

CBSE Board
Class IX Mathematics
Sample Paper 2

Time: 3 hrs

Total Marks: 80

General Instructions:

1. All questions are **compulsory**.
 2. The question paper consists of **30** questions divided into **four sections** A, B, C, and D. **Section A** comprises of **6** questions of 1 mark each, **Section B** comprises of **6** questions of 2 marks each, **Section C** comprises of **10** questions of 3 marks each and **Section D** comprises of **8** questions of 4 marks each.
 3. Question numbers **1 to 6** in **Section A** are multiple choice questions where you are to select **one** correct option out of the given four.
 4. Use of calculator is **not** permitted.
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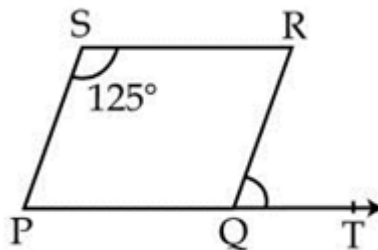
Section A
(Questions 1 to 6 carry 1 mark each)

1. Simplify: $(6 + \sqrt{27}) - (3 + \sqrt{3}) + (1 - 2\sqrt{3})$
2. Find the value of the polynomial $x^2 - x - 1$ at $x = -1$.
3. Give the definition of Parallel Lines.
4. Is $(2, 0)$ a solution of $x - 2y = 4$?

OR

The graph of the linear equation $2x - y = 4$ cut x-axis at?

5. PQRS is a parallelogram in which $m \angle PSR = 125^\circ$. What is the measurement of $\angle RQT$?



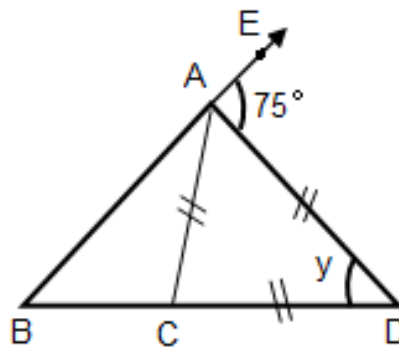
6. Find the Class size, if the Class marks of a frequency distribution are 6, 10, 14, 18, 22, 26 and 30?

OR

The class marks of a distribution are : 47, 52, 57, 62, 67, and 72
Determine the class size.

Section B
(Questions 7 to 12 carry 2 marks each)

7. The volume of a cuboid is given by the algebraic expression $ky^2 - 6ky + 8k$. Find the possible expressions of the dimensions of the cuboid.
8. If a point C lies between two points A and B such that $AC = BC$, then prove that $AC = \frac{1}{2} AB$. Explain by drawing a figure.
9. In the figure below, $BC = AC = AD$ and $\angle DAE = 75^\circ$. Find the value of y .

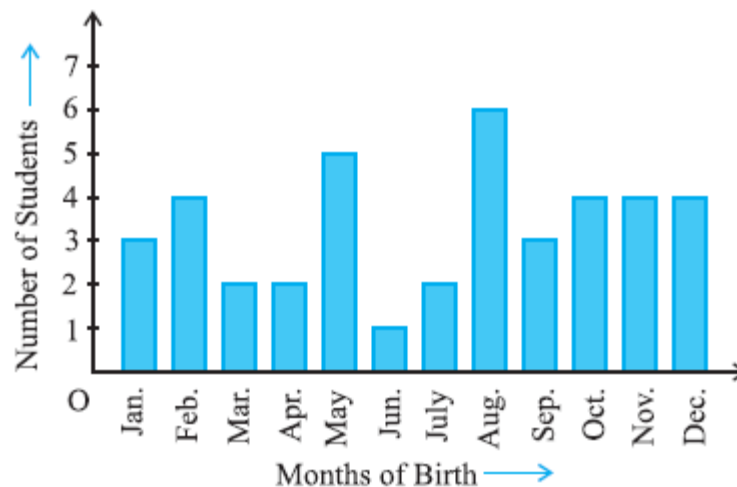


10. The total surface area of a cube is 294 cm^2 . Find its volume.

OR

A metal cube of side 4 cm is immersed in a water tank. The length and breadth of the tank are 8 cm and 4 cm respectively. Find the rise in level of the water.

11. In a particular section of Class IX, 40 students were asked about their birth month and the following graph was prepared for the data so obtained:



Find the probability that a student of Class IX was born in August.

12. The angles of a quadrilateral are in the ratio 2 : 5 : 8 : 9. Find all the angles in the quadrilateral.

OR

Three angles of a quadrilateral are 50° , 110° and 40° . Find the fourth angle of a quadrilateral.

Section C

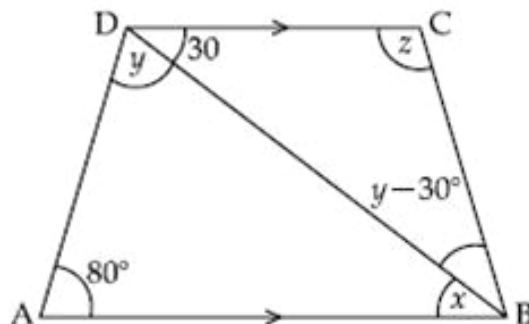
(Questions 13 to 22 carry 3 marks each)

13. If $a = 3 + b$, then prove that $a^3 - b^3 - 9ab = 27$.

OR

If $3x + 2y = 12$ and $xy = 6$, find the value of $9x^2 + 4y^2$.

14. In the figure, $AB \parallel DC$, $\angle BDC = 30^\circ$ and $\angle BAD = 80^\circ$, find the values of x , y and z .



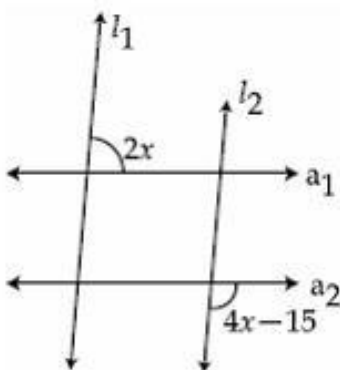
OR

PQRS is a square. Determine $\angle SRP$.

15. Use a suitable identity to factorise $27p^3 + 8q^3 + 54p^2q + 36pq^2$.

16. Factorise: $b^2 + c^2 + 2(ab + bc + ca)$.

17. In the figure, $l_1 \parallel l_2$ and $a_1 \parallel a_2$. Find the value of x .



18. A bag contains 12 balls out of which x are white. If one ball is taken out from the bag, find the probability of getting a white ball. If 6 more white balls are added to the bag and the probability now for getting a white ball is twice the previous one, find the value of x .
19. A storehouse measures $40 \text{ m} \times 25 \text{ m} \times 10 \text{ m}$. Find the maximum number of wooden crates, each measuring $1.5 \text{ m} \times 1.25 \text{ m} \times 0.5 \text{ m}$, which can be stored in the storehouse.

OR

The diameter of a garden roller is 1.4 m and it is 2 m long. How much area will it cover in 5 revolutions? ($\pi = 22/7$)

20. A hemispherical bowl, made of steel, is 0.25 cm thick. The inner radius of the bowl is 5 cm. Find the outer curved surface area of the bowl.

OR

Find the area of the base of a right circular cone is 314 cm^2 and its height is 15 cm. Find the volume of the cone. Also find the slant height of the cone if the radius is 10 cm.

21. The length of 40 leaves of a plant are measured correct to one millimeter, and the data obtained is represented in the following table:

| Length (in mm) | Number of leaves |
|----------------|------------------|
| 118 – 126 | 3 |
| 127 – 135 | 5 |
| 136 – 144 | 9 |
| 145 – 153 | 12 |
| 154 – 162 | 5 |
| 163 – 171 | 4 |
| 172 – 180 | 2 |

Draw a histogram to represent the given data.

- Is there any other suitable graphical representation for the same data?
 - Is it correct to conclude that maximum leaves are 153 mm long? Why?
22. In a parallelogram, show that the angle bisectors of two adjacent angles intersect at right angles.

Section D

(Questions 23 to 30 carry 4 marks each)

23. If AD is the median of $\triangle ABC$, then prove that $AB + AC > 2AD$.

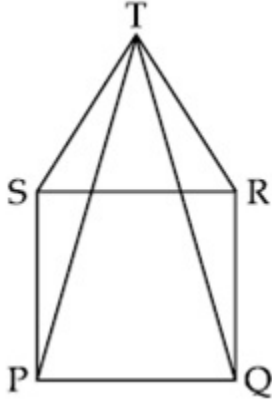
24. Simplify: $\frac{16 \times 2^{n+1} - 4 \times 2^n}{16 \times 2^{n+2} - 2 \times 2^{n+2}}$

OR

If $25^{x-1} = 5^{2x-1} - 100$, find the value of x .

25. In the figure, PQRS is a square and SRT is an equilateral triangle. Prove that:

- a) $\angle PST = \angle QRT$
- b) $PT = QT$
- c) $\angle TQR = 15^\circ$



OR

Ajay was asked to find the sum of the four angles of a quadrilateral. He found the sum of the four angles as 270° by giving the reasoning as follows:

Sum of the three angles of a triangle [made up of three sides]
= 2 right angles = $(3 - 1)$ right angles.

So, the sum of the four angles of quadrilateral [made up of four sides]
= $(4 - 1)$ right angles = 3 right angles = 270° .

His classmate Anju pointed out that the sum obtained is incorrect and found the correct sum. Ajay accepted his mistake and thanked Anju for the same. Write the correct solution. What value is depicted from this action?

26. (a) Simplify: $\left\{ 5 \left(8^{\frac{1}{3}} + 27^{\frac{1}{3}} \right)^3 \right\}^{\frac{1}{4}}$

(b) Represent $\sqrt{7}$ on the number line.

27. Find the median of 41, 43, 127, 99, 61, 92, 71, 58, and 57.

If 58 is replaced by 85, what will be the new median?

28. The following table gives the distribution of students of two sections according to the marks obtained by them:

| Section A | | Section B | |
|-----------|-----------|-----------|-----------|
| Marks | Frequency | Marks | Frequency |
| 0 – 10 | 3 | 0 – 10 | 5 |
| 10 – 20 | 9 | 10 – 20 | 19 |
| 20 – 30 | 17 | 20 – 30 | 15 |
| 30 – 40 | 12 | 30 – 40 | 10 |
| 40 – 50 | 9 | 40 – 50 | 1 |

Represent the marks of the students of both the sections on the same graph by two frequency polygons. From the two polygons compare the performance of the two sections.

29. A circus tent is cylindrical up to a height of 11 m and conical above it. If the diameter of the base is 24 m and the height of the cone is 5 m, find the length of the canvas required to make the tent if the width of the canvas is 5 m.

OR

Find the cost of sinking a tube well 350 m deep, having a diameter of 4 m at the rate of Rs 16 per m^3 . Find also the cost of cementing its inner curved surface at Rs 12 per m^2

30. Laxmi purchases some bananas and some oranges. Each banana costs Rs. 2 while each orange costs Rs. 3. If the total amount paid by Laxmi was Rs. 30 and the number of oranges purchased by her was 6, then how many bananas did she purchase?

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Section A

1.

$$\begin{aligned} & (6 + \sqrt{27}) - (3 + \sqrt{3}) + (1 - 2\sqrt{3}) \\ &= 6 + 3\sqrt{3} - 3 - \sqrt{3} + 1 - 2\sqrt{3} \\ &= 4 \end{aligned}$$

2.

Given polynomial is $x^2 - x - 1$
Substituting $x = -1$ in $x^2 - x - 1$, we have
 $(-1)^2 - (-1) - 1 = 1 + 1 - 1 = 1$

3.

Two lines l and m in a plane are said to be parallel lines if they do not have common point, i.e. they do not intersect.

4.

Substituting $x = 2$ and $y = 0$ in $x - 2y = 4$, we get
L.H.S = $2 - 2 \times 0 = 2 \neq 4$
i.e. L.H.S. \neq R.H.S
Therefore, $(2, 0)$ is not a solution of $x - 2y = 4$.

OR

Put $y = 0$ to find the coordinate of x -axis.

$$\therefore 2x - y = 4$$

$$\therefore 2x = 4$$

$$\therefore x = 2$$

Hence, the graph of the linear equation $2x - y = 4$ cut x -axis at $(2, 0)$.

5.

$\angle PSR = \angle RQP = 125^\circ$ (opposite angles will be equal since PQRS is a parallelogram)
 $\angle PQT = 180^\circ$ (PQT is a straight line)
 $\Rightarrow \angle PQR + \angle RQT = 180^\circ$
 $\Rightarrow 125^\circ + \angle RQT = 180^\circ$
 $\therefore \angle RQT = 55^\circ$

6.

Class size is the difference between two successive class marks.
 \therefore Class size = $10 - 6 = 4$

OR

According to the given distribution,
Class size = $52 - 47 = 5$.

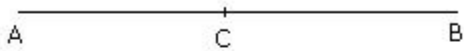
Section B

7. $ky^2 - 6ky + 8k$
 $= k(y^2 - 6y + 8)$
 $= k(y^2 - 4y - 2y + 8)$
 $= k(y - 4)(y - 2)$

Thus, the dimensions of the cuboid are given by the expressions k , $(y - 4)$ and $(y - 2)$.

8.

Given: $AC = BC$



$$AC + AC = BC + AC$$

(If equals are added to equal the wholes are equal)

$$\Rightarrow 2AC = AB$$

$$\text{Hence, } AC = \frac{1}{2} AB$$

9. Here $\angle ADC = y = \angle ACD$
 Ext. $\angle ACD = \angle ABC + \angle BAC$
 $\therefore 2\angle BAC = \angle ACD = y$

$$\Rightarrow \angle BAC = \frac{y}{2}$$

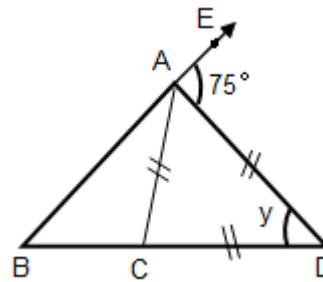
$$\therefore \frac{y}{2} + (180^\circ - 2y) = 180^\circ - 75^\circ$$

$$\Rightarrow \frac{y}{2} + 180^\circ - 2y = 180^\circ - 75^\circ$$

$$\Rightarrow \frac{y}{2} - 2y = -75^\circ$$

$$\Rightarrow -\frac{3y}{2} = -75^\circ$$

$$\Rightarrow y = 50^\circ$$



10. Let 'l' be the length of the cube.

Now, T.S.A. of the cube = 294 cm^2 (given)

$$\therefore 6l^2 = 294$$

$$\therefore l^2 = \frac{294}{6} = 49$$

$$\therefore \text{Side } (l) = 7 \text{ cm.}$$

$$\text{Volume of cube} = l \times l \times l = 7 \times 7 \times 7 = 343 \text{ cm}^3$$

OR

Given that:

Side (S) of metal cube = 4 cm

Length (l) of the tank = 8 cm

Breadth (b) of the tank = 4 cm

Since the volume of cube immersed = volume of the cuboidal tank

We get,

$$S \times S \times S = l \times b \times h$$

$$4^3 = 8 \times 4 \times h$$

$$h = \frac{64}{32}$$

$$\therefore h = 2 \text{ cm}$$

Thus, rise in water level = 2 cm

11. Number of students born in August = 6

Total number of students = 40

$$\text{Required probability} = \frac{\text{Number of students born in August}}{\text{Total number of students}} = \frac{6}{40} = \frac{3}{20}$$

12. Let the angles of a quadrilateral be $2x$, $5x$, $8x$ and $9x$ respectively.

By the angle sum property of a quadrilateral, we have

$$2x + 5x + 8x + 9x = 360^\circ$$

$$\therefore 24x = 360^\circ$$

$$\therefore x = 15^\circ$$

Now,

$$\text{First angle} = 2x = 2 \times 15 = 30^\circ,$$

$$\text{Second angle} = 5x = 5 \times 15 = 75^\circ,$$

$$\text{Third angle} = 8x = 8 \times 15 = 120^\circ \text{ and}$$

$$\text{Fourth angle} = 9x = 9 \times 15 = 135^\circ.$$

Thus, the angles of a quadrilateral are 30° , 75° , 120° and 135° .

OR

Let x be the fourth angle of a quadrilateral.

According to the question,

The sum of the angles of a quadrilateral is 360° .

$$\therefore 50^\circ + 110^\circ + 40^\circ + x = 360^\circ$$

$$\therefore 200^\circ + x = 360^\circ$$

$$\therefore x = 160^\circ$$

Hence, the fourth angle of a quadrilateral is 160° .

Section C

13. Given: $a = 3 + b$

$$\Rightarrow a - b = 3$$

Applying the cubic identity on both the sides, we have

$$(a - b)^3 = 3^3$$

$$\Rightarrow a^3 - b^3 - 3(a)(b)(a - b) = 27$$

$$\Rightarrow a^3 - b^3 - 3ab(3) = 27 \quad (\because a - b = 3)$$

$$\Rightarrow a^3 - b^3 - 9ab = 27$$

OR

$$(3x + 2y)^2 = 12^2$$

$$9x^2 + 12xy + 4y^2 = 144$$

$$9x^2 + 4y^2 + 12xy = 144$$

$$9x^2 + 4y^2 + 12 \times 6 = 144 \quad \because xy = 6$$

$$9x^2 + 4y^2 = 144 - 72$$

$$9x^2 + 4y^2 = 72$$

14. Since $AB \parallel DC$,

$$\angle x = 30^\circ \text{ [Alternate angles]}$$

In $\triangle ABD$,

$$80^\circ + 30^\circ + \angle y = 180^\circ$$

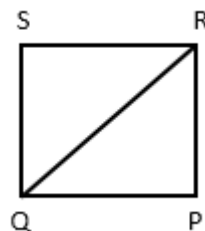
$$\Rightarrow \angle y = 180^\circ - 110^\circ = 70^\circ$$

In $\triangle BDC$,

$$30^\circ + (70^\circ - 30^\circ) + \angle z = 180^\circ$$

$$\Rightarrow \angle z = 110^\circ$$

OR



Since, PQRS is a square. $PS = SR$ and $\angle PSR = 90^\circ$.

In $\triangle PSR$,

$$PS = SR$$

$$\angle SRP = \angle QRP \quad \text{angles opposite to equal sides}$$

$$\angle SRP + \angle QRP + \angle PSR = 180^\circ$$

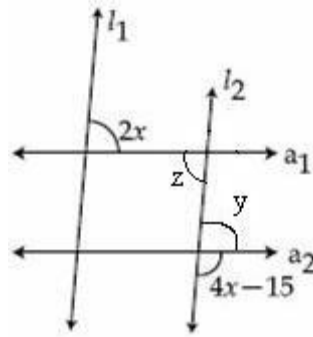
$$2\angle SRP + 90^\circ = 180^\circ$$

$$\angle SRP = 45^\circ$$

$$\begin{aligned}
15. \quad & 27p^3 + 8q^3 + 54p^2q + 36pq^2 \\
&= (3p)^3 + (2q)^3 + 18pq(3p+2q) \\
&= (3p)^3 + (2q)^3 + 3 \times 3p \times 2q (3p + 2q) \\
&= (3p + 2q)^3 [(a + b)^3 = a^3 + b^3 + 3ab(a + b) \quad \text{[where } a = 3p \text{ and } b = 2q \text{]}] \\
&= (3p + 2q) (3p + 2q) (3p + 2q)
\end{aligned}$$

$$\begin{aligned}
16. \quad & b^2 + c^2 + 2(ab + bc + ca) \\
&= a^2 + b^2 + c^2 + 2ab + 2bc + 2ca - a^2 \quad \text{[Adding and subtracting } a^2 \text{]} \\
&= [a^2 + b^2 + c^2 + 2ab + 2bc + 2ca] - a^2 \\
&= (a + b + c)^2 - (a)^2 \quad \text{[Using } x^2 + y^2 + 2xy + 2yz + 2zx = (x + y + z)^2 \text{]} \\
&= (a + b + c + a)(a + b + c - a) \quad \text{[Because } a^2 - b^2 = (a + b)(a - b) \text{]} \\
&= (2a + b + c)(b + c)
\end{aligned}$$

$$\begin{aligned}
17. \quad & 2x = z \quad \text{(Alternate angles, as } l_1 \parallel l_2 \text{)} \\
& y = z \quad \text{(Alternate angles, as } a_1 \parallel a_2 \text{)} \\
& \text{So, } 2x = y \\
& \text{Now, } y + 4x - 15 = 180^\circ \quad \text{(linear pair)} \\
& 2x + 4x - 15 = 180^\circ \\
& \Rightarrow 6x = 195^\circ \\
& \Rightarrow x = 32.5
\end{aligned}$$



$$\begin{aligned}
18. \quad & \text{Number of white balls} = x \\
& \text{Total number of balls} = 12 \\
& \therefore P(\text{white ball}) = \frac{x}{12} \\
& \text{If 6 white balls are added, we have} \\
& \text{Total number of balls} = 18 \\
& \text{Number of white balls} = x + 6 \\
& \text{Now, } P(\text{getting a white ball}) = \frac{x+6}{18} \\
& \text{According to the given information,} \\
& \frac{x+6}{18} = 2 \left(\frac{x}{12} \right) \\
& \therefore \frac{x+6}{18} = \frac{x}{6} \\
& \therefore 6x + 36 = 18x \\
& \therefore 12x = 36 \\
& \therefore x = 3
\end{aligned}$$

19. Length (l_1) of the storehouse = 40 m

Breadth (b_1) of the storehouse = 25 m

Height (h_1) of the storehouse = 10 m

Volume of storehouse = $l_1 \times b_1 \times h_1 = (40 \times 25 \times 10) \text{ m}^3 = 10000 \text{ m}^3$

Length (l_2) of a wooden crate = 1.5 m

Breadth (b_2) of a wooden crate = 1.25 m

Height (h_2) of a wooden crate = 0.5 m

Volume of a wooden crate = $l_2 \times b_2 \times h_2 = (1.5 \times 1.25 \times 0.5) \text{ m}^3 = 0.9375 \text{ m}^3$

Let the number of wooden crates stored in the storehouse be 'n'.

Hence, volume of 'n' wooden crates = Volume of storehouse

$$0.9375 \times n = 10000$$

$$\therefore n = \frac{10000}{0.9375} = 10666.66$$

Thus, 10666 wooden crates can be stored in the storehouse.

OR

Area covered = Curved surface \times Number of revolutions

$$R = 1.4/2 = 0.7 \text{ m and } h = 2 \text{ m}$$

$$\text{Curved surface} = 2\pi rh = 2 \times \frac{22}{7} \times 0.7 \times 2 = 8.8 \text{ m}^2$$

$$\text{Area covered} = 8.8 \times 5 = 44 \text{ m}^2$$

20. Inner radius of hemispherical bowl = 5 cm

Thickness of the bowl = 0.25 cm

$$\therefore \text{Outer radius (r) of hemispherical bowl} = (5 + 0.25) \text{ cm} = 5.25 \text{ cm}$$

$$\text{Outer C.S.A. of hemispherical bowl} = 2\pi r^2 = 2 \times \frac{22}{7} \times (5.25)^2 = 173.25 \text{ cm}^2$$

Thus, the outer curved surface area of the bowl is 173.25 cm^2 .

OR

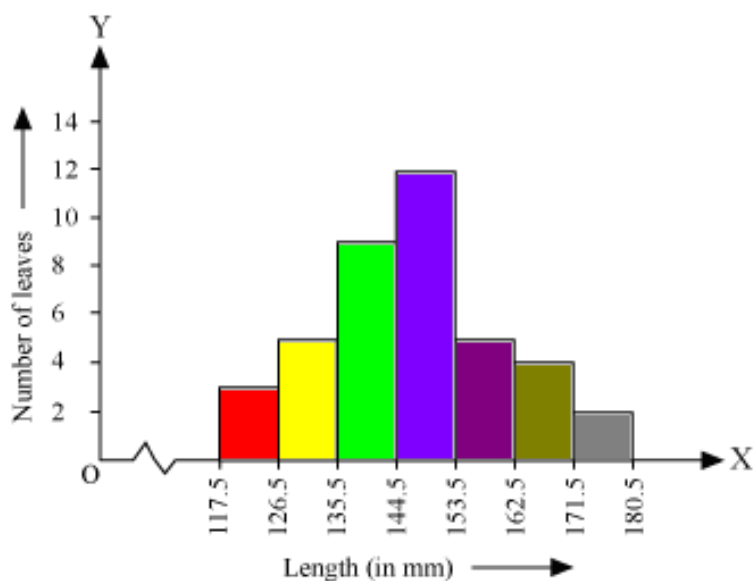
$$\text{Volume of the cone} = \frac{1}{3} \times \text{Area of base} \times \text{height} = \frac{1}{3} \times 314 \times 15 = 1570 \text{ cm}^3$$

$$l = \sqrt{r^2 + h^2} = \sqrt{10^2 + 15^2} = \sqrt{100 + 225} = \sqrt{325} = 18.02 \text{ cm.}$$

21. Lengths of the leaves are represented in discontinuous class intervals. Hence we have to add 0.5 mm to each upper class limit and also have to subtract 0.5 mm from the lower class limits so as to make our class intervals continuous.

| Length (in mm) | Number of leaves |
|----------------|------------------|
| 117.5 – 126.5 | 3 |
| 126.5 – 135.5 | 5 |
| 135.5 – 144.5 | 9 |
| 144.5 – 153.5 | 12 |
| 153.5 – 162.5 | 5 |
| 162.5 – 171.5 | 4 |
| 171.5 – 180.5 | 2 |

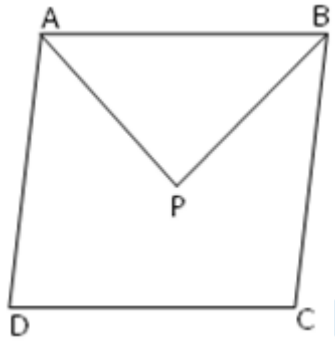
Now taking the length of leaves on the x-axis and number of leaves on the y-axis we can draw the histogram of this information as below:



Here 1 unit on the y-axis represents 2 leaves.

- Other suitable graphical representation of this data could be a frequency polygon.
 - No, as maximum numbers of leaves (i.e. 12) have their length in between of 144.5 mm and 153.5 mm. It is not necessary that all have a length of 153 mm.
22. Given: ABCD is a parallelogram such that angle bisector of adjacent angles A and B intersect at point P.

To prove: $\angle APB = 90^\circ$



$AD \parallel BC$

$\therefore \angle A + \angle B = 180^\circ$ [Consecutive interior angles] $\therefore \frac{1}{2}\angle A + \frac{1}{2}\angle B = 90^\circ$

But, $\frac{1}{2}\angle A + \frac{1}{2}\angle B + \angle APB = 180^\circ$... (Angle sum property of a Δ)

$\therefore 90^\circ + \angle APB = 180^\circ \Rightarrow \angle APB = 90^\circ$

Thus, the angle bisectors of two adjacent angles intersect at right angles.

Section D

23. Given: AD is median of triangle ABC

To Prove: $AB + AC > 2AD$

Proof: Produce AD so that $AD = DE$

Now, in triangles ADB and EDC,

$AD = DE$

$BD = DC$

$\angle ADB = \angle EDC$

Thus, $\triangle ADB \cong \triangle EDC$ (By SAS congruence criterion)

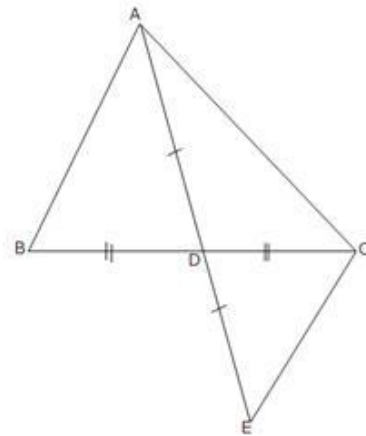
Hence, $AB = EC$ (CPCT)

Now, in $\triangle AEC$,

$AC + CE > AE$

$AC + CE > 2AD$

$AC + AB > 2AD$ (since, $AB = EC$, proved above)



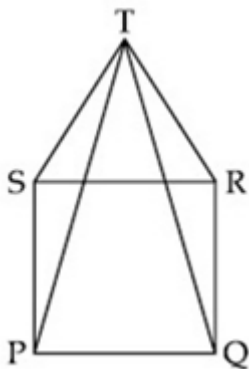
24.

$$\begin{aligned}
 \frac{16 \times 2^{n+1} - 4 \times 2^n}{16 \times 2^{n+2} - 2 \times 2^{n+2}} &= \frac{2^4 \times 2^{n+1} - 2^2 \times 2^n}{2^4 \times 2^{n+2} - 2 \times 2^{n+2}} \\
 &= \frac{2^{n+5} - 2^{n+2}}{2^{n+6} - 2^{n+3}} \\
 &= \frac{2^{n+5} - 2^{n+2}}{2 \cdot 2^{n+5} - 2 \cdot 2^{n+2}} \\
 &= \frac{(2^{n+5} - 2^{n+2})}{2(2^{n+5} - 2^{n+2})} \\
 &= \frac{1}{2}
 \end{aligned}$$

OR

$$\begin{aligned}
 25^{x-1} &= 5^{2x-1} - 100 \\
 (5^2)^{x-1} &= (5^x)^2 \times 5^{-1} - 100 \\
 5^{2x-2} - 5^{2x-1} &= -100 \\
 5^{2x-2} - 5^{2x-2} \times 5 &= -100 \\
 5^{2x-2} (1 - 5) &= -100 \\
 5^{2x-2} &= 25 \\
 5^{2x-2} &= 5^2 \\
 2x - 2 &= 2 \\
 2x &= 4 \\
 x &= 2
 \end{aligned}$$

25. □PQRS is a square.



$$\therefore PQ = QR = RS = SP \quad \dots(i)$$

$$\text{Also } \angle RSP = \angle SRQ = \angle RQP = \angle SPQ = 90^\circ \quad \dots(ii)$$

Also $\triangle TSR$ is equilateral.

$$TS = TR = SR \dots\dots(iii)$$

$$\text{Also } \angle STR = \angle TSR = \angle TRS = 60^\circ$$

$$TR = QR \dots\dots\text{from (i) and (ii)}$$

$$\text{Also } \angle TSP = \angle RSP + \angle TSR$$

$$\angle TSP = 90^\circ + 60^\circ = 150^\circ$$

$$\text{Similarly } \angle TRQ = 150^\circ$$

In $\triangle TSP$ and $\triangle TRQ$,

$$PS = QR \dots\dots(\because \text{by (i)})$$

$$\angle TSP = \angle TRQ \dots\dots(\because \text{Both } 150^\circ)$$

$$TS = TR \dots\dots(\because \text{by (iii)})$$

$$\therefore \triangle TSP \cong \triangle TRQ \quad \dots(\text{by SAS criterion})$$

$$\therefore PT = QT \quad \dots\dots(\text{c.p.c.t})$$

Now, in $\triangle TRQ$

$$TR = RQ \quad \text{Given}$$

$$\therefore \angle TQR = \angle RTQ$$

$$\therefore \angle RTQ + \angle RQT + \angle TRQ = 180^\circ \quad (\text{angle sum property})$$

$$\therefore 2\angle TQR + 150^\circ = 180^\circ$$

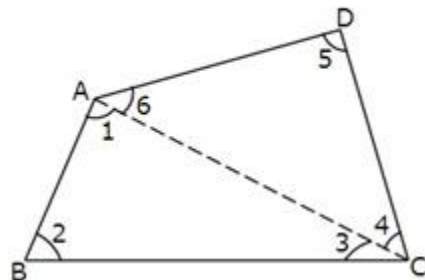
$$\therefore \angle TQR = 15^\circ$$

OR

Let ABCD be a quadrilateral.

We have to find $\angle A + \angle B + \angle C + \angle D$.

Join AC and mark the angles as shown in the figure.



From $\triangle ABC$, we have:

$$\angle 1 + \angle 2 + \angle 3 = 180^\circ \quad (\text{Angle sum property of a triangle}) \quad \dots (1)$$

Form $\triangle ADC$, we have:

$$\angle 6 + \angle 5 + \angle 4 = 180^\circ \quad (\text{Angle sum property of a triangle}) \dots (2)$$

Adding (1) and (2),

$$\angle 1 + \angle 2 + \angle 3 + \angle 6 + \angle 5 + \angle 4 = 180^\circ + 180^\circ$$

$$\Rightarrow (\angle 1 + \angle 6) + \angle 2 + (\angle 3 + \angle 4) + \angle 5 = 360^\circ$$

$$\Rightarrow \angle A + \angle B + \angle C + \angle D = 360^\circ$$

Thus, the required sum is 360° and not 270° .

26.

a)

$$\begin{aligned} & \left\{ 5 \left(2^{3 \times \frac{1}{3}} + 3^{3 \times \frac{1}{3}} \right)^3 \right\}^{\frac{1}{4}} \\ &= \left[5(2+3)^3 \right]^{\frac{1}{4}} \\ &= (5 \times 5^3)^{\frac{1}{4}} \\ &= 5^{4 \times \frac{1}{4}} \\ &= 5 \end{aligned}$$

b) In order to represent $\sqrt{7}$ on number line, we follow the steps given below:

Step 1: Draw a line and mark a point A on it.

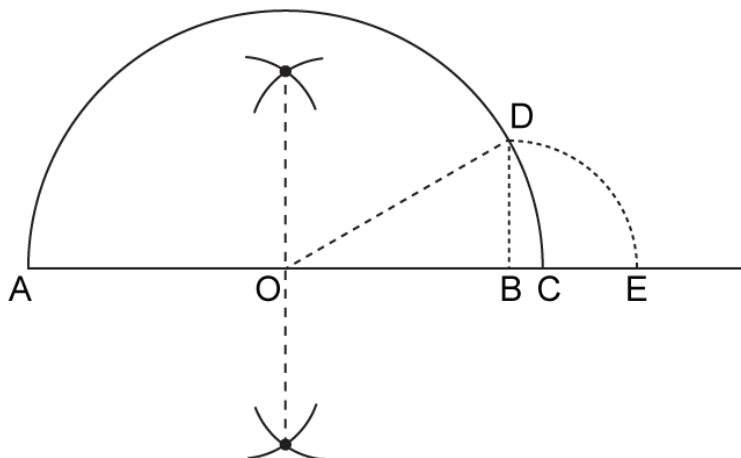
Step 2: Mark a point B on the line drawn in step 1 such that $AB = 7$ cm.

Step 3: Mark a point C on AB produced such that $BC = 1$ unit.

Step 4: Find mid-point of AC. Let the mid-point be O.

Step 5: Taking O as the centre and $OC = OA$ as radius draw a semicircle. Then, draw a line passing through B perpendicular to OB. Let the perpendicular cut the semicircle at D.

Step 6: Taking B as the centre and radius BD draw an arc cutting OC produced at E. Point E so obtained represents $\sqrt{7}$.



27. Arranging the given data in ascending order, we have

41, 43, 57, 58, 61, 71, 92, 99, 127

Here, $n = 9$ (odd)

$$\therefore \text{Median} = \left(\frac{n+1}{2} \right)^{\text{th}} \text{ value} = \left(\frac{9+1}{2} \right)^{\text{th}} \text{ value} = 5^{\text{th}} \text{ value} = 61$$

If 58 is replaced by 85, we get the following data:

41, 43, 57, 61, 71, 85, 92, 99, 127

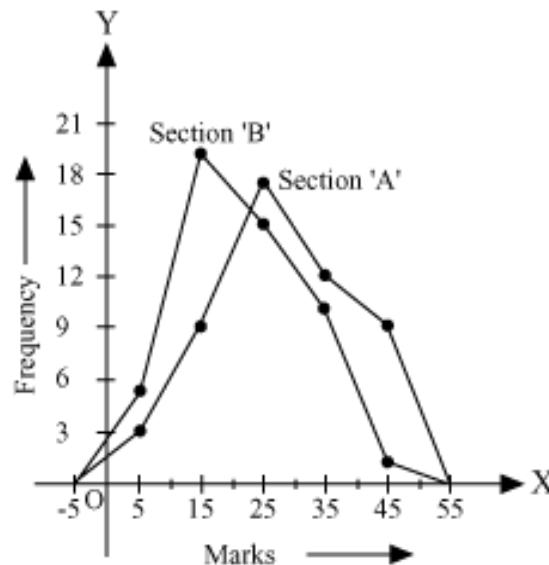
$$\therefore \text{New median} = \left(\frac{n+1}{2} \right)^{\text{th}} \text{ value} = \left(\frac{9+1}{2} \right)^{\text{th}} \text{ value} = 5^{\text{th}} \text{ value} = 71$$

28. We can find class marks of the given class intervals by using the formula –

$$\text{Class mark} = \frac{\text{upper class limit} + \text{lower class limit}}{2}$$

| Section A | | | Section B | | |
|-----------|-------------|-----------|-----------|-------------|-----------|
| Marks | Class marks | Frequency | Marks | Class marks | Frequency |
| 0 – 10 | 5 | 3 | 0 – 10 | 5 | 5 |
| 10 – 20 | 15 | 9 | 10 – 20 | 15 | 19 |
| 20 – 30 | 25 | 17 | 20 – 30 | 25 | 15 |
| 30 – 40 | 35 | 12 | 30 – 40 | 35 | 10 |
| 40 – 50 | 45 | 9 | 40 – 50 | 45 | 1 |

Now taking the class marks on the x-axis and frequency on the y-axis and choosing an appropriate scale (1 cm = 3 units on the y-axis) we can draw a frequency polygon as below:



From the graph we can see that the performance of students of section 'A' is better than the students of section 'B'.

29. Diameter = 24 m \Rightarrow radius = 12 m

Radius of the conical part = Radius of the cylindrical part (r) = 12 m

Height of cylindrical part (h) = 11 m, height of the cone (h) = 5 m

For the conical part of the circus tent,

$$l^2 = r^2 + h^2$$

$$\therefore l = \sqrt{r^2 + h^2} = \sqrt{12^2 + 5^2} = \sqrt{144 + 25} = \sqrt{169} = 13 \text{ m}$$

Surface area of the tent = Curved surface area of the conical part + Curved surface area of the cylindrical part

$$\begin{aligned} \therefore \text{Surface area of the tent} &= \pi r l + 2\pi r h \\ &= \pi r (l + 2h) \\ &= \frac{22}{7} \times 12 (13 + 22) \\ &= \frac{22}{7} \times 12 \times 35 \\ &= 1320 \text{ m}^2 \end{aligned}$$

Breadth of the canvas (B) = 5 m

Let the length of the canvas = L

Now, area of canvas required = surface area of the tent

$$\therefore L \times B = 1320 \Rightarrow L \times 5 = 1320 \Rightarrow L = 264 \text{ m}$$

Thus, 264 m long canvas is required to make the tent.

OR

Height (h) = 350 m

Diameter = 4 m

\therefore Radius (r) = 2 m

$$\begin{aligned}\text{Volume of tube well} &= \pi \times r^2 \times h \\ &= \frac{22}{7} \times 2^2 \times 350 \\ &= 4400 \text{ m}^3\end{aligned}$$

$$\begin{aligned}\text{Cost of sinking the tube well} &= 4400 \times \text{Rs } 16 \\ &= \text{Rs } 70400\end{aligned}$$

$$\begin{aligned}\text{L.S.A. of cylindrical tube well} &= 2 \times \pi \times r \times h \\ &= 2 \times \frac{22}{7} \times 2 \times 350 \\ &= 4400 \text{ m}^2\end{aligned}$$

$$\begin{aligned}\text{Cost of cementing inner curved surface of tube well} &= 4400 \times \text{Rs } 12 \\ &= \text{Rs } 52800\end{aligned}$$

30. Let us assume that Laxmi purchased x bananas and y oranges.

Since each banana costs Rs. 2, x bananas cost Rs. $2 \times x = \text{Rs. } 2x$

Similarly, each orange costs Rs. 3.

Thus, y oranges cost Rs. $3 \times y = \text{Rs. } 3y$

Thus, the total amount paid by Laxmi is Rs. $(2x + 3y)$, which equals Rs. 30

Thus, we can express the given information in the form of a linear equation as $2x + 3y = 30$

Now, we know that Laxmi purchased 6 oranges, i.e., the value of y is 6.

Substitute this value of y in the equation $2x + 3y = 30$, thereby reducing it to a linear equation in one variable.

We can then solve the equation to obtain the value of x.

$$2x + 3 \times 6 = 30 \Rightarrow 2x + 18 = 30$$

This is a linear equation in one variable.

$$\Rightarrow 2x = 30 - 18$$

$$\Rightarrow 2x = 12$$

$$\Rightarrow x = 6$$

Thus, we see that the value of x is 6, i.e., Laxmi purchased 6 bananas.