

SECTION - I

Straight Objective Type

1.

$$\begin{array}{r}
 5814 \overline{) 5958} \quad 1 \\
 \underline{5814} \\
 144 \quad 5814 \overline{) 40} \\
 \underline{5760} \\
 54 \quad 144 \overline{) 2} \\
 \underline{108} \\
 36 \quad 54 \overline{) 1} \\
 \underline{36} \\
 18 \quad 36 \overline{) 2} \\
 \underline{36} \\
 0
 \end{array}$$

18 is G.CD of 5814, 5958

$$\begin{array}{r}
 5430 \overline{) 5814} \quad 1 \\
 \underline{5430} \\
 384 \quad 5430 \overline{) 14} \\
 \underline{384} \\
 1590 \\
 \underline{1536} \\
 54 \quad 384 \overline{) 7} \\
 \underline{378} \\
 6 \quad 54 \overline{) 9} \\
 \underline{54} \\
 0
 \end{array}$$

G.CD of 5814, 598

= 6

12 is the largest possible value of n

Hence (b) is the correct option.

2.

$$\frac{x_1}{x_2} = \frac{x_2}{x_3} = \frac{x_3}{x_4} = \dots = \frac{x_{15}}{x_{16}}$$

If $x_1 + x_2 + x_3 + x_4 = 20$,

$$x_5 + x_6 + x_7 + x_8 = 320$$

$$x_{13} + x_{14} + x_{15} + x_{16} = 19680$$

Hence (b) is the correct option.

3. Unit digit of $5^{2003} = 5$

Unit digit of $\frac{1}{5^{2003}} = 8$

Since

$$\frac{1}{5} = 0.2, \quad \frac{1}{5^2} = 0.04,$$

$$\frac{1}{5^3} = 0.008, \quad \frac{1}{5^4} = 0.0016$$

$$\frac{1}{5^5} = 0.00032, \quad \frac{1}{5^6} = 0.000064 \dots\dots$$

$$2003 = 5 \times 400 + 3$$

Hence (b) is the correct option.

4. $S_n = 1 - 2 + 3 - 4 + 5 - 6 + 7 - 8 + \dots\dots\dots + n$ terms

$$= \frac{n}{2} \text{ if } n \text{ is even}$$

$$= \frac{n+1}{2} \text{ if } n \text{ is odd}$$

$$S_{2002} \frac{2002}{2} = -1001$$

$$S_{2003} \frac{2003+1}{2} = -1002$$

$$S_{2004} \frac{2004}{2} = -1002$$

$$\begin{aligned} \therefore S_{2002} - S_{2003} + S_{2004} \\ = -1001 - 1002 - 1002 \\ = -3005 \end{aligned}$$

Hence (c) is the correct option.

5. Let $x = 121^2 - 25^n + 1900^n - (-4)^n$
by mathematical induction method $\forall n \in N$ x is divisible by 2000
 \Rightarrow Remainder is zero
Hence (c) is the correct option.

6. Highest power of n that divides $P!$

$$= \sum_{k=1}^{\alpha} \left[\frac{P}{n^k} \right]$$
Highest power of 2003 that divides

$$2003! = \sum_{k=1}^{\alpha} \left[\frac{2003}{2003^k} = 101 \right]$$
Hence (c) is the correct option.

7. The smallest positive integer n such
 $\sqrt{n} - \sqrt{n-1} < 0.01$ is 2501
Hence (c) is the correct option.

8. $n^{200} < 5^{300}$
 $\Rightarrow (n^2)^{100} < (5^3)^{100}$
 $\Rightarrow (n^2)^{100} < (125)^{100}$
 $\Rightarrow n^2 < 125$
 $\Rightarrow 125 > n^2$
 $121 = 11^2$ is nearest possible volume for n .
Hence (d) is the correct option.

9. Unit digit of $(3^{1001} \times 7^{1002} \times 13^{1003})$
Unit digit of $3^{1001} = 9$
Unit digit of $7^{1002} = 3$
Unit digit of $13^{1003} = 1$

Unit digit of $13^{1001} \times 7^{1002} \times 13^{1003}$
 = UD of $(9 \times 3 \times 1)$
 = UD of (27)
 = 7
 Hence (d) is the correct option.

10. $1260x = N^3$
 $\Rightarrow 1260 = 22 \times 32 \times 7 \times 5 \times x = N^3$
 $\Rightarrow x = 2 \times 3 \times 7^2 \times 5^2 = 7350$
 Hence (d) is the correct option.

11. $2^{13-1} \equiv 1 \pmod{13}$
 $2^{12} \equiv 1 \pmod{13}$
 $(2^{12})^{83} \equiv 1^4 \pmod{13}$
 $2^{996} \equiv 1 \pmod{13}$
 $2^4 \equiv 3 \pmod{13}$
 $\Rightarrow 2^{1000} \equiv 3 \pmod{13}$
 Hence (c) is the correct option.

12. $51 + 61 + 71 + \dots + 341$
 $= \frac{29}{2} [51 + 341]$
 $\left[s_n = \frac{n}{2} [a + l] \right]$
 $= \frac{29}{2} [51 + 341]$
 $= \frac{29}{2} \times 392$
 $= 5684$
 Hence (a) is the correct option.

13. The number of positive integral solution of

$$2x + 3y = 763 \text{ is } 128$$

Hence (c) is the correct option.

14. 895

Hence (b) is the correct option.

15. $!5 = 4 + 6 - 5 = 5$

$$!12 = 11 + 13 - 12 = 12$$

$$!23 = 22 + 24 - 23 = 23 \text{ then}$$

$$!40 = 40$$

$$!41 = 41 \dots \dots \dots !50 = 50$$

$$!40 + !41 + !42 + \dots \dots \dots + !40 = 495$$

Hence (b) is the correct option.

16. $(a-1)^2 + (b-2)^2 + (c-3)^2 + (d-4)^2 = 0$

$$\Rightarrow a-1=0, b-2=0, c-3=0, d-4=0$$

$$\Rightarrow a=1, b=2, c=3, d=4$$

$$\Rightarrow a \times b \times c \times d + 1$$

$$= 1 \times 2 \times 3 \times 4 + 1 = 25 = 5^2$$

Hence (c) is the correct option.

17. (29, 37)

Hence (d) is the correct option.

18. $422 \times 9 = 3798$

\Rightarrow The sum of the digits of the number

$$10^{422} - 1 = 3798$$

$$\Rightarrow n = 422$$

Hence (c) is the correct option.

19. $29030 = 2 \times 3 \times 5 \times 7 \times 11 \times 13$

Hence (c) is the correct option.

20. Greater than 350
Hence (d) is the correct option.

21. $1260n = 2^2 = 32 \times 7 \times 5 \times n$ is a perfect cube
 $\Rightarrow n = 7^2 \times 5^2 \times 3 \times 2$
 $\Rightarrow 1000 < n < 1000$
Hence (d) is the correct option.

22. $\sqrt{9 - (n+2)^2} > 0$
 $\Rightarrow -(n+2)^2 > -9$
 $(n+2)^2 < 9$
 $n^2 + 4n + 4 - 9 < 0$
 $n^2 + 4n - 5 < 0$
 $(n+5)(n-1) < 0$
 $\Rightarrow -5 < n < 1$ and $n \in \mathbb{Z}$
 $\Rightarrow n = \{-4, -3, -2, -1, 0\}$
 \Rightarrow possible values for n is 5
Hence (b) is the correct option.

23. $99 \mid 7ab73$
 $\Rightarrow 11 \mid 7ab73$ and $9 \mid 7ab73$
 $(7+6+3) - (a+7) = 0$ or multiple of 11
 $b-a+3=0 \mid 17+a+b$
 $b-a=-3 \mid 17+a+b=18$ = multiple of 9
 $a+b=1$
 $-a+b=-3$
 $\underline{a+b=1}$
 $b = -1$
not possible

$$\text{Let } 17 + a + b = 21$$

$$a + b = 4$$

$$-a + b = 8$$

$$2b = 12$$

$$\text{and } b - a + 3$$

$$b - a + 8$$

$$b = 6 \text{ and } a = -2$$

Hence number of solution for (a, b) is zero.

Hence (c) is the correct option.

24. $x^n - y^n$ is divisible by $x - y$

$$\forall n \in N$$

$$\Rightarrow 31 \mid 107^{90} - 76^{90}$$

$$\Rightarrow 62 \mid 107^{90} - 76^{90}$$

Hence (b) is the correct option.

25. When $1^{2003} + 3^{2003} + \dots + 2003^{2003}$ is divided by 2004 then the remainder is 1

Hence (b) is the correct option.

26. 18

Hence (c) is the correct option.

27. When 9999 is divided by 4, it leaves the remainder 3

$$\Rightarrow \text{the unit digit of } 7^{9999}$$

$$= \text{unit digit of } 7^3$$

$$\text{similarly} \quad \quad \quad = 3$$

$$\text{Ten's digit of } 7^{9999} \quad \quad \quad = 2$$

$$\text{Hundred's digit of } 7^{9999} = 5$$

Hence (d) is the correct option.

- 28.** The number of items the digit l appears in 123456
979899100 is 20
Hence (c) is the correct option.
- 29.** $n! = 1 \times 2 \times 3 \times \dots \times n$ has four zero at the end
 $\Rightarrow n! = 20! \text{ or } 21! \text{ or } 22! \text{ or } 23! \text{ or } 24!$
 $(n+1)! = 25!$ has six zeros at the end
 $\Rightarrow n = 24$
Hence (g) is the correct option.
- 30.** Number of ordered pairs satisfying the equation
Hence (b) is the correct option.

SECTION - II

Assertion - Reason Questions

- 31.** $17 \mid 5 \mid 17^8 - 5^8$
 $\Rightarrow 12 \mid 17^8 - 5^8$
 $\Rightarrow 3 \mid 17^8 - 5^8$
 $13 + 2 \mid 13^7 + 2^7$
 $\Rightarrow 15 \mid 13^7 - 2^7 \Rightarrow 3 \mid 13^7 + 2^7$
 $\Rightarrow 3 \mid 17^8 - 5^8 + 13^7 + 2^7$
since $x - y \mid x^n - y^n \quad \forall n \in \mathbb{N}$
and $x + y \mid x^n - y^n$ if n is odd
Hence (b) is the correct option.
- 32.** Let $X = A3640548981270644B$
 $99 \mid X \Rightarrow 9 \mid X$ and $11 \mid X$
 $9 \mid X \Rightarrow 71 + A + B = \text{multiple of } 9$
 $11 \mid X \Rightarrow (37 + A) - (34 + B)$
 $= \text{either } 0 \text{ or multiple of } 11$

$$71 + A + B = 81$$

$$A + B = 10$$

$$(37 + A) - (34 + B) = 11$$

$$A - B + 3 = 11$$

$$A - B = 8$$

$$\Rightarrow A + B = 10$$

$$\underline{A - B = 8}$$

$$\oplus 2A = 18 \Rightarrow A = 9, B = 1$$

Statement 1 is correct

7 or 13 divides a number which is n

The form ABC ABC

Hence Statement 2 is correct but

Statement 2 is not a correct explanation for Statement 1.

Hence (b) is the correct option.

33. Let

$$\begin{aligned} X &= 2222^{5555} + 5555^{222} \\ &= 2222^{5555} + 4^{5555} - 4^{555} + 5555^{2222} - 4^{2222} + 4^{2222} \\ &= 7 \mid 2222^{5555} + 4^{5555} \end{aligned}$$

$$5555 - 4 \mid 5555^{2222} - 4^{2222} \text{ and } 7 \mid 555 \mid$$

$$\Rightarrow 7 \mid 5555^{2222} \mid -4^{2222}$$

$$-4^{5555} + 4^{2222} = -4^{2222}(4^{3333} - 1)$$

$$= -4^{2222} \left((4^3)^{1111} - 1 \right)$$

$$7 \mid 4^3 - 1 \Rightarrow 7 \mid (4^3)^{1111} - 1^{1111}$$

$$\Rightarrow 7 \mid -4^{2222} (4^{333} - 1)$$

Hence 7 divides X

Statement 1 is correct

$x^n + y^n$ is divisible by $x + y$ If n is odd is also true

Statement 2 is a correct explanation for Statement 1.

Hence (a) is the correct option.

34. $5^{11-1} \equiv 1 \pmod{11}$

$3^{11-1} \equiv 1 \pmod{11}$

$\Rightarrow 5^{10} - 3^{10} \equiv 0 \pmod{11}$

$\Rightarrow 5^{10} - 3^{10}$ is divisible by 11

If P is a prime number, G. CD of (a, P) = 1

Them $a^{P-1} \equiv 1 \pmod{P}$ is well known as fermet theorem.

Statement 2 is a correct explanation for Statement one.

Hence (a) is the correct option

35. $3600 = 2^4 \times 3^2 \times 5^2$

The number of +ve integer ≤ 3600 that co-prime to 3600

$$= 3600 \times \left[1 - \frac{1}{2}\right] \left[1 - \frac{1}{3}\right] \left[1 - \frac{1}{5}\right]$$

$= 960$

Hence (a) is the correct option.

36. The product of three consecutive integers is always divisible by 6

$$n(n^2 - 1) = (n-1)n(n+1)$$

$\Rightarrow 6 \mid n(n^2 - 1)$

Hence (a) is the correct option.

37. $9504 = 2^5 \times 3^3 \times 11^1$

Number of factors of

$$9504 = (5+1)(3+1)(1+1)$$

$$= 6 \times 4 \times 2$$

$$= 48$$

Hence (a) is the correct option.

38. $2160 = 2^4 \times 3^3 \times 5^1$

Sum of the factors of 2160

$$= \left[\frac{2^{4+1} - 1}{2 - 1} \right] \left[\frac{3^{3+1} - 1}{3 - 1} \right] \left[\frac{5^{1+1} - 1}{5 - 1} \right]$$

$$= 31 \times 40 \times 6$$

$$= 7440$$

Hence (a) is the correct option.

39. The highest power of 7 contains in 1000!

$$= \sum_{k=1}^{\alpha} \left[\frac{1000}{7^k} \right]$$

$$= \left[\frac{1000}{7} \right] + \left[\frac{1000}{7^2} \right] + \left[\frac{1000}{7^3} \right] + \left[\frac{1000}{7^4} \right] + \dots = 164$$

The highest power of 3 contains in 1000!

$$= \sum_{k=1}^{\alpha} \left[\frac{1000}{3^k} \right]$$

$$= \left[\frac{1000}{3} \right] + \left[\frac{1000}{3^2} \right] + \left[\frac{1000}{3^3} \right] + \left[\frac{1000}{3^4} \right]$$

$$+ \left[\frac{1000}{3^5} \right] + \left[\frac{1000}{3^6} \right] + \dots = 498$$

Hence (b) is the correct option.

40. The number of zero at the end

$$= \sum_{k=1}^{\alpha} \left[\frac{4000}{5^k} \right]$$

$$= \left[\frac{400}{5} \right] + \left[\frac{400}{5^2} \right] + \left[\frac{400}{5^3} \right] + \left[\frac{400}{5^4} \right] + \dots$$

$$= 80 + 16 + 3 + 0 + \dots$$

$$= 99$$

Hence (a) is the correct option.

SECTION - III

Linked Comprehension Type

41. $2^{7-1} \equiv 1 \pmod{7}$

$\Rightarrow 2^6 \equiv 1 \pmod{7}$

$2^{18} \equiv 4 \pmod{7}$

$2^2 \equiv 4 \pmod{7}$

$\Rightarrow 220 \equiv 4 \pmod{7}$

Hence (a) is the correct option.

42. $3^{23-1} \equiv 1 \pmod{23}$

$3^{22} \equiv 1 \pmod{23}$

$3^3 \equiv 4 \pmod{23}$

$(3^3)^3 \equiv 4^3 \pmod{23}$

$\equiv -5 \pmod{23}$

$3^9 \equiv -5 \pmod{23}$

$3^{18} \equiv 2 \pmod{23}$

$\Rightarrow 3^{40} \equiv 2 \pmod{23}$

Hence (b) is the correct option.

43. $2^3 \equiv 0 \pmod{8}$

$(2^3)^{19} \equiv 0 \pmod{8}$

$2^{57} \equiv 0 \pmod{18}$

Hence (c) is the correct option.

44. The last three digit of $25^{63} \times 63^{25}$ are 3 and 7

Hence (b) is the correct option.

45. The last three digit of $25^{63} \times 63^{25}$ are 4, 7 and 5

Hence (c) is the correct option.

$$\begin{aligned}
46. \quad 56789 &\equiv -11 \pmod{100} \\
(56789)^2 &\equiv 21 \pmod{100} \\
(56789)^4 &\equiv 41 \pmod{100} \\
(56789)^6 &\equiv 61 \pmod{100} \\
(56789)^{10} &\equiv 1 \pmod{100} \\
(56789)^{40} &\equiv 1 \pmod{100} \\
(56789)^{41} &\equiv 89 \pmod{100}
\end{aligned}$$

Hence (c) is the correct option.

47. When the number $10^{10} + 10^{10^2} + \dots + 10^{(10^{10})}$ is divisible by 7 it leaves the remainder 4
Hence (a) is the correct option.

48. $13^{73} + 14^3$ is divided by 11 it leaves the remainder 5
Hence (c) is the correct option.

$$\begin{aligned}
49. \quad (2000)^{13-1} &\equiv 1 \pmod{13} \\
(2000)^{12} &\equiv 1 \pmod{13} \\
(2000^{12})^{83} &\equiv 1 \pmod{13} \\
2000^{996} &\equiv 1 \pmod{13} \\
2000 &\equiv 1 \pmod{13} \\
2000^2 &\equiv 1^2 \pmod{13} \\
2000^2 &\equiv 4 \pmod{13} \\
2000^4 &\equiv 4 \pmod{13} \\
2000^{1000} &\equiv 3 \pmod{13}
\end{aligned}$$

Hence (c) is the correct option.

$$50. \quad 4^{4n} - 5^{3n} = (256)^n - (125)^n$$

$$256 - 125 \mid 4^{4n} - 5^{3n}$$

$$= 131 \mid 4^{4n} - 5^{3n}$$

Hence (a) is the correct option.

$$51. \quad 2^{4n} - 1 = (2^4)^n - 1^n$$

$$= 16^n - 1^n$$

$$16 - 1 \mid 16^n - 1^n \Rightarrow 15 \mid 16^n - 1^n$$

Hence (b) is the correct option.

$$52. \quad 3^{2n} + 7 \text{ is divisible by } 16$$

Hence (d) is the correct option.

$$53. \quad \left[\frac{1}{2} \right] + \left[\frac{1}{2} + \frac{1}{100} \right] + \dots + \left[\frac{1}{2} + \frac{99}{100} \right]$$

$$= 45$$

Hence (c) is the correct option.

$$54. \quad \text{The number of zeros at the end of}$$

$$400! = \sum_{k=1}^{\alpha} \left[\frac{400}{5^k} \right] + \dots$$

$$= 80 + 16 + 3 + 0$$

$$= 99$$

Hence (b) is the correct option.

$$55. \quad \left[\frac{n+1}{2} \right] + \left[\frac{n+2}{4} \right] + \left[\frac{n+4}{8} \right] + \dots$$

$$= \left[\frac{n}{4} \right]$$

Hence (c) is the correct option.

SECTION - IV

Matrix - Match Type

56.

	p	q	r	s
A	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
B	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
C	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>
D	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>

57.

	p	q	r	s
A	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
B	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>
C	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>
D	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>

58.

	p	q	r	s
A	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>
B	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
C	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>
D	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>

59.

	p	q	r	s
A	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
B	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
C	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>
D	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>

60.

	p	q	r	s
A	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
B	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>
C	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>
D	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>