5. Playing with Number

EXERCISE 5(A)

Question 1.

Write the quotient when the sum of 73 and 37 is divided by

- (i) 11
- (ii) 10

Solution:

Sum of 73 and 37 is to be divided by

(i) 11

(ii) 10

Let ab = 73

and ba = 37

 $\therefore a = 7$

and b = 3

(i) The quotient of ab + bc i.e. (73 + 37) when divided by 11 is a + b = 7 + 3 = 10

$$\left(\because \frac{ab+ba}{11} = a+b\right)$$

(ii) The quotient of ab + ba i.e. (73 + 37) when divided by 10 (i.e. a + b) is 11

$$\left(\because \frac{ab+ba}{a+b} = 11\right)$$

Question 2.

Write the quotient when the sum of 94 and 49 is divided by

- (i) 11
- (ii) 13

Solution:

Sum of 94 and 49 is to be divided by

- (i) 11
- (ii) 13

Let ab = 94

and ba = 49

- $\therefore a = 9 \text{ and } b = 4$
- (i) The quotient of 94 + 49 (i.e. ab + ba)

When divided by 11 is a + b i.e. 9 + 4 = 13

$$\left(\because \frac{ab+ba}{11} = a+b\right)$$

(ii) The quotient of 94 + 49 (i.e. ab + ba)

When divided by 13 i.e. (a + b) is 11

$$\left(\because \frac{ab+ba}{a+b} = 11\right)$$

Question 3.

Find the quotient when 73 - 37 is divided by

- (i) 9
- (ii) 4

Solution:

Difference of 73 - 37 is to be divided by

(i) 9

(ii) 4

Let ab = 73 and ba = 37

- $\therefore a = 7 \text{ and } b = 3$
- (i) The quotient of 73 37 (i.e. ab bc) when divided by 7 is a b i.e. 7 3 = 4

$$\left(\because \frac{ab-ba}{9} = a-b\right)$$

(ii) The quotient of 73 - 37 (i.e. ab - ba) when divided by 4 i.e. (a - b) is 9

$$\left(\because \frac{ab-ba}{a-b} = 9\right)$$

Question 4.

Find the quotient when 94 – 49 is divided by

(i) 9

(ii) 5

Solution:

Difference of 94 and 49 is to be divided by

(i) 9

Let ab = 94 and ba = 49

$$\therefore a = 9 \text{ and } b = 4$$

(i) The quotient of 94 - 49 i.e. (ab - ba) when divided by 9 is (a - b) i.e. 9 - 4 = 5

$$\left(\because \frac{ab-ba}{9} = a-b\right)$$

(ii) The quotient of 94 - 49 i.e. (ab - ba) when divided by 5 i.e. (a - b) is 9

$$\left(\because \frac{ab-ba}{a-b} = 9\right)$$

Question 5.

Show that 527 + 752 + 275 is exactly divisible by 14.

Solution:

Property:

abc = 100a + 106 + c(i)

bca = 1006 + 10c + a(ii)

and cab = 100c + 10a + b(iii)

Adding, (i), (ii) and (iii), we get abc + bca + cab = $111a + 111b + 111c = 111(a + b + c) = 3 \times 37(a + b + c)$

Now, let us try this method on

527 + 752 + 275 to check is it exactly divisible by 14

Here, a = 5, 6 = 2, c = 7

 $527 + 752 + 275 = 3 \times 37(5 + 2 + 7) = 3 \times 37 \times 14$

Hence, it shows that 527 + 752 + 275 is exactly divisible by 14

Question 6.

If a = 6, show that abc = bac.

Solution:

Given: a = 6

To show: abc = bac

Proof: $abc = 100a + 106 + c \dots (i)$

(By using property 3)

bac = 1006 + 10a + c - (ii)

(By using property 3)

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Since, a = 6

Substitute the value of a = 6 in equation (i) and (ii), we get abc = 1006 + 106 + c .......(iii)

bac = 1006 + 106 + c .......(iv)

Subtracting (iv) from (iii) abc – bac = 0

abc = bac

Hence proved.
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Question 7.

If a > c; show that abc - cba = 99(a - c).

Solution:

Given, a > c

To show: abc - cba = 99(a - c)

Proof: abc = 100a + 10b + c(i)

(By using property 3)

cba = 100c + 10b + a(ii)

(By using property 3)

Subtracting, equation (ii) from (i), we get

abc - cba = 100a + c - 100c - a

abc - cba = 99a - 99c

abc - cba = 99(a - c)

Hence proved.

Question 8.

If c > a; show that cba - abc = 99(c - a).

Solution:

Given: c > a

To show: cba - abc = 99(c - a)

Proof:

cba = 100c + 106 + a(i)

(By using property 3)

abc = 100a + 106 + c(ii)

(By using property 3)

Subtracting (ii) from (i)

cba - abc= 100c+ 106 + a- 100a- 106-c

=> cba - abc = 99c - 99a

=> cba - abc = 99(c - a)

Hence proved.

Question 9.

If a = c, show that cba - abc = 0.

Solution:

Given: a = c

To show: cba - abc = 0

Proof:

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cba = 100c + 106 + a .................(i)
(By using property 3)
abc = 100a + 106 + c ................(ii)
(By using property 3)
Since, a = c,
Substitute the value of a = c in equation (i) and (ii), we get cba = 100c + 10b + c ................(iv)
Subtracting (iv) from (iii), we get cba - abc - 100c + 106 + c - 100c - 106 - c => cba - abc = 0 => cba = abc
Hence proved.
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Question 10.

Show that 954 – 459 is exactly divisible by 99.

Solution:

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To show: 954 - 459 is exactly divisible by 3 99, where a = 9, b = 5, c = 4 abc = 100a + 10b + c
=> 954 = 100 \times 9 + 10 \times 5 + 4
=> 954 = 900 + 50 + 4 ......(i)
and 459 = 100 \times 4 + 10 \times 5 + 9
=> 459 = 400 + 50 + 9 ......(ii)
Subtracting (ii) from (i), we get
954 - 459 = 900 + 50 + 4 - 400 - 50 - 9
=> 954 - 459 = 500 - 5
=> 954 - 459 = 495
=> 954 - 459 = 99 \times 5
Hence, 954 - 459 is exactly divisible by 99
Hence proved.
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EXERCISE 5(B)

Question 1.

$$\frac{3 \text{ A}}{+25}$$

Solution:

A = 7 as 7 + 5 = 12. We want 2 at units place and 1 is carry over. Now 3 + 2 + 1 = 6.

$$B = 6$$

Hence A = 7 and B = 6

$$\frac{37}{62}$$

Question 2.

Solution:

A = 5 as 8 + 5 = 13. We want 3 at units place and 1 is carry over. Now 9 + 4 + 1 = 14.

$$B = 4$$
 and $C = 1$

Hence A = 5 and B = 4 and C = 1

$$98 + 45 \over 143$$

Question 3.

$$\begin{array}{c} A I \\ + \underline{1} B \\ \hline B 0 \end{array}$$

Solution:

B = 9 as 9 + 1 = 10. We want 0 at units place and 1 is carry over. Now B - 1 - 1 = A.

$$A = 9 - 2 = 7$$

Hence A = 7 and B = 9

$$71 + 19 \over 90$$

Question 4.

$$\begin{array}{r} 2AB \\ + \underline{AB1} \\ \hline B18 \end{array}$$

Solution:

B = 7 as 7 + 1 = 8. We want 8 at unit place.

Now

$$7 + A = 11$$

$$A = 11 - 7 = 4$$

Hence A = 4 and B = 7

$$\begin{array}{r}
 247 \\
 +471 \\
 \hline
 718
 \end{array}$$

Question 5.

$$\begin{array}{r}
12A \\
+6AB \\
\hline
A09
\end{array}$$

Solution:

$$A + B = 9$$

and
$$2 + A = 10$$

$$A = 10 - 2 = 8$$

and
$$8 + B = 9$$

$$B = 9 - 8 = 1$$

Hence
$$A = 8$$
 and $B = 1$

$$\frac{128}{681}$$

Question 6.

$$\frac{\times A}{9 A}$$

Solution:

As we need A at unit place and 9 at ten's place,

$$A = 6$$
 as $6 \times 6 = 36$

$$\frac{\times 6}{96}$$

Question 7.

$$\frac{\times 6}{BBB}$$

Solution:

As we need B at unit place and B at ten's place,

$$B = 4 \text{ as } 6 \times 4 = 24$$

Now we want to find A, $6 \times A + 2 = 4$ (at unit's place)

Question 8.

$$\frac{\times 3}{\text{CAB}}$$

Solution:

As we need B at unit place and A at ten's place,

$$\therefore$$
 B = 0 as 3 × 0 = 0

Now we want to find A, $3 \times A = A$ (at unit's place)

$$A = 5$$
, as $3 \times 5 = 15$

$$\therefore$$
 C = 1

$$\frac{\times 3}{150}$$

Question 9.

Solution:

As we need B at unit place and A at ten's place,

$$B = 0$$
 as $5 \times 0 = 0$

Now we want to find A, $5 \times A = A$ (at unit's place)

$$A = 5$$
, as $5 \times 5 = 25$

$$C = 2$$

$$\frac{\times 5}{250}$$

Question 10.

$$\frac{+94A}{1A33}$$

Solution:

$$5 + A = 13$$

and
$$A + 4 = 13$$

$$A = 13 - 5 = 8$$

Hence
$$A = 8$$

Question 11.

Solution:

C+5=11

$$\therefore$$
 C=11-5=6
and 8+B+1=15
 \therefore B=15-9=6
and A+5+1=13
 \therefore A=13-6=7
and 6+D+1=9
 \therefore D=9-7=2
Hence A=7, B=6, C=6 and D=2
6765
+2586
9351

EXERCISE 5(C)

Question 1.

Find which of the following nutpbers are divisible by 2:

- (i) 192
- (ii) 1660
- (iii) 1101
- (iv) 2079

Solution:

A number having its unit digit 2,4,6,8 or 0 is divisible by 2, So, Number 192, 1660 are divisible by 2.

Question 2.

Find which of the following numbers are divisible by 3:

- (i) 261
- (ii) 111
- (iii) 6657
- (iv) 2574

Solution:

A number is divisible by 3 if the sum of its digits is divisible by 3, So, 261, 111 are divisible by 3.

Question 3.

Find which of the following numbers are divisible by 4:

- (i) 360
- (ii) 3180
- (iii) 5348

(iv) 7756

Solution:

A number is divisible by 4, if the number formed by the last two digits is divisible by 4. So, Number 360, 5348, 7756 are divisible by 4.

Question 4.

Find which of the following numbers are divisible by 5:

- (i) 3250
- (ii) 5557
- (iii) 39255
- (iv) 8204

Solution:

A number having its unit digit 5 or 0, is divisible by 5.

So, 3250, 39255 are all divisible by 5.

Question 5.

Find which of the following numbers are divisible by 10:

- (i) 5100
- (ii) 4612
- (iii) 3400
- (iv) 8399

Solution:

A number having its unit digit 0, is divisible by 10.

So, 5100, 3400 are all divisible by 10.

Question 6.

Which of the following numbers are divisible by 11:

- (i) 2563
- (ii) 8307
- (iii) 95635

Solution:

A number is divisible by 11 if the difference of the sum of digits at the odd places and sum of the digits at even places is zero or divisible by 11.

So, 2563 is divisible by 11.

EXERCISE 5(D)

For what value of digit x, is:

Question 1.

1x5 divisible by 3?

Solution:

1x5 is divisible by 3

=> 1 + x + 5 is a multiple of 3

=> 6 + x = 0, 3, 6, 9,

=> x = -6, -3, 0, 3, 6, 9Since, x is a digit x = 0, 3, 6 or 9

Question 2.

31x5 divisible by 3?

Solution:

31x5 is divisible by 3 => 3 + 1 + x + 5 is a multiple of 3 => 9 + x = 0, 3, 6, 9, \Rightarrow x = -9, -6, -3, 0, 3, 6, 9, Since, x is a digit x = 0, 3, 6 or 9

Question 3.

28×6 a multiple of 3?

Solution:

28×6 is a multiple of 3 2 + 8 + x + 6 is a multiple of 3 \Rightarrow 16 + x = 0, 3, 6, 9, 12, 15, 18 => x = -18, -5, -2, 0, 2, 5, 8Since, x is a digit = 2, 5, 8

Question 4.

24x divisible by 6?

Solution:

24x is divisible by 6 => 2 + 4 + x is a multiple of 6 => 6 + x = 0, 6, 12=> x = -6, 0, 6Since, x is a digit x = 0, 6

Question 5.

3x26 a multiple of 6?

Solution:

3x26 is a multiple of 6 3 + x + 2 + 6 is a multiple of 3 \Rightarrow 11 + x = 0, 3, 6, 9, 12, 15, 18,21, => x = -11, -8, -5, -2, 1, 4, 7, 10, ...Since, x is a digit x = 1, 4 or 7

Question 6.

42×8 divisible by 4?

Solution:

 42×8 is divisible by 4 => 4 + 2 + x + 8 is a multiple of 2 => 14 + x = 0, 2, 4, 6, 8,

=> x = -8, -6, -4, -2, 2, 4, 6, 8,

Since, x is a digit 2, 4, 6, 8

Question 7.

9142x a multiple of 4?

Solution:

9142x is multiple of 4

=> 9 + 1 + 4 + 2 + x is a multiple of 4

=> 16 + x = 0, 4, 8,

x = -8, -4, 0, 4, 8

Since, x is a digit

4, 8

Question 8.

7x34 divisible by 9?

Solution:

7x34 is multiple of 9

=> 7 + x + 3 + 4 is a multiple of 9

 \Rightarrow 14 + x = 0, 9, 18, 27,

 \Rightarrow x = -1, 4, 13,

Since, x is a digit

x = 4

Question 9.

5×555 a multiple of 9?

Solution:

Sum of the digits of 5×555

=5 + x + 5 + 5 + 5 = 20 + x

It is multiple by 9

The sum should be divisible by 9

Value of x will be 7

Question 10.

3x2 divisible by 11?

Solution:

Sum of the digit in even place = x

and sum of the digits in odd place = 3 + 2 = 5

Difference of the sum of the digits in even places and in odd places = x - 5 3x2 is a multiple of 11

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=> x - 5 = 0, 11, 22,
=> x = 5, 16, 27,
Since, x is a digit x = 5
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Question 11.

5x2 a multiple of 11?

Solution:

Sum of a digit in even place = x and sum of the digits in odd place = x =