

Practice Problems

Problems based on Progressive waves

Basic level

1.	In a progressive wave,	the distance between two con	nsecutive crests is		[Orissa JEE 2004]	
	(a) λ/2	(b) λ	(c) 3/2λ	(d) $\lambda/2$		
2. The equation of a wave is $3 \cos \pi (50t - x)$. The wavelength of the wave is [Orissa]						
	(a) 3 units	(b) 2 units	(c) 50 units	(d) 47 units		
3.	If the wave equation <i>y</i>	$= 0.08 \sin \frac{2\pi}{\lambda} (200 t - x)$ then the	velocity of the wave will t	De	[BCECE 2004]	
	(a) $400\sqrt{2}$	(b) $200\sqrt{2}$	(c) 400	(d) 200		
4.	A wave of frequency 50 is	00 Hz has velocity 360 m/sec	. The distance between two	o nearest points	s 60° out of phase,	
			[NCERT 1979; MP PET 1989;	JIPMER 1997; CI	PMT 1979, 90, 2003]	
	(a) 0.6 <i>cm</i>	(b) 12 cm	(c) 60 cm	(d) 120 cm		
5٠	The equation of a trans	sverse wave is given by $y = 10$	$\sin \pi (0.01 x - 2t)$			
	The equation of a transverse wave is given by $y = 10 \sin \pi (0.01 x - 2t)$ where x and y are in cm and t is in second. Its frequency is (a) 10 sec ⁻¹ (b) 2 sec ⁻¹ (c) 1 sec ⁻¹ (d) 0.01 sec ⁻¹ If the frequency of a wave is $360s^{-1}$, the distance between two nearest compression & rarefaction is 1m. The the velocity of wave is					
	(a) 10 sec ⁻¹	(b) 2 sec^{-1}	(c) 1 <i>sec</i> ⁻¹	(d) 0.01 sec ⁻¹	1	
6.			etween two nearest comp	ression & raref	action is 1m. Then	
					[CPMT 2003]	
			,			
7.		r a sound wave to travel betw	-		erature is 10° C. If	
	-	30° C the sound wave travel	-			
0	(a) 1.9 <i>sec</i>	(b) 2.0 sec	(c) 2.1 sec	(d) 2.2 sec	· · · · · · · · · · · · · · · · · · ·	
8.	statement is	e is given as $y = 0.07 \sin(12\pi x - x)$	5000π). where x is in me	tre and t in se	c, then the correct	
	statement is				[UPSEAT 2003]	
	(a) $\lambda = 1/6m, v = 250m/$	s (b) $a = 0.07m, v = 300m/s$	(c) $n = 1500, v = 200 m / s$	(d) None of t		
9.	The equation of the pr statement is not true	copagating wave is $y = 25 \sin(x)$	(20t+5x), where y is displ	lacement. Whic	ch of the following	
					[MP PET 2003]	
	(a) The amplitude of t	he wave is 25 units	(b) The wave is propag	ating in positiv	e <i>x</i> -direction	
	(c) The velocity of the wave is 4 units (d) The maximum velocity of the particles is 500 units					
10.	In a plane progressive	wave given by $y = 25 \cos(2\pi t - \pi)$	πx), the amplitude and freq	uency are resp	ectively [BCECE 2003]	
	(a) 25,100	(b) 25, 1	(c) 25, 2	(d) 50π, 2		
11.	If v_m is the velocity of pressure and temperat	sound in moist air, v_d is the ture	velocity of sound in dry	air, under iden	tical conditions of	

	(a) $v_m > v_d$	(b) $v_m < v_d$	(c) $v_m = v_d$	(d) $v_m v_d = 1$				
12.	The displacement y	of a wave travelling in the <i>x</i> -o	direction is given by $y = 10^{-10}$	$4\sin\left(600t-2x+\frac{\pi}{3}\right)$ metres, where x is				
	expressed in metres and t in seconds. The speed of the wave-motion, in ms^{-1} , is							
	(a) 200	(b) 300	(c) 600	(d) 1200				
13.	The equation $y = A \cos \theta$	$\cos^2\left(2\pi nt - 2\pi \frac{x}{\lambda}\right)$ represents a v	vave with					
	(a) Amplitude A/2, f	frequency 2n and wavelength	$\lambda/2$ (b) Amplitude A/2, from the second se	equency $2n$ and wavelength λ				
	(c) Amplitude A, fre	equency $2n$ and wavelength 2λ	(d) Amplitude A, freq	uency n and wavelength λ				
4.	v_1 and v_2 are the ve	elocities of sound at the same	temperature in two monoa	tomic gases of densities ρ_1 and ρ_2				
	respectively. If ρ_1 / ρ_2	$p_2 = \frac{1}{4}$ then the ratio of velocit	ies v_1 and v_2 will be					
	(a) 1:2	(b) 4:1	(c) 2:1	(d) 1:4				
15.	The temperature at	which the speed of sound in ai	r becomes double of its val	ue at $0^{\circ}C$ is				
-	(a) 273° K	(b) $546^{\circ} K$	(c) $1092^{\circ} K$	(d) $0^{\circ} K$				
16.				360 <i>m</i> /sec. if $\lambda = 60m$, then correct				
10.	expression for the w	-		-				
	(a) $y = 0.2 \sin \left[2\pi \left(6t + 1 \right) \right]$	$\left[+\frac{x}{60}\right]$	(b) $y = 0.2 \sin \left[\pi \left(6t + \frac{x}{60} \right) \right]$	$\overline{5}$				
	(c) $y = 0.2 \sin \left[2\pi \left(6t - 1 \right)^2 \right]$	$\left[-\frac{x}{60}\right]$	(d) $y = 0.2 \sin \left[\pi \left(6t - \frac{x}{60} \right) \right]$	$\overline{\mathbf{b}}$				
17.	The equation for sph	nerical progressive wave is		[CPMT 2002]				
	(a) $y = a\sin(\omega t - kx)$	(b) $y = \frac{a}{\sqrt{r}}\sin(\omega t - kx)$	(c) $y = \frac{a}{2}\sin(\omega t - kx)$	(d) $y = \frac{a}{r}\sin(\omega t - kx)$				
18.	A stone is dropped i approximately after		<i>metre</i> high. The sound of t	he splash will be heard by the man				
				[CPMT 1992; JIPMER 2001, 2002]				
	(a) 11.5 <i>sec</i>	(b) 21 <i>sec</i>	(c) 10 sec	(d) 14 sec				
19.	The equation of a pl	ane progressive wave is given	by $y = 0.25 \sin(100 t + 0.25 x)$. The frequency of this wave would				
	be							
				[CPMT 1993; JIPMER 2001, 2002]				
	(a) $\frac{50}{\pi} Hz$	(b) $\frac{100}{\pi} Hz$	(c) 100 <i>Hz</i>	(d) 50 Hz				
20.	The equation of a so	und wave is						
	$y = 0.0015 \sin(62.4 x + 316 t)$							
	The wavelength of the							
	(a) 0.2 unit	(b) 0.1 unit	(c) 0.3 unit	(d) Cannot be calculated				
21.	The equation of a tr	0						
		$y = 60\cos(1800 t - 6x)$						
		where y is in microns, t in seconds and x in meters. The ratio of maximum particle velocity to velocity of wave propagation is						

where y is in microns, t in seconds and x in meters. The ratio of maximum particle velocity to velocity of wave propagation is
[CBSE PMT 1997; JIPMER 2001, 2002]

(a) 3.6×10^{-11} (b) 3.6×10^{-6} (c) 3.6×10^{-4} (d) 3.6

The wave equation is $y = 0.30 \sin(314 t - 1.57 x)$ where *t*, *x* and *y* are in second, meter and centimeter respectively. 22. The speed of the wave is [CPMT 1997; AFMC 1999; CPMT 2001] (c) 300 *m/s* (a) 100 m/s (b) 200 *m/s* (d) 400 m/s Transverse waves can propagate 23. (a) Both in a gas and a metal (b) In a gas but not in a metal (c) Not in a gas but in a metal (d) Neither in a gas nor in a metal The sound carried by air from a sitar to a listener is a wave of the following type 24. (a) Longitudinal stationary (b) Transverse progressive (c) Transverse stationary (d) A tuning fork produces wave in medium. If the temperature of the medium changes then which of following 25. will change [MH CET 2001] (a) Time period (b) Wavelength (c) Frequency (d) Amplitude 26. The equation of a longitudinal wave is represented as $y = 20 \cos \pi (50t - x)$. Its wavelength is (a) 5 m (b) 2 m (c) 50 m (d) 20 m The rope shown at an instant is carrying a wave travelling towards right, created by a source vibrating at a 27. frequency n. Consider the following statements I. The speed of the wave is $4n \times ab$ II. The medium at *a* will be in the same phase as *d* after $\frac{4}{3n}s$ ¦ c III. The phase difference between b and e is $\frac{3\pi}{2}$ Which of these statements are correct [AMU 2001] (a) I, II and III (b) II only (c) I and III (d) III only 28. To increase the frequency from 100 Hz to 400 Hz the tension in the string has to be changed by (a) 4 times (b) 16 times (c) 20 times (d) None of these 29. Velocity of sound in air I. Increases with temperature II. Decreases with temperature III. Increase with pressure IV. Is independent of pressure V. Is independent of temperature Choose the correct answer. (a) Only I and II are true (b) Only I and III are true (c) Only II and III are true (d) Only I and IV are true The speed of a wave in a medium is 760 m/s. If 3600 waves are passing through a point, in the medium in 2 30. minutes, then its wavelength is (a) 13.8 m (b) 25.3 m (c) 41.5 m (d) 57.2 m A string of 7 m length has a mass of 0.035 kg. If tension in the string is 60.5N, then speed of a wave on the 31. [CBSE PMT 2001] string is (a) 77 *m/s* (b) 102 *m/s* (c) 110 m/s (d) 165 m/sThe relation between phase difference and path difference is 32. (c) $\Delta \phi = \frac{2\pi\lambda}{\Delta x}$ (d) $\Delta \phi = \frac{2\Delta x}{\lambda}$ (a) $\Delta \phi = \frac{2\pi}{\lambda} \Delta x$ (b) $\Delta \phi = 2\pi \lambda \Delta x$ The frequency of a rod is 200 Hz. If the velocity of sound in air is 340 ms^{-1} , the wavelength of the sound 33. produced is [EAMCET (Med.) 1995; Pb. PMT 1999; CPMT 2000] (a) 1.7 cm (b) 6.8 cm (c) 1.7 m (d) 6.8 m

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34. If the pressure amplitude in a sound wave is tripled, then the intensity of sound is increased by a factor of [CPMT 1992;

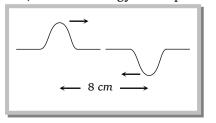
	(a) 9	(b) 3	(c) 6	(d) $\sqrt{3}$				
35.	Two monoatomic ideal gases 1 and 2 of molecular masses m_1 and m_2 respectively are enclosed in separate containers kept at the same temperature. The ratio of the speed of sound in gas 1 to that in gas 2 is given by							
	(a) $\sqrt{\frac{m_1}{m_2}}$	(b) $\sqrt{\frac{m_2}{m_1}}$	(c) $\frac{m_1}{m_2}$	(d) $\frac{m_2}{m_1}$				
6.		e distance between the cli	and fires a gun. If he hears i iffs is (Velocity of sound in a	first and second echoes after 1.5 s and air = 340 ms^{-1})				
	(a) 1190 m	(b) 850 m	(c) 595 m	(d) 510 m				
7.		re of an ideal gas is incre n it. The initial temperatur		of sound in the gas becomes $\sqrt{3}$ times				
	(a) $-73^{\circ}C$	(b) 27°C	(c) 127°C	(d) 327°C				
8.	The frequency of a so wave will be	ound wave is <i>n</i> and its ve	elocity is v. If the frequency	y is increased to $4n$, the velocity of the				
	(-)	(L) <u>)</u> .		[MP PET 2000]				
	(a) <i>v</i>	(b) 2 <i>v</i>	(c) 4 <i>v</i>	(d) v/4				
9.	In a transverse progr The wavelength of the	-	A, the maximum particle vel	locity is four times of its wave velocity.				
	(a) $\frac{\pi A}{4}$	(b) $\frac{\pi A}{2}$	(c) <i>πA</i>	(d) 2 <i>π</i> A				
0.		•	liffs. First echo is heard afte o <i>m/s</i> , then the distance betw	er 3 seconds and second echo is heard ween the cliffs is				
	(a) 1650 m	(b) 1320 m	(c) 990 m	(d) 660 m				
1.			n long and its fundamental equired length of the string i	frequency is 270 <i>Hz</i> . If the desired is				
	(a) 13.5 <i>cm</i>	(b) 2.7 <i>cm</i>	(c) 5.4 <i>cm</i>	(d) 10.3 <i>cm</i>				
2.	Consider the followir	ng statements.						
	Assertion (A) : Like	sound, light can not propa	agate in vacuum.					
	Reason (<i>R</i>) : Sound i	is a square wave. It propa	agates in a medium by a virtu	ue of damping oscillation				
	Of these statements							
	(a) Both A and R are	e true and the <i>R</i> is a correc	ct explanation of the A					
	(b) Both A and R are	true but the <i>R</i> is not a co	orrect explanation of the A					
	(c) A is true but the	R is false						
	(d) Both A and R are	(d) Both A and R are false						
	(e) A is false but the	R is true						
3.	Sound velocity is max	ximum in						
	(a) <i>H</i> ₂	(b) N ₂	(c) <i>He</i>	(d) <i>O</i> ₂				
4.	The minimum distan	ice of reflector surface fro	om the source for listening t	he echo of sound is [KCET (Engg./Med.) 2				
	(a) 28 <i>m</i>	(b) 18 m	(c) 19 m	(d) 16.5 <i>m</i>				
1 5.		described by the equatio	on $Y = Y_0 \sin 2\pi \left(ft - \frac{x}{\lambda} \right)$. The m	naximum particle velocity is four times				
	the wave velocity if	77						
	(a) $\lambda = \frac{\pi Y_0}{4}$	(b) $\lambda = \frac{\pi Y_0}{2}$	(c) $\lambda = \pi Y_0$	(d) $\lambda = 2\pi Y_0$				
46.	The equation of a wə	ave travelling in a string c	can be written as $y = 3\cos \pi (10^{\circ})$	00t - x). Its wavelength is				

Wave Motion 235 [MNR 1985; CPMT 1991; MP PMT 1994, 97] (d) None of the above (a) 100 cm (b) 2 cm (c) 5 cm 47. Which of the property makes difference between progressive and stationary waves (a) Amplitude (b) Frequency (c) Propagation of energy (d) Phase of the wave Which of the following equation does not represent the progressive wave 48. (a) $y = A \sin \omega \left(t - \frac{x}{y} \right)$ (b) $y = A \sin 2\pi \left(\frac{t}{T} + \frac{x}{\lambda} \right)$ (c) $y = A \sin \frac{2\pi}{\lambda} (vt - x)$ (d) $y = A \sin 2\pi \left(\frac{t}{T} - \frac{x}{y} \right)$ Problems based on Superposition of waves In an open organ pipe......wave is present 49. [Orissa JEE 2004] (a) Transverse standing wave (b) Longitudinal standing wave (c) Longitudinal moving wave (d) Transverse moving wave Two waves are propagating to the point P along a straight line produced by two sources A and B of simple 50. harmonic and of equal frequency. The amplitude of every wave at P is 'a' and the phase of A is ahead by $\frac{\pi}{3}$ than that of *B* and the distance *AP* is greater than *BP* by 50 *cm*. Then the resultant amplitude at the point *P* will be, if the wavelength is 1 meter [BVP 2003] (c) $a\sqrt{2}$ (b) $a\sqrt{3}$ (d) a (a) 2a Two tuning forks have frequencies 450 Hz and 454 Hz respectively. On sounding these forks together, the time 51. interval between successive maximum intensities will be (a) 1/4 sec (b) 1/2 sec (c) 1 sec (d) 2 sec Two waves of lengths 50 cm and 51 cm produced 12 beats per second. The velocity of sound is 52. (a) 306 m/s (b) 331 m/s (c) 340 m/s (d) 360 m/s In stationary longitudinal waves, nodes are points of 53. [SCRA 1994; MP PET 2003] (a) Minimum pressure (b) Maximum pressure (c) Minimum pressure variation (d) Maximum pressure variation A cylindrical tube, open at both ends, has a fundamental frequency f_0 in air. The tube is dipped vertically into 54. water such that half of its length is inside water. The fundamental frequency of the air column now is [RPET 1999; RPMT 2000; KCET (Engg.) 2002; BHU 2002; BCECE 2003] (a) $3f_0/4$ (b) f_0 (c) $f_0/2$ (d) $2f_0$ Equation of motion in the same direction is given by $y_1 = A \sin(\omega t - kx)$, $y_2 = A \sin(\omega t - kx - \theta)$. The amplitude of the 55. medium particle will be [BHU 2003] (a) $2A\cos\frac{\theta}{2}$ (b) $2A\cos\theta$ (c) $f, 1.2\lambda$ (d) $1.2f, 1.2\lambda$ 56. A closed organ pipe and an open organ pipe are tuned to the same fundamental frequency. What is the ratio of lengths [BHU 2003] (a) 1:2 (b) 2:1 (c) 2:3 (d) 4:3An open pipe resonates with a tuning fork of frequency 500 Hz. it is observed that two successive nodes are 57. formed at distances 16 and 46 cm from the open end. The speed of sound in air in the pipe is (a) 230 *m/s* (b) 300 *m/s* (c) 320 m/s (d) 360 m/s In the experiment for the determination of the speed of sound in air using the resonance column method, the 58. length of the air column that resonates in the fundamental mode, with a tuning fork is 0.1 m. when this length is changed to 0.35 m, the same tuning fork resonates with the first overtone. Calculate the end correction

	(a) 0.012 <i>m</i>	(b) 0.025 <i>m</i>	(c) 0.05 <i>m</i>	(d) 0.024 <i>m</i>
).	Two sound sources frequencies must be	-	produce four beats	in 0.25 second. the difference in their
				[BCECE 2003]
	(a) 4	(b) 8	(c) 16	(d) 1
•	At nodes in stationa	-		
		ure and density are maximum		essure and density are minimum
	(c) Strain is zero		(d) Energy is mir	
•	Find the fundament $= 332 \text{ m/sec}$	al frequency of a closed pipe, if	the length of the air	c column is 42 <i>m</i> . (speed of sound in air
				[RPET 2003]
	(a) 2 <i>Hz</i>	(b) 4 <i>Hz</i>	(c) 7 <i>Hz</i>	(d) 9 <i>Hz</i>
•	If <i>v</i> is the speed of s	sound in air then the shortest len	gth of the closed pip	be which resonates to a frequency n [KCE
	(a) $\frac{v}{4n}$	(b) $\frac{v}{2n}$	(c) $\frac{2n}{v}$	(d) $\frac{4n}{v}$
•				he same tension. if the first overtone of hat of B , the ratio of the lengths of the
	(a) 1:2	(b) 1:3	(c) 1:4	(d) 1:6
•	•	retched string is shortened by 4 fundamental frequencies is	0% and the tension	n is increased by 44%, then the ratio of
	(a) 2:1	(b) 3:2	(c) 3:4	(d) 1:3
•	The diameters are i		e materials are in th	1. The lengths are in the ratio 36 : 35. ne ratio 1 : 2. If the higher frequency in ed together is
	(a) 5	(b) 8	(c) 6	(d) 10
•	supports 1 metre ap	part. The wire passes at its mide	lle point between th	sion of 10 kg weight between two rigid he poles of a permanent magnet, and it by n . The frequency n of the alternating
	(a) 25 <i>Hz</i>	(b) 50 <i>Hz</i>	(c) 100 <i>Hz</i>	(d) 200 <i>Hz</i>
•	beat frequency deci		en the tension in the	with the vibrating string of a piano. The e piano string is slightly increased. The
	(a) 256 + 5 <i>Hz</i>	(b) 256 + 2 <i>Hz</i>	(c) 256 – 2 <i>Hz</i>	(d) 256 – 5 <i>Hz</i>
•		indamental tone in an open orga f fundamental tone in closed orga		48 <i>m is</i> 320 <i>Hz</i> . Speed of sound is 320
	(a) 153.8 <i>Hz</i>	(b) 160.0 <i>Hz</i>	(c) 320.0 <i>Hz</i>	(d) 143.2 <i>Hz</i>
•	two bridges when a	mass of 9 kg is suspended from	the wire. When this	waves with five antinodes between the mass is replaced by a mass M , the wire ne positions of the bridges. The value of g) 2002]
	(a) 25 <i>kg</i>	(b) 5 <i>kg</i>	(c) 12.5 <i>kg</i>	(d) 1/25 <i>kg</i>
•	-		%. In order to keep	its frequency of vibration constant, its
	(a) 20%	(b) 30%	(c) $\sqrt{69}$ %	(d) 69%
•	A tuning fork arra		s/sec with one fork	c of frequency 288 cps. A little wax is

Wave Motion 237 (a) 286 cps (b) 292 cps (c) 294 cps (d) 288 cps Two wires are in unison. If the tension in one of the wires is increased by 2%, 5 beats are produced per second. 72. The initial frequency of each wire is (a) 200 Hz (b) 400 Hz (c) 500 Hz (d) 1000 Hz Two closed organ pipes, when sounded simultaneously gave 4 beats per sec. If longer pipe has a length of 1m. 73. Then length of shorter pipe will be, (v = 300 m/s)(a) 185.5 cm (b) 94.9 cm (c) 90 cm (d) 80 cm A source of sound placed at the open end of a resonance column sends an acoustic wave of pressure amplitude 74. P_0 inside the tube. If the atmospheric pressure is p_A , then the maximum and minimum pressure at the closed end of the tube will be [UPSEAT 2002] (d) $\left(P_A + \frac{1}{2}P_0\right), \left(P_A - \frac{1}{2}P_0\right)$ (a) $(P_A + P_0), (P_A - P_0)$ (b) $(P_A + 2P_0), (P_A - 2P_0)$ (c) P_A, P_A Ten tuning forks are arranged in increasing order of frequency in such a way that any two nearest tuning forks 75. produce 4 beats/sec. The highest frequency is twice of the lowest. Possible highest and the lowest frequencies are [MP PMT 1990; MH CET 2002] (a) 80 and 40 (b) 100 and 50 (c) 44 and 22 (d) 72 and 36 If two waves of same frequency and same amplitude respectively, on superimposition produced a resultant 76. disturbance of the same amplitude, the waves differ in phase by (a) π (b) $2\pi/3$ (c) *π*/2 (d) Zero In stationary waves all particles between two nodes pass through the mean position 77. (a) At different times with different velocities (b) At different times with the same velocity (c) At the same time with equal velocity (d) At the same time with different velocities For production of beats, the two sources must have [CBSE PMT 1992; DPMT 2000, 2001] 78. (b) Different frequencies (a) Different frequencies and same amplitude (c) Different frequencies, same amplitude and same phase (d) Different frequencies and same phase Sixteen tuning forks are arranged in order of increasing frequencies. Adjacent successive forks, when sounded 79. together, give 8 beats per second. If the frequency of the last tuning fork is twice that of the first fork, the frequency of the last fork is [AMU 1999; MP PET 2001] (a) 256 Hz (b) 240 Hz (c) 128 Hz (d) 120 Hz 80. It is possible to hear beats from the two vibrating sources of frequency (a) 100 *Hz* and 150 *Hz* (b) 20 *Hz* and 25 *Hz* (c) 400 Hz and 500 Hz (d) 1000 Hz and 1500 Hz The ends of a stretched wire of length *L* are fixed at x = 0 and x = L. In one experiment, the displacement of the 81. wire is $y_1 = A \sin(\pi x / L) \sin \omega t$ and energy is E_1 , and in another experiment its displacement is $y_2 = A \sin(2\pi x / L) \sin 2\omega t$ and energy is E_2 . Then (a) $E_2 = E_1$ (b) $E_2 = 2E_1$ (c) $E_2 = 4E_1$ (d) $E_2 = 16E_1$ Two pulses in a stretched string whose centres are initially 8 cm apart are moving towards each other as shown 82. in the figure. The speed of each pulse is 2 *cm/s*. After 2 seconds, the total energy of the pulses will be

- (a) Zero
- (b) Purely kinetic
- (c) Purely potential



(d) Partly kinetic and partly potential

83. In order to double the frequency of the fundamental note emitted by a stretched string, the length is reduced to $\frac{3}{4}^{th}$ of the original length and the tension is changed. The factor by which the tension is to be changed, is

(a)
$$\frac{3}{8}$$
 (b) $\frac{2}{3}$ (c) $\frac{8}{9}$ (d) $\frac{9}{4}$

84. Two sound waves of wavelengths 5*m* and 6*m* formed 30 beats in 3 seconds. The velocity of sound is

(a) $300 ms^{-1}$ (b) $310 ms^{-1}$ (c) $320 ms^{-1}$ (d) $330 ms^{-1}$

85. If the length of a closed organ pipe is 1m and velocity of sound is 330 m/s, then the frequency for the second note is [AFMC 2001]

(a)
$$4 \times \frac{330}{4} Hz$$
 (b) $3 \times \frac{330}{4} Hz$ (c) $2 \times \frac{330}{4} Hz$ (d) $2 \times \frac{4}{330} Hz$

86. The fundamental note produced by a closed organ pipe is of frequency *f*. The fundamental note produced by an open organ pipe of same length will be of frequency

- (a) $\frac{f}{2}$ (b) f (c) 2f (d) 4f
- **87.** Two open organ pipes give 4 beats/sec, when sounded together in their fundamental notes. If the length of the pipes are 100 *cm* and 102.5 *cm* respectively, then the velocity of sound is
 - (a) 160 *m/s* (b) 240 *m/s* (c) 328 *m/s* (d) 496 *m/s*
- **88.** A second harmonic has to be generated in a string of length *l* stretched between two rigid supports. The point where the string has to be plucked and touched are
 - (a) Plucked at $\frac{l}{4}$ and touch at $\frac{l}{2}$ (b) Plucked at $\frac{l}{4}$ and touch at $\frac{3l}{4}$ (c) Plucked at $\frac{l}{2}$ and touched at $\frac{l}{4}$ (d) Plucked at $\frac{l}{2}$ and touched at $\frac{3l}{4}$
- **89.** If the velocity of sound in air is 336 m/s. The maximum length of a closed pipe that would produce a just audible sound will be

[KCET (Engg./Med.) 2001]

(a) 3.2 cm (b) 4.2 m (c) 4.2 cm (d) 3.2 m
90. A resonance air column of length 20 cm resonates with a tuning fork of frequency 250 Hz. The speed of the air is
[AFMC 1999; BHU 2000; CPMT 2001]
(a) 300 m/s (b) 200 m/s (c) 150 m/s (d) 75 m/s
91. Two waves are approaching each other with a velocity of 16 m/s and frequency n. The distance between two
consecutive nodes is
[Pb. PMT 1999; CPMT 2001]
(a)
$$\frac{16}{n}$$
 (b) $\frac{8}{n}$ (c) $\frac{n}{16}$ (d) $\frac{n}{8}$
92. An organ pipe P_1 closed at one end vibrating in its first overtone and another pipe P_2 open at both ends
vibrating in its third overtone are in resonance with a given tuning fork. The ratio of lengths of P_1 and P_2 is
(a) $1: 2$ (b) $1: 3$ (c) $3: 8$ (d) $3: 4$
93. 16 tuning forks are arranged in the order of increasing frequencies. Any two successive forks give 8 beats per
sec when sounded together. If the frequency of the last fork is twice the first, then the frequency of the first
fork is [CBSE PMT 2001]

(a) 120 (b) 160 (c) 180 (d) 220

Two waves $y = 0.25 \sin 316t$ and $y = 0.25 \sin 310t$ are travelling in same direction. The number of beats produced 94. per second will be [CPMT 1993; JIPMER 2000] (b) 3 (c) $3/\pi$ (d) 3π (a) 6 If the temperature increases, then what happens to the frequency of the sound produced by the organ pipe[RPMT 1996; D 95. (a) Increases (b) Decreases (c) Unchanged (d) Not definite Standing waves are produced in a 10 *m* long stretched string. If the string vibrates in 5 segments and the wave 96. velocity is 20 *m/s*, the frequency is (c) 5 Hz (a) 2 Hz (b) 4 Hz (d) 10 Hz An unknown frequency x produces 8 beats per seconds with a frequency of 250 Hz and 12 beats with 270 Hz 97. source, then *x* is [CPMT 1997; KCET (Engg./Med.) 2000] (a) 258 Hz (b) 242 Hz (c) 262 Hz (d) 282 Hz 98. $y = a \cos(kx + \omega t)$ superimposes on another wave giving a stationary wave having node at x = 0. What is the equation of the other wave (a) $-a\cos(kx + \omega t)$ (b) $a\cos(kx - \omega t)$ (c) $-a\cos(kx - \omega t)$ (d) $-a\sin(kx + \omega t)$ Two sound waves of slightly different frequencies propagating in the same direction produce beats due to[MP PET 200 99. (b) Diffraction (c) Polarization (d) Refraction (a) Interference 100. On sounding tuning fork A with another tuning fork B of frequency 384 Hz, 6 beats are produced per second. After loading the prongs of A with some wax and then sounding it again with B, 4 beats are produced per second. What is the frequency of the tuning fork A [MP PMT 2000] (a) 388 Hz (b) 380 Hz (c) 378 Hz (d) 390 Hz 101. Four wires of identical length, diameters and of the same material are stretched on a sonometre wire. If the ratio of their tensions is 1:4:9:16 then the ratio of their fundamental frequencies are (a) 16 : 9 : 4 : 1 (b) 4:3:2:1 (c) 1:4:2:16 (d) 1:2:3:4 **102.** If you set up the ninth harmonic on a string fixed at both ends, what is its frequency compared to the seventh harmonic [AMU (Engg.) 2000] (a) Higher (b) Lower (c) Equal (d) None of the above **103.** The frequency of a stretched uniform wire under tension is in resonance with the fundamental frequency of a closed tube. If the tension in the wire is increased by 8 N, it is in resonance with the first overtone of the closed tube. The initial tension in the wire is [EAMCET (Engg.) 2000] (b) 4 N (c) 8 N (d) 16 N (a) 1 N **104.** Two waves $y_1 = A_1 \sin(\omega t - \beta_1)$ and $y_2 = A_2 \sin(\omega t - \beta_2)$ Superimpose to form a resultant wave whose amplitude is **[CPMT 19**] (a) $\sqrt{A_1^2 + A_2^2 + 2A_1A_2\cos(\beta_1 - \beta_2)}$ (b) $\sqrt{A_1^2 + A_2^2 + 2A_1A_2}\sin(\beta_1 - \beta_2)$ (d) $|A_1 + A_2|$ (c) $A_1 + A_2$ **105.** In stationary wave [MP PET 1987; BHU 1995] (a) Strain is maximum at nodes (b) Strain maximum is at antinodes (c) Strain is minimum at nodes (d) Amplitude is zero at all the points

106. A wave of frequency 100 Hz is sent along a string towards a fixed end. When this wave travels back after reflection, a node is formed at a distance of 10 cm from the fixed end of the string. The speed of incident (and reflected) wave are [CBSE PMT 1994]

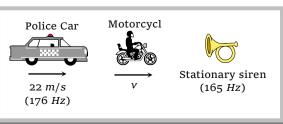
	(a) 40 <i>m/s</i>	(b) 20 <i>m/s</i>	(c) 10 <i>m/s</i>	(d) 5 <i>m/s</i>	
l 07.	The stationary wave and	$y = 2a \sin kx \cos \omega t$ in a closed or	gan pipe is the result of t	the superposition of $y = a \sin(\omega t - kx)$	
				[Roorkee 1994]	
	(a) $y = -a\cos(\omega t + kx)$	(b) $y = -a\sin(\omega t + kx)$	(c) $y = a\sin(\omega t - kx)$	(d) $y = a\cos(\omega t + kx)$	
08 .	Out of the given four	waves			
	$y = a\sin(kx + \omega t)$	(1)	$y = a\sin(\omega t - kx)$	(2)	
	$y = a\cos(kx + \omega t)$	(3)	$y = a\cos(\omega t - kx)$	(4)	
	Emitted by four diffe space under appropria		respectively, interference	e phenomena would be observed in	
	(a) Source S1 emits w	ave (1) and S_4 emits wave (4)			
	(b) Source S ₂ emits w	vave (2) and S_4 emits wave (4))		
	(c) Source S_1 emits w	rave (1) and S_2 emits wave (3)			
	(d) Interference phen	omenon cannot be observed b	by the combination of any	of the above waves	
9 .	The phase difference	between the two particles situ	lated on both the sides of	a node is	
	(a) 0°	(b) 90°	(c) 180°	(d) 360°	
10.	waves from the same		eing reflected from the 2	ers away from him. He also receive 25 <i>meter</i> high ceiling at the point th of	
	(a) 20, 20/3, 20/5 etc	c. (b) 10, 5, 2.5 etc.	(c) 10, 20, 30 etc	(d) 15, 25, 35 <i>etc</i>	
		Problems based	on Doppler's effec	•	
11.	Doppler effect is inde	pendent of		[Orissa JEE 2004]	
	(a) Distance between	source and listener	(b) Velocity of source		
	(c) Velocity of listene	er	(d) None of these		
2 .	A source and an obset then the real frequent		h same velocity 50 <i>m/s</i> . In	f the apparent frequency is 435 s^{-1} ,	
	(a) 320 <i>s</i> ⁻¹	(b) 360 <i>s</i> ⁻¹	(c) 390 <i>s</i> ⁻¹	(d) 420 s^{-1}	
3.	A source emits a soun	d of frequency of 400 Hz, but	the listener hears it to be	390 <i>Hz</i> . Then	
	(a) The listener is mo	oving towards the source	(b) The source is moving towards the listener		
	(c) The listener is mo	ving away from the source	(d) The listener has a defective ear		
4.	A source and an obse	erver are moving towards ea	ch other with a speed eq	ual to $\frac{v}{2}$ where v is the speed of	
	sound. The source is e	emitting sound of frequency <i>n</i>	. The frequency heard by t	the observer will be	
	(a) Zero	(b) <i>n</i>	(c) $\frac{n}{3}$	(d) 3 <i>n</i>	
			-		

115. A police car moving at 22 *m/s*, chases a motorcyclist. The police man sounds his horn at 176 *Hz*, while both of them move towards a stationary siren of frequency 165 *Hz*. Calculate the speed of the motorcycle, if it is given that he does not observes any beats

(a) 33 *m/s*

(b) 22 *m/s*

(c) Zero



[IIT-JEE (Screening) 2003]

(d) 11 *m/s* **116.** An observer moves towards a stationary source of sound with a speed $1/5^{\text{th}}$ of the speed of sound. The wavelength and frequency of the source emitted are λ and f respectively. The apparent frequency and wavelength recorded by the observer are respectively [CBSE PMT 2003] (c) $0.8f, 0.8\lambda$ (a) 1.2 f, λ (b) $f_{1.1.2\lambda}$ (d) $1.2f, 1.2\lambda$ When an engine passes near to a stationary observer then its apparent frequencies occurs in the ratio 5/3. If the velocity of engine is [MP PMT 2003] (c) 85 m/s(a) 540 *m/s* (b) 270 m/s (d) 52.5 m/s **118.** A siren placed at a railway platform is emitting sound of frequency 5 kHz. A passenger sitting in a moving train A records a frequency of 5.5 kHz while the train approaches the siren. During his return journey in a different train *B* he records a frequency of 6.0 *kHz* while approaching the same siren. The ratio of the velocity of train *B* to that of train A is [IIT-JEE (Screening) 2002] (a) 242/252 (b) 2 (c) 5/6 (d) 11/6 **119.** A racing car moving towards a cliff, sounds its horn. The driver observes that the sound reflected from the cliff has a pitch one octave higher than the actual sound of the horn. If v is the velocity of sound, then the velocity of the car is [KCET 2002] (a) $v/\sqrt{2}$ (b) v/2(c) v/3(d) v/4**120.** A person carrying a whistle emitting continuously a note of 272 Hz is running towards a reflecting surface with a speed of 18 km/hour. The speed of sound in air is $345ms^{-1}$. The number of beats heard by him is (a) 4 (b) 6 (c) 8(d) 3 **121.** A bus is moving with a velocity of 5 m/s towards a huge wall, the driver sounds a horn of frequency 165 Hz. If the speed of sound in air is 355 m/s, the number of beats heard per second by a passenger on the bus will be (a) 6 (b) 5 (c) 3 (d) 4

122. A car sounding a horn of frequency 1000 Hz passes an observer. The ratio of frequencies of the horn noted by the observer before and after passing of the car is 11 : 9. If the speed of sound is v, the speed of the car is

(a) $\frac{1}{10}v$ (b) $\frac{1}{2}v$	(c) $\frac{1}{5}v$	(d) <i>v</i>
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123. What should be the velocity of a sound source moving towards a stationary observer so that apparent frequency is double the actual frequency (Velocity of sound is *v*)

(a) v (b)
$$2v$$
 (c) $\frac{v}{2}$ (d) $\frac{v}{4}$

(b) 585 Hz

124. Two trains are moving towards each other at speeds of 20 *m/s* and 15 *m/s* relative to the ground. The first train sounds a whistle of frequency 600 Hz. the frequency of the whistle heard by a passenger in the second train before the train meets is (the speed of sound in air is 340 m/s)

125. A small source of sound moves on a circle as shown in the figure and an observer is sitting on O. Let n_1, n_2 and n_3 be the frequencies heard when the source is at A, B and C respectively. Then

(c) 645 Hz

(a) $n_1 > n_2 > n_3$

(a) 600 Hz

117.

- (b) $n_2 > n_3 > n_1$
- (c) $n_1 = n_2 > n_3$

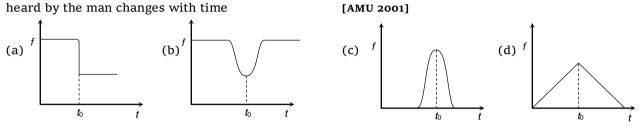
(d)
$$n_2 > n_1 > n_2$$

(d) $n_2 > n_1 > n_2$ 126. Two sirens situated one kilometer apart are producing sound of frequency 330 Hz. An observer starts moving from one siren to the other with a speed of 2 m/s. If the speed of sound be 330 m/s, what will be the beat frequency heard by the observer

В 0 Α

(d) 666 Hz

- (a) 8 (b) 4 (c) 6 (d) 1
- 127. Suppose that the speed of sound in air at a given temperature is 400 *m/sec*. An engine blows a whistle at 1200 *Hz* frequency. It is approaching an observer at the speed of 100 *m/sec*. What is the apparent frequency as heard by the observer [DPMT 2001]
 - (a) 1600 *Hz* (b) 1500 *Hz* (c) 1200 *Hz* (d) 600 *Hz*
- **128.** A man is standing on a railway platform listening to the whistle of an engine that passes the man at constant speed without stopping. If the engine passes the man at time t_0 . How does the frequency f of the whistle as



- **129.** A source is moving towards an observer with a speed of 20 *m/s* and having frequency of 240 *Hz*. The observer is now moving towards the source with a speed of 20 *m/s*. Apparent frequency heard by observer, if velocity of sound is 340 *m/s*, is
- (a) 240 Hz
 (b) 270 Hz
 (c) 280 Hz
 (d) 360 Hz **130.** A source and an observer move away from each other with a velocity of 10 *m/s* with respect to ground. If the observer finds the frequency of sound coming from the source as 1950 Hz, then actual frequency of the source is (velocity of sound in air = 340 *m/s*) **[MH CET 2000; AFMC 2000; CBSE PMT 2001]**

			C	,			
	(a) 1950 <i>Hz</i>	(b) 2068 <i>Hz</i>	(c) 2132 <i>Hz</i>	(d) 2486 Hz			
131. Maximum number of beat frequency heard by a human being is							
	(a) 10	(b) 4	(c) 20	(d) 6			

132. A source of sound of frequency 90 *vibrations/ sec* is approaching a stationary observer with a speed equal to 1/10 the speed of sound. What will be the frequency heard by the observer

(a) 80 vibrations/sec (b) 90 vibrations/sec (c) 100 vibrations/sec (d) 120 vibrations/sec

133. A train moves towards a stationary observer with speed 34 m/s. The train sounds a whistle and its frequency registered by the observer is f_1 . If the train's speed is reduced to 17 m/s, the frequency registered is f_2 . If the speed of sound is 340 m/s then the ratio f_1/f_2 is

	(a) 18/19	(b) 1/2	(c) 2	(d) 19/18	
134.	The frequency of a whi	stle of an engine is 60	00 cycles/sec is moving	with the speed of 30 <i>m/sec</i>	towards an

observer. The apparent frequency will be (velocity of sound = 330 m/s)
(a) 600 cps
(b) 660 cps
(c) 990 cps
(d) 330 cps

135. A source of sound of frequency 450 cycles/sec is moving towards a stationary observer with 34 m/sec speed. If

the speed of sound is 340 *m/sec*, then the apparent frequency will be(a) 410 cycles/sec(b) 500 cycles/sec(c) 550 cycles/sec(d) 450 cycles/sec

- **136.** When the source is moving towards the stationary observer, the apparent frequency is given by
 - (a) $n_1 = \frac{vn}{v v_s}$ (b) $n_1 = \frac{vn}{v + v_s}$ (c) $n_1 = \frac{(v + v_o)n}{v}$ (d) $n_1 = \frac{v + v_o}{v v_s}$

[CPMT 2000; KCET (Engg./Med.) 2001]

[IIT-JEE (Screening) 2000]

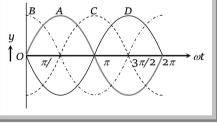
[RPMT 1996; CPMT 2002]

137. Two passenger trains moving with a speed of 108 *km/hour* cross each other. One of them blows a whistle whose frequency is 750 Hz. If sound speed is 330 m/s, then passengers sitting in the other train, after trains cross each other will hear sound whose frequency will be (a) 900 Hz (b) 625 Hz (c) 750 Hz (d) 800 Hz 138. A boy is walking away from a wall towards an observer at a speed of 1 meter/second and blows a whistle whose frequency is 680 Hz. The number of beats heard by the observer per second is (Velocity of sound in air = 340 meters/sec) [MP PMT 1995] (a) Zero (b) 2 (c) 8 (d) 4 Miscellaneous problems **139.** If fundamental frequency of closed pipe is 50 Hz then frequency of 2^{nd} overtone is (a) 100 Hz (c) 250 Hz (b) 50 Hz (d) 150 Hz 140. The phase difference between two waves, represented by $y_1 = 10^{-6} \sin[100t + (x/50) + 0.5]m$ $y_2 = 10^{-6} \cos[100 t + (x / 50)]m$ where x is expressed in meters and t is expressed in seconds, is approximately (a) 1.07 radians (c) 0.5 radians (b) 2.07 radians (d) 1.5 radians **141.** In forced oscillation of a particle the amplitude is maximum for a frequency ω_1 of the force, while the energy is maximum for a frequency ω_2 of the force, then (a) $\omega_1 = \omega_2$ (b) $\omega_1 > \omega^2$ (c) $\omega_1 < \omega_2$ when damping is small and $\omega_1 > \omega_2$ when damping is large (d) $\omega_1 < \omega_2$ 142. A man x can hear only upto 10 kHz and another man y upto 20 kHz. A note of frequency 500 Hz is produced before them from a stretched string. Then (a) Both will hear sounds of same pitch but different quality (b) Both will hear sounds of different pitch but same quality (c) Both will hear sounds of different pitch and different quality (d) Both will hear sounds of same pitch and same quality 143. A light pointer fixed to one prong of a tuning fork touches a vertical plate. The fork is set vibrating and the plate is allowed to fall freely. If eight oscillations are counted when the plate falls through 10 cm, the frequency of the tuning fork is [KCET 2002] (a) 360 Hz (b) 280 Hz (c) 560 Hz (d) 56 Hz 144. Consider the following statements **Assertion** (*A*) : The flash of lightening is seen before the sound of thunder is heard. **Reason** (*R*) : Speed of sound is greater than speed of light Of these statements [AIIMS 2002] (a) Both A and R are true and the R is a correct explanation of the A (b) Both A and R are true but the R is not a correct explanation of the A (c) A is true but the R is false (d) Both A and R are false

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244 Wave Motion (e) A is false but the R is true **145.** Consider the following I. Waves created on the surfaces of a pond water by a vibrating sources. II. Wave created by an oscillating electric field in air. III. Sound waves travelling under water. Which of these can be polarized (a) I and II (b) II only (c) II and III (d) I, II and III 146. An air column in a pipe, which is closed at one end, will be in resonance with a vibrating body of frequency 166 *Hz*, if the length of the air column is (c) 1.00 m (a) 2.00 m (b) 1.50 m (d) 0.50 m 147. An empty vessel is partially filled with water, then the frequency of vibration of air column in the vessel[KCET (Engg./ (a) Remains same (b) Decreases (c) Increases (d) First increases then decreases 148. It is desired to increase the fundamental resonance frequency in a tube which is closed at one end. This can be achieved by [Roorkee 2000] (a) Replacing the air in the tube by hydrogen gas (b) Increasing the length of the tube (c) Decreasing the length of the tube (d) Opening the closed end of the tube 149. Quality of a musical note depends on [KCET (Engg./Med.) 1999; RPET 2000] (a) Harmonics present (b) Amplitude of the wave (c) Fundamental frequency (d) Velocity of sound in the medium 150. A wave is reflected from a rigid support. The change in phase on reflection will be (a) $\pi/4$ (b) $\pi/2$ (c) π (d) 2π

151. The figure shows four progressive waves *A*, *B*, *C*, and *D* with their phases expressed with respect to the wave *A*. It can be concluded from the figure t



- (a) The wave C is ahead by a phase angle of $\pi/2$ and the wave B lags behind by a phase angle of $\pi/2$
- (b) The wave C lags behind by a phase angle of $\pi/2$ and the wave B is ahead by a phase angle of $\pi/2$
- (c) The wave C is ahead by a phase angle of π and the wave B lags behind by a phase angle of π
- (d) The wave *C* lags behind by a phase angle of π and the wave *B* ahead by a phase angle of π
- **152.** Amplitude of a wave is represented by

$$A = \frac{c}{a+b+c}$$

Then resonance will occur when

(a) b = -c/2 (b) b = 0 and a = -c (c) b = -a/2 (d) None of these



${\cal A}$ nswer Sheet (Practice problems)

1. 2. 3. 4. 5. 6. 7. 8. 9. 10. b b d b c a a a b b 11. 12. 13. 14. 15. 16. 17. 18. 19. 20. a b a c c d a b a b b a b a b a b a b a b b c d a b b b b b b b b b b a b b b b b b b b a b b b a b b a b b a b b b b a a b b a b b a a b b b b <										
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a a b b a a b b c a a a b b a a b b c a a a b a d b d b d b c a a a b a d b d b d b a b a a b a d b d b d b a b a a b a d b d b d b a b a a b a d b d d b a b b b b b a b b a b b a b b a b b a b b a b b a b b a b b a b b a b <	а	d	а	d	b	b	с	d	b	d
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b c b a d b d b b b B1. 82. 83. 84. 85. 86. 87. 88. 89. 90. c b d a b c c a b b b b b b c b d a b c c a b b b b b b g1. 92. 93. 94. 95. 96. 97. 98. 99. 100. b c a c a c a c a d b c a c a c a c a d b c a c a a a a a a a b a a a b a b b a a a b a c d b a b	а	a	b	a	d	b	d	b	a	b
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c b d a b c c a b b 91. 92. 93. 94. 95. 96. 97. 98. 99. 100. b c a c a c a c a d b c a c a c a c a d b c a c a c a c a d b c a c a c a c a d d a a a a a b b b a a d a a a a a b b b a a d a a a a a a b b a a d a c d b a c b a a a a c d<	b	с	b	a	d	b	d	b	b	b
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b c a c a c a c a d 101. 102. 103. 104. 105. 106. 107. 108. 109. 110. d a a a a b b b a a d11. 112. 113. 114. 115. 116. 117. 118. 119. 120. a a c d b a c c c c a a c d b a c b a a a a c d b a c b a c c a a c d b a c b a c c b a c d b a c b b a c c b a c d b b a c b b a <th< td=""><td>с</td><td>b</td><td>d</td><td>a</td><td>b</td><td>с</td><td>с</td><td>a</td><td>b</td><td>b</td></th<>	с	b	d	a	b	с	с	a	b	b
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	151.	152.								