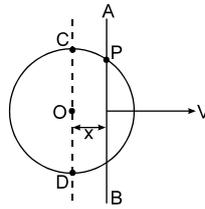
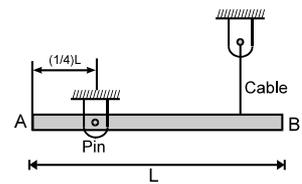


4. A rod AB is moving on a fixed circle of radius R with constant velocity 'v' as shown in figure. P is the point of intersection of the rod and the circle. At an instant the rod is at a distance $x = \frac{3R}{5}$ from centre of the circle. The velocity of the rod is perpendicular to the rod and the rod is always parallel to the diameter CD.

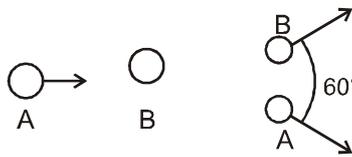


- (a) Find the speed of point of intersection P.
 (b) Find the angular speed of point of intersection P with respect to centre of the circle.
5. A uniform beam of length L and mass 'm' is supported as shown. If the cable suddenly breaks, determine; immediately after the release.
 (a) the acceleration of end B.
 (b) the reaction at the pin support.



COMPREHENSION

A smooth ball 'A' moving with velocity 'V' collides with another smooth identical ball at rest. After collision both the balls move with same speed with angle between their velocities 60° . No external force acts on the system of balls.



6. The speed of each ball after the collision is
 (A) $\frac{V}{2}$ (B) $\frac{V}{3}$ (C) $\frac{V}{\sqrt{3}}$ (D) $\frac{2V}{\sqrt{3}}$
7. If the kinetic energy lost is fully converted to heat then heat produced is
 (A) $\frac{1}{3}mV^2$ (B) $\frac{2}{3}mV^2$ (C) 0 (D) $\frac{1}{6}mV^2$
8. The value of coefficient of restitution is
 (A) 1 (B) $\frac{1}{3}$ (C) $\frac{1}{\sqrt{3}}$ (D) 0

Answers Key

1. (C) 2. (C) 3. (B)(C)(D)
4. (a) $V_p = \frac{5}{4} V$ (b) $V \operatorname{cosec} \theta$
5. (a) $\frac{9g}{7} \downarrow$ (b) $\frac{4w}{7} \uparrow$ 6. (C) 7. (D)
8. (B)

Hint & Solutions

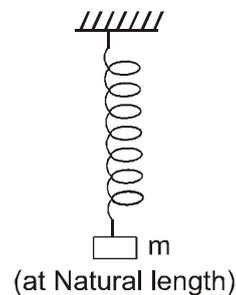
2. since torque about O is zero,
angular momentum of mass m is conserved

$$\therefore m v l = m v_{\perp} (l + x) ; v_{\perp} = \frac{v l}{l + x}$$

3. initial velocity = final velocity = 0
from energy conservation

$$mgx - \frac{1}{2} kx^2 = 0$$

$$x = \frac{2mg}{k}$$



at descended length = $\frac{x}{2}$

$$\frac{kx}{2} = k \cdot \frac{2mg}{2k} = mg$$

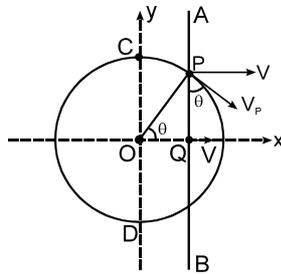
Net force = 0

$\Rightarrow a = 0$ at lower most position

$$\text{force} = Kx - mg = K \frac{2mg}{K} - mg = mg$$

$\Rightarrow a = g \uparrow$

4.



As a rod AB moves, the point 'P' will always lie on the circle.

\therefore its velocity will be along the circle as shown by ' V_P ' in the figure. If the point P has to lie on the rod 'AB' also then it should have component in 'x' direction as 'V'.

$$\therefore V_P \sin \theta = V$$

$$\Rightarrow V_P = V \operatorname{cosec} \theta$$

$$\text{here } \cos \theta = \frac{x}{R} = \frac{1}{R} \cdot \frac{3R}{5} = \frac{3}{5}$$

$$\therefore \sin \theta = \frac{4}{5} \quad \therefore \operatorname{cosec} \theta = \frac{5}{4} \quad \therefore V_P = \frac{5}{4} V$$

...Ans.

$$\omega = \frac{V_P}{R} = \frac{5V}{4R}$$

ALTERNATIVE SOLUTION :

Sol. (a) Let 'P' have coordinate (x, y)

$$x = R \cos \theta, \quad y = R \sin \theta.$$

$$V_x = \frac{dx}{dt} = -R \sin \theta \frac{d\theta}{dt} = V \quad \Rightarrow \quad \frac{d\theta}{dt} = \frac{-V}{R \sin \theta}$$

$$V_y = R \cos \theta \frac{d\theta}{dt} = R \cos \theta \left(-\frac{V}{R \sin \theta} \right)$$

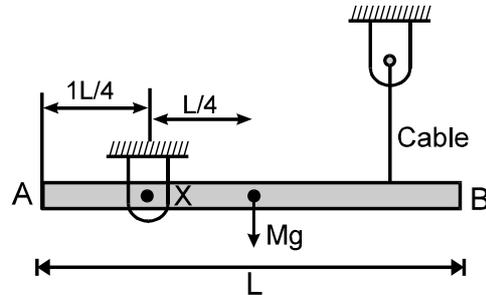
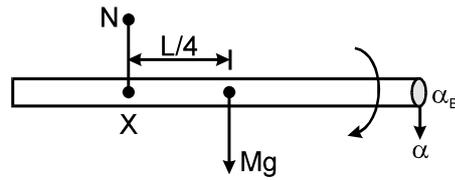
$$= -V \cot \theta$$

$$\therefore V_P = \sqrt{V_x^2 + V_y^2} = \sqrt{V^2 + V^2 \cot^2 \theta}$$

$$= V \operatorname{cosec} \theta \quad \text{...Ans.}$$

$$\text{Sol. (b)} \quad \omega = \frac{V_P}{R} = \frac{5V}{4R}$$

5. Taking torques w.r.t 'x'



M.I. of the rod w.r.t axis of rotation

$$I_x = I_{cm} + \frac{ML^2}{16}$$

$$= \frac{ML^2}{12} + \frac{ML^2}{16} = \frac{7ML^2}{48}$$

$$(i) \quad Mg \cdot \frac{L}{4} = I \cdot \alpha$$

$$Mg \cdot \frac{L}{4} = \frac{7ML^2}{48} \cdot \alpha$$

$$\Rightarrow \alpha = \frac{12g}{7L} \quad a_B = Ra$$

$$= \frac{3L}{4} \cdot \frac{12g}{7L} = \frac{9g}{7} \downarrow$$

$$(ii) \quad a_{cm} = \frac{L}{4} \cdot \alpha = \frac{3g}{7}$$

also apply equation of motion on COM

$$Mg - N = M \cdot \frac{3g}{7}$$

$$N = Mg - \frac{3Mg}{7} = \frac{4Mg}{7} \uparrow$$

$$[\text{Ans.: (a)} \frac{9g}{7} \downarrow \text{(b)} \frac{4w}{7} \uparrow]$$

6.to 8 From conservation of momentum

$$mv = mv' \cos 30^\circ + mv' \cos 30^\circ$$

$$\therefore v' = \frac{v}{2 \cos 30^\circ} = \frac{v}{\sqrt{3}}$$

7. Loss in kinetic energy

$$= \frac{1}{2}mv^2 - 2 \times \frac{1}{2}m \left(\frac{v}{\sqrt{3}} \right)^2 = \frac{1}{6}mv^2$$

8. Initially B was at rest, therefore line of impact is along final velocity of B.

$$\therefore e = \frac{v' - v' \cos 60^\circ}{v \cos 30^\circ} = \frac{\frac{1}{2} \frac{v}{\sqrt{3}}}{v \times \frac{\sqrt{3}}{2}} = \frac{1}{3}$$

