

Quadrilaterals

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BOOK

MATHEMATICS

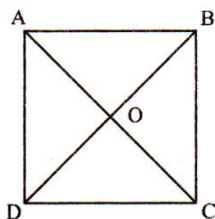
NOTES

FUNDAMENTALS

- Quadrilateral is a figure which is bounded by four straight lines. A quadrilateral has four vertices, four sides, four angles and sum of angles is 360° .

TYPES OF QUADRILATERAL

- **Square:-**



A quadrilateral whose sides are equal and each angle is equal to 90° is called square.

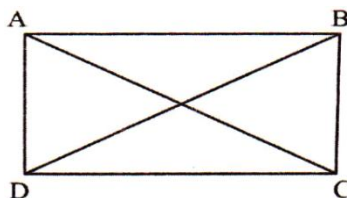
Diagonals of square are equal and cut each other at 90° .

i.e., $AB = BC = CD = DA$.

$\angle A = \angle B = \angle C = \angle D$

and $AC = BD$.

- **Rectangle**

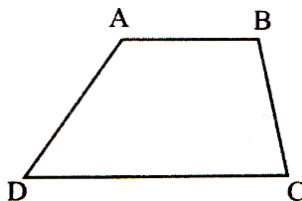


A quadrilateral whose all angles are right angles and each pair of opposite sides are equal is called Rectangle.

i.e., $\angle A = \angle B = \angle C = \angle D = 90^\circ$, and $AB = CD, AD = BC$. The diagonals of rectangle are equal and bisect each other at right angle. Each diagonal divides rectangle into congruent triangles.

i.e., $AC = BD$ and $\triangle ADC = \triangle ABC, \triangle ABD = \triangle BCD$

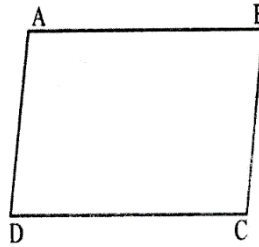
- **Trapezium:** A quadrilateral in which exactly one pair of parallel sides are equal is called a trapezium



$AB \parallel CD$

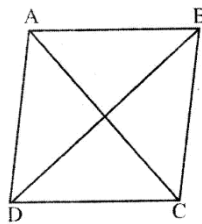
- A trapezium, is an isosceles trapezium if its non - parallel sides are equal.
- ABCD is a isosceles trapezium if
 $AB \parallel CD$ and $AD = BC$.

➤ **Parallelogram:-** A quadrilateral having both pairs of opposite sides are equal is called a. parallelogram,



- In parallelogram ABCD $AB \parallel CD$ and $AD = BC$,
- In a parallelogram two opposite sides are equal.
i.e., $AD = BC, AB = CD$
- In a. parallelogram two opposite angles are equal
i.e., $\angle A = \angle C$ and $\angle B = \angle D$.
- In a parallelogram sum of two adjacent angles is 180° i.e., $\angle A + \angle B = 180^\circ, \angle B + \angle C = 180^\circ$
 $\angle C + \angle D = 180^\circ$ and $\angle D + \angle A = 180^\circ$
- Each diagonal of a parallelogram divides it into two congruent triangles.
i.e., $\triangle ABC = \triangle ADC$
 $\triangle ABD = \triangle BCD$

➤ **Rhombus:-** A quadrilateral which all sides are equal is called a rhombus.



- The opposite side of a rhombus are parallel.
i.e., $AB \parallel CD$ and $BC \parallel AD$
- Opposite angles of a rhombus are equal
i.e., $\angle A = \angle C$ and $\angle B = \angle D$
- Each diagonal of a rhombus divides it into two congruent triangles.