = 130^\circ$$

$$\angle RPS = ?$$

$$\angle PQS = 53^\circ$$



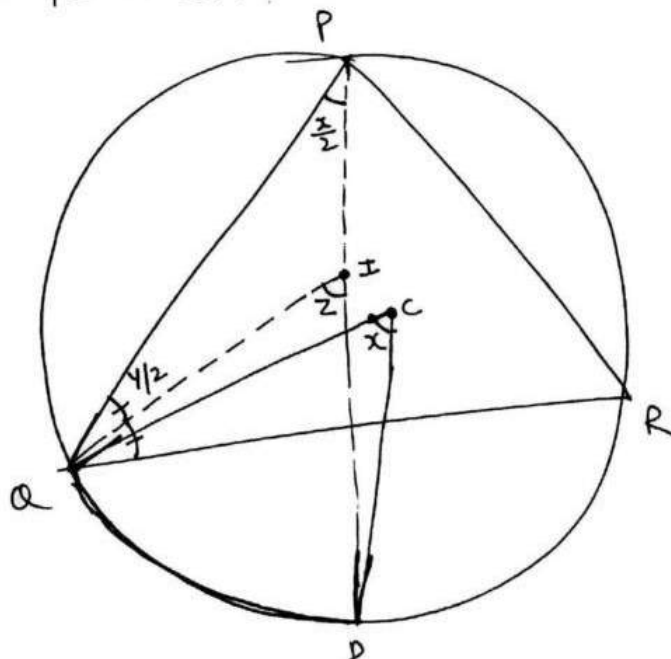
- 80) In ΔPQR , I & C are resp. incentre & circumcentre of the Δ . The line PI is extended w/c intersect the circumcircle at point D.

$$\angle QCB = x^\circ$$

$$\angle PQR = y^\circ$$

$$\angle QID = z^\circ$$

$$\frac{5x + 5y}{3z} = ?$$

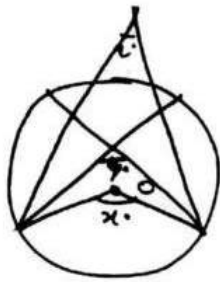


$$z = \frac{x}{2} + \frac{y}{2}$$

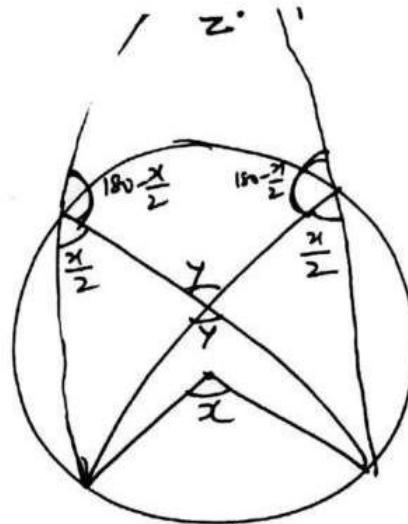
$$2z = x + y$$

$$\frac{5x + 5y}{3z} = \frac{5(x + y)}{3z} = \frac{5 \times 2z}{3z} = \frac{10}{3} \text{ Ans}$$

81



$$\frac{4y+4z}{3x}$$



$$\frac{4(y+z)}{3x}$$

$$\frac{4x}{3x}$$

$$= \frac{4}{3} \text{ Ans.}$$

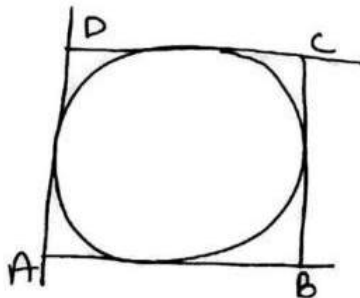
$$y+z+180-\frac{x}{2}+180-\frac{y}{2}+180-\frac{z}{2}=360^\circ$$

$$y+z-x=0$$

$$\boxed{y+z=x}$$

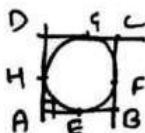
CLASS
55.

82



$$\boxed{AB+DC = AD+BC}$$

82

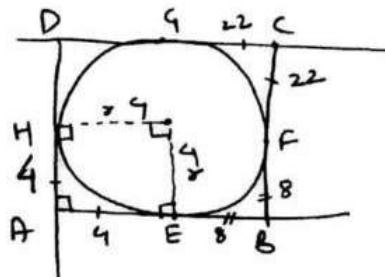


$$CD = 22$$

$$BC = 30$$

$$AB = 12$$

$$r = ?$$

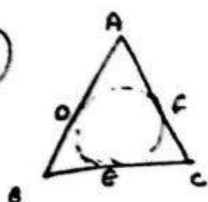


$$\boxed{r = 4} \text{ Ans}$$

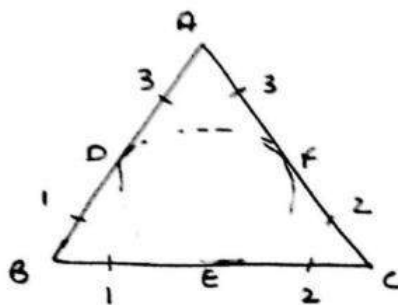
Rakesh Yadav

132 Advance Maths (Volume-2)

Q3



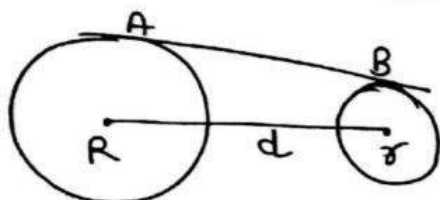
BE=1 what type
CF=2 of Δ it is
AD=3



sides of $\Delta = 3, 4, 5$
So: ABC is right angle Δ .

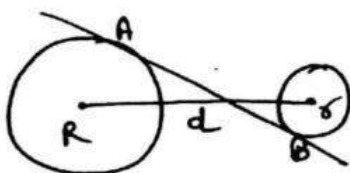
TANGENTS

#



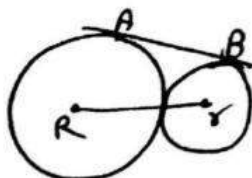
$$DCT (AB) = \sqrt{d^2 - (R-r)^2}$$

#



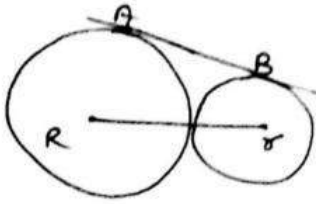
$$T.C.T = AB = \sqrt{d^2 - (R+r)^2}$$

#



$$AB = 2\sqrt{Rr}$$

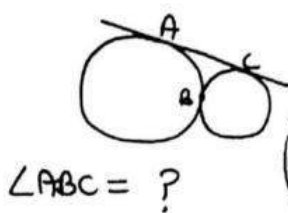
- (84) find the area of the square formed by the common direct tangent of two circles of radii 9 cm and 4 cm touch each other externally.



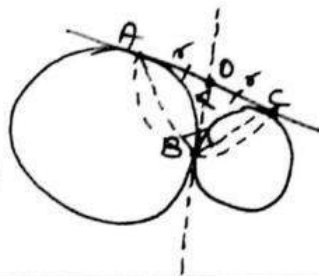
$$AB = 2\sqrt{9 \times 4} = 12$$

$$\text{Area of square of side } AB = 12^2 = 144 \text{ cm}^2$$

(85)

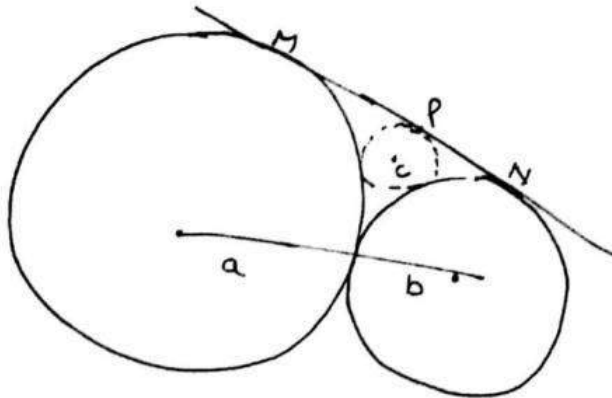


$\angle ABC = ?$



$\angle B = 90^\circ$

- (86) Two circles of radii a cm and b cm touch each other externally. Another circle of radius c touches both these circles externally & also touches their direct common tangent. find the relation b/w a , b and c .



$$\begin{array}{ccc} MN & MP & PN \\ 2\sqrt{ab} & 2\sqrt{ac} & 2\sqrt{bc} \end{array}$$

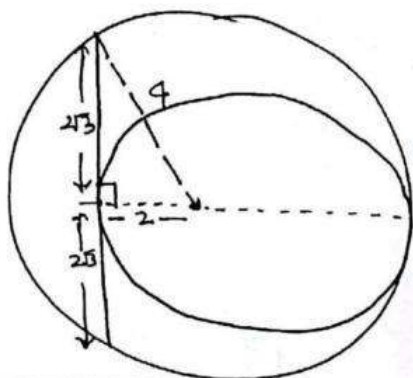
$$MN = MP + PN$$

$$2\sqrt{ab} = 2\sqrt{ac} + 2\sqrt{bc}$$

$$\frac{2\sqrt{ab}}{2\sqrt{abc}} = \frac{2\sqrt{ac}}{2\sqrt{abc}} + \frac{2\sqrt{bc}}{2\sqrt{abc}}$$

$$\boxed{\frac{1}{\sqrt{c}} = \frac{1}{\sqrt{b}} + \frac{1}{\sqrt{a}}}$$

- 87) Two circles of radius 4 cm & 3 cm touch each other internally. find the length of largest chord of the larger circle w/c is just outside the smaller circle.



$$\sqrt{4^2 - 2^2} = \sqrt{12} = 2\sqrt{3}$$

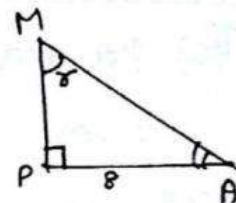
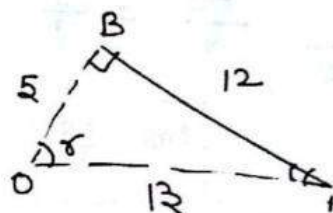
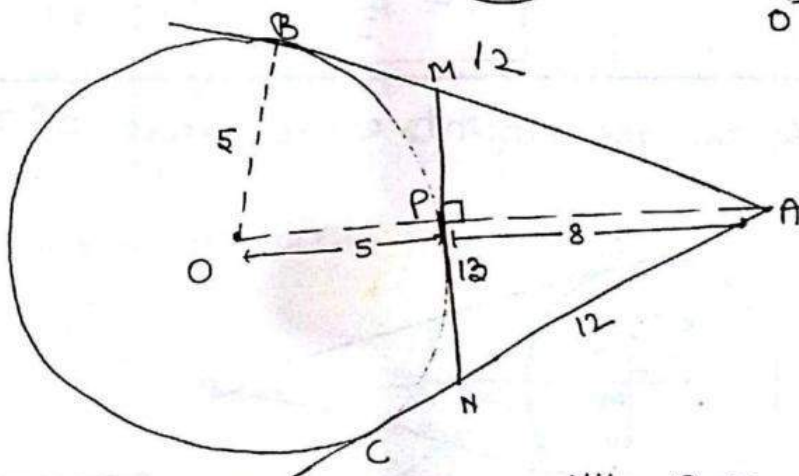
$$2\sqrt{3} + 2\sqrt{3} = 4\sqrt{3} \quad \underline{\text{Ans}}$$

- 88) ~~Find~~ AB and AC are the length of two tangents from a circle of radius 5 cm. find the length (minimum) of another tangent w/c intersects AB and AC at M & N.

$$MN = ?$$

$$r = 5$$

$$AB = 12$$



$$\frac{MP}{5} = \frac{8}{12}$$

$$MP = \frac{10}{3}$$

$$MN = \frac{10}{3} + \frac{10}{3} = \frac{20}{3}$$

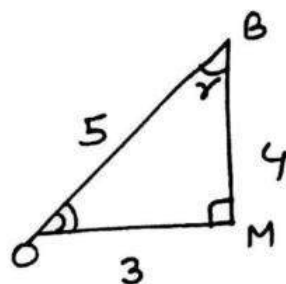
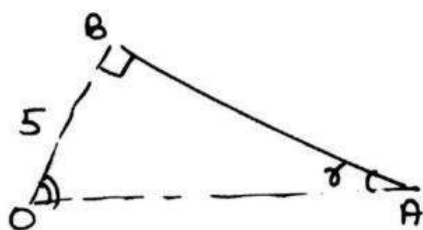
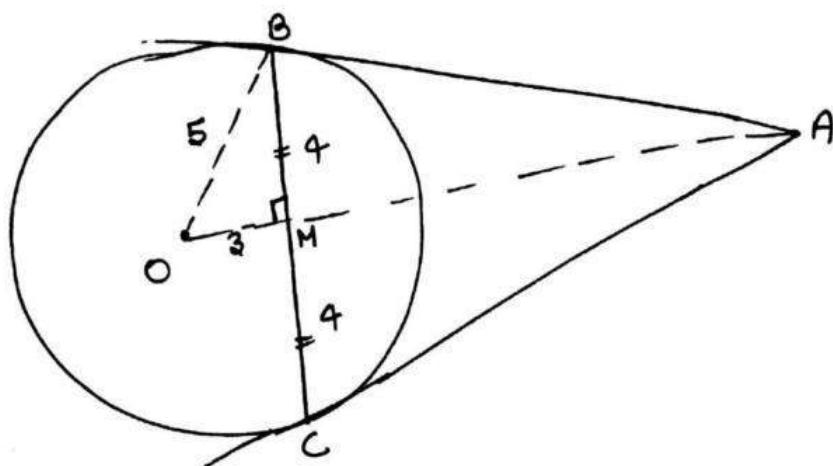
- 89) AB & AC are two tangents of circle of radius 5 cm.

$$r = 5 \text{ cm}$$

$$AB = ?$$

$$AO = ?$$

$$BC = 8$$



$$\frac{AB}{4} = \frac{5}{3}$$

$$AB = \frac{20}{3}$$

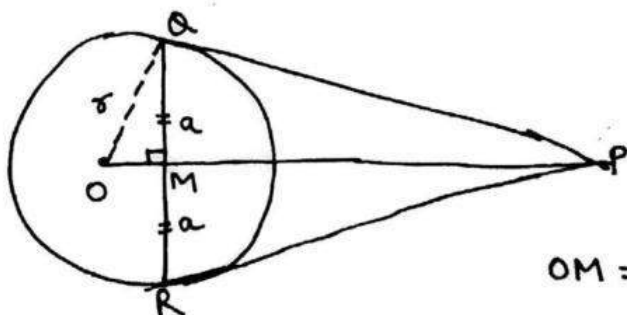
$$\frac{OA}{5} = \frac{5}{3}$$

$$OA = \frac{25}{3}$$

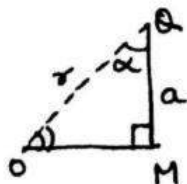
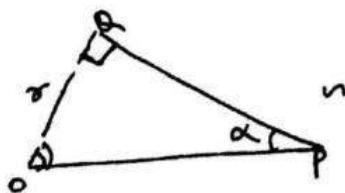
90) PQ and PR are the tangents of a circle of radius r cm

$$QR = 2a$$

$$PQ = ?$$



$$OM = \sqrt{r^2 - a^2}$$

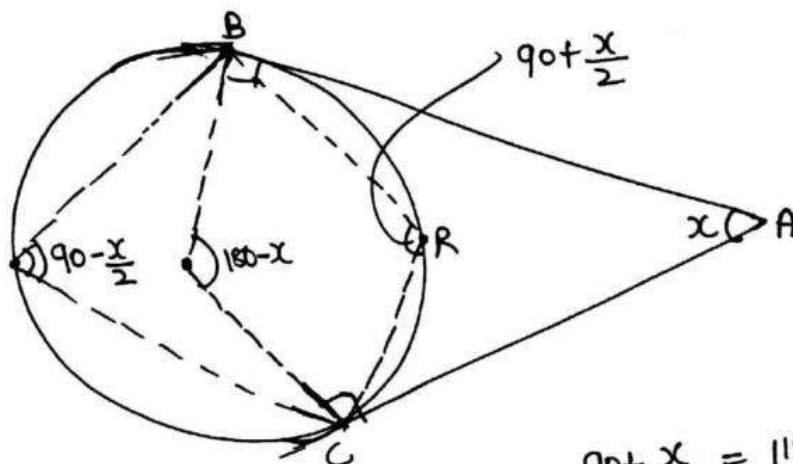


$$\frac{PQ}{a} = \frac{r}{\sqrt{r^2 - a^2}}$$

$$PQ = \frac{ar}{\sqrt{r^2 - a^2}}$$

Ans.

- 91) AB and AC are two tangents of a circle. R is a point on minor arc BC.
 $\angle BRC = 115^\circ$
 $\angle A = ?$



$$\angle BRC = 90 + \frac{x}{2}$$

$$90 + \frac{x}{2} = 115$$

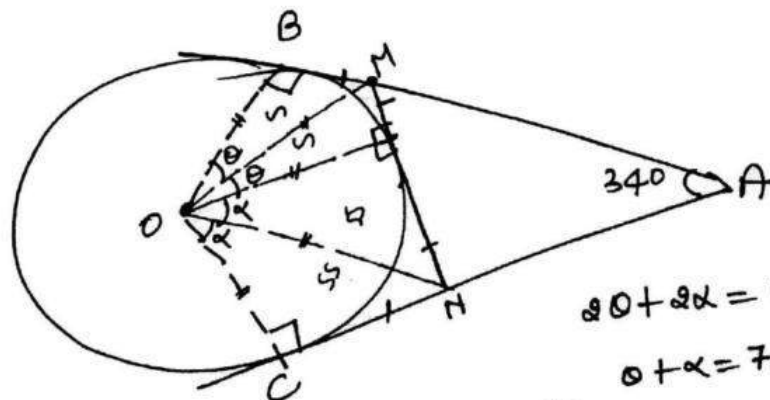
$$\frac{x}{2} = 25$$

$$x = 50^\circ$$

- 92) AB and AC are two tangents of a circle. O is the centre of the circle. MN is a tangent on the circle w/c intersects AB & AC at M & N. The tangent MN does not touch the circle at the point where the line OA intersects the circle.

$$\angle A = 34^\circ$$

$$\angle MON = ?$$



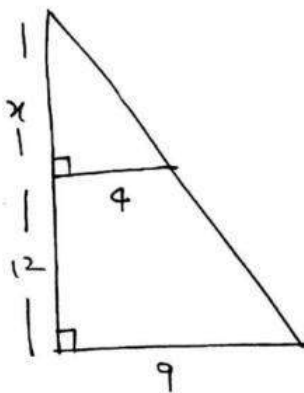
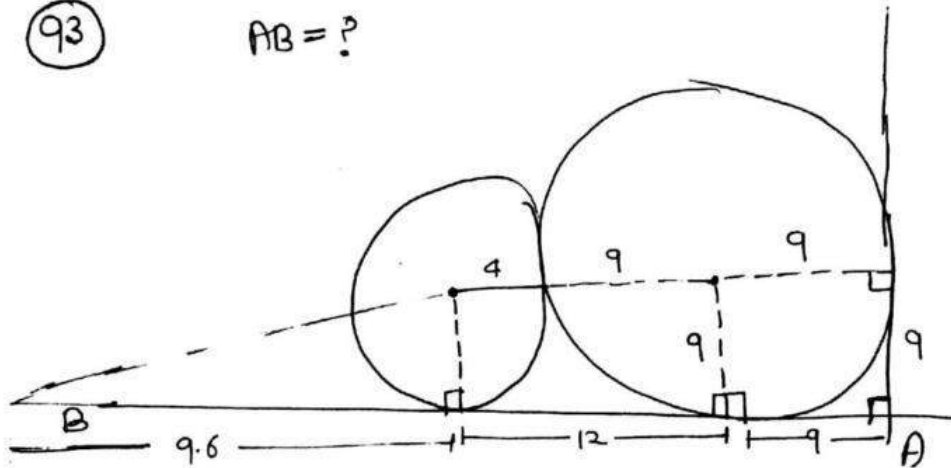
$$20 + 2\alpha = 146^\circ$$

$$0 + \alpha = 73^\circ$$

$$\angle MON = 73^\circ$$

93

AB = ?



$$\frac{x}{x+12} = \frac{4}{9}$$

$$9x = 4x + 48$$

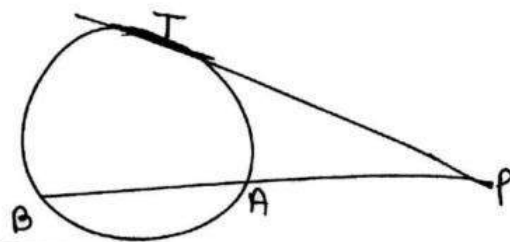
$$5x = 48$$

$$x = \frac{48}{5} = 9.6 \text{ cm}$$



$$AB = 9.6 + 12 + 9 = 30.6 \text{ cm}$$

94



$$PT^2 = PA \times PB$$

94 In an isosceles $\triangle ABC$ a circle goes through vertex B and touches the midpoint of line AC and intersects the line AB at M.

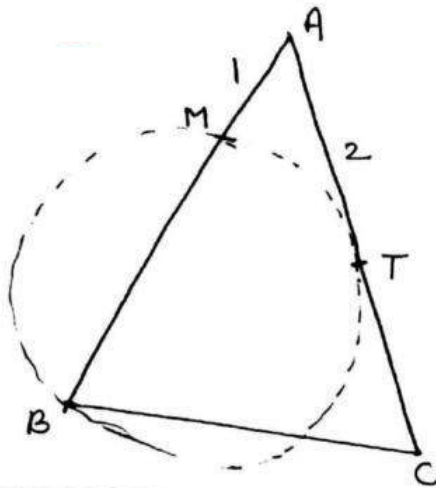
$$AB = AC$$

$$AM : MB = ?$$

Rakesh Yadav

138

Advance Maths (Volume-2)



$$AB = AC = 4 \text{ (cm)}$$

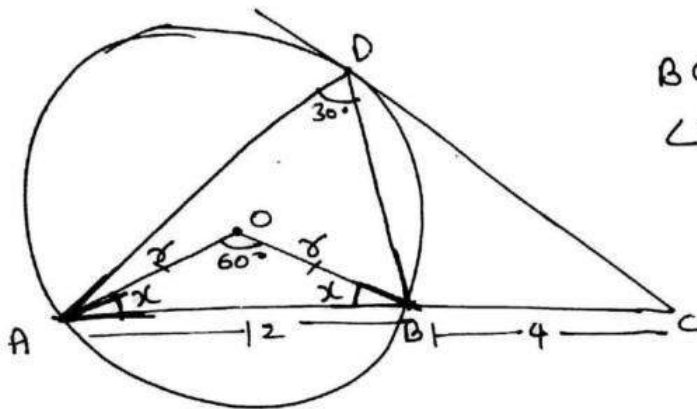
$$AT^2 = AM \times AB$$

$$AM = 1$$

$$AM : MB$$

$$1 : 3$$

Q5



$$BC = 4$$

$$\angle APB = 30^\circ$$

$$r = 12$$

$$CD = ?$$

$$x + x + 60 = 180$$

$$x = 60^\circ$$

$\triangle AOB$ is equilateral.



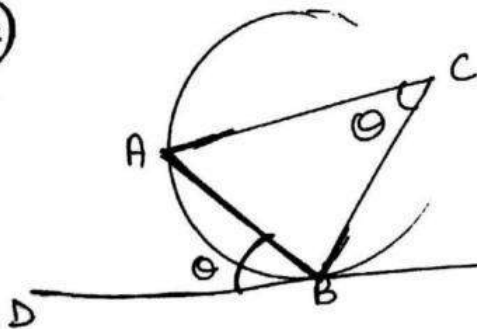
$$CD^2 = CB \times CA$$

$$CD^2 = 4 \times 16 = 64$$

$$CD = \sqrt{64}$$

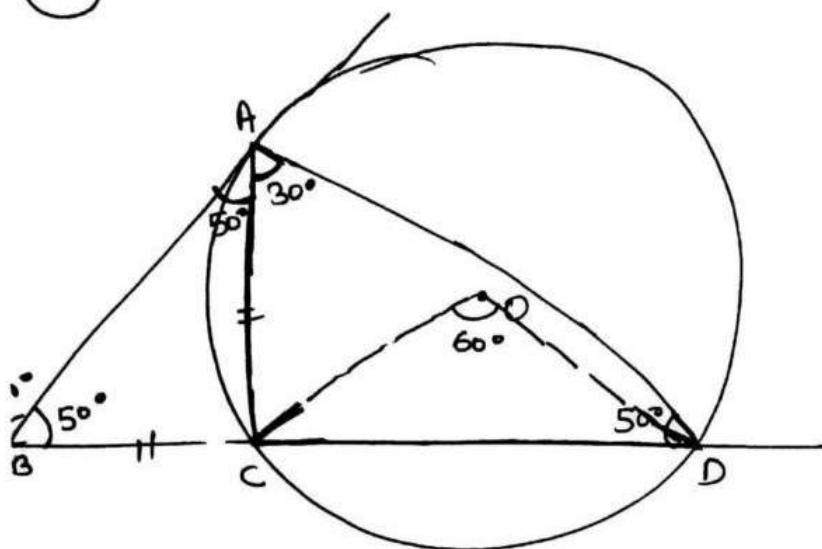
$$CD = 8 \text{ cm}$$

#



If angle θ is made from chord AB and tangent BD then the angle made by the chord AB in any part of the circle will be equal to θ .

96



$$BC = CA$$

$$\angle COD = ?$$

$\triangle ABD$

$$\angle B = 50^\circ, \angle D = 50^\circ$$

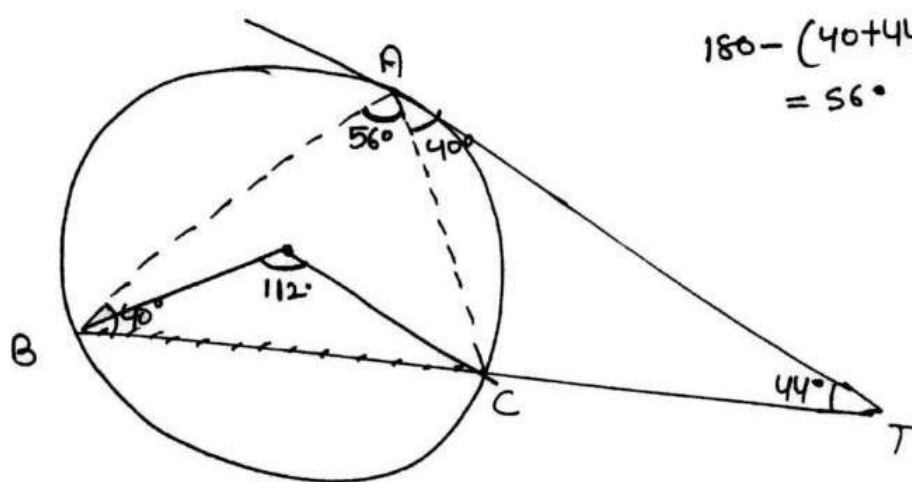
$$\angle BAC = 50^\circ$$

$$\therefore \angle CAD = 30^\circ$$

- 97) A, B, C are three points on a circle. A tangent touches the circle at A and intersects the extended part of line BC at T. Find the central angle made by chord BC.

$$\angle ATC = 44^\circ$$

$$\angle CAT = 40^\circ$$



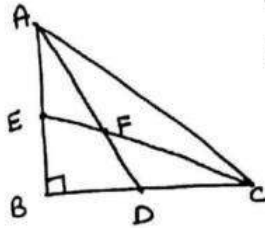
$$180 - (40 + 44 + 40)$$

$$= 56^\circ$$

$$\angle BOC = 112^\circ$$

CLASS
56

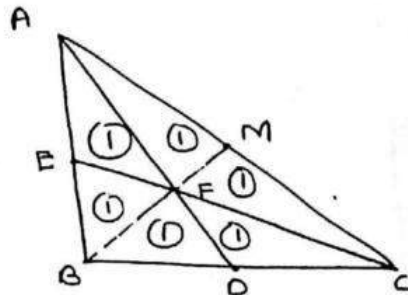
98



D is the mid point of BC

E is the mid point of AB

find Ar. $\triangle AFC$: Ar $\square BDFE$.



$$\frac{2}{2} = 1:1$$

99

In a $\triangle ABC$, $\angle A = 90^\circ$, BL and CN are two medians

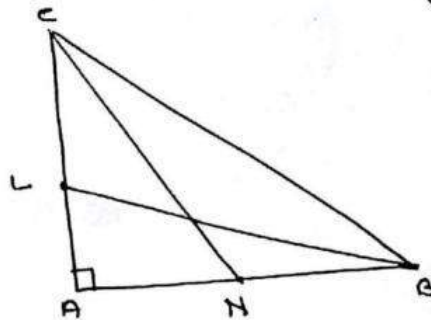
$$BC = 5$$

$$BL = \frac{3\sqrt{5}}{2}$$

$$CN = ?$$

#

$$4(BL^2 + CN^2) = 5(BC)^2$$



$$4\left(\left(\frac{3\sqrt{5}}{2}\right)^2 + (CN)^2\right) = 5 \times 25$$

$$4\left(\frac{45}{4} + CN^2\right) = 125$$

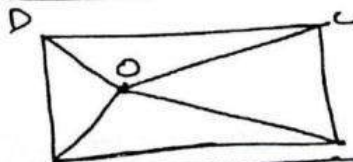
$$45 + 4CN^2 = 125$$

$$4CN^2 = 80$$

$$CN^2 = 20$$

$$CN = 2\sqrt{5}$$

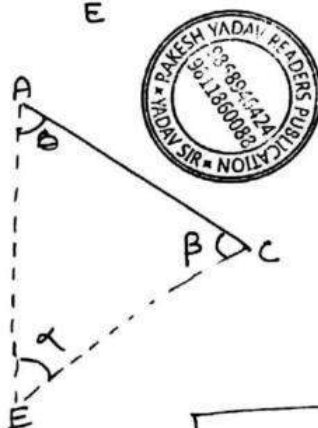
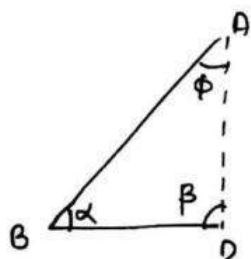
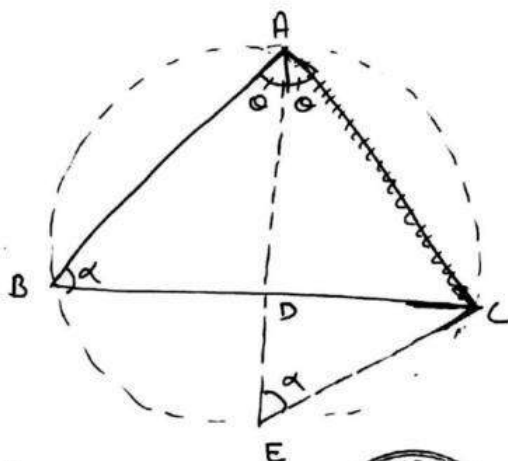
#



$$OD^2 + OB^2 = OA^2 + OC^2$$

(100) The bisector of $\angle A$ of a ΔABC intersects the side BC at D and meets the circumference of the ΔABC at E .

$$AB \times AC + DE \times AE = ?$$



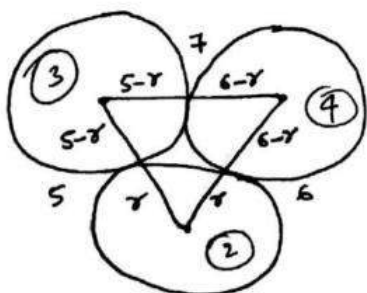
$$\frac{AB}{AE} = \frac{AD}{AC}$$

$$AB \times AC = (AE - DE) \times AE$$

$$= AE^2 - AE \times DE$$

$$AB \times AC + AE \times DE = AE^2 \quad \underline{\text{Ans.}}$$

(101) Three circles of ~~radius~~ touch each other externally and the distance b/w their centres is 5cm, 6cm & 7cm. Find the radius of all the centres.



$$5 - r + 6 - r = 7$$

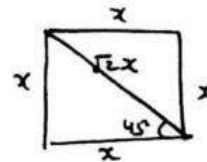
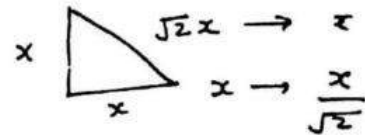
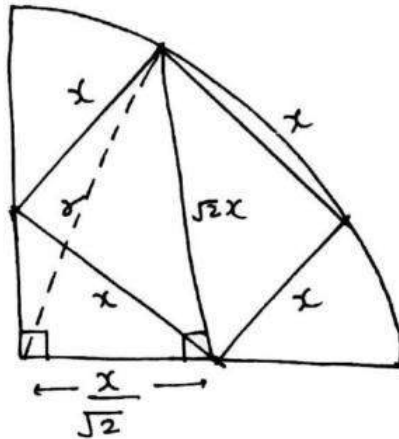
$$-2r = -4$$

$$r = 2$$

$$6 - 2 = 4$$

$$5 - 2 = 3$$

- 102) A square is inscribed in a quarter circle in such a manner that two vertices at equal distance from center while the other 2 vertices lie on the circular arc. If the square has side of the length x cm. find the radius of the circle.



$$r^2 = \frac{x^2}{2} + 2x^2$$

$$r^2 = \frac{5x^2}{2}$$

$$r = \sqrt{\frac{5}{2}} x$$



- 103) In a $\triangle ABC$, D & E are two points on AC & BC

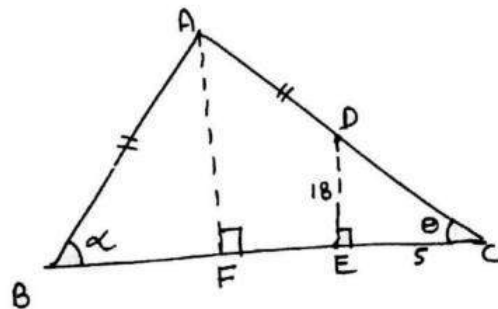
$$DE = 18$$

$$CE = 5$$

$$\angle DEC = 90^\circ$$

$$\tan \angle ABC = 3.6$$

$$AC : CD = ?$$



$$\tan \theta = \frac{P}{B} = \frac{18}{5} = 3.6$$

$$\tan \alpha = 3.6$$

$$\tan \theta = \tan \alpha \Rightarrow \theta = \alpha$$

$$\therefore AB = AC$$

$$BF = FC$$

$$FC = \frac{BC}{2}$$

$$\triangle AFC \sim \triangle DEC$$

$$\frac{CD}{CA} = \frac{CE}{CF}$$

$$\frac{CD}{CA} = \frac{2CE}{BC}$$

$$CA : CD =$$

$$BC : 2CE$$

(A) $BC : 2CE$

(B) $2CE : BC$

(C) $2BC : CE$

(D) $CE : 2BC$

104) In a ΔABC , D is a point on line BC and E is a point on line AD in such a way -

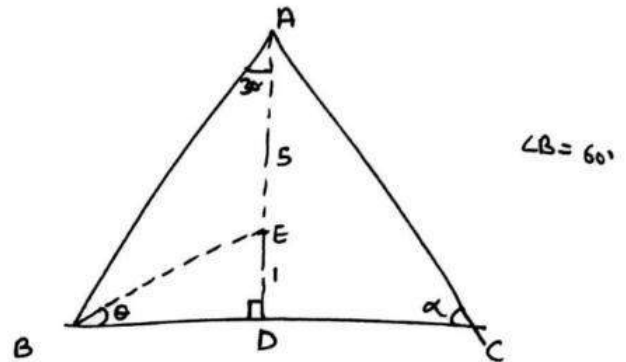
$$AD \perp BC$$

$$AE : ED = 5 : 1$$

$$\angle BAD = 30^\circ$$

$$\tan \angle ACB = 6 \tan \angle DBE$$

$$\angle ACB = ?$$



$$\tan \theta = \frac{1}{BD}$$

$$\tan \alpha = \frac{6}{DC}$$

$$\tan \alpha = 6 \tan \theta$$

$$\frac{6}{DC} = \frac{6}{BD}$$

$$\boxed{DC = BD}$$

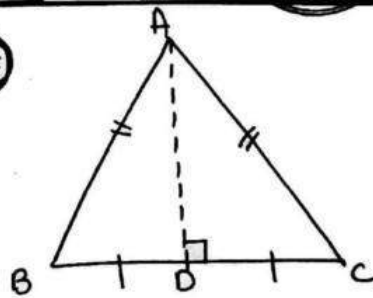
$$\therefore AB = AC$$

$$\therefore \angle B = \angle C$$

$$\therefore \boxed{\angle C = 60^\circ}$$



#



In an isosceles Δ , if a $\perp$ is drawn from the common vertex of two equal sides on the opposite side then it will divide the opposite side in two equal parts.

ABC is isosceles Δ

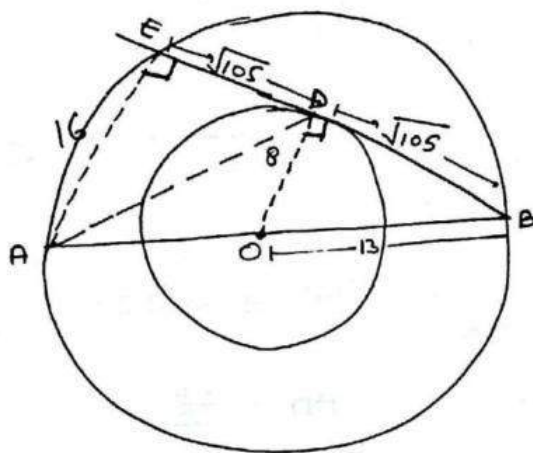
$$AB = AC$$

$$AD \perp BC$$

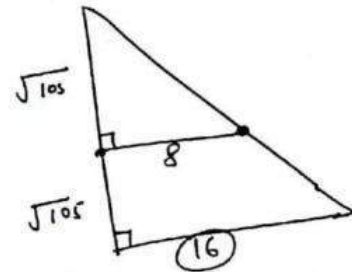
$$\therefore \boxed{BD = DC}$$

& vice-versa.

- 105) The radius of two concentric circles are 13 cm & 8 cm. AB is the diameter of larger circle and BD is a tangent to the smaller circle touching it at D and the larger circle at E. Point A is joined to D. find AD.



$$BD = \sqrt{105}$$



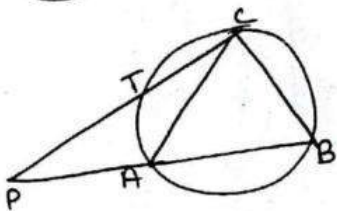
$$AD = \sqrt{(\sqrt{105})^2 + 16^2}$$

$$= \sqrt{105 + 256} = \sqrt{361}$$

$$AD = 19$$

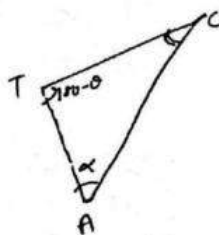
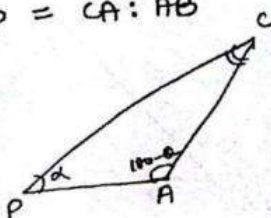


- 106) AC and BC are two chords.



A) $CT:TP = AB:CA$

B) $CT:TP = CA:AB$



$$\frac{CT}{CA} = \frac{CA}{PC}$$

- 107) In an isosceles Δ $\angle B$ is right angle. D is a point in ΔABC and P & Q are points on AB and AC in such a way

$$DP \perp AB$$

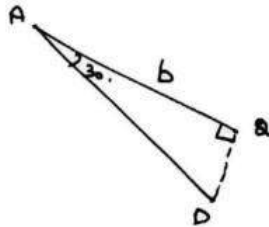
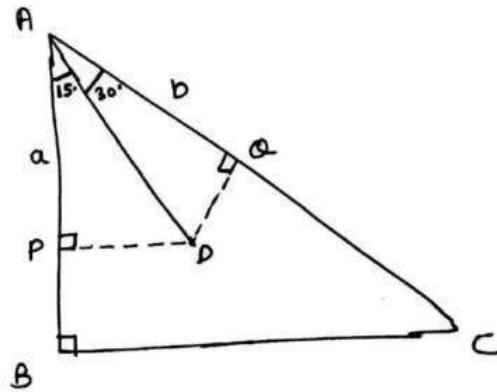
$$DQ \perp AC$$

$$AP = a$$

$$AQ = b$$

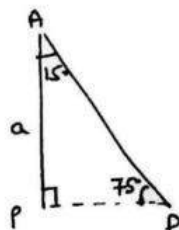
$$\angle BAD = 15^\circ$$

$$\sin 75^\circ = ?$$



$$\frac{AD}{b} = \sec 30^\circ$$

$$AD = \frac{2b}{\sqrt{3}}$$



$$\sin 75^\circ = \frac{a}{AD} = \frac{a}{\frac{2b}{\sqrt{3}}} = \frac{\sqrt{3}a}{2b}$$

$$\sin 75^\circ = \frac{a\sqrt{3}}{2b}$$



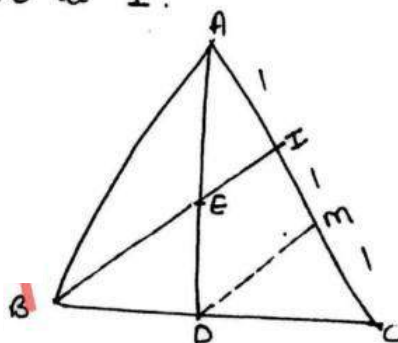
- 108) E is the mid point of median AD of ΔABC . On extending BE it intersects AC at I.

$$AB = 18$$

$$AC = 15$$

$$BC = 20$$

$$CI = ?$$



$$\begin{matrix} 3 \rightarrow 15 \\ 1 \rightarrow 5 \end{matrix}$$

$$CI = 10$$

Ans

CO-ORDINATE Geometry.

#

$$4x + 3y = 12$$

$$2x + 5y = 10$$

$$x = \frac{15}{7}, y = \frac{8}{7}$$



#

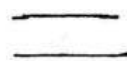
$$a_1x + b_1y = c_1$$

$$a_2x + b_2y = c_2$$

unique solution $\Rightarrow \frac{a_1}{a_2} \neq \frac{b_1}{b_2}$
(meet at a point)



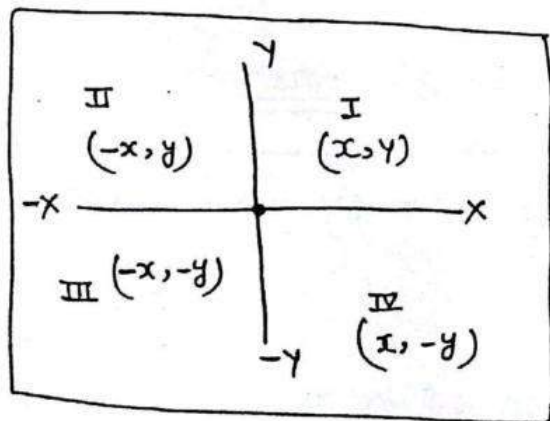
No solution $\Rightarrow \frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$
(doesn't meet)



infinite many soln $\Rightarrow \frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$
(one line on another line)



#

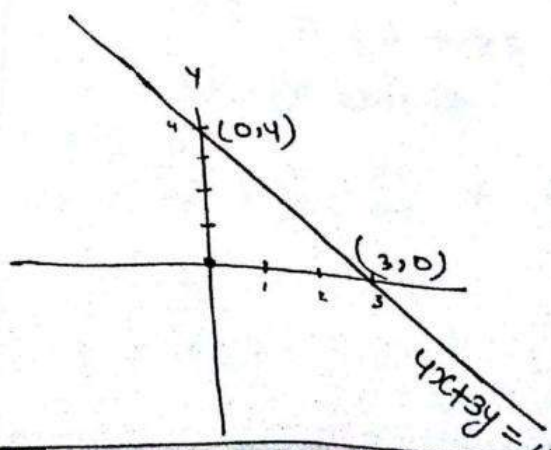


①

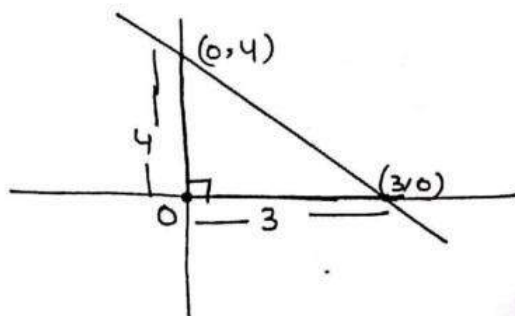
$$4x + 3y = 12$$

$$x=0, y=4 \Rightarrow (0, 4)$$

$$y=0, x=3 \Rightarrow (3, 0)$$



- ② find area of Δ made by $4x + 3y = 12$, x-axis and y-axis



Area of $\Delta =$

$$\frac{1}{2} \times 3 \times 4 = 6 \text{ Ans.}$$

(OR)

if two sides of a Δ are x-axis and y-axis then it will be a right angle Δ .

Q. $4x + 3y = 12$

divide by 12

$$\frac{4x}{12} + \frac{3y}{12} = \frac{12}{12}$$

$$\frac{x}{3} + \frac{y}{4} = 1$$

base $\swarrow$ $\searrow$ perpendicular

$$\text{Area of } \Delta = \frac{1}{2} \times 3 \times 4 = 6 \text{ Ans.}$$

- ③ find area of Δ made by $8x + 6y = 60$, x-axis and y-axis.

$$8x + 6y = 60$$

divide by 60

$$\frac{8x}{60} + \frac{6y}{60} = \frac{60}{60}$$

$$\frac{x}{7.5} + \frac{y}{10} = 1$$

B $\swarrow$

P $\searrow$

Area of $\Delta =$

$$\Rightarrow \frac{1}{2} \times 7.5 \times 10$$

$$\Rightarrow 37.5 \text{ Ans.}$$

- 2) find the area of trapezium made by $8x + 6y = 60$, $4x + 3y = 12$, x-axis and y-axis. (1)

$$8x + 6y = 60$$

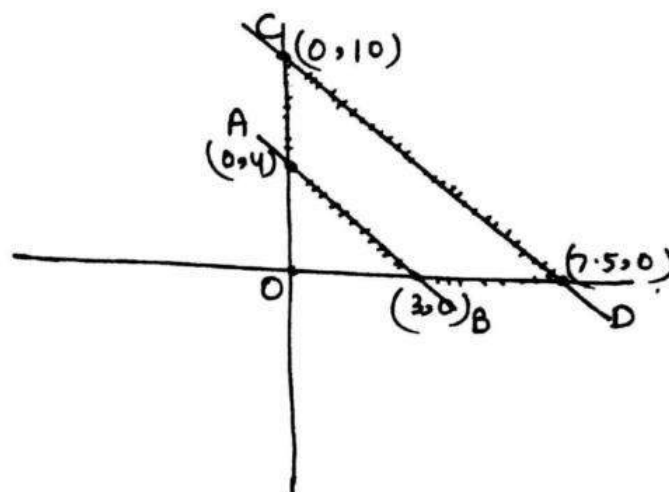
$$x=0, y=10 \Rightarrow (0, 10)$$

$$y=0, x=7.5 \Rightarrow (7.5, 0)$$

$$4x + 3y = 12$$

$$x=0, y=4 \Rightarrow (0, 4)$$

$$y=0, x=3 \Rightarrow (3, 0)$$



$$\text{Area of } \triangle OCD = \frac{1}{2} \times 10 \times 7.5 = 37.5$$

$$\text{Area of } \triangle OAB = \frac{1}{2} \times 4 \times 3 = 6$$

$$\begin{aligned} \text{Area of trapezium } ABCD &= \text{Area of } \triangle OCD - \text{Area of } \triangle OAB \\ &\Rightarrow 37.5 - 6 = 31.5 \text{ Ans.} \end{aligned}$$

- 3) find the area ~~made~~ of the trapezium made by $5x + 3y = 15$, $15x + 9y = 270$, x-axis and y-axis.

Area of $\triangle$ made by line $15x + 9y = 270$

$$\frac{15x}{270} + \frac{9y}{270} = \frac{270}{270}$$

$$\frac{x}{18} + \frac{y}{30} = 1$$

$$\Rightarrow \frac{1}{2} \times 18 \times 30 = 270$$

Area of $\triangle$ made by line $5x + 3y = 15$

$$\frac{5x}{15} + \frac{3y}{15} = \frac{15}{15}$$

$$\frac{x}{3} + \frac{y}{5} = 1$$

$$\Rightarrow \frac{1}{2} \times 3 \times 5 = 7.5$$

Area of trapezium =

$$270 - 7.5$$

$$= 262.5 \text{ Ans.}$$

- ⑥ find the area of Δ made by $4x+3y=12$, $5x+7y=35$ and x -axis.

$$4x+3y=12$$

$$y=0, x=3 \Rightarrow (3,0)$$

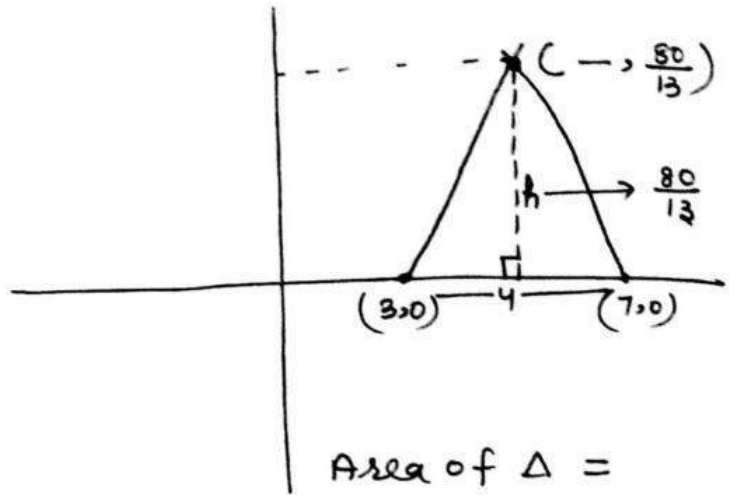
$$5x+7y=35$$

$$y=0, x=7 \Rightarrow (7,0)$$

$$4x+3y=12$$

$$5x+7y=35$$

$$y = \frac{80}{13}$$



Area of $\Delta =$

$$\frac{1}{2} \times 4 \times \frac{80}{13}$$

$$= \frac{160}{13} \text{ Ans}$$

- ⑦ find the area of Δ made by $x+2y=8$, $5x+3y=15$ and y -axis.

$$x+2y=8$$

$$x=0, y=4 \Rightarrow (0,4)$$

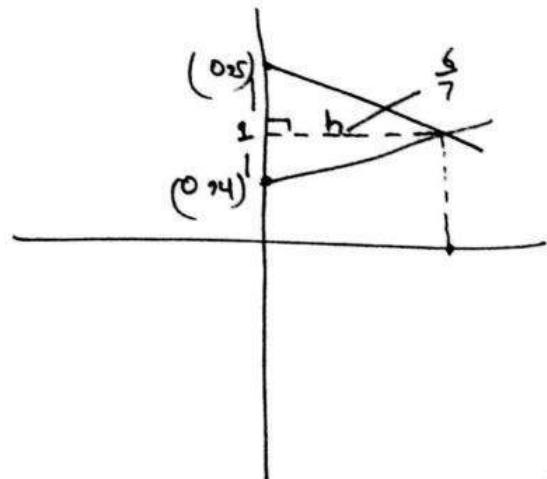
$$5x+3y=15$$

$$x=0, y=5 \Rightarrow (0,5)$$

$$x+2y=8$$

$$5x+3y=15$$

$$x = \frac{6}{7}$$



$$\text{Area} = \frac{1}{2} \times 1 \times \frac{6}{7}$$

$$= \frac{3}{7} \text{ Ans}$$

Linear Inequalities

③ $4x + 3y \geq 12$

$4x + 3y = 12$

$x=0, y=4 \Rightarrow (0, 4)$

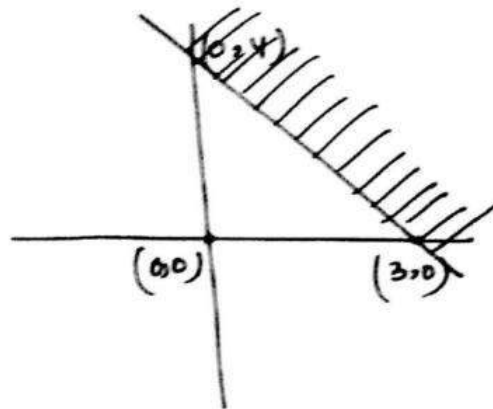
$y=0, x=3 \Rightarrow (3, 0)$

$4x + 3y \geq 12$

put $x=0, y=0$

$0+0 \geq 12$ (Not satisfied means shadow will be away from the origin.)

↓ if this condition satisfies then shadow will be towards the origin.



⑨ $x \geq -y$

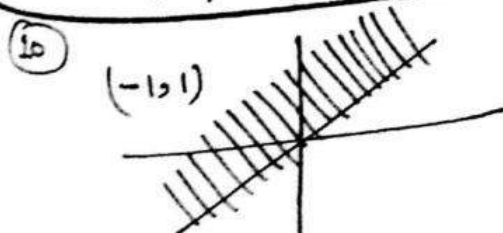
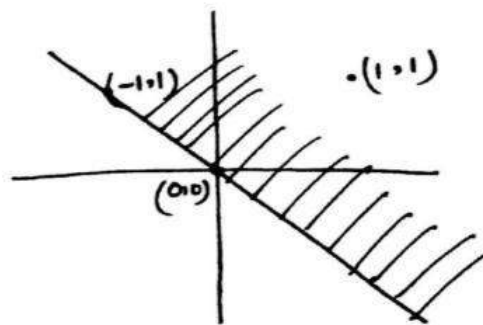
$x = -y$

x	y
0	0
-1	1

$x \geq -y$

put $x=1, y=1$

$1 \geq -1$ (true - so shadow will be towards (1, 1))



A) $x \geq y$

C) $x \geq -y$

B) $x \leq y$

D) $x \leq -y$

In this line either both positive or both -ve. So, option C & D can be

option A $\rightarrow x \geq y$
 $-1 \geq 1$

Hence B ✓

(X)

Put $x = -1, y =$
($\because$ in 2nd quad
to check the
condition).

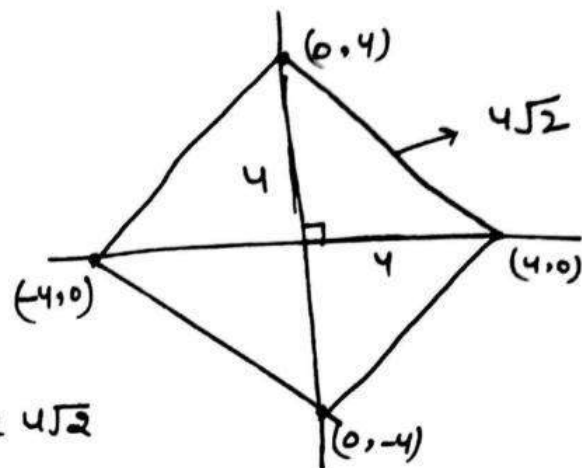
⑪ find the area of the figure bounded by $|x| + |y| = 4$

$$x + y = 4$$

$$-x + y = 4$$

$$x - y = 4$$

$$-x - y = 4$$



Square formed with side $4\sqrt{2}$

$$\text{Area} = (4\sqrt{2})^2 = 32 \text{ Ans}$$

⊕

$$\text{if } |x| + |y| = K$$

$$\text{Area} = 2K^2$$

⊕

$$\text{Area} = 2(4)^2$$

$$= 32 \text{ Ans}$$

⊕

$$x + |y| = K$$

$$|x| + y = K$$

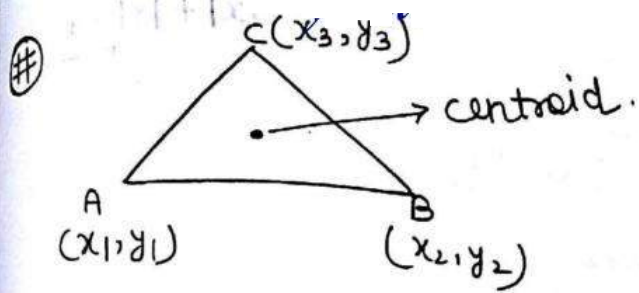
In both cases

$$\text{Area} = K^2$$

⊕

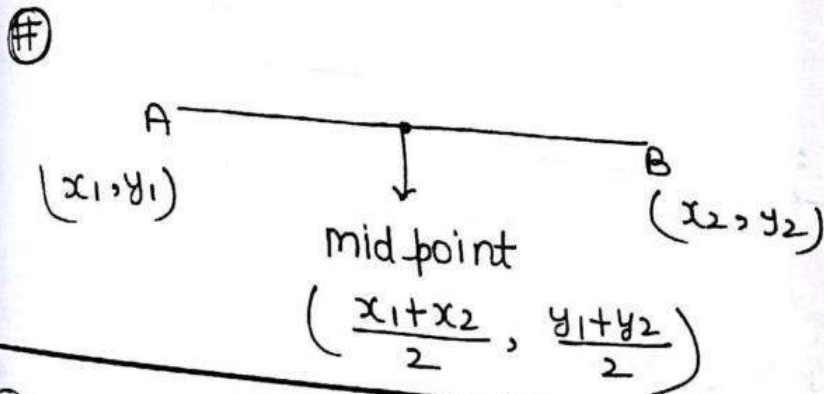
$$\begin{array}{cc} A & B \\ (x_1, y_1) & (x_2, y_2) \end{array}$$

$$AB = \sqrt{(y_2 - y_1)^2 + (x_2 - x_1)^2}$$



$$\text{Area}_{\triangle ABC} = \frac{1}{2} \left| x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2) \right|$$

Vertex of centroid = $\left(\frac{x_1 + x_2 + x_3}{3}, \frac{y_1 + y_2 + y_3}{3} \right)$



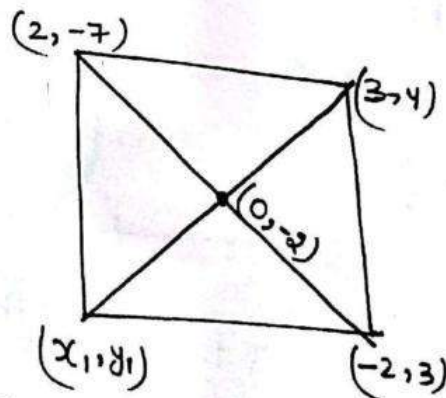
$$\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

12) Find 4th vertex of a rhombus whose 3 vertices are - $(-2, 3)$, $(3, 4)$, $(2, -7)$

mid point of diagonal $\Rightarrow$

$$\frac{-2-2}{2}, \frac{-7+3}{2}$$

$$(0, -2)$$



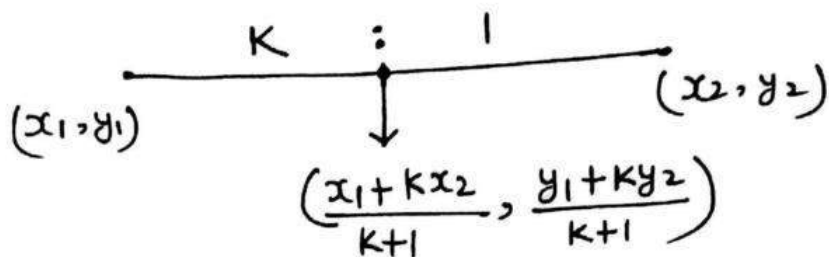
$\therefore$ diagonals bisect each other

$$\frac{x_1 + 3}{2} = 0 \Rightarrow x_1 = -3$$

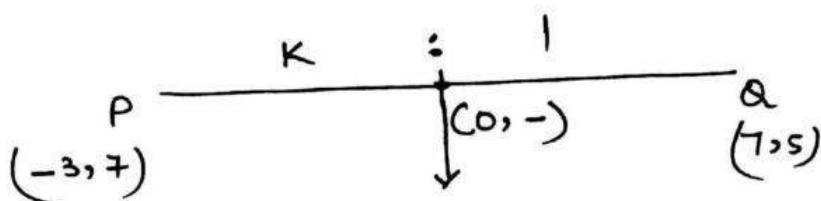
$$\frac{y_1 + 4}{2} = -2 \Rightarrow y_1 = -8$$

$(-3, -8)$ Ans.

##



⑬ find the ratio in w/c y-axis intersect the line PA



$$\frac{-3 + K \times 7}{K+1}, \frac{7 + K \times 5}{K+1}$$

$$\frac{-3 + 7K}{K+1} = 0 \quad (\text{on y axis, x is zero})$$

$$-3 + 7K = 0$$

$$K = \frac{3}{7}$$

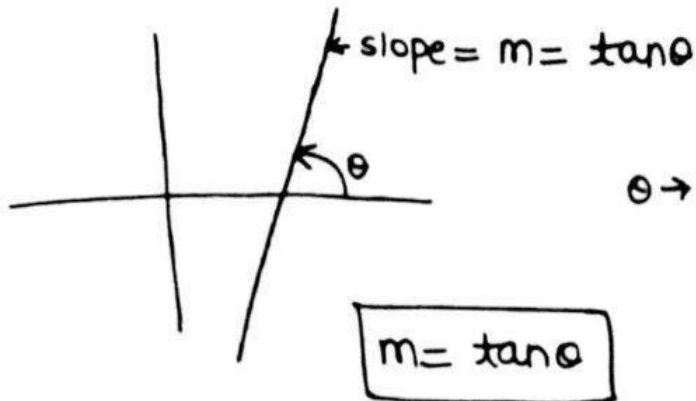
$$\text{Ratio} \Rightarrow \frac{3}{7} : 1$$

$$3 : 7 \quad \underline{\text{Ans.}}$$



SLOPE

⑧



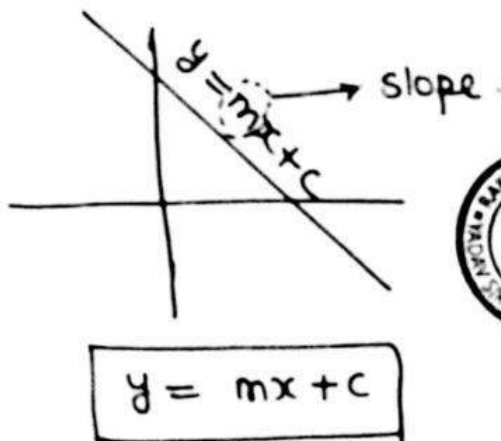
$\theta \rightarrow$ always anticlockwise वाला लेना है ।

⑨



$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

⑩



$$4x + 3y = 12$$

$$3y = -4x + 12$$

$$y = -\frac{4}{3}x + \frac{12}{3}$$

$$\text{slope}(m) = -\frac{4}{3}$$

⑪

$$\sqrt{3}y - 3x = 5, \text{ find slope } (\theta = ?)$$

$$\sqrt{3}y = 3x + 5$$

$$y = \frac{3}{\sqrt{3}}x + \frac{5}{\sqrt{3}}$$

$$y = \underbrace{(\sqrt{3})}_{\text{slope}}x + \frac{5}{\sqrt{3}}$$

$$\tan \theta = \sqrt{3}$$

$$\tan \theta = \tan 60^\circ$$

$$\theta = 60^\circ \quad \underline{\text{Ans}}$$

⑮ Find the angle between lines

$$x - y\sqrt{3} = 5$$

$$\sqrt{3}x + y = 7$$

$$x - y\sqrt{3} = 5$$

$$y\sqrt{3} = x - 5$$

$$y = \left(\frac{1x}{\sqrt{3}}\right) - \frac{5}{\sqrt{3}}$$

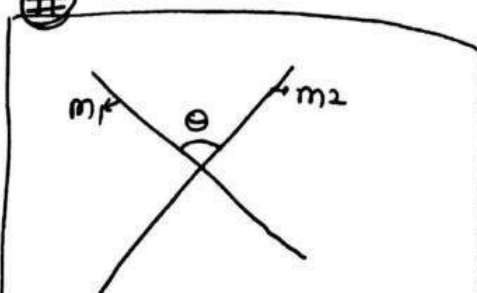
$$m_2 = \frac{1}{\sqrt{3}}$$

$$\sqrt{3}x + y = 7$$

$$y = -\sqrt{3}x + 7$$

$$m_1 = -\sqrt{3}$$

⑮



$$\tan \theta = \left| \frac{m_1 - m_2}{1 + m_1 m_2} \right|$$

$$\tan \theta = \left| \frac{-\sqrt{3} - \frac{1}{\sqrt{3}}}{1 + (-\sqrt{3})\frac{1}{\sqrt{3}}} \right|$$

$$\tan \theta = \infty = \tan 90^\circ$$

$$\theta = 90^\circ$$

⑯ Find the perpendicular distance b/w $4x + 3y = 16$ &

$$8x + 6y = 18$$

$$4x + 3y = 16$$

$$4x + 3y = 9$$



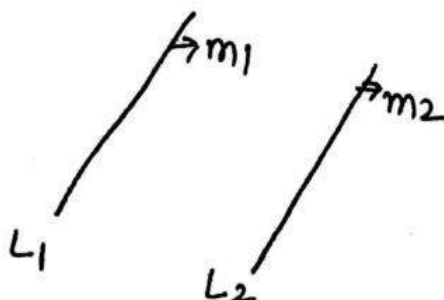
$$\perp \text{ distance} = \left| \frac{16-9}{\sqrt{4^2+3^2}} \right| = \frac{7}{5} \text{ Ans}$$

$$ax + by = c_1$$

$$ax + by = c_2$$

$$\perp \text{ distance} = \left| \frac{c_1 - c_2}{\sqrt{a^2 + b^2}} \right|$$

⑰



if $L_1 \parallel L_2$

$$m_1 = m_2$$

7) find the $\perp$ distance from a vertex $(-3, 2)$ to the line $3x + 4y = 16$.

$$\perp \text{ distance} = \left| \frac{-9 + 8 + 16}{\sqrt{4^2 + 3^2}} \right|$$

$$= \frac{+5}{5} = 3 \text{ Ans.}$$

