# Sample Question Paper - 29 Mathematics-Basic (241) Class- X, Session: 2021-22 TERM II

Time Allowed : 2 hours

## **General Instructions :**

- 1. The question paper consists of 14 questions divided into 3 sections A, B, C.
- 2. Section A comprises of 6 questions of 2 marks each. Internal choice has been provided in two questions.
- *3. Section B comprises of 4 questions of 3 marks each. Internal choice has been provided in one question.*
- 4. Section C comprises of 4 questions of 4 marks each. An internal choice has been provided in one question. It contains two case study based questions.

## **SECTION - A**

- 1. Find the roots of the quadratic equation  $x^2 + 4\sqrt{2}x + 6 = 0$ .
- 2. If the distance between two parallel tangents drawn to a circle is 20 cm, then find the radius of the circle.
- 3. Find the discriminant of the quadratic equation  $\sqrt{3}x^2 2\sqrt{2}x 2\sqrt{3} = 0$ .

#### OR

The sum of the squares of two consecutive natural numbers is 41. Represent this situation in the form of a quadratic equation.

- 4. If  $d_i = x_i 25$ ,  $\sum f_i d_i = 200$ ,  $\sum f_i = 100$ , then find the mean ( $\overline{x}$ ).
- 5. If 7 is the common difference of an A.P., whose  $k^{\text{th}}$  term is  $a_k$ . Find  $a_{k+1} a_k$ . If  $a_9 = 16$ , then find  $a_{10}$ .
- **6.** If the areas of three adjacent faces of a cuboid are *x*, *y* and *z* respectively, then find the volume of the cuboid is the terms of *xyz*.

OR

The material of a cone is converted into the shape of a cylinder of equal radius. If height of the cylinder is 8 cm, then find the height of the cone.

## **SECTION - B**

7. Find the mode of the given data.

Class interval	Less than 20	Less than 40	Less than 60	Less than 80	Less than 100
Frequency	15	37	56	87	115

8. If the length of shadow of a tower on the plane ground is  $\sqrt{3}$  times the height of the tower. Then find the angle of elevation of the sun.

Maximum Marks : 40

If the angle of elevation of the sun is 30°, then find the length of the shadow cast by a tower of 150 feet height. And, if the angle of elevation changes to 45° from 30°, then find the relation between the length of tower and its shadow.

- 9. Draw a line segment of length 3.3 cm and divide it in the ratio 3 : 8. Measure the two parts.
- 10. Find the median for the following data.

Class interval	20-40	40-60	60-80	80-100
Frequency	10	12	20	22

## **SECTION - C**

11. A circle touches the side *BC* of a  $\triangle ABC$  at *P* and *AB* and *AC* when produced touches the circle at *Q* and *R*, respectively as shown in the figure. Show that  $AQ = \frac{1}{2}$  (Perimeter of  $\triangle ABC$ ).





A chord *PQ* of a circle is parallel to the tangent drawn at a point *R* of the circle. Prove that *R* bisects the arc *PRQ*.

- **12.** A manufacturer of laptop produced 6000 units in 3<sup>rd</sup> year and 7000 units in the 7<sup>th</sup> year. Assuming that production increases uniformly by a fixed number every year, find
  - (i) the production in the 1<sup>st</sup> year,
  - (ii) the production in the 5<sup>th</sup> year,
  - (iii) the production in 6<sup>th</sup> year.

# Case Study - 1

**13.** Suraj took 4 small spherical balls of silver of surface area 887.04 sq.cm each from a blacksmith. He wanted them to be made into cylindrical coins of radius one-fourth of that of the silver ball and height 4 cm.



- (i) Find the radius of each spherical ball.
- (ii) Find the curved surface area of each coin.

## Case Study - 2

14. Karan and his sister Riddhima visited at their uncle's place-Bir, Himachal Pradesh. During day time Karan, who is standing on the ground spots a paraglider at a distance of 24 m from him at an elevation of 30°. His sister Riddhima is also standing on the roof of a 6 m high building, observes the elevation of the same paraglider as 45°. Karan and Riddhima are on the opposite sides of the paraglider.



Based on the above information, answer the following questions.

- (i) Find the distance of paraglider from the ground.
- (ii) Find the distance between the paraglider and the Riddhima.

#### Solution

#### **MATHEMATICS BASIC 241**

## **Class 10 - Mathematics**

1. We have,  $x^2 + 4\sqrt{2}x + 6 = 0$   $\Rightarrow x^2 + 3\sqrt{2}x + \sqrt{2}x + 6 = 0$   $\Rightarrow x(x + 3\sqrt{2}) + \sqrt{2}(x + 3\sqrt{2}) = 0$   $\Rightarrow (x + \sqrt{2})(x + 3\sqrt{2}) = 0$   $\Rightarrow x = -\sqrt{2} \text{ or } x = -3\sqrt{2}$  $\therefore$  Roots are  $-\sqrt{2}$  and  $-3\sqrt{2}$ .

**2.** Distance between two parallel tangents drawn to a circle is the diameter of the circle.

So, radius of the circle  $=\frac{20}{2} = 10$  cm. 3. The given equation is  $\sqrt{3}x^2 - 2\sqrt{2}x - 2\sqrt{3} = 0$ . Here,  $a = \sqrt{3}$ ,  $b = -2\sqrt{2}$  and  $c = -2\sqrt{3}$ Now,  $D = b^2 - 4ac$ 

 $\Rightarrow D = (-2\sqrt{2})^2 - 4 \times \sqrt{3} \times (-2\sqrt{3}) = 8 + 24 = 32$ OR

Let the two consecutive natural numbers be *x* and x + 1. Then, their squares are  $x^2$  and  $(x + 1)^2$  respectively.

 $\therefore \text{ The required equation is, } x^2 + (x+1)^2 = 41$  $\Rightarrow x^2 + x^2 + 1 + 2x = 41$  $\Rightarrow 2x^2 + 2x - 40 = 0 \Rightarrow x^2 + x - 20 = 0$  $\textbf{4. Here, } d_i = x_i - 25 \Rightarrow a = 25.$ 

Also,  $\sum f_i d_i = 200$  and  $\sum f_i = 100$  [ $\because d_i = x_i - a$ ] Now, mean,  $\overline{x} = a + \left(\frac{\Sigma f_i d_i}{\Sigma f_i}\right) = 25 + \frac{200}{100} = 27$ 

5.  $a_k$  and  $a_{k+1}$  are successive terms of given A.P.

$$\therefore \quad a_{k+1} - a_k = d \implies a_{k+1} - a_k = 7.$$

Now,  $a_9 = 16$ 

:.  $a_{10} - a_9 = 7$  $a_{10} = 7 + 16 = 23$ 

6. Let *l*, *b* and *h* respectively be the length, breadth and height of the cuboid.

Since *x*, *y* and *z* are the areas of three adjacent faces of cuboid.

$$\therefore \quad x = lb, y = bh, z = hl$$
  
Now,  $xyz = (lb)(bh)(hl) = (lbh)^2 \Longrightarrow lbh = \sqrt{xyz}$ 

Hence, volume of the cuboid =  $\sqrt{xyz}$ 

OR

Let r be the radius of cone & cylinder and h be the height of cone.

: Volume of cone = Volume of cylinder

$$\therefore \quad \frac{1}{3}\pi r^2 h = \pi r^2(8) \Longrightarrow h = 3 \times 8 = 24 \text{ cm}$$

7. The frequency distribution table from the given data can be drawn as :

<b>Class interval</b>	Frequency
0-20	15
20-40	37 - 15 = 22
40-60	56 - 37 = 19
60-80	87 - 56 = 31
80-100	115 - 87 = 28

The modal class is 60–80 as it has the maximum frequency.

:. 
$$l = 60, f_0 = 19, f_1 = 31, f_2 = 28$$
 and  $h = 20$ 

$$\Rightarrow \text{ mode} = l + \left(\frac{f_1 - f_0}{2f_1 - f_0 - f_2}\right) \times h$$
$$= 60 + \left(\frac{31 - 19}{2 \times 21 - 19 - 28}\right) \times 20 = 76$$

8. Let *AB* be the tower of height *h* m and *BC* be the shadow of the tower, such that  $BC = \sqrt{3} h$  m. Let  $\theta$  be the angle of elevation of the sun. In  $\triangle ABC$ ,  $\tan \theta = \frac{AB}{B} = \frac{h}{B} = \frac{1}{B}$ 

$$\tan \theta = \frac{AB}{BC} = \frac{h}{\sqrt{3}h} = \frac{1}{\sqrt{3}} \qquad C \qquad \sqrt{3}h \text{ m} \qquad B$$

 $\Rightarrow \tan \theta = \tan 30^\circ \Rightarrow \theta = 30^\circ$ 

Hence, angle of elevation of the sun is 30°.

### OR

Let *AB* be the tower and *BC* be its shadow.

In 
$$\triangle ABC$$
,  $\tan 30^\circ = \frac{AB}{BC}$   
 $\Rightarrow \frac{1}{\sqrt{3}} = \frac{150}{BC}$   
 $\Rightarrow BC = 150\sqrt{3}$  feet

Hence, length of shadow of tower is  $150\sqrt{3}$  feet.

Now, angle of elevation  $= 45^{\circ}$ 

 $\therefore$  In  $\triangle ABC$ , tan  $45^\circ = \frac{AB}{BC}$  $\Rightarrow 1 = \frac{AB}{BC} \Rightarrow AB = BC$ 

 $\therefore$  Length of tower and length of its shadow are equal.

#### Steps of construction : 9.

**Step-I** : Draw a line segment AB = 3.3 cm.

**Step-II**: Draw any ray *AX*, making an acute angle with AB.

<45°

**Step-III**: Locate 11 (= 3 + 8) points  $A_1, A_2, A_3, A_4, A_5$ ,  $A_6, A_7, A_8, A_9, A_{10}$  and  $A_{11}$  on AX such that  $AA_1 = A_1A_2 = A_2A_3 = A_3A_4 = A_4A_5 = A_5A_6 = A_6A_7 =$  $A_7A_8 = A_8A_9 = A_9A_{10} = A_{10}A_{11}$ 

**Step-IV** : Join *BA*<sub>11</sub>.

**Step-V** : Through the point  $A_3$ , draw a line parallel to  $A_{11}B$  intersecting AB at the point C.

Then, AC: CB = 3:8



By measurement, we have

AC = 0.9 cm and CB = 2.4 cm.

10. The cumulative frequency distribution table from the given data can be drawn as :

Class interval	Frequency $(f_i)$	Cumulative frequency ( <i>c.f.</i> )
20-40	10	10
40-60	12	22
60-80	20	42
80-100	22	64

Here,  $n = 64 \implies \frac{n}{2} = 32$ 

So, the median class is 60-80. Thus, *f* = 20, *c.f.* = 22

$$\therefore \quad \text{Median} = l + \left(\frac{\frac{n}{2} - c.f.}{f}\right) \times h$$
$$= 60 + \left(\frac{32 - 22}{20}\right) \times 20 = 60 + 10 = 70$$

11. We know that tangents from an exterior point to a circle are equal in length.

 $\therefore$  AQ = AR ...(i), BP = BQ ...(ii), CP = CR ...(iii) Now, perimeter of  $\triangle ABC$ 

$$= AB + BC + AC = AB + BP + CP + AC$$
  
= (AB + BQ) + (CR + AC) [Using (ii) and (iii)]  
= AQ + AR  
= AQ + AQ [From (i)]  
= 2AQ

Hence,  $AQ = \frac{1}{2}$  (Perimeter of  $\triangle ABC$ )

## OR

Let tangent MN is drawn at point R of the circle having centre O. Chord PQ is drawn parallel to the tangent line MN. Draw a perpendicular line OR on MN and extend it to intersect PQ at S.



 $\therefore RS \perp PO$ 

...

In  $\Delta RPS$  and  $\Delta RQS$ ,

RS = RS	[Cor	nmon]
$\angle PSR = \angle QSR = 90^{\circ}$	['.' RS	$\perp PQ$ ]
PS = SQ [:: Perpendicular from centre t	to the	chord

bisects the chord]  $\Delta RPS \cong \Delta RQS$ [By SAS congruence criterion]  $\Rightarrow PR = QR$ [By CPCT]

We know that, if two chords are equal, then their corresponding arcs are also equal. Hence, R bisects the arc PRQ.

**12.** Let production in  $1^{st}$  year be *a* units and increase in production (every year) be *d* units.

Increase in production is constant. •.•

Unit produced every year forms an A.P. ...

Now,  $a_3 = 6000 \Longrightarrow a + 2d = 6000$ 

$$\Rightarrow a = 6000 - 2d$$
 ...(i)

and  $a_7 = 7000 \Longrightarrow a + 6d = 7000$ 

$$\Rightarrow$$
 (6000 - 2d) + 6d = 7000 [Using (i)]

 $\Rightarrow 4d = 1000 \Rightarrow d = 250$ 

Putting d = 250 in (i), we get

 $a = 6000 - 2 \times 250 = 5500$ (i) Production in first year = 5500 (ii) Production in fifth year,  $a_5 = a + 4d$  $= 5500 + 4 \times 250 = 6500$ (iii) Production in sixth year,  $a_6 = a + 5d$  $= 5500 + 5 \times 250 = 6750$ 13. (i) Let *r* be the radius of a small spherical ball.

Surface area of a spherical ball =  $887.04 \text{ cm}^2$ 

- $\Rightarrow 4\pi r^2 = 887.04$
- $\Rightarrow$  r = 8.4 cm

(ii) Radius of a cylindrical coin  $=\frac{1}{4} \times 8.4 = 2.1$  cm and height of a cylindrical coin = 4 cm

Now, curved surface area of a coin =  $2\pi rh$ 

$$=2 \times \frac{22}{7} \times 2.1 \times 4 = 52.8 \text{ cm}^2$$

14. (i) In the right  $\triangle ADQ$ , we have

$$\sin 30^\circ = \frac{DQ}{AD} \implies \frac{1}{2} = \frac{DQ}{24}$$

 $\Rightarrow DQ = 12 \text{ m}$ 

Thus, distance of paraglider from the ground is 12 m.

(ii) We have, PQ = BC = 6 m

Now, as DQ = 12 m

:. DP = DQ - PQ = 12 - 6 = 6 m

In right  $\triangle BDP$ , we have

$$\sin 45^\circ = \frac{DP}{BD} \implies \frac{1}{\sqrt{2}} = \frac{6}{BD}$$

 $\Rightarrow BD = 6\sqrt{2} m$ 

Thus, the distance of paraglider from the girl (Riddhima) is  $6\sqrt{2}$  m.