

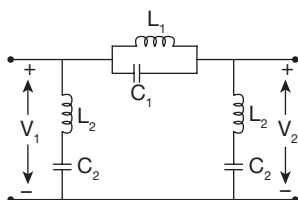
NETWORKS TEST I

Number of Questions: 35

Time: 90 min.

Directions for questions 1 to 35: Select the correct alternative from the given choices.

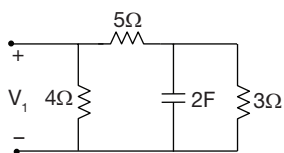
1.



Given filter is

- (A) Band pass filter
- (B) Band stop filter
- (C) Low pass filter
- (D) high pass filter

2. The driving point impedance of the circuit shown in below figure is

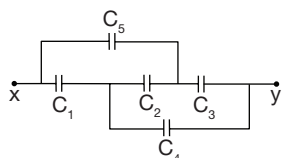


- (A) $\frac{60s+16}{27s+6}$
- (B) $\frac{27s+6}{60s+16}$
- (C) $\frac{64s+60}{24s+27}$
- (D) $\frac{24s+27}{64s+60}$

3. A parallel RLC circuit has $R = 1k\Omega$, $L = 4mH$ and $C = 10\mu F$ then Q is

- (A) 2×10^{-2}
- (B) 200
- (C) 100
- (D) 50

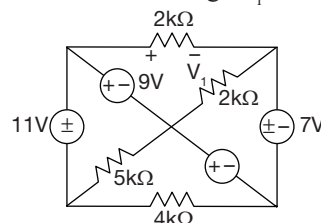
4.



In given figure the capacitors – C_1 , C_2 , C_3 , C_4 , C_5 have capacitance of 4F, 10F 4F, 8F, 2F respectively. Then the effective capacitance between the points x & y will be

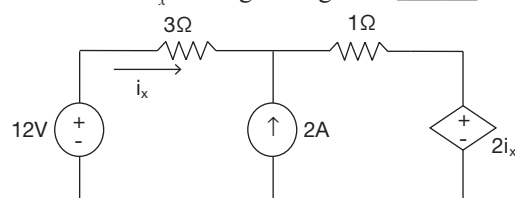
- (A) 4F
- (B) $\frac{4}{3}$ F
- (C) $\frac{8}{3}$ F
- (D) $\frac{1}{4}$ F

5. In given below circuit the voltage V_1 is



- (A) 2V
- (B) 6V
- (C) 1V
- (D) 10V

6. The value of i_x in the given figure is _____ Amp.



7. Function $s + 4 + \frac{5}{s}$ can be realized

- (A) as an admittance but not as an impedance.
- (B) as an impedance but not as an admittance
- (C) both as driving point impedance and as a driving point admittance
- (D) neither as an impedance nor as an admittance

8. Width of resonance curve in a $R - L - C$ network is determined by

- (A) R alone
- (B) L alone
- (C) C alone
- (D) All R , L , and C

9. If two, two – port networks, are connected such that, the short circuit admittance matrix of the overall network is sum of the short circuit admittance matrices of individual networks, find type of connection?

- (A) Series connection
- (B) Parallel connection
- (C) Cascade connection
- (D) None of these

10. With respect to Hybrid parameters, which one of the following statement is correct ?

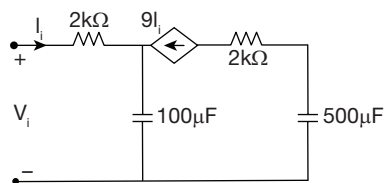
- (A) h_{11} and h_{22} are dimension less
- (B) h_{12} and h_{21} are dimension less
- (C) h_{21} and h_{12} are dimension less
- (D) h_{11} and h_{21} are dimension less

11. It is required to find the current through a particular branch of a linear bilateral network without mutual coupling when the branch impedance takes five different values which one of the following method is preferred?

3.6 | Networks Test 1

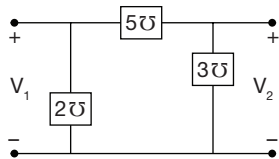
- (A) Mesh analysis
(B) Super position theorem
(C) Thevenin's equivalent circuit
(D) Nodal analysis
12. The Number of fundamental cut – sets of any graph will be equal to
(A) Number of tree branches
(B) Number of twigs
(C) Number of nodes
(D) Number of loops
13. Consider a 48V battery of internal resistance is $6\ \Omega$ connected to a load resistance. The rate of heat dissipated in the resistor is maximum when the current drawn from the battery is i . the current drawn from the battery will be $\frac{i}{3}$ when R_L is equal to
(A) $30\ \Omega$ (B) $24\ \Omega$
(C) $6\ \Omega$ (D) $12\ \Omega$

14.



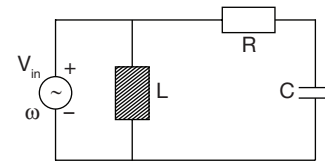
The input capacitance is

- (A) $600\ \mu\text{F}$ (B) $50\ \mu\text{F}$
(C) $10\ \mu\text{F}$ (D) $200\ \mu\text{F}$
15. Reactive power is given as 500 VAR and leading power factor is 0.6, then Apparent power is
(A) 833.33VA (B) 625VA
(C) 666.67VA (D) 500VA
16. For given Two port network. The Transmission matrix is



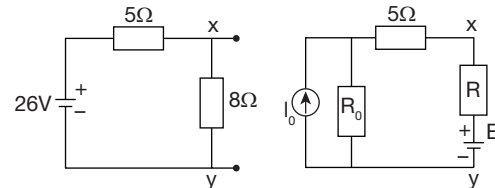
- (A) $\begin{bmatrix} 2 & 5 \\ 5 & 3 \end{bmatrix}$ (B) $\begin{bmatrix} 7 & -5 \\ -5 & 8 \end{bmatrix}$
(C) $\begin{bmatrix} 1.6 & 0.2 \\ 6.2 & 1.4 \end{bmatrix}$ (D) $\begin{bmatrix} 2.67 & 0.67 \\ 10.67 & 1.67 \end{bmatrix}$
17. For a series $R-L-C$ circuit, the characteristic equation is given by $S^2 + \frac{R}{L}S + \frac{1}{LC} = 0$. If $\frac{R}{2L}$ is denoted by α and $\frac{1}{\sqrt{LC}}$ by β , then under the condition $\beta^2 < \alpha^2$, the system will be
(A) critically damped (B) under damped
(C) undamped (D) over damped

18.



Consider given circuit and find the value of ω where circuit exhibits unity power factor?

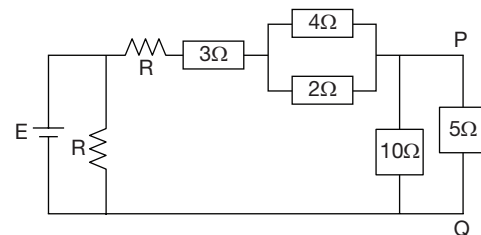
- (A) $\frac{1}{\sqrt{LC}}$ (B) $\frac{1}{RC}$
(C) $\frac{1}{\sqrt{LC + R^2C^2}}$ (D) $\frac{1}{\sqrt{LC - R^2C^2}}$
19. If two circuits shown below are equivalent then which one of the following is correct



- 1 $E = -2\text{V}$ and $R = 9\ \Omega$
2 $E = -4\text{V}$ and $R = 6\ \Omega$
3 $E = -1\text{V}$ and $R = 4\ \Omega$
4 without knowing R_0 value we cannot find R and E values

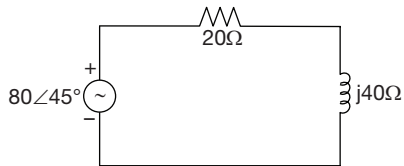
Select the correct option

- (A) 1 and 2 only (B) 4 only
(C) 2 and 3 only (D) 1, 2 and 3 only.
20. In given circuit, the voltage across $3\ \Omega$ resistor is 30V. The $5\ \Omega$ resistor is connected between the terminal P and Q can be replaced by an ideal



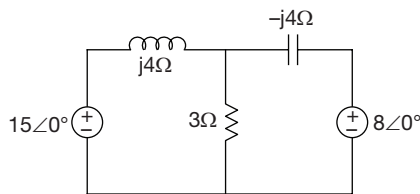
- (A) voltage source of $\frac{100}{3}\text{V}$ with + terminal in upward direction
(B) voltage source of $\frac{100}{3}\text{V}$ with + terminal in downward direction
(C) current source of $\frac{10}{3}\text{A}$ in upward direction
(D) current source $\frac{10}{3}\text{A}$ in downward direction

21. Find the change in current in below given circuit by compensation theorem, when the reactance has changed to $j20\Omega$



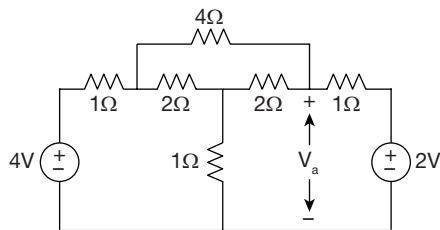
- (A) $1.79 \angle -18.438$ (B) $0.56 \angle -18.438$
(C) $28.28 \angle 45^\circ$ (D) $1.26 \angle 26.57^\circ$

22. The average power absorbed by inductor, resistor and capacitor respectively are



- (A) 0W, 0W, 4.6W (B) 0W, 4.6W, 0W
(C) 4.6W, -4.6W, 0W (D) 4.6W, -4.6W, 4.6W

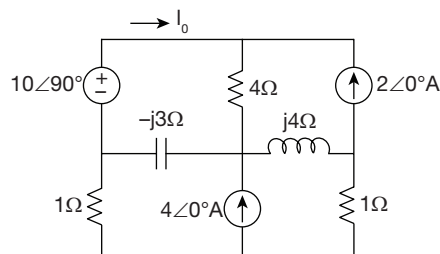
23.



The value of V_a in the given network is?

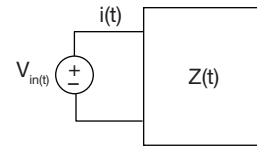
- (A) 2.9 V (B) 1.2 V
(C) 1.9 V (D) 2.5 V

24. In the given circuit the current I_o is



- (A) $6 \angle 0^\circ$ (B) $2 \angle 0^\circ$
(C) $5 \angle 107.4$ (D) $4 \angle 57^\circ$

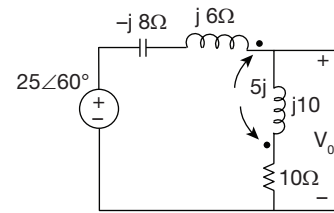
25. The circuit given below has input impedance. Assume zero initial conditions for an input $V_{in}(t) = 10t e^{-10t} u(t)$. Current in the circuit at $t = 50\text{ms}$ will be



Where $Z(t) = e^{-10t} (1 + 10t) u(t)$

- (A) 10A (B) 6.7mA
(C) 6mA (D) 3.6A

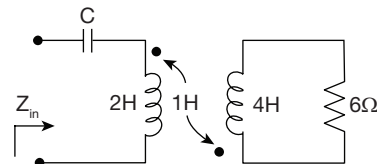
26.



The output voltage V_o is

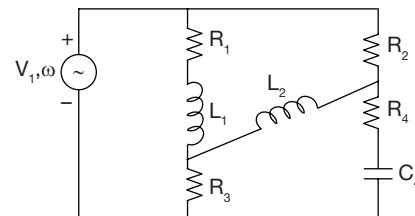
- (A) $21.88 \angle 55.36^\circ \text{ V}$ (B) $30.35 \angle 89.06^\circ \text{ V}$
(C) $28.4 \angle 80^\circ \text{ V}$ (D) $35.13 \angle 77.65^\circ \text{ V}$

27. In the following circuit if $\omega = 3\text{rad/s}$, the resonance occurs when C is



- (A) $\frac{5}{81} \text{ F}$
(B) 4F
(C) $\frac{1}{324} \text{ F}$
(D) Not possible to get resonance

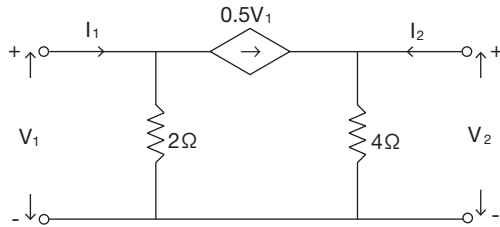
28. The circuit shown in below figure, if the current through inductor ' L_2 ' is Zero Then Which one of the following relation is correct



- (A) $\frac{\omega L_1}{R_1} = \frac{1}{\omega C_4 R_4}$
(B) $\tan^{-1} \frac{\omega L_1}{R} + \tan^{-1} \omega C_4 R_3 = 0$
(C) $\tan^{-1} \frac{\omega L_1}{R_1} + \tan^{-1} \frac{1}{\omega C_4 R_3} = 0$
(D) $\frac{\omega L_1}{R} = R_4 C_4 \omega$

3.8 | Networks Test 1

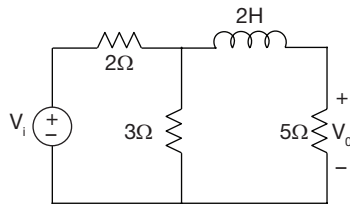
29.



The admittance parameters (Z_{11} and Z_{21}) would be

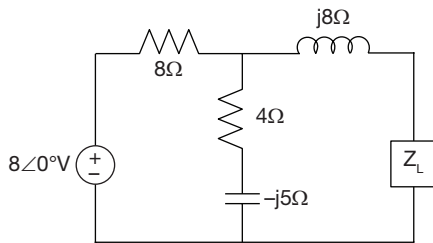
- (A) 1Ω and 4Ω (B) 0 and 2Ω
(C) 1Ω and 2Ω (D) -1.5Ω and $\left(\frac{2}{3}\right)\Omega$

30. Find the response of given network when $V_i = 6\cos 3t$ volts.



- (A) $0.29\cos 3t + 0.36\sin 3t$ V
(B) $e^{-2.4t} + 0.29\cos 3t$ V
(C) $\frac{12}{41}e^{-2.4t} - 0.36\cos 3t$ V
(D) $2\cos(3t - 44)^\circ$ V

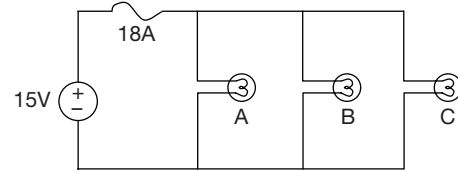
31. Maximum average power can be transferred by given network is



- (A) zero Watts (B) 0.283 Watts
(C) 0.56 Watts (D) 0.637 Watts

Common data for questions 32 and 33:

In given circuit bulb *A* uses 30W when it is ON, Bulb *B*, uses 20W when it is ON, bulb *C* uses 15W when light is ON,



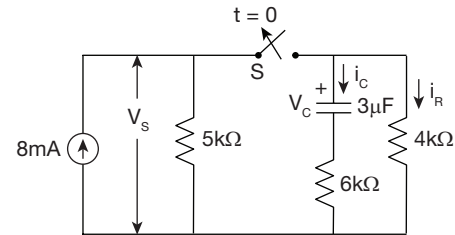
32. The additional *A* bulbs in parallel to this circuit, that would be required to blow the fuse?

- (A) 5 (B) 7
(C) 4 (D) 8

33. How many additional parallel *A*, *B*, *C* bulbs in parallel are required to blow the fuse?

- (A) 5 (B) 4
(C) 3 (D) 6

Data for Linked Answer questions 34 and 35:



34. The value of V_s is

- (A) 17.8 V (B) 40 V
(C) 22.2 V (D) zero V

35. Find the voltage across capacitor for $t \geq 0$.

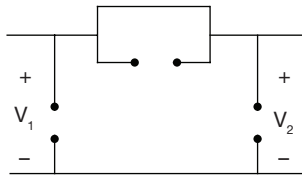
- (A) $\frac{160}{9} \left(e^{\frac{-100t}{3}} - 1 \right)$ V (B) $\frac{160}{9} e^{\frac{-100t}{3}}$ V
(C) $\frac{-16}{9} \times \left(e^{\frac{-100t}{3}} - 1 \right)$ mV (D) None of the above

ANSWER KEYS

- | | | | | | | | | | |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 1. B | 2. A | 3. D | 4. A | 5. D | 7. C | 8. D | 9. B | 10. C | 11. D |
| 12. B | 13. A | 14. C | 15. B | 16. C | 17. D | 18. D | 19. D | 20. A | 21. D |
| 22. B | 23. C | 24. C | 25. D | 26. A | 27. A | 28. A | 29. C | 30. D | 31. C |
| 32. B | 33. B | 34. A | 35. B | | | | | | |

HINTS AND EXPLANATIONS

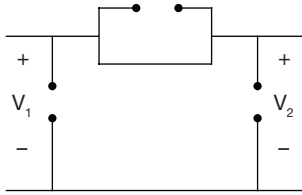
1. If $\omega = 0$ then $L \rightarrow S.C$



$C \rightarrow O.C$ then output is across capacitor.

If $\omega = \infty$ then $L \rightarrow O.C$

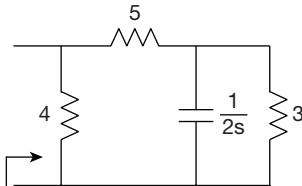
$C \rightarrow S.C$ then outputs is across inductor



So it is Band stop filter

Choice (B)

- 2.



$$Z_{\frac{i}{p}} = 4 \left[5 + \left(3 \parallel \frac{1}{2s} \right) \right]$$

$$\frac{60s + 16}{27s + 6}$$

Choice (A)

3. $Q = \omega CR$

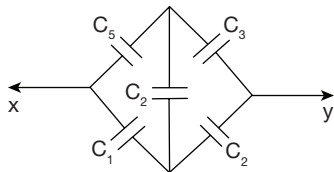
$$= RC \frac{1}{\sqrt{LC}} = R \sqrt{\frac{C}{L}}$$

$$= 10^3 \sqrt{\frac{10 \times 10^{-6}}{4 \times 10^{-3}}}$$

$$= 10^3 \sqrt{\frac{10^{-2}}{4}} = \frac{100}{2} = 50$$

Choice (D)

4. Redraw given circuit



$$C_1 C_3 = C_4 C_5$$

Given Network is balanced bridge

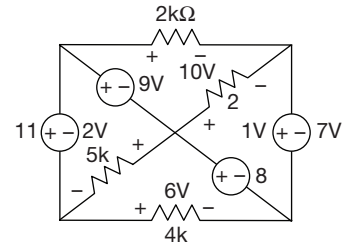
$$C_{eq} = \frac{C_5 \times C_3}{C_5 + C_3} + \frac{C_4 C_1}{C_4 + C_1}$$

$$= \frac{4 \times 8}{12} + \frac{4 \times 2}{6}$$

$$C_{eq} = 4F$$

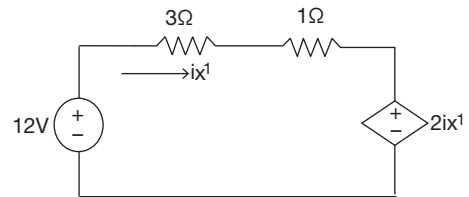
Choice (A)

- 5.



Choice (D)

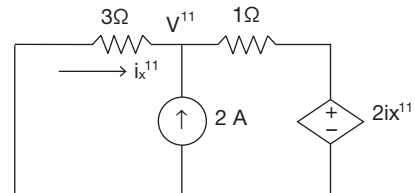
6. Due to 12V source:



$$\Rightarrow 12 - 4i_x^1 - 2i_x^1 = 0$$

$$i_x^1 = 2 \text{ amp}$$

Due to 2A source:



$$-3i_x^{11} - V^{11} = 0$$

$$\Rightarrow V^{11} = -3i_x^{11}$$

KCL:

$$i_x^{11} = \frac{V^{11} - 2i_x^{11}}{1\Omega} - 2$$

$$\Rightarrow i_x^{11} = -2/6 = -\frac{1}{3} \text{ amp}$$

$$\therefore \text{Total current } i_x = i_x^1 + i_x^{11}$$

$$\Rightarrow i_x = 2 - \frac{1}{3} = \frac{5}{3} \text{ amp} = 1.66 \text{ A}$$

7. $F(S) = s + 4 + \frac{5}{3}$

If $F(S)$ is a driving point admittance then capacitor of

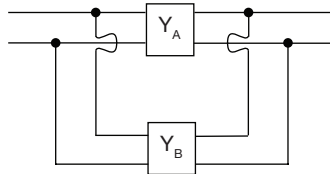
1F, resistor of $\frac{1}{5}\Omega$, inductor of $\frac{1}{5}H$

If $F(S)$ is a driving point impedance then capacitor of

0.2F, Resistor of 4Ω , inductor of 1H. Choice (C)

3.10 | Networks Test 1

8. Bandwidth of resonance curve is determined by all R , L , C . Choice (D)
 9. Short circuit admittance matrix means y -matrix.



$$Y_{eq} = Y_A + Y_B \text{ For parallel connection} \quad \text{Choice (B)}$$

10. $h_{11} = \frac{V_1}{I_1}$ ohms $h_{22} = \frac{I_2}{V_2}$ mho

$$h_{12} = \frac{V_1}{V_2} \text{ No dimensions}$$

$$h_{21} = \frac{V_1}{I_1} \text{ No dimensions} \quad \text{Choice (C)}$$

11. In order to find current through a particular branch in a linear Network, Nodal Analysis is preferred Choice (D)
 12. Choice (B)
 13. Maximum heat dissipation will occur when $r R_L = 6 \Omega$

$$i = \frac{48}{12} = 4A$$

$$\frac{i}{3} = \frac{48}{6 + R_L} = \frac{4}{3}$$

$$R_L = 30 \quad \text{Choice (A)}$$

14. $V_i(s) = 2 \times 10^3 (s) + \frac{1}{s \times 10^{-4}} \times 10 I_i(s)$

$$\Rightarrow \frac{V_i(s)}{I_i(s)} = 2 \times 10^3 + \frac{10^5}{s}$$

$$C_{\frac{i}{p}} = \frac{1}{10^5} = 10 \mu F \quad \text{Choice (C)}$$

15. $Q = 500 \text{ VAR}$

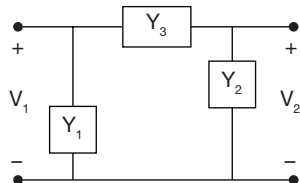
$$P.F = 0.6 = \cos \theta$$

$$\sin \theta = 0.8$$

$$s = \frac{Q}{\sin \theta} = \frac{500}{0.8} = 625 \text{ VA} \quad \text{Choice (B)}$$

16.
$$\begin{bmatrix} A & B \\ C & D \end{bmatrix} = \begin{bmatrix} 1 + \frac{Y_2}{Y_3} & \frac{1}{Y_3} \\ Y_1 + Y_2 + \frac{Y_1 Y_2}{Y_3} & 1 + \frac{Y_1}{Y_3} \end{bmatrix}$$

Where



$$= \begin{bmatrix} 1 + \frac{3}{5} & \frac{1}{5} \\ 2 + 3 + \frac{6}{5} & 1 + \frac{2}{5} \end{bmatrix} = \begin{bmatrix} 1.6 & 0.2 \\ 6.2 & 1.4 \end{bmatrix}$$

Choice (C)

17. From given equation

$$2\xi\omega_n = \frac{R}{L}$$

$$\xi = \frac{R}{2L \times \frac{1}{LC}} = \frac{R}{2} \sqrt{\frac{C}{L}}$$

$$\beta^2 < \alpha^2 \Rightarrow \frac{1}{LC} < \left(\frac{R}{2L}\right)^2$$

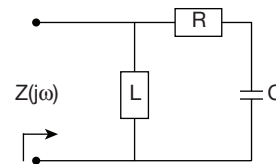
$$\Rightarrow \frac{R}{2} \sqrt{\frac{C}{L}} > 1$$

$$\xi > 1$$

So it is over damped

Choice (D)

- 18.



$$z(j\omega) = \frac{j\omega L \left(R - \frac{j}{\omega C} \right)}{R + j\omega L - \frac{j}{\omega C}}$$

$$= \frac{j\omega L \left(R - \frac{j}{\omega C} \right) \left(R - j\omega L + \frac{j}{\omega C} \right)}{\left(R + j\omega L - \frac{j}{\omega C} \right) \left(R - j\omega L + \frac{j}{\omega C} \right)}$$

Equating imaginary part to zero

$$R^2 - \frac{L}{C} + \frac{1}{\omega^2 C^2}$$

$$\Rightarrow \omega = \frac{1}{\sqrt{LC - R^2 C^2}}$$

Choice (D)

19. Voltage across $xy = \frac{8 \times 26}{13} = 16V$

$$\text{Current through } 8\Omega \text{ is } \frac{16}{8} = 2A$$

$$\text{In second circuit } IR + E = 16V \Rightarrow 2R + E = 16$$

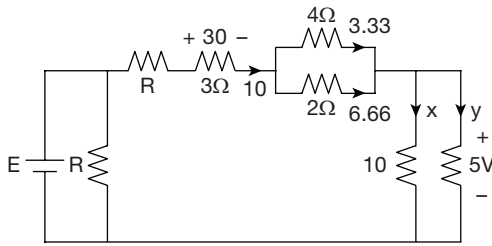
$$R = 4 \text{ and } E = 8$$

$$R = 6 \text{ and } E = 4$$

$$R = 9 \text{ and } E = -2$$

Choice (D)

20.

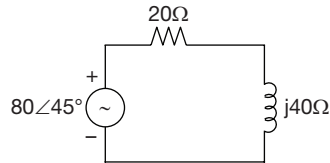


$$\begin{aligned} x + y &= 10 \\ 10x &= 5y \\ \Rightarrow 2 &= y \\ x &= \frac{10}{3}; y = \frac{20}{3} \end{aligned}$$

$$\Rightarrow \text{voltage across of } 5\Omega \text{ resistor is } \frac{100}{3}V$$

Choice (A)

21.



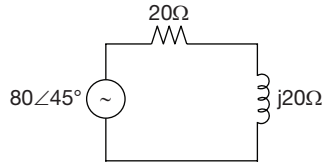
From compensation theorem, change in current

$$\Delta I = \frac{I \Delta Z}{Z_{\text{total}}}$$

$$I = \frac{V}{Z} = \frac{80\angle 45^\circ}{20 + j40} = \frac{80\angle 45^\circ}{44.7\angle 63.43^\circ} = 1.79 \angle -18.434^\circ$$

$$\Delta Z = j40 - j20 = j20\Omega$$

$$Z_{\text{total}} = 20 + j20 = 28.28$$



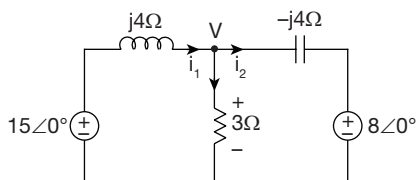
$$\Delta I = \frac{1.79\angle -18.434^\circ \times j20}{28.28\angle 45^\circ}$$

$$= \frac{1.79 \times 20}{28.28} \angle 90^\circ - 45^\circ - 18.434^\circ$$

$$= 1.26 \angle 26.566^\circ$$

Choice (D)

22. We know that the average power observed by the two reactive elements is zero



$$\frac{V-15}{j4} + \frac{V}{3} + \frac{V-8}{-j4} = 0$$

$$\Rightarrow V \left[\frac{j}{4} + \frac{1}{3} + \frac{1}{j4} \right] = \frac{15}{j4} - \frac{8}{j4}$$

$$\frac{V}{3} = \frac{7}{j4} \Rightarrow V = \frac{-j21}{4}$$

$$\text{Current flowing through } R \text{ is } \frac{V}{R} = \frac{-j21}{4 \times 3}$$

$$\frac{-7}{4} \angle 90^\circ = \frac{7}{4} \angle -90^\circ$$

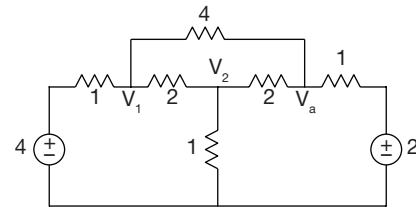
$$\text{So } I_{\text{max}} = \frac{7}{4}$$

$$\text{The average power absorbed by resistor is } P_R = \frac{1}{2} I_m^2 R$$

$$P_R = \frac{1}{2} \times \frac{49}{16} \times 3 = 4.6W$$

Choice (B)

23.


 Nodal Analysis at V_1

$$\frac{V_1 - 4}{1} + \frac{V_1 - V_2}{2} + \frac{V_1 - V_a}{4} = 0$$

$$7V_1 - 2V_2 - V_a = 16 \quad \rightarrow (1)$$

 Nodal Analysis at V_2

$$\frac{V_2}{1} + \frac{V_2 - V_1}{2} + \frac{V_2 - V_a}{2} = 0$$

$$4V_2 - 2V_1 = V_a \quad \rightarrow (2)$$

 At V_a

$$\frac{V_a - 2}{1} + \frac{V_a - V_2}{2} + \frac{V_a - V_1}{4} = 0$$

$$-4V_1 - 13V_2 = 4 \quad \rightarrow (3)$$

After solving three equations we will get

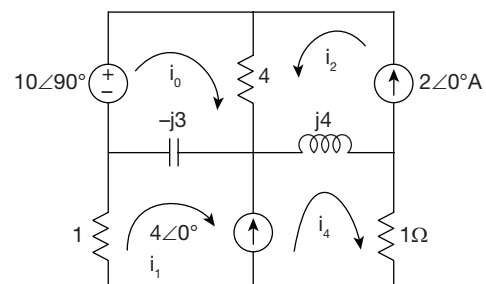
$$V_1 = 2.9$$

$$V_2 = 1.2$$

$$V_a = 1.9V$$

Choice (C)

24. Given circuit is



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$$i_2 = 2\angle 0^\circ$$

$$i_o - i_1 + i_4 = 4\angle 0^\circ \rightarrow @$$

$$I_1 - j3(I_1 - I_o) + j4(I_2 + I_4) + i_4 = 0$$

$$I_1[1 - 3j] + 3jI_o + j4i_2 + I_4(1 + j4) = 0$$

$$I_1[1 - j3] + j3I_o + j8\angle 0^\circ + I_4(1 + j4) = 0$$

$$I_1[1 - j3] + j3I_o + j8 + I_4(1 + j4) = 0 \quad \text{--- (b)}$$

$$10\angle 90^\circ = 4(2\angle 0^\circ + I_o) + (I_o - I_1)(-j3)$$

$$10\angle 90^\circ - 8 = I_o(4 - j3) + j3I_1$$

$$-8 + 10j = I_o[4 - j3] + j3I_1 \rightarrow (C)$$

Solving above equation we will get

$$I_o = 5.01 \angle 107.4$$

Choice (C)

25. Given that $Z(t) = e^{-10t} [1 + 10t] u(t)$

$$Z(s) = \frac{1}{s+10} + \frac{10}{(s+10)^2} = \frac{s+20}{(s+10)^2}$$

$$V(s) = I(s) \cdot Z(s)$$

$$I(s) = \frac{V(s)}{Z(s)} = \frac{10}{(s+10)^2} \frac{(s+10)^2}{(s+20)} = 10e^{-20t}$$

At $t = 50 \text{ ms}$

$$= 10 e^{-20 \times 50 \times 10^{-3}} = 10 e^{-1} = 3.6 \text{ A}$$

Choice (D)

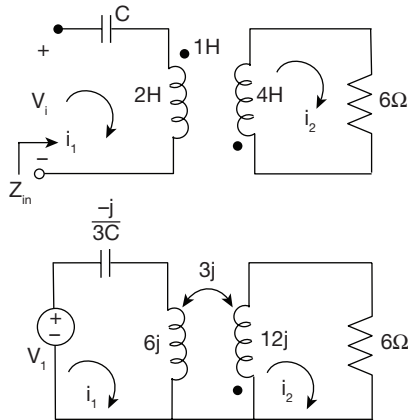
$$26. V_o = \frac{25\angle 60^\circ \times [j10 + j5 + 10]}{-j8 + j6 + j10 + (2 \times j5) + 10}$$

$$= \frac{25\angle 60^\circ (10 + j15)}{10 + j18} = \frac{25 \times 18 \angle 116.3}{20.59 \angle 60.94}$$

$$= 21.88 \angle 55.36 \text{ volts}$$

Choice (A)

27. Given circuit is



$$V_1 = \frac{-jI_1}{3C} + j6I_1 - j3I_2$$

$$12jI_2 + 6I_2 - 3jI_1 = 0$$

$$I_2[2 + j4] = jI_1$$

$$I_2 = \frac{j}{(2 + j4)} I_1$$

$$V_1 = \frac{-jI_1}{3C} + j6I_1 + \frac{3I_1}{(2 + j4)}$$

$$V_1 = I_1 \left[\frac{-j}{3C} + j6 + \frac{3(2 - j4)}{20} \right]$$

At resonance imaginary part equal to zero

$$\frac{-j}{3C} + j6 - \frac{12j}{20} = 0$$

$$6 - \frac{12}{20} = \frac{1}{3C}$$

$$C = \frac{5}{81}$$

Choice (A)

28. The condition to balance given circuit is

$$\frac{R_2}{R_1 + j\omega L_1} = \frac{R_4 - \frac{j}{\omega C_4}}{R_3}$$

$$R_2 R_3 = \left(R_4 - \frac{j}{\omega C_4} \right) (R_1 + j\omega L_1)$$

Imaginary part is equal to zero

$$\omega L_1 R_4 - \frac{R_1}{\omega C_4} = 0$$

$$\frac{\omega L_1}{R_1} = \frac{1}{\omega C_4 R_4}$$

Choice (A)

29. Applying nodal analysis at node V_1

$$-I_1 + \frac{V_1}{2} + 0.5V_1 = 0$$

$$V_1 = I_1 \rightarrow (1)$$

At node V_2

$$-I_2 + \frac{V_2}{4} - 0.5V_1 = 0$$

$$0.25V_2 = 0.5V_1 + I_2$$

$$V_2 = 4\{0.5I_1 + I_2\}$$

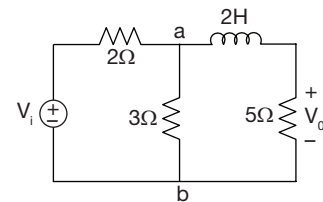
$$V_2 = 2I_1 + 4I_2 \rightarrow (ii)$$

from (i) and (ii)

$$[Z] = \begin{bmatrix} 1 & 0 \\ 2 & 4 \end{bmatrix} \Omega$$

Choice (C)

30. Given circuit is



$$V = \frac{5}{5 + 2s} V_{ab}$$

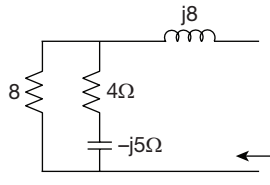
$$V_{ab} = \frac{3 / (5 + 2s)}{2 + [3 / (5 + 2s)]} V_i = \frac{15 + 6s}{31 + 10s} V_i$$

$$V_{o(s)} = \frac{5(15+6s)}{(5+2s)(31+10s)} V_i = \frac{15}{31+10s} V_{i(s)}$$

$$\begin{aligned} V_o &= \frac{15}{31+10s} V_i(s) \\ &= 2.08 \cos(3t-4) \\ &= 1.49 \cos 3t + 1.44 \sin 3t \end{aligned}$$

Choice (D)

31.



$$[8 / 4 - j5] + j8 = z_{th}$$

$$\begin{aligned} Z_{th} &= 60.88 \angle 83.53^\circ \\ &= 6.38 + j60.497 \end{aligned}$$

$$P_{\max \text{ avg}} = \frac{(V_{th})^2}{4R_{th}}$$

$$V_{th} = \frac{8 \times (4 - j5)}{8 + 4 - j5}$$

$$= \frac{8(4 - j5)}{12 - j5} = \frac{51.22}{13} \angle -51.34 + 22.61$$

$$= 3.94 \angle -28.73$$

$$P_{\max \text{ avg}} = \frac{(3.92)^2}{4 \times 6.86} = 0.56 \text{ W}$$

Choice (C)

$$32. \quad i_A = \frac{30}{15} = 2 \text{ A}$$

$$i_B = \frac{20}{15} = \frac{4}{3} \text{ A}$$

$$i_C = \frac{15}{15} = 1 \text{ A}$$

current required to blow the fuse is = 18A
so additional bulbs must draw

$$= 18 - \left(2 + \frac{4}{3} + 1\right) = 13.66$$

$$\text{No. of additional bulbs} = 13.66/2 = 6.833 = 7$$

Choice (B)

33. Each set of parallel A, B, C bulbs is drawing 4.33 Amperes of current

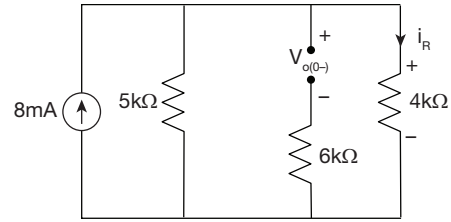
Current required to blow the fuse is 18A

$$\text{No. of bulbs required} = \frac{18 \times 3}{13} = 4.15 \approx 5$$

Additional No. of sets are 4

Choice (B)

34. For $t < 0$ (switch is closed)



$$i_R = \frac{5}{9} \times 8 = \frac{40}{9} \text{ mA}$$

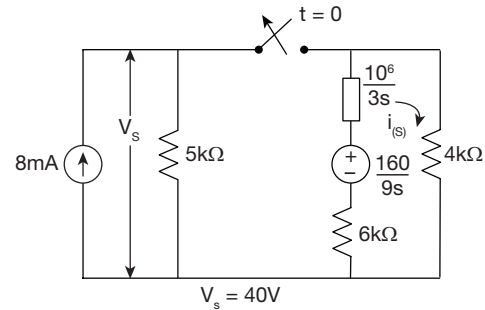
Current through 5k ohm resistor is

$$= \left(8 - \frac{40}{9}\right) \text{ A} = \frac{32}{9} \text{ mA}$$

$$V_C(0^-) = V_S = 5 \times \frac{32}{9} \text{ V} = 17.8 \text{ V}$$

Choice (A)

35. At $t > 0$, switch is opened, the network is redrawn in s-domain form.



Capacitor will discharge through 6 k ohm and 4 k ohm resistors

$$I_c = -i_R$$

Applying KVL

$$\left(\frac{10^6}{3s} + 6 \times 10^3 + 4 \times 10^3\right) I_{(s)} = -\frac{160}{9s}$$

$$i_c(s) \left[\frac{10^6}{3s} + 10^4\right] = \frac{-160}{9s}$$

$$I_c(s) = \frac{-16}{9 \left(\frac{100}{3} + s\right)} \text{ A}$$

$$I_c(t) = \frac{-16}{9} e^{\frac{-100t}{3}} \text{ mA} = -i_R$$

$$\text{we know that } V_C(t) = \frac{1}{C} \int_0^t i_c(t) dt + V_C(0^-)$$

$$V_C(t) = \left[\frac{10^6}{3} \int_0^t \frac{-16}{9} \times 10^{-3} e^{\frac{-100t}{3}} dt\right] + \frac{160}{9}$$

$$= \frac{10^3}{3} \times \frac{-16}{9} \times \frac{3}{-100} e^{\frac{-100t}{3}} + \frac{160}{9}$$

$$= \frac{+160}{3} \left[e^{\frac{-100t}{3}} - 1\right] + \frac{160}{9}$$

$$= \frac{160}{9} e^{\frac{-100t}{3}} \text{ V}$$

Choice (B)