

Average (Mean)

Average of odd terms
$$= \frac{\text{last odd number} + 1}{2}$$

Average of $1^2, 2^2, 3^2, 4^2, \dots, n^2$
$$= \frac{(n+1)(2n+1)}{6}$$

Geometric Mean (GM)
$$\text{G.M.} = \sqrt[n]{x_1 x_2 x_3 \dots x_n}$$

Harmonic Mean (HM)
$$\text{H.M.} = \frac{1}{\frac{1}{x_1} + \frac{1}{x_2} + \dots + \frac{1}{x_n}}$$

Average of different
type of terms

Average of even terms
$$= \frac{\text{last even number} + 2}{2}$$

Average of first terms $= \frac{n+1}{2}$

If m observations having average $= a$
and n observations having average $= b$
Then, net average $= \frac{ma + nb}{m + n}$

Arithmetic Mean (AM)

Simple Average
$$\text{A.M.} = \frac{x_1 + x_2 + \dots + x_n}{n}$$

When each variable increases/decreases
by k the average increases/decreases by k

When each variable is multiplied/divided
by k the average multiplied/divided by k

Weighted Average

Trace the Mind Map

► First Level ► Second Level ► Third Level