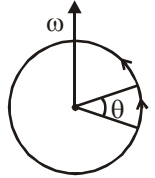


CIRCULAR MOTION

1. Average angular velocity $\Rightarrow \omega_{av} = \frac{\theta_2 - \theta_1}{t_2 - t_1} = \frac{\Delta\theta}{\Delta t}$

2. Instantaneous angular velocity $\Rightarrow \omega = \frac{d\theta}{dt}$



3. Average angular acceleration $\Rightarrow \alpha_{av} = \frac{\omega_2 - \omega_1}{t_2 - t_1} = \frac{\Delta\omega}{\Delta t}$

4. Instantaneous angular acceleration $\Rightarrow \alpha = \frac{d\omega}{dt} = \omega \frac{d\omega}{d\theta}$

5. Relation between speed and angular velocity $\Rightarrow v = r\omega$ and $\vec{v} = \vec{\omega} \times \vec{r}$

7. Tangential acceleration (rate of change of speed)

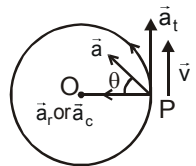
$$\Rightarrow a_t = \frac{dv}{dt} = r \frac{d\omega}{dt} = \omega \frac{dr}{dt}$$

8. Radial or normal or centripetal acceleration $\Rightarrow a_r = \frac{v^2}{r} = \omega^2 r$

9. Total acceleration

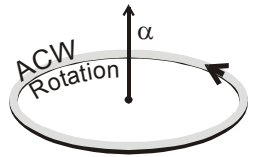
$$\Rightarrow \vec{a} = \vec{a}_t + \vec{a}_r \Rightarrow a = (a_t^2 + a_r^2)^{1/2}$$

Where $\vec{a}_t = \vec{\alpha} \times \vec{r}$ and $\vec{a}_r = \vec{\omega} \times \vec{v}$



10. Angular acceleration

$$\Rightarrow \quad \vec{\alpha} = \frac{d\vec{\omega}}{dt} \quad (\text{Non-uniform circular motion})$$



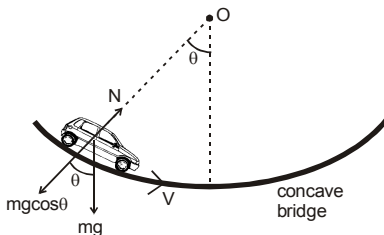
12. Radius of curvature $R = \frac{v^2}{a_{\perp}} = \frac{mv^2}{F_{\perp}}$

If y is a function of x . i.e. $y = f(x) \quad \Rightarrow$

$$R = \frac{\left[1 + \left(\frac{dy}{dx} \right)^2 \right]^{3/2}}{\frac{d^2y}{dx^2}}$$

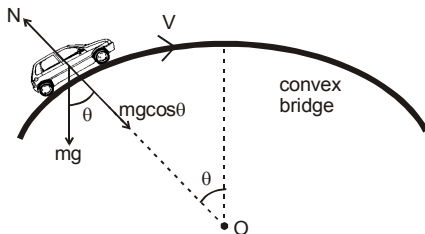
13. Normal reaction of road on a concave bridge

$$\Rightarrow \quad N = mg \cos \theta + \frac{mv^2}{r}$$



14. Normal reaction on a convex bridge

$$\Rightarrow \quad N = mg \cos \theta - \frac{mv^2}{r}$$



15. Skidding of vehicle on a level road

$$\Rightarrow \quad v_{\text{safe}} \leq \sqrt{\mu g r}$$

16. Skidding of an object on a rotating platform

$$\Rightarrow \quad \omega_{\text{max}} = \sqrt{\mu g / r}$$

17. Bending of cyclist $\Rightarrow \tan \theta = \frac{v^2}{rg}$

18. Banking of road without friction $\Rightarrow \tan \theta = \frac{v^2}{rg}$

19. Banking of road with friction $\Rightarrow \frac{v^2}{rg} = \frac{\mu + \tan \theta}{1 - \mu \tan \theta}$

20. Maximum also minimum safe speed on a banked frictional road

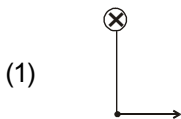
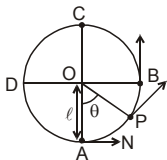
$$V_{\max} = \left[\frac{rg(\mu + \tan \theta)}{(1 - \mu \tan \theta)} \right]^{1/2} \quad V_{\min} = \left[\frac{rg(\tan \theta - \mu)}{(1 + \mu \tan \theta)} \right]^{1/2}$$

21. Centrifugal force (pseudo force) $\Rightarrow f = m\omega^2 r$, acts outwards when the particle itself is taken as a frame.

22. Effect of earth's rotation on apparent weight $\Rightarrow N = mg - mR\omega^2 \cos^2 \theta$;

where $\theta \Rightarrow$ latitude at a place

23. Various quantities for a critical condition in a vertical loop at different positions



$$V_{\min} = \sqrt{4gL}$$

(for completing the circle)



$$V_{\min} = \sqrt{4gL}$$

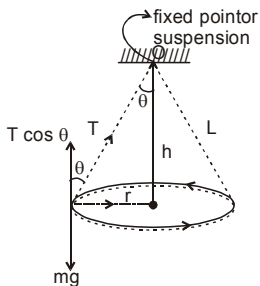
(for completing the circle)



$$V_{\min} = \sqrt{4gL}$$

(for completing the circle)

24. Conical pendulum :



$$T \cos \theta = mg$$

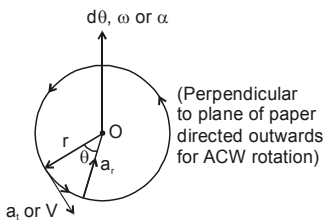
$$T \sin \theta = m\omega^2 r$$

$$\therefore \text{Time period} = 2\pi \sqrt{\frac{L \cos \theta}{g}}$$

25. Relations among angular variables :

$\omega_0 \Rightarrow$ Initial ang. velocity

$$\omega = \omega_0 + \alpha t$$



$\omega \Rightarrow$ Find angular velocity

$$\theta = \omega_0 t + \frac{1}{2} \alpha t^2$$

$\omega \Rightarrow$ Const. angular acceleration

$$\omega^2 = \omega_0^2 + 2\alpha \theta$$

$\theta \Rightarrow$ Angular displacement