## 8. Three Dimensional Geometry

## • Direction cosines (d.c.'s) of a line:

- d.c.'s of a line are the cosines of angles made by the line with the positive direction of the coordinate axes.
- If l, m, and n are the d.c.'s of a line, then  $l^2 + m^2 + n^2 = 1$
- d.c.'s of a line joining two points  $P(x_1, y_1, z_1)$  and  $Q(x_2, y_2, z_2)$  are  $\frac{x_2 x_1}{PQ}$ ,  $\frac{y_2 y_1}{PQ}$ , where  $PQ = \sqrt{(x_2 x_1)^2 + (y_2 y_1)^2 + (z_2 z_1)^2}$

## • Direction ratios (d.r.'s) of a line:

- d.r.'s of a line are the numbers which are proportional to the d.c.'s of the line.
- d.r.'s of a line joining two points P  $(x_1, y_1, z_1)$  and Q  $(x_2, y_2, z_2)$  are given by  $x_1 x_2, y_1 y_2, z_1 z_2$  or  $x_2 x_1, y_2 y_1, z_2 z_1$ .
- If a, b, and c are the d.r.'s of a line and l, m, and n are its d.c.'s, then  $\frac{1}{a} = \frac{m}{b} = \frac{n}{c}$

$$1 = \pm \frac{a}{\sqrt{a^2 + b^2 + c^2}}, m = \pm \frac{b}{\sqrt{a^2 + b^2 + c^2}}, \text{ and } n = \pm \frac{c}{\sqrt{a^2 + b^2 + c^2}}$$