

Chapter : 20. VOLUME AND SURFACE AREA OF SOLIDS

Exercise : 20A

Question: 1

Find the volume,

Solution:

(i) We know that,

Volume of cuboid = Length $\times$ Breadth $\times$ Height

$$= (22 \times 12 \times 7.5)$$

$$= 1980 \text{ cm}^3$$

We also know that,

Total Surface Area of cuboid = $2 (lb + bh + hl)$

$$= 2 (22 \times 12) + (22 \times 7.5) + (12 \times 7.5)$$

$$= 2 (264 + 165 + 90)$$

$$= 1038 \text{ cm}^2$$

Now,

Lateral surface area of cuboid = $[2 (l + b) \times h]$

$$= 2 (22 + 12) \times 7.5$$

$$= 510 \text{ cm}^2$$

(ii) We know that,

Volume of cuboid = Length $\times$ Breadth $\times$ Height

$$= (15 \times 6 \times 0.9)$$

$$= 81 \text{ m}^3$$

We also know that,

Total Surface Area of cuboid = $2 (lb + bh + hl)$

$$= 2 (15 \times 6) + (15 \times 0.9) + (6 \times 0.9)$$

$$= 2 (90 + 13.5 + 5.4)$$

$$= 217.8 \text{ m}^2$$

Now,

Lateral surface area of cuboid = $[2 (l + b) \times h]$

$$= 2 (15 + 6) \times 0.9$$

$$= 37.8 \text{ m}^2$$

(iii) We know that,

Volume of cuboid = Length $\times$ Breadth $\times$ Height

$$= (24 \times 0.25 \times 6)$$

$$= 36 \text{ m}^3$$

We also know that,

Total Surface Area of cuboid = $2 (lb + bh + hl)$

$$= 2 (24 \times 0.25) + (24 \times 6) + (0.25 \times 6)$$

$$= 2 (6 + 144 + 1.5)$$

$$= 303 \text{ m}^2$$

Now,

$$\text{Lateral surface area of cuboid} = [2 (l + b) \times h]$$

$$= 2 (24 + 0.25) \times 6$$

$$= 291 \text{ m}^2$$

(iv) We know that,

$$\text{Volume of cuboid} = \text{Length} \times \text{Breadth} \times \text{Height}$$

$$= (0.48 \times 0.6 \times 1)$$

$$= 0.288 \text{ m}^3$$

We also know that,

$$\text{Total Surface Area of cuboid} = 2 (lb + bh + hl)$$

$$= 2 (0.48 \times 0.6) + (0.48 \times 1) + (0.6 \times 1)$$

$$= 2 (0.288 + 0.48 + 0.6)$$

$$= 2.736 \text{ m}^2$$

Now,

$$\text{Lateral surface area of cuboid} = [2 (l + b) \times h]$$

$$= 2 (0.48 + 0.6) \times 1$$

$$= 2.16 \text{ m}^2$$

Question: 2

The dimensions of

Solution:

We know that,

$$1\text{m} = 100 \text{ cm}$$

Therefore,

$$\text{Dimensions of the tank will be: } 2\text{m } 75\text{cm} \times 1\text{m } 80 \text{ cm} \times 1\text{m } 40\text{cm}$$

$$= 275 \text{ cm} \times 180 \text{ cm} \times 140 \text{ cm}$$

We know that,

$$\text{Volume of cuboid} = \text{Length} \times \text{Breadth} \times \text{Height}$$

$$= 275 \times 180 \times 140$$

$$= 6930000 \text{ cm}^3$$

We also know that,

$$1000 \text{ cm}^3 = 1\text{L}$$

Therefore,

$$\text{Volume} = \frac{6930000}{1000}$$

$$= 6930 \text{ Litres}$$

Question: 3

A solid rectangular

Solution:

We know that,

$$1\text{m} = 100\text{cm}$$

Therefore,

Dimensions of the iron piece will be: $105\text{ cm} \times 70\text{ cm} \times 1.5\text{ cm}$

We know that,

Volume of cuboid = Length $\times$ Breadth $\times$ Height

Total volume of the piece of iron = $105 \times 70 \times 1.5$

$$= 11025\text{ cm}^3$$

We also know that,

$$1\text{ cm}^3 = 8\text{ gms}$$

Therefore,

Weight of the piece = 11025×8

$$= 88200\text{ g}$$

$$= \frac{88200}{1000}$$

$$= 88.2\text{ kg}$$

Question: 4

The area of a cou

Solution:

We know that,

$$1\text{cm} = 0.01\text{m}$$

Therefore,

Volume of the gravel used = Area $\times$ Height

$$= 3750 \times 0.01$$

$$= 37.5\text{ m}^3$$

It is given in the question that cost of the gravel is Rs. 6.40 per cubic meter

Therefore,

Total cost of covering = (37.5×6.4)

$$= \text{Rs. } 240$$

Question: 5

How many persons

Solution:

We know that,

Volume of cuboid = Length $\times$ Breadth $\times$ Height

Therefore,

Total volume of hall = $16 \times 12.5 \times 4.5$

$$= 900\text{ m}^3$$

It is given in the question that 3.6 m^3 of air is required for each person

Therefore,

$$\begin{aligned}\text{Total number of persons that can be accommodated in the hall} &= \frac{\text{Total volume}}{\text{Volume required by each person}} \\ &= \frac{900}{3.6}\end{aligned}$$

$$= 250 \text{ people}$$

Question: 6

A cardboard box i

Solution:

We know that,

$$\text{Volume of cuboid} = \text{Length} \times \text{Breadth} \times \text{Height}$$

Firstly, we have to find out volume of cardboard box

$$\text{Volume of cardboard box} = 120 \times 72 \times 54$$

$$= 466560 \text{ cm}^3$$

Now,

$$\text{Volume of each bar of soap} = 6 \times 4.5 \times 4$$

$$= 108 \text{ cm}^3$$

Therefore,

$$\begin{aligned}\text{Total number of bars of soap that can be accommodated in that box} &= \frac{\text{Volume of the box}}{\text{Volume of each soap}} \\ &= \frac{466560}{108}\end{aligned}$$

$$= 4320 \text{ bars}$$

Question: 7

The size of a mat

Solution:

We know that,

$$\text{Volume of cuboid} = \text{Length} \times \text{Breadth} \times \text{Height}$$

Firstly, we have to find out volume occupied by a single matchbox

$$\text{Volume occupied by a single matchbox} = (4 \times 2.5 \times 1.5)$$

$$= 15 \text{ cm}^3$$

Now,

$$\text{Volume of a packet containing 144 matchboxes} = (15 \times 144)$$

$$= 2160 \text{ cm}^3$$

Also,

$$\text{Volume of carton} = (150 \times 84 \times 60)$$

$$= 756000 \text{ cm}^3$$

Therefore,

$$\text{Total number of packets that can be placed in a carton} = \frac{\text{Volume of the carton}}{\text{Volume of a packet}}$$

$$= \frac{75600}{2160}$$

= 350 packets

Question: 8

How many planks o

Solution:

We know that,

Volume of cuboid = Length $\times$ Breadth $\times$ Height

Therefore,

Total volume of the block = (500 $\times$ 70 $\times$ 32)

= 1120000 cm³

Total volume of each plank = 200 $\times$ 25 $\times$ 8

= 40000 cm³

Hence,

Total number of planks that can be made = $\frac{\text{Total volume of the block}}{\text{Volume of each plank}}$

$$= \frac{1120000}{40000}$$

= 28 planks

Question: 9

How many bricks,

Solution:

We know that,

Volume of cuboid = Length $\times$ Breadth $\times$ Height

Firstly,

Volume of the brick = 25 $\times$ 13.5 $\times$ 6

= 2025 cm³

Now,

Volume of the wall = 800 $\times$ 540 $\times$ 33

= 14256000 cm³

Hence,

Total number of bricks required = $\frac{\text{Volume of the wall}}{\text{Volume of each brick}}$

$$= \frac{14256000}{2025}$$

= 7040 bricks

Question: 10

A wall 15 m long,

Solution:

We know that,

Volume of cuboid = Length $\times$ Breadth $\times$ Height

Therefore,

$$\text{Volume of the wall} = 1500 \times 30 \times 400$$

$$= 18000000 \text{ cm}^3$$

$$\text{Total quantity of mortar} = \frac{1}{12} \times 18000000$$

$$= 1500000 \text{ cm}^3$$

Therefore,

$$\text{Volume of bricks} = 18000000 - 1500000$$

$$= 16500000 \text{ cm}^3$$

Now,

$$\text{Volume of a single brick} = 22 \times 12.56 \times 7.5$$

$$= 2062.5 \text{ cm}^3$$

Therefore,

$$\text{Total number of bricks} = \frac{\text{Total volume of the bricks}}{\text{Volume of a single brick}}$$

$$= \frac{16500000}{2062.5}$$

$$= 8000 \text{ bricks}$$

Question: 11

Find the capacity

Solution:

We know that,

$$\text{Volume of cuboid} = \text{Length} \times \text{Breadth} \times \text{Height}$$

Therefore,

$$\text{Volume of the cistern} = 11.2 \times 6 \times 5.8$$

$$= 389.76 \text{ m}^3$$

$$= 389.76 \times 1000$$

$$= 389760 \text{ litres}$$

Now,

$$\text{Area of iron sheet that is required to make the cistern} = \text{Total surface area of the cistern}$$

We also know that,

$$\text{Total Surface Area of cuboid} = 2 (lb + bh + hl)$$

$$= 2 (11.2 \times 6 + 11.2 \times 5.8 + 6 \times 5.8)$$

$$= 2 (67.2 + 64.96 + 34.8)$$

$$= 333.92 \text{ cm}^2$$

Question: 12

The volume of a b

Solution:

It is given that,

$$\text{Volume of the block} = 0.5 \text{ m}^3$$

We know that,

$$1 \text{ hectare} = 10000 \text{ m}^2$$

Therefore,

$$\text{Thickness of the sheet} = \text{volume/area}$$

$$= 0.5/10000$$

$$= 0.00005 \text{ m}$$

$$= 0.005 \text{ cm}$$

$$= 0.05 \text{ mm}$$

Question: 13

The rainfall reco

Solution:

It is given that,

$$\text{Rain recorded in a certain day} = 5 \text{ cm} = 0.05 \text{ m}$$

$$\text{Area of the field} = 2 \text{ hectare}$$

$$= 2 \times 10000 \text{ m}^2$$

$$= 20000 \text{ m}^2$$

Therefore,

$$\text{Total rain over the field} = \text{Area of the field} \times \text{Height of the field}$$

$$= 0.05 \times 20000$$

$$= 1000 \text{ m}^3$$

Question: 14

A river 2 m deep

Solution:

It is given in the question that,

$$\text{Area of cross section of river} = 45 \text{ m} \times 2 \text{ m} = 90 \text{ m}^2$$

$$\text{Rate of flow} = 3 \text{ km/hr}$$

$$= \frac{3 \times (1000 \text{ m})}{(60 \text{ m})}$$

$$= 50 \text{ m/min}$$

Therefore,

$$\text{Volume of water flowing through the cross-section in one minute} = 90 \text{ m}^2 \times 50 \text{ m/min}$$

$$= 4500 \text{ m}^3 \text{ per minute}$$

Question: 15

A pit 5 m long an

Solution:

We know that,

$$\text{Volume of cuboid} = \text{Length} \times \text{Breadth} \times \text{Height}$$

Let the depth of the pit be x m

Therefore,

$$\text{Volume} = 5 \times 3.5 \times x$$

It is given in the question that,

$$\text{Volume} = 14 \text{ m}^3$$

Therefore,

$$\text{Depth, } x = \frac{\text{Volume}}{\text{Length} \times \text{Width}}$$

$$x = \frac{14}{5 \times 3.5}$$

$$= 0.8 \text{ m}$$

$$= 80 \text{ cm}$$

Question: 16

A rectangular wat

Solution:

It is given that,

$$\text{Capacity of the water tank} = 576 \text{ Litres} = 0.576 \text{ m}^3$$

$$\text{Width} = 90 \text{ cm} = 0.9 \text{ m}$$

$$\text{Depth} = 40 \text{ cm} = 0.4 \text{ m}$$

Therefore,

$$\text{Length} = \frac{\text{Capacity}}{\text{Width} \times \text{Depth}}$$

$$= \frac{0.576}{0.9 \times 0.4}$$

$$= 1.600 \text{ m}$$

Question: 17

A beam of wood is

Solution:

It is given in the question that,

$$\text{Volume of the beam} = 1.35 \text{ m}^3$$

$$\text{Length} = 5 \text{ m}$$

$$\text{Thickness} = 36 \text{ cm} = 0.36 \text{ m}$$

We know that,

$$\text{Volume of cuboid} = \text{Length} \times \text{Breadth} \times \text{Height}$$

Therefore,

$$\text{Width} = \frac{\text{Volume}}{\text{Thickness} \times \text{Length}}$$

$$= \frac{1.35}{5 \times 0.36}$$

$$= 0.75 \text{ m}$$

$$= 75 \text{ cm}$$

Question: 18

The volume of a r

Solution:

We know that,

$$\text{Volume} = \text{Height} \times \text{Area}$$

Given that,

$$\text{Volume} = 378 \text{ m}^3$$

$$\text{Area} = 84 \text{ m}^2$$

Therefore,

$$\text{Height} = \frac{\text{Volume}}{\text{Area}}$$

$$= \frac{378}{84}$$

$$= 4.5 \text{ m}$$

Question: 19

A swimming pool i

Solution:

It is given in the question that,

$$\text{Length of the pool} = 260 \text{ m}$$

$$\text{Width of the pool} = 140 \text{ m}$$

Also,

$$\text{Volume of water in the pool} = 54600 \text{ cubic metres}$$

Therefore,

$$\text{Height of water} = \frac{\text{Volume}}{\text{Length} \times \text{Width}}$$

$$= \frac{54600}{200 \times 140}$$

$$= 1.5 \text{ metres}$$

Question: 20

Find the volume o

Solution:

Given that,

$$\text{External length} = 60 \text{ cm}$$

$$\text{External width} = 45 \text{ cm}$$

$$\text{External height} = 32 \text{ cm}$$

We know that,

$$\text{Volume of cuboid} = \text{Length} \times \text{Breadth} \times \text{Height}$$

Therefore,

$$\text{External volume of the box} = 60 \times 45 \times 32$$

$$= 86400 \text{ cm}^3$$

It is also given that,

$$\text{Thickness of the wood} = 2.5 \text{ cm}$$

Therefore,

$$\text{Internal length} = 60 - (2.5 \times 2) = 55 \text{ cm}$$

$$\text{Internal width} = 45 - (2.5 \times 2) = 40 \text{ cm}$$

$$\text{Internal height} = 32 - (2.5 \times 2) = 27 \text{ cm}$$

As we know that,

$$\text{Volume of cuboid} = \text{Length} \times \text{Breadth} \times \text{Height}$$

Therefore,

$$\text{Internal volume of the box} = 55 \times 40 \times 27$$

$$= 59400 \text{ cm}^3$$

Hence,

$$\text{Volume of wood} = \text{External volume} - \text{Internal volume}$$

$$= 86400 - 59400$$

$$= 27000 \text{ cm}^3$$

Question: 21

Find the volume of

Solution:

Given that,

$$\text{External length} = 36 \text{ cm}$$

$$\text{External width} = 25 \text{ cm}$$

$$\text{External height} = 16.5 \text{ cm}$$

We know that,

$$\text{Volume of cuboid} = \text{Length} \times \text{Breadth} \times \text{Height}$$

Therefore,

$$\text{External volume of the box} = 36 \times 25 \times 16.5$$

$$= 14850 \text{ cm}^3$$

It is also given that,

$$\text{Thickness of iron} = 1.5 \text{ cm}$$

Therefore,

$$\text{Internal length} = 36 - (1.5 \times 2) = 33 \text{ cm}$$

$$\text{Internal width} = 25 - (1.5 \times 2) = 22 \text{ cm}$$

$$\text{Internal height} = 16.5 - 1.5 = 15 \text{ cm (As the box is open)}$$

As we know that,

$$\text{Volume of cuboid} = \text{Length} \times \text{Breadth} \times \text{Height}$$

Therefore,

$$\text{Internal volume of the box} = 33 \times 22 \times 15$$

$$= 10890 \text{ cm}^3$$

Hence,

$$\text{Volume of iron} = \text{External volume} - \text{Internal volume}$$

$$= 14850 - 10890$$

$$= 3960 \text{ cm}^3$$

Also given that,

$$1 \text{ cm}^3 \text{ of iron} = 8.5 \text{ grams}$$

Therefore,

$$\text{Total weight of the box} = 3960 \times 8.5$$

$$= 33660 \text{ grams}$$

$$= 33.66 \text{ kilograms}$$

Question: 22

A box with a lid

Solution:

Given that,

$$\text{External length} = 56 \text{ cm}$$

$$\text{External width} = 39 \text{ cm}$$

$$\text{External height} = 30 \text{ cm}$$

We know that,

$$\text{Volume of cuboid} = \text{Length} \times \text{Breadth} \times \text{Height}$$

Therefore,

$$\text{External volume of the box} = 56 \times 39 \times 30$$

$$= 65520 \text{ cm}^3$$

It is also given that,

$$\text{Thickness of the wood} = 3 \text{ cm}$$

Therefore,

$$\text{Internal length} = 56 - (3 \times 2) = 50 \text{ cm}$$

$$\text{Internal width} = 39 - (3 \times 2) = 33 \text{ cm}$$

$$\text{Internal height} = 30 - (3 \times 2) = 24 \text{ cm}$$

As we know that,

$$\text{Volume of cuboid} = \text{Length} \times \text{Breadth} \times \text{Height}$$

Therefore,

$$\text{Capacity of box} = \text{Internal volume of the box} = 50 \times 33 \times 24$$

$$= 39600 \text{ cm}^3$$

Hence,

$$\text{Volume of wood} = \text{External volume} - \text{Internal volume}$$

$$= 65520 - 39600$$

$$= 25920 \text{ cm}^3$$

Question: 23

The external dimensions

Solution:

Given that,

$$\text{External length} = 62 \text{ cm}$$

$$\text{External width} = 30 \text{ cm}$$

$$\text{External height} = 18 \text{ cm}$$

We know that,

$$\text{Volume of cuboid} = \text{Length} \times \text{Breadth} \times \text{Height}$$

Therefore,

$$\text{External volume of the box} = 62 \times 30 \times 18$$

$$= 33480 \text{ cm}^3$$

It is also given that,

$$\text{Thickness of the wood} = 2 \text{ cm}$$

Therefore,

$$\text{Internal length} = 62 - (2 \times 2) = 58 \text{ cm}$$

$$\text{Internal width} = 30 - (2 \times 2) = 26 \text{ cm}$$

$$\text{Internal height} = 18 - (2 \times 2) = 14 \text{ cm}$$

As we know that,

$$\text{Volume of cuboid} = \text{Length} \times \text{Breadth} \times \text{Height}$$

Therefore,

$$\text{Capacity of box} = \text{Internal volume of the box} = 58 \times 26 \times 14$$

$$= 21112 \text{ cm}^3$$

Question: 24

A closed wooden b

Solution:

Given that,

$$\text{External length} = 80 \text{ cm}$$

$$\text{External width} = 65 \text{ cm}$$

$$\text{External height} = 45 \text{ cm}$$

We know that,

$$\text{Volume of cuboid} = \text{Length} \times \text{Breadth} \times \text{Height}$$

Therefore,

$$\text{External volume of the box} = 80 \times 65 \times 45$$

$$= 234000 \text{ cm}^3$$

It is also given that,

$$\text{Thickness of the wood} = 2.5 \text{ cm}$$

Therefore,

$$\text{Internal length} = 80 - (2.5 \times 2) = 75 \text{ cm}$$

$$\text{Internal width} = 65 - (2.5 \times 2) = 60 \text{ cm}$$

$$\text{Internal height} = 45 - (2.5 \times 2) = 40 \text{ cm}$$

As we know that,

$$\text{Volume of cuboid} = \text{Length} \times \text{Breadth} \times \text{Height}$$

Therefore,

$$\text{Capacity of box} = \text{Internal volume of the box} = 75 \times 60 \times 40$$

$$= 180000 \text{ cm}^3$$

Hence,

Volume of wood = External volume - Internal volume

$$= 234000 - 180000$$

$$= 54000 \text{ cm}^3$$

It is also given that,

100 cm³ of wood weighs 8 g

Therefore,

$$\text{Weight of wood} = \frac{54000}{100} \times 8$$

$$= 4320 \text{ g}$$

$$= 4.32 \text{ kg}$$

Question: 25

Find the volume,

Solution:

(i) We have,

Length of the edge of the cube = a = 7 cm

We know that,

$$\text{Volume of cube} = a^3 = 7^3 = 343 \text{ m}^3$$

Also,

$$\text{Lateral surface area of the cube} = 4a^2$$

$$= 4 \times 7 \times 7$$

$$= 196 \text{ m}^2$$

$$\text{Total surface area of the cube} = 6a^2$$

$$= 6 \times 7 \times 7$$

$$= 294 \text{ m}^2$$

(ii) We have,

Length of the edge of the cube = a = 5.6 cm

We know that,

$$\text{Volume of cube} = a^3 = (5.6)^3 = 175.616 \text{ cm}^3$$

Also,

$$\text{Lateral surface area of the cube} = 4a^2$$

$$= 4 \times 5.6 \times 5.6$$

$$= 125.44 \text{ cm}^2$$

$$\text{Total surface area of the cube} = 6a^2$$

$$= 6 \times 5.6 \times 5.6$$

$$= 188.16 \text{ cm}^2$$

(iii) We have,

Length of the edge of the cube = a = 8 dm 5 cm = 85 cm

We know that,

$$\text{Volume of cube} = a^3 = 85^3 = 614125 \text{ cm}^3$$

Also,

$$\text{Lateral surface area of the cube} = 4a^2$$

$$= 4 \times 85 \times 85$$

$$= 28900 \text{ cm}^2$$

$$\text{Total surface area of the cube} = 6a^2$$

$$= 6 \times 85 \times 85$$

$$= 43350 \text{ cm}^2$$

Question: 26

The surface area

Solution:

Let us assume the edge of the cube be a

We know that,

$$\text{Total surface area of the cube} = 6a^2$$

$$6a^2 = 1176 \text{ cm}^2$$

$$a = \sqrt{\frac{1176}{6}}$$

$$a = \sqrt{196}$$

$$a = 14 \text{ cm}$$

We also know that,

$$\text{Volume of the cube} = a^3 = (14)^3$$

$$= 2744 \text{ cm}^3$$

Question: 27

The volume of a c

Solution:

Let us assume the edge of the cube be a

We know that,

$$\text{Volume of the cube} = a^3$$

$$a^3 = 729 \text{ cm}^3$$

$$a = \sqrt[3]{729}$$

$$a = 9 \text{ cm}$$

We also know that,

$$\text{Total surface area of cube} = 6a^2$$

$$= 6 \times 9 \times 9$$

$$= 486 \text{ cm}^2$$

Question: 28

The dimensions of

Solution:

We know that,

$$1 \text{ m} = 100 \text{ cm}$$

Also,

$$\text{Volume of a cuboid} = \text{Length} \times \text{Breadth} \times \text{Height}$$

Therefore,

$$\text{Volume of the original block} = 225 \times 150 \times 27$$

$$= 911250 \text{ cm}^3$$

Given that,

$$\text{Length of the edge of the cube} = 45 \text{ cm}$$

Therefore,

$$\text{Volume of one cube} = a^3 = (45)^3$$

$$= 91125 \text{ cm}^3$$

Hence,

$$\text{Total number of blocks that can be cast} = \frac{\text{Volume of the block}}{\text{Volume of the cube}}$$

$$= \frac{911250}{91125}$$

$$= 10$$

Question: 29

If the length of

Solution:

Let us assume a be the length of the edge of the cube

We know that,

$$\text{Volume of cube} = a^3$$

Also,

$$\text{Total surface area of the cube} = 6a^2$$

Now, if the length is doubled, then the new length becomes $2a$

Now,

$$\text{New volume} = (2a)^3 = 8a^3$$

Also,

$$\text{New surface area} = 6(2a)^2 = 24a^2$$

Therefore,

The total volume of the cube is increased by the factor of 8 whereas the surface area is increased by the factor of 4.

Question: 30

A solid cubical b

Solution:

It is given that,

Cost of wood = Rs. 500/m³

Also,

Cost of the given block = Rs 256

We know that,

Volume of cube = a³

Therefore,

Volume of the given block = a³ = $\frac{256}{500}$

= 0.512 m³

= 512000 cm³

Also,

Length of its edge = a = $\sqrt[3]{0.512}$

= 0.8 m

= 80 cm

Exercise : 20B

Question: 1

Find the volume,

Solution:

(i) At first,

In order to find volume, we will use the following formula:

Volume of a cylinder = $\pi r^2 h$

Where,

'r' = radius of the base

'h' = height of the cylinder

Hence,

Volume of the cylinder = $\pi(7)^2(50)$

= $\frac{22}{7} \times 7 \times 7 \times 50$

= 22 × 7 × 50

= 7700 cm³

Now,

In order to find curved surface area, we will use the following formula:

Curved surface area of cylinder = $2\pi rh$

Where,

'r' = radius of the base

'h' = height of the cylinder

Hence,

Curved surface area of cylinde

$$\begin{aligned}
 r &= 2\pi rh \\
 &= 2 \times \frac{22}{7} \times 7 \times 50 \\
 &= 22 \times 2 \times 50 \\
 &= 2200 \text{ cm}^2
 \end{aligned}$$

Now,

In order to find the total surface area we will use the following formula:

$$\text{Total surface area of cylinder} = 2\pi r(r + h)$$

Where,

'r' = radius of the base

'h' = height of the cylinder

Hence,

$$\begin{aligned}
 \text{Total surface area of cylinder} &= 2\pi r(r + h) \\
 &= 2 \times \frac{22}{7} \times 7(7 + 50) \\
 &= 22 \times 2 \times 57 \\
 &= 2508 \text{ cm}^2
 \end{aligned}$$

(ii) At first,

In order to find volume we will use the following formula:

$$\text{Volume of a cylinder} = \pi r^2 h$$

Where,

'r' = radius of the base

'h' = height of the cylinder

Hence,

$$\begin{aligned}
 \text{Volume of the cylinder} &= \pi(5.6)^2(1.25) \\
 &= \frac{22}{7} \times 5.6 \times 5.6 \times 1.25 \\
 &= 22 \times 0.8 \times 7 \times 50 \\
 &= 123.2 \text{ cm}^3
 \end{aligned}$$

Now,

In order to find curved surface area we will use the following formula:

$$\text{Curved surface area of cylinder} = 2\pi rh$$

Where,

'r' = radius of the base

'h' = height of the cylinder

Hence,

$$\begin{aligned}
 \text{Curved surface area of cylinder} &= 2\pi rh \\
 &= 2 \times \frac{22}{7} \times 5.6 \times 1.25 \\
 &= 22 \times 2 \times 0.8 \times 1.25
 \end{aligned}$$

$$= 44 \text{ cm}^2$$

Now,

In order to find the total surface area we will use the following formula:

$$\text{Total surface area of cylinder} = 2\pi r(r + h)$$

Where,

'r' = radius of the base

'h' = height of the cylinder

Hence,

$$\text{Total surface area of cylinder} = 2\pi r(r + h)$$

$$= 2 \times \frac{22}{7} \times 5.6(5.6 + 1.25)$$

$$= 22 \times 2 \times 0.8 \times 6.85$$

$$= 241.12 \text{ cm}^2$$

(iii) At first,

We will convert the radius into metre

$$\text{Radius} = 14\text{dm} = 1.4\text{m}$$

Now,

In order to find volume we will use the following formula:

$$\text{Volume of a cylinder} = \pi r^2 h$$

Where,

'r' = radius of the base

'h' = height of the cylinder

Hence,

$$\text{Volume of the cylinder} = \pi(7)^2(50)$$

$$= \frac{22}{7} \times 1.4 \times 1.4 \times 15$$

$$= 22 \times 0.2 \times 1.4 \times 1.5$$

$$= 92.4\text{cm}^3$$

Now,

In order to find curved surface area we will use the following formula:

$$\text{Curved surface area of cylinder} = 2\pi rh$$

Where,

'r' = radius of the base

'h' = height of the cylinder

Hence,

$$\text{Curved surface area of cylinder} = 2\pi rh$$

$$= 2 \times \frac{22}{7} \times 1.4 \times 1.5$$

$$= 22 \times 2 \times 0.2 \times 1.5$$

$$= 132\text{cm}^2$$

Now,

In order to find the total surface area we will use the following formula:

$$\text{Total surface area of cylinder} = 2\pi r(r + h)$$

Where,

'r' = radius of the base

'h' = height of the cylinder

Hence,

$$\text{Total surface area of cylinder} = 2\pi r(r + h)$$

$$= 2 \times \frac{22}{7} \times 1.4(1.4 + 1.5)$$

$$= 22 \times 2 \times 0.2 \times 2.9$$

$$= 144.32 \text{ cm}^2$$

Question: 2

A milk tank is in

Solution:

It is given in the question that,

Radius of the cylindrical milk tank (r) = 1.5m

Height of the cylindrical milk tank (h) = 10.5m

Now,

In order to find the capacity of the tank we'll find the volume of the milk tank

Hence,

$$\text{Volume of the cylindrical milk tank} = \pi r^2 h$$

$$= \pi (1.5)^2 (10.5)$$

$$= \frac{22}{7} \times 1.5 \times 1.5 \times 10.5$$

$$= 74.25 \text{ m}^3$$

Now,

We know that,

$$1 \text{ m}^3 = 1000 \text{ L}$$

$$\therefore 74.25 \text{ m}^3 = 74250 \text{ L}$$

Question: 3

A wooden cylinder

Solution:

It is given in the question that,

Radius of the cylindrical pole (r) = 10cm = 0.1m

Height of the cylindrical pole (h) = 7m

Now,

$$\text{Volume of the cylindrical wooden pole} = \pi r^2 h$$

$$= \pi (0.1)^2 (7)$$

$$= \frac{22}{7} \times 0.1 \times 0.1 \times 7$$

$$= 0.22 \text{ cm}^3$$

Now,

We know that,

$$\text{Weight of the wood} = 225 \text{ kg/m}^3$$

$$\therefore \text{Weight of the pole} = 0.22 \times 225$$

$$= 49.5 \text{ kg}$$

Question: 4

Find the height o

Solution:

It is given in the question that,

$$\text{Volume of cylinder} = 1.54 \text{ m}^3$$

$$\text{Diameter of the base} = 140 \text{ cm} = 1.4 \text{ m}$$

Hence,

$$\text{Radius of the base} = \frac{1.4}{2}$$

$$= 0.7 \text{ m}$$

Now,

$$\text{Volume of cuboid} = \pi r^2 h$$

$$1.54 = \pi (0.7)^2 (h)$$

$$1.54 = \frac{22}{7} \times 0.7 \times 0.7 \times h$$

$$h = 1 \text{ m}$$

Hence, height of the cuboid = 1 m

Question: 5

The volume of a c

Solution:

It is given in the question that,

$$\text{Volume of cylindrical rod} = 3850 \text{ cm}^3$$

$$\text{Height of the rod} = 1 \text{ m} = 100 \text{ cm}$$

Now,

In order to find the diameter of the rod we need to find the radius of the rod

Hence,

$$\text{Volume of cuboid} = \pi r^2 h$$

$$3850 = \pi (r)^2 (100)$$

$$3850 = \frac{22}{7} \times r^2 \times 100$$

$$r^2 = \frac{3850 \times 7}{100 \times 22}$$

$$r = 1.75 \times 7$$

$$r = 3.5 \text{ cm}$$

Hence,

$$\text{Diameter} = 2(\text{radius})$$

$$= 2 \times 3.5$$

$$= 7 \text{ cm}$$

Question: 6

A closed cylindri

Solution:

It is given in the question that,

$$\text{Diameter of the cylindrical tank} = 14 \text{ m}$$

$$\text{Radius of the cylindrical tank} = \frac{14}{2}$$

$$= 7 \text{ m}$$

$$\text{Height of the cylindrical tank} = 5 \text{ m}$$

Now,

In order to find the total area of the metal sheet required we need to find the total surface area of the tank.

Hence,

$$\text{Total surface area of the cylindrical tank} = 2\pi r(h + r)$$

$$= 2 \times \frac{22}{7} \times 7(5 + 7)$$

$$= 44 \times 12$$

$$= 528 \text{ m}^2$$

Question: 7

The circumference

Solution:

It is given in the question that,

$$\text{Circumference of the base of the cylinder} = 88 \text{ cm}$$

$$\text{Height of the cylinder} = 60 \text{ cm}$$

Hence,

$$\text{Curved surface area} = \text{Circumference} \times \text{height}$$

$$= 88 \times 60$$

$$= 5280 \text{ cm}^2$$

Now,

$$\text{The circumference of the base} = 2\pi r = 88 \text{ cm}$$

Hence,

$$\text{The radius of the base}(r) = \frac{88}{2\pi}$$

$$= \frac{88 \times 7}{2 \times 22}$$

$$= 14 \text{ cm}$$

Hence,

We can find the volume as follows:

$$\text{Volume of the cylinder} = \pi r^2 h$$

$$= \frac{22}{7} \times (14)^2 \times 60$$

$$= 22 \times 2 \times 14 \times 60$$

$$= 36960 \text{ cm}^3$$

Question: 8

The lateral surfa

Solution:

In the question it is given that

$$\text{Length of the cylinder} = 14 \text{ m}$$

Which means,

$$\text{That the height of the cylinder} = 14 \text{ m}$$

$$\text{Lateral surface area of the cylinder} = 2\pi rh$$

$$220 = 2 \times \frac{22}{7} \times r \times 14$$

$$r = \frac{10}{4}$$

$$r = 2.5 \text{ m}$$

Hence,

We can find the volume as,

$$\text{Volume of the cylinder} = \pi r^2 h$$

$$= \frac{22}{7} \times (2.5)^2 \times 14$$

$$= 22 \times 2 \times 2.5 \times 2.5$$

$$= 275 \text{ m}^3$$

Question: 9

The volume of a c

Solution:

It is given in the question that,

$$\text{Height of the cylinder} = 8 \text{ cm}$$

And,

$$\text{Volume of the cylinder} = \pi r^2 h = 1232 \text{ cm}^3$$

Hence,

We can find the radius as,

$$r = \sqrt{\frac{1232}{\pi h}}$$

$$r = \sqrt{\frac{1232 \times 7}{22 \times 8}}$$

$$r = \sqrt{49}$$

$$r = 7 \text{ cm}$$

Now,

$$\text{Curved surface area of the cylinder} = 2\pi rh$$

$$= 2 \times \frac{22}{7} \times 7 \times 8$$

$$= 252 \text{ cm}^2$$

Therefore,

$$\text{The total surface area of the cylinder} = 2\pi r(r + h)$$

$$= 2 \times \frac{22}{7} \times 7 \times 15$$

$$= 2 \times 22 \times 15$$

$$= 660 \text{ cm}^2$$

Question: 10

The radius and height

Solution:

It is given in the question that,

The ratio of radius and height is 7 : 2

This means that,

$$\frac{\text{radius}}{\text{height}} = \frac{7}{2}$$

$$\frac{r}{h} = \frac{7}{2}$$

$$r = \frac{7}{2}h$$

Now,

We can find the volume of the cylinder as:

$$\text{Volume of the cylinder} = \pi r^2 h$$

$$8316 = \pi \left(\frac{7}{2}h \right)^2 h$$

$$8316 = \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2} \times h^3$$

$$h^3 = \frac{8316 \times 2}{11 \times 7}$$

$$h^3 = 216$$

$$h = 6$$

Hence,

$$\text{Radius, } r = \frac{7}{2}h$$

$$= \frac{7}{2} \times 6$$

$$= 21 \text{ cm}$$

Therefore,

$$\text{Total surface area of the cylinder} = 2\pi r(r + h)$$

$$= 2 \times \frac{22}{7} \times 21 \times 27$$

$$= 2 \times 22 \times 3 \times 27$$

$$= 3564 \text{ cm}^2$$

Question: 11

The curved surface

Solution:

In the above question it is given that

$$\text{Curved surface area of the cylinder} = 2\pi rh = 4400 \text{ cm}^2$$

And,

$$\text{The circumference of the base of the cylinder} = 2\pi r = 110 \text{ cm}$$

Now,

$$\text{The height of the cylinder} = h = \frac{\text{curved surface area}}{\text{circumference}}$$

$$= \frac{4400}{110}$$

$$= 40 \text{ cm}$$

Also,

$$\text{Radius of the cylinder} = r = \frac{4400}{2\pi h}$$

$$= \frac{4400 \times 7}{2 \times 22 \times 40}$$

$$= \frac{35}{2}$$

Hence,

We can find the volume of the cylinder as:

$$\text{Volume of the cylinder} = \pi r^2 h$$

$$= \frac{22}{7} \times \frac{35}{2} \times \frac{35}{2} \times 40$$

$$= 38500 \text{ cm}^3$$

Question: 12

A particular bran

Solution:

In the above given question,

In order to find the greater capacity pack

At first, we'll calculate the volume of the cubic pack,

Length of the side of pack, $a = 5 \text{ cm}$

Height of the pack, $h = 14 \text{ cm}$

Hence,

$$\text{Volume of the pack} = a^2 h$$

$$= (5)^2 (14)$$

$$= 5 \times 5 \times 14$$

$$= 350 \text{ cm}^3$$

Now,

We'll calculate the volume of the cylindrical pack,

Radius of the base, $r = 35\text{cm}$

Height of the cylinder, $h = 12\text{ cm}$

Hence,

Volume of the pack = $\pi r^2 h$

$$= \frac{22}{7} \times 35 \times 35 \times 12$$

$$= 22 \times 5 \times 35 \times 12$$

$$= 462\text{ cm}^3$$

Hence,

It's clear that the pack with the circular has a greater capacity than the than the pack with square base.

And,

The deference between their volume = $462 - 350$

$$= 112\text{ cm}^3$$

Question: 13

Find the cost of

Solution:

It is given in the question that,

Diameter of the cylindrical pillars = 48 cm

Hence,

The radius of the cylindrical pillars = $\frac{48}{2}$

$$= 24\text{ cm}$$

$$= 0.24\text{ m}$$

Height of the cylindrical pillars = 7 m

Now,

Lateral surface area of one pillar = πdh

$$= \frac{22}{7} \times 0.48 \times 7$$

$$= 10.56\text{ m}^2$$

Now,

The surface area to be painted = total surface area of 15 pillars

$$= 15 \times 10.56$$

$$= 158.4\text{ m}^2$$

Therefore,

The total cost of painting = $\text{Rs}(158.4 \times 2.5)$

$$= \text{Rs } 396$$

Question: 14

A rectangular ves

Solution:

It can be concluded from the question that,

$$\text{Volume of the rectangular vessel} = 22 \times 16 \times 14$$

$$= 4928 \text{ cm}^3$$

$$\text{Radius of the cylindrical vessel} = 4\text{cm}$$

$$\text{Volume of the cylindrical vessel} = \pi r^2 h$$

Now,

Since, the water is poured from the rectangular vessel to a cylindrical vessel

Therefore, the volume of the water will remain same.

Hence,

$$\text{Volume of the cylindrical vessel} = \text{volume of rectangular vessel}$$

$$\pi r^2 h = 4928$$

$$\frac{22}{7} \times 4 \times 4 \times \text{height} = 4928$$

$$\text{Height} = 24.5$$

Question: 15

A piece of ductil

Solution:

It is given in the question that,

$$\text{Diameter of the wire} = 1\text{cm}$$

Hence,

$$\text{Radius of the wire} = 0.5 \text{ cm}$$

$$\text{Length or the height of the wire} = 11 \text{ cm}$$

Hence,

$$\text{The volume of the wire} = \pi r^2 h$$

$$= \frac{22}{7} \times 0.5 \times 0.5 \times 11$$

$$= 8.643 \text{ cm}^3$$

Now,

We know that,

The volumes of both the cylinders would be the same.

And,

$$\text{Diameter of the new wire} = 1\text{mm} = 0.1 \text{ cm}$$

$$\text{Radius} = 0.05\text{cm}$$

$$\text{Therefore the new length of the wire would be} = \frac{\text{volume}}{\pi r^2}$$

$$= \frac{8.643 \times 7}{22 \times 0.05 \times 0.05}$$

$$= 1100.02 \text{ cm}$$

$$= 11 \text{ m}$$

Question: 16

A solid cube of m

Solution:

It is given in the question that

Length of the edge, $a = 2.2 \text{ cm}$

Hence,

Volume of the cube $= a^3$

$$= (2.2)^3$$

$$= 10.648 \text{ cm}^3$$

Now,

Volume of the wire $= \pi r^2 h$

Radius of the wire $= 1 \text{ mm} = 0.1 \text{ cm}$

We know that,

Volume of the cube $=$ volume of the wire

Hence,

$$\text{Length of the wire} = \frac{\text{volume}}{\pi r^2}$$

$$= \frac{10.648 \times 7}{22 \times 0.1 \times 0.1}$$

$$= 338.8 \text{ cm}$$

Question: 17

How many cubic me

Solution:

It is given in the question that,

Diameter $= 7 \text{ m}$

Hence,

Radius $= 3.5 \text{ m}$

Depth $= 20 \text{ m}$

Volume of the earth to be dug out $= \pi r^2 h$

$$= \frac{22}{7} \times 3.5 \times 3.5 \times 20$$

$$= 770 \text{ m}^3$$

Volume of the earth piled upon the given plot $= 28 \times 11 \times h$

Therefore,

$$\text{Height} = \frac{770}{28 \times 11}$$

$$= \frac{70}{28}$$

$$= 2.5 \text{ m}$$

Question: 18

A well of inner d

Solution:

Given that,

Inner diameter = 14 cm

Therefore,

Radius = 7 cm

Also, Depth = 12 m

Therefore,

Volume of earth dug out = $\pi r^2 h$

$$= \frac{22}{7} \times 7 \times 7 \times 12$$

$$= 1848 \text{ m}^3$$

It is also given that,

Width of embankment = 7 m

Therefore,

Total radius = 7 + 7 = 14 m

Volume of embankment = Total volume - Inner volume

$$= \pi r_o^2 h - \pi r_1^2 h$$

$$= \pi h (r_o^2 - r_1^2)$$

$$= \frac{22}{7} h (14^2 - 7^2)$$

$$= \frac{22}{7} h (196 - 49)$$

$$= \frac{22}{7} h \times 147$$

$$= 21 \times 22h$$

$$= 462 \times h \text{ m}^3$$

Since,

Volume of embankment = Volume of earth dug out

Therefore,

$$1848 = 462 h$$

$$h = \frac{1848}{462}$$

$$h = 4 \text{ m}$$

Therefore,

Height of the embankment = 4 m

Question: 19

A road roller tak

Solution:

It is given in the question that,

Diameter = 84 cm

Hence,

Radius = 42cm

Length = 1m = 100cm

Now,

$$\text{Lateral surface area} = 2\pi rh$$

$$= 2 \times \frac{22}{7} \times 42 \times 100$$

$$= 26400 \text{ cm}^2$$

Hence, the area of the road will be

$$= \text{lateral surface area} \times \text{no. of rotations}$$

$$= 26400 \times 750$$

$$= 19800000 \text{ cm}^2$$

$$= 1980 \text{ m}^2$$

Question: 20

A cylinder is open

Solution:

It is given in the question that,

Thickness of the cylinder = 1.5 cm

External diameter of the cylinder = 12 cm

Hence,

$$\text{Radius} = 6 \text{ cm}$$

And,

$$\text{Internal radius} = 4.5 \text{ cm}$$

$$\text{Height} = 84 \text{ cm}$$

Hence,

We have the following measurements now,

$$\text{Total volume} = \pi r^2 h$$

$$= \frac{22}{7} \times 6 \times 6 \times 84$$

$$= 9504 \text{ cm}^3$$

$$\text{Inner volume of the cylinder} = \pi r^2 h$$

$$= \frac{22}{7} \times 4.5 \times 4.5 \times 84$$

$$= 5346 \text{ cm}^3$$

Hence,

$$\text{The volume of the metal} = \text{total volume} - \text{internal volume}$$

$$= 9504 - 5346$$

$$= 4158 \text{ cm}^3$$

Therefore,

$$\text{Weight of the iron} = 4158 \times 7.5$$

$$= 31.185 \text{ kg}$$

Question: 21

The length of a m

Solution:

It is given in the question that,

$$\text{Length} = 1\text{m}$$

$$= 100\text{cm}$$

$$\text{Inner diameter} = 12 \text{ cm}$$

$$\text{Inner Radius} = 6 \text{ cm}$$

Hence,

$$\text{Inner volume} = \pi r_1^2 h$$

$$\text{Thickness} = 1 \text{ cm}$$

$$\text{outer radius} = 7 \text{ cm}$$

Now,

We can calculate the following measurements:

$$\text{Total volume} = \pi r_2^2 h$$

Now,

$$\text{Volume of the tube} = \text{total volume} - \text{inner volume}$$

$$= \pi r_2^2 h - \pi r_1^2 h$$

$$= \pi h (r_2^2 - r_1^2) = 3.14 \times 100 \times (7^2 - 6^2) = 3.14 \times 100 \times (49 - 36) = 314 \times 13 = 4082 \text{ cm}^3$$

We have,

$$\text{Density of the tube} = 7.7 \text{ g/cm}^3$$

Therefore,

$$\text{Weight of the tube} = \text{volume} \times \text{density}$$

$$= 4082 \times 7.7$$

$$= 31431\text{g}$$

$$= 31.43 \text{ kg}$$

Exercise : 20C

Question: 1

The maximum length

Solution:

We know that,

$$\text{Length of the diagonal of the cuboid} = \sqrt{l^2 + b^2 + h^2}$$

$$= \sqrt{12^2 + 9^2 + 8^2}$$

$$= \sqrt{144 + 81 + 64}$$

$$= \sqrt{289}$$

$$= 17 \text{ cm}$$

Therefore, option B is correct

Question: 2

The total surface

Solution:

We know that,

$$\text{Total surface area of cube} = 6a^2$$

$$6a^2 = 150 \text{ cm}^2$$

$$a = \sqrt{\frac{150}{6}}$$

$$a = \sqrt{25}$$

$$a = 5 \text{ cm}$$

Therefore,

$$\text{Volume of the cube} = a^3 = 5^3 = 125 \text{ cm}^3$$

Hence, option B is correct

Question: 3

The volume of a c

Solution:

Given that,

$$\text{Volume of cube} = 343 \text{ cm}^3$$

$$a^3 = 343 \text{ cm}^3$$

$$a = \sqrt[3]{343}$$

$$a = 7 \text{ cm}$$

We know that,

$$\text{Total surface area of cube} = 6a^2$$

$$= 6 \times 7 \times 7$$

$$= 294 \text{ cm}^2$$

Hence, option C is correct

Question: 4

The cost of paint

Solution:

Let the side of cube be 'a'

$$\text{Hence total surface area of cube} = 6a^2$$

$$\text{Cost of painting the cube} = 6a^2 \times 10$$

$$264.6 = 60 a^2$$

$$a^2 = \frac{264.6}{60}$$

$$a^2 = 4.41$$

$$a = 2.1$$

Hence,

$$\text{Volume of the cube} = a^3$$

$$= (2.1)^3$$

$$= 9.261 \text{ cm}^3$$

Hence, option B is correct

Question: 5

How many bricks,

Solution:

We know that,

Volume of cuboid = Length $\times$ Breadth $\times$ Height

Therefore,

$$\text{Volume of each brick} = 25 \times 11.25 \times 6$$

$$= 1687.5 \text{ cm}^3$$

$$\text{Volume of wall} = 800 \times 600 \times 22.5$$

$$= 10800000 \text{ cm}^3$$

Therefore,

$$\text{Number of bricks} = \frac{10800000}{1687.5}$$

$$= 6400$$

Hence, option C is correct

Question: 6

How many cubes of

Solution:

$$\text{Volume of smaller cube} = a^3 = (10)^3 = 1000 \text{ cm}^3$$

$$\text{Volume of box} = (100)^3 = 1000000 \text{ cm}^3$$

Therefore,

$$\text{Total number of cubes} = \frac{1000000}{1000}$$

$$= 1000$$

Hence, option C is correct

Question: 7

The edges of a cu

Solution:

Let a be the length of the smallest edge

Therefore,

The edges are in proportion a: 2a: 3a

We know that,

$$\text{Surface area of cuboid} = 2 (lb + bh + hl)$$

$$= 2 (a \times 2a + a \times 3a + 2a \times 3a)$$

$$= 2 (2a^2 + 3a^2 + 6a^2)$$

$$= 22a^2$$

$$= 88 \text{ cm}^2$$

$$a = \sqrt{\frac{88}{22}}$$

$$= \sqrt{4} = 2$$

Also,

$$2a = 2 \times 2 = 4$$

And,

$$3a = 3 \times 2 = 6$$

Therefore,

$$\text{Volume} = a \times 2a \times 3a$$

$$= 2 \times 4 \times 6$$

$$= 48 \text{ cm}^3$$

Hence, option A is correct

Question: 8

Two cubes have th

Solution:

Given that,

Volumes are in the ration 1: 27

Therefore,

$$\frac{\text{Volume 1}}{\text{Volume 2}} = \frac{1}{27} = \frac{a^3}{b^3}$$

$$a = \frac{b}{\sqrt[3]{27}}$$

$$a = \frac{b}{3}$$

$$\text{Or } b = 3a$$

$$\text{Or } \frac{b}{a} = 3$$

We have to find out ratio of their surface areas:

$$\frac{\text{Surface area 1}}{\text{Surface area 2}} = \frac{6a^2}{6b^2}$$

$$= \frac{a^2}{b^2}$$

$$= \frac{\left(\frac{b}{3}\right)^2}{b^2}$$

$$= \frac{1}{9}$$

Therefore, the surface areas are in the ratio 1: 9

Hence, option B is correct

Question: 9

The surface area

Solution:

We know that,

$$\text{Surface area of a cuboid} = 2 (lb + bh + hl)$$

$$= 2 (10 \times 4 + 10 \times 3 + 4 \times 3)$$

$$= 2 (40 + 30 + 12)$$

$$= 164 \text{ cm}^2$$

Hence, option C is correct

Question: 10

An iron beam is 9

Solution:

We know that,

Volume of a cuboid = Length $\times$ Breadth $\times$ Height

$$= 9 \times 0.4 \times 0.2$$

$$= 0.72 \text{ m}^3$$

Therefore,

$$\text{Weight} = 0.72 \times 50$$

$$= 36 \text{ kg}$$

Question: 11

A rectangular wat

Solution:

We know that,

Volume of a cuboid = Length $\times$ Breadth $\times$ Height

$$42000 \text{ L} = 42 \text{ m}^3 \text{ (As } 1 \text{ m}^3 = 1000 \text{ L)}$$

Therefore,

$$\text{Height (h)} = \frac{\text{Volume}}{\text{lb}}$$

$$= \frac{42}{6 \times 3.5}$$

$$= 2 \text{ m}$$

Hence, option A is correct

Question: 12

The dimensions of

Solution:

We know that,

Volume of a cuboid = Length $\times$ Breadth $\times$ Height

Therefore,

$$\text{Volume of the room} = 10 \times 8 \times 3.3$$

$$= 264 \text{ m}^3$$

$$\text{Space required by 1 person} = 3 \text{ m}^3$$

Therefore,

$$\text{Total number of people that can be accommodated} = \frac{264}{3}$$

$$= 88$$

Hence, option B is correct

Question: 13

A rectangular wat

Solution:

For this we have to find out volume of the water tank

We know that,

Volume of a cuboid = Length $\times$ Breadth $\times$ Height

Therefore,

Volume of water tank = $3 \times 2 \times 5$

= 30 m^3

= 30000 L (As, $1 \text{ m}^3 = 1000 \text{ L}$)

Hence, option A is correct

Question: 14

The area of the c

Solution:

We know that,

Surface area of cuboid = $2 (lb + bh + hl)$

Therefore,

Area of the cardboard required to make a box = $2 (23 \times 15 + 15 \times 8 + 25 \times 8)$

= $2 (375 + 120 + 200)$

= 1390 cm^2

Hence, option B is correct

Question: 15

The diagonal of a

Solution:

Given that,

Diagonal of the cube = $a\sqrt{3} = 4\sqrt{3} \text{ cm}$

i.e. $a = \text{cm}$

Therefore,

Volume of the cube = $a^3 = 4^3$

= 64 cm^3

Hence, option D is correct

Question: 16

The diagonal of a

Solution:

We know that,

Diagonal of the cube = $a\sqrt{3}$

= $9\sqrt{3}$

i.e. $a = 9$

Therefore,

$$\text{Total surface area of the cube} = 6a^2$$

$$= 6 \times 9 \times 9$$

$$= 486 \text{ cm}^2$$

Hence, option B is correct

Question: 17

If each side of a

Solution:

Let the side of the cube be a units

$$\text{Original volume} = a^3$$

Now, when each side of the cube is doubled then its volume:

$$\text{New side} = 2a \text{ units}$$

$$\text{New Volume} = (2a)^3 = 8a^3 \text{ cubic units}$$

Therefore, the volume of the cube is 8 times than its original volume

Hence, option D is correct

Question: 18

If each side of a

Solution:

Let the side of the cube be " a " unit

$$\text{Original Surface area} = 6a^2 \text{ sq units}$$

Now, when each side of a cube is doubled than its surface area:

$$\text{New surface area} = 6 (2a)^2 \text{ sq units}$$

$$= 24a^2 \text{ sq units}$$

Therefore, the surface area of the cube is 4 times than its original area

Hence, option B is correct

Question: 19

Three cubes of ir

Solution:

We know that,

$$\text{Volume of cube} = a^3$$

$$\text{Total Volume of cube} = 6^3 + 8^3 + 10^3$$

$$= 216 + 512 + 1000$$

$$= 1728 \text{ cm}^3$$

Therefore,

$$\text{Edge of the new cube} = \sqrt[3]{1728}$$

$$= 12 \text{ cm}$$

Hence, option A is correct

Question: 20

Five equal cubes,

Solution:

Length of the cuboid so formed = 25 cm

Breadth of the cuboid = 5 cm

Height of the cuboid = 5 cm

We know that,

Volume of cuboid = Length $\times$ Breadth $\times$ Height

$$= 25 \times 5 \times 5$$

$$= 625 \text{ cm}^3$$

Hence, option D is correct

Question: 21

A circular well w

Solution:

Given that,

Diameter of the circular well = 2 m

Radius = 1 m

Height = 14 m

Therefore,

Volume of cylindrical well = $\pi r^2 h$

$$= \frac{22}{7} \times 1 \times 1 \times 14$$

$$= 44 \text{ m}^3$$

Hence, option D is correct

Question: 2

If the capacity o

Solution:

Given that,

Volume of cylindrical tank = 1848 m³

Diameter = 14 m

So, Radius = 7 m

We know that,

Volume of cylinder = $\pi r^2 h$

$$1848 = \frac{22}{7} \times 7 \times 7 \times h$$

$$h = \frac{1848}{22 \times 7}$$

$$h = 12 \text{ m}$$

Hence, option B is correct

Question: 23

The ratio of the

Solution:

We have,

$$\frac{\text{Total surface area}}{\text{Lateral surface area}} = \frac{2\pi r(h+r)}{2\pi rh}$$

$$= \frac{h+r}{h}$$

$$= \frac{20+60}{60}$$

$$= \frac{4}{3}$$

$$= 4: 3$$

Therefore, option C is correct

Question: 24

The number of coi

Solution:

$$\text{Total number of coins} = \frac{\text{Volume of cylinder}}{\text{Volume of each coin}}$$

$$= \frac{\pi \times 3 \times 3 \times 8}{\pi \times 0.75 \times 0.75 \times 0.2}$$

$$= 640$$

Hence, option D is correct

Question: 25

$$66 \text{ cm}^3$$

Solution:

We have to find out length of the wire:

$$\text{Length} = \frac{\text{Volume}}{\pi r^2}$$

$$\text{Diameter} = 1 \text{ mm (Given)}$$

Therefore,

$$\text{Radius} = 0.05 \text{ cm}$$

$$\text{Length} = \frac{66 \times 7}{22 \times 0.05 \times 0.05}$$

$$= 8400 \text{ cm}$$

$$= 84 \text{ m}$$

Hence, option B is correct

Question: 26

The height of a c

Solution:

We know that,

$$\text{Volume of cylinder} = \pi r^2 h$$

Given that,

$$\text{Diameter} = 10 \text{ cm}$$

Radius = 5 cm

Height = 14 cm

Therefore,

$$\text{Volume} = \pi r^2 h$$

$$= \frac{22}{7} \times 5 \times 5 \times 14$$

$$= 1100 \text{ cm}^3$$

Hence, option A is correct

Question: 27

The height of a c

Solution:

We know that,

$$\text{Total surface area of the cylinder} = 2\pi r (r + h)$$

Given that,

$$\text{Diameter} = 7 \text{ cm}$$

$$\text{So, Radius} = 3.5 \text{ cm}$$

$$\text{Height} = 80 \text{ cm}$$

Therefore,

$$\text{Total surface area} = 2 \times \frac{22}{7} \times 3.5 (3.5 + 80)$$

$$= 22 (83.5)$$

$$= 1837 \text{ cm}^2$$

Hence, option A is correct

Question: 28

The height of a c

Solution:

We know that,

$$\text{Curved surface area of the cylinder} = 2\pi r h$$

$$264 = 2\pi r h$$

$$r = \frac{264 \times 7}{2 \times 22 \times 14}$$

$$r = 3 \text{ cm}$$

We know that,

$$\text{Volume of cylinder} = \pi r^2 h$$

$$= \frac{22}{7} \times 3 \times 3 \times 14$$

$$= 396 \text{ cm}^3$$

Hence, option B is correct

Question: 29

The diameter of a

Solution:

Given that,

$$\text{Diameter} = 14 \text{ cm}$$

$$\text{So, Radius} = 7 \text{ cm}$$

We know that,

$$\text{Curved surface area of cylinder} = 2\pi rh$$

$$220 \text{ cm}^2 = 2\pi rh$$

$$h = \frac{220 \times 7}{2 \times 22 \times 7}$$

$$h = 5 \text{ cm}$$

Therefore,

$$\text{Volume of cylinder} = \pi r^2 h$$

$$= \frac{22}{7} \times 7 \times 7 \times 5$$

$$= 770 \text{ cm}^3$$

Hence, option A is correct

Question: 30

The ratio of the

Solution:

Given that,

$$\frac{r_1}{r_2} = \frac{2}{3}$$

Also,

$$\frac{h_1}{h_2} = \frac{5}{3}$$

We know that,

$$\text{Volume of cylinder} = \pi r^2 h$$

Therefore,

$$\frac{V_1}{V_2} = \frac{\pi r_1^2 h_1}{\pi r_2^2 h_2}$$

$$= \frac{20}{27}$$

Therefore, the volume of given two cylinders will be in the ratio 20: 27

Hence, option C is correct

Exercise : CCE TEST PAPER-20**Question: 1**

Find the volume of

Solution:

We know that,

$$\text{Total surface area of a cube} = 6a^2$$

$$384 = 6a^2$$

$$a = \sqrt{\frac{384}{6}}$$

$$= 8 \text{ cm}$$

Therefore,

$$\text{Volume of cone} = a^3 = (8)^3$$

$$= 512 \text{ cm}^3$$

Question: 2

How many soap cak

Solution:

We know that,

$$\text{Volume of cuboid} = \text{Length} \times \text{Breadth} \times \text{Height}$$

Therefore,

$$\text{Volume of a soap cake} = 7 \times 5 \times 2.5$$

$$= 87.5 \text{ cm}^3$$

Also,

$$\text{Volume of the box} = 56 \times 40 \times 25$$

$$= 56000 \text{ cm}^3$$

Therefore,

$$\text{Number of soap cakes} = \frac{56000}{87.5}$$

$$= 640 \text{ units}$$

Hence,

640 cakes of soap can be placed in a box of the given size

Question: 3

The radius and he

Solution:

Given that,

$$\frac{\text{Radius}}{\text{Height}} = \frac{r}{h} = \frac{5}{7}$$

We know that,

$$\text{Volume of cylinder} = \pi r^2 h$$

$$= \frac{22}{7} \times \frac{5}{7} h \times \frac{5}{7} h \times h$$

$$= 550 \text{ cm}^3$$

Therefore,

$$h = \sqrt[3]{\frac{550 \times 7 \times 7 \times 7}{22 \times 5 \times 5}}$$

$$= 7 \text{ cm}$$

Therefore,

$$r = \frac{5}{7} h$$

$$= \frac{5}{7} \times 7$$

$$= 5 \text{ cm}$$

Question: 4

Find the number of

Solution:

$$\text{Volume of coin} = \pi r^2 h = \frac{22}{7} \times 0.75 \times 0.75 \times 0.2$$

$$\text{Volume of cylinder} = \pi r^2 h = \frac{22}{7} \times 2.25 \times 2.25 \times 10$$

Therefore,

$$\text{Total number of coins} = \frac{\text{Volume of cylinder}}{\text{Volume of coin}}$$

$$= \frac{\frac{22}{7} \times 2.25 \times 2.25 \times 10}{\frac{22}{7} \times 0.75 \times 0.75 \times 0.2}$$

$$= 450 \text{ coins}$$

Thus, 450 coins must be melted to form the required cylinder

Question: 5

Find the surface

Solution:

Given that,

$$\text{Length} = 18 \text{ cm}$$

$$\text{Breadth} = 10 \text{ cm}$$

$$\text{Height} = 8 \text{ cm}$$

We know that,

$$\text{Total surface area of cuboid} = 2 (lb + bh + hl)$$

$$= 2 (18 \times 10 + 18 \times 8 + 10 \times 8)$$

$$= 2 (180 + 144 + 80)$$

$$= 808 \text{ cm}^2$$

Question: 6

The curved surface

Solution:

We know that,

$$\text{Curved surface area of cylinder} = 2\pi rh$$

$$264 = 2\pi rh$$

$$r = \frac{264}{2\pi h}$$

$$r = \frac{132}{\pi h} \text{ m}$$

We also know that,

$$\text{Volume of cylinder} = \pi r^2 h$$

$$= \pi \times \frac{132}{\pi h} \times \frac{132}{\pi h} \times h$$

$$= 924 \text{ m}^3$$

Now,

$$r = \frac{132}{\pi h}$$

$$= \frac{132 \times 7}{22 \times 6} = 7 \text{ m}$$

Therefore,

Diameter of the pillar, $d = 7 \times 2 = 14 \text{ m}$

Question: 7

The circumference

Solution:

Given that,

Height = 15 cm

Circumference = $2\pi r$

$$r = \frac{44 \times 7}{2 \times 22}$$

$$= 7 \text{ cm}$$

We know that,

Volume of cylinder = $\pi r^2 h$

$$= \frac{22}{7} \times 7 \times 7 \times 15$$

$$= 2310 \text{ cm}^3$$

Hence, option B is correct

Question: 8

The area of the b

Solution:

Given that,

Area of the base of the cylinder = 35 cm^2

Height = 8 cm

Therefore,

Volume = Base area $\times$ Height

$$= 35 \times 8$$

$$= 280 \text{ cm}^3$$

Hence, option B is correct

Question: 9

A cuboid having d

Solution:

We know that,

Volume of cuboid = Length $\times$ Breadth $\times$ Height

$$= 16 \times 11 \times 8$$

$$= 1408 \text{ m}^3$$

Also,

$$\text{Volume of cylinder} = \pi r^2 h = 1408 \text{ m}^3$$

Therefore,

$$h = \frac{1408 \times 7}{22 \times 4 \times 4}$$

$$= 28 \text{ m}$$

Hence, option A is correct

Question: 10

The dimensions of

Solution:

We know that,

$$\text{Lateral surface area of cuboid} = 2 [(l + b) \times h]$$

$$= 2 [(8 + 6) \times 4]$$

$$= 2 (56)$$

$$= 112 \text{ m}^2$$

Hence, option C is correct

Question: 11

The length, bread

Solution:

We know that,

$$\text{Volume of cuboid} = \text{Length} \times \text{Breadth} \times \text{Height}$$

$$576 = 3x \times 4x \times 6x$$

$$576 = 72x^3$$

$$x = \sqrt[3]{\frac{576}{72}}$$

$$= 2$$

Therefore,

$$\text{Total surface area of cuboid} = 2 (lb + bh + hl)$$

$$= 2 (3x \times 4x + 4x \times 6x + 6x \times 3x)$$

$$= 2 (48 + 96 + 72)$$

$$= 432 \text{ cm}^2$$

Question: 12

The surface area

Solution:

We know that,

$$\text{Surface area of cube} = 6a^2$$

$$384 = 6a^2$$

$$a = \sqrt{\frac{384}{6}}$$

$$a = \sqrt{64}$$

$$a = 8 \text{ cm}$$

Therefore,

$$\text{Volume of cube} = a^3 = 8^3$$

$$= 512 \text{ cm}^3$$

Hence, option A is correct

Question: 13

Fill in the blank

Solution:

(i) We know that,

$$\text{Total surface area of the cuboid} = 2 (lb + bh + hl)$$

(ii) We know that,

$$\text{Lateral surface area of cuboid} = 2 [(l + b) \times h]$$

(iii) We know that,

$$\text{Lateral surface area of cube} = 4a^2$$

(iv) We know that,

$$\text{Volume of cylinder} = \pi r^2 h$$

(v) We know that,

$$\text{Lateral surface area of cylinder} = 2\pi rh$$