

SPEEDS OF GAS MOLECULES

Root Mean Square Speed:

- Square root of mean of square of speed of different molecules.

$$V_{rms} = \sqrt{\frac{V_1^2 + V_2^2 + \dots + V_n^2}{n}}$$

$$V_{rms} = \sqrt{\frac{3RT}{M}} = \sqrt{\frac{3P}{\rho}}$$

Average Speed:

- Arithmetic mean of speed of molecules of gas at given temperature.

$$V_{avg} = \frac{|\vec{V}_1| + |\vec{V}_2| + \dots + |\vec{V}_n|}{n}$$

$$V_{avg} = \sqrt{\frac{8RT}{\pi M}} = \sqrt{\frac{8P}{\pi \rho}}$$

SPECIAL RELATIONS

- Pressure exerted by a gas.

$$P = \frac{1}{3} \rho V_{rms}^2$$

- Relation between pressure and kinetic energy.

$$E = \frac{3}{2} PV$$

Most Probable Speed:

- Speed possessed by maximum number of molecules of gas.

$$V_{mp} = \sqrt{\frac{2RT}{M}} = \sqrt{\frac{2P}{\rho}}$$

RELATION BETWEEN KINETIC ENERGY AND TEMPERATURE

$$\text{Kinetic Energy} = \frac{3KT}{2} = \frac{1}{2} m v_{rms}^2$$

Kinetic Energy of Gas molecule.

$$\text{K.E} = \frac{1}{2} m v_{rms}^2 = \frac{3RT}{2}$$

Kinetic energy of one mole of molecule.

$$\text{K.E} = \frac{1}{2} m v_{rms}^2 = \frac{3RT}{2m}$$

Kinetic energy of one gram of gas molecule.

SPECIFIC HEAT CAPACITY

- Specific heat capacity for an ideal gas.

$$C_p - C_v = R$$

$$\text{For diatomic gas, } \frac{C_p}{C_v} = \gamma = \frac{5}{3}$$

$$\text{For diatomic gas, } \frac{C_p}{C_v} = \gamma = \frac{7}{5}$$

$$\text{For polyatomic gas, } \frac{C_p}{C_v} = \gamma = \frac{4+f}{3+f}$$

and f is degrees of freedom.

$$C_p = (1 + \frac{f}{2})R \quad C_v = fR/2$$

$$\gamma = \frac{C_p}{C_v} = 1 + \frac{2}{f}$$

DEGREES OF FREEDOM

$$\text{For monoatomic gas, } F = 3$$

- For diatomic gas.

$$(a) \text{ at room temperature, } F = 5$$

$$(b) \text{ at high temperature, } F = 7$$

- For polyatomic gas.

$$(a) \text{ at room temperature, } F = 6$$

$$(b) \text{ at high temperature, } F = 8 \quad f \rightarrow \text{degree of freedom.}$$

ASSUMPTIONS IN KINETIC THEORY OF GASES

Gas consists of small particles known as molecules.

Molecules of gas are identical rigid sphere and elastic points mass.

Molecules of gas move randomly in all directions with possible velocity.

IDEAL GAS LAWS

- Pressure, Temperature and volume of gas are related to each other by following equation, $PV = nRT$.

- P – Pressure, V – volume, n – No. of moles; R = Universal Gas Constant = 8.314 J/mol.k ; T – Temperature.

$$PV = \frac{m}{M_A} RT \quad ; \quad PV = \frac{n}{n_A} KT$$

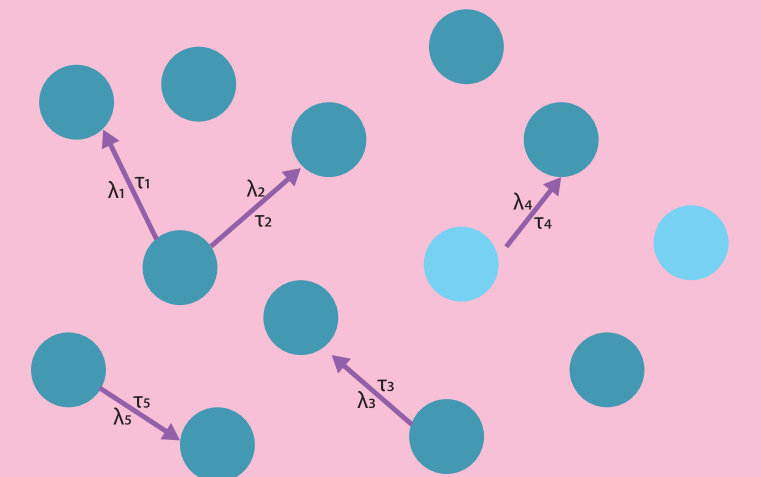
KINETIC THEORY OF GASES

Average distance travelled by molecules between two successive collision

$$\lambda_{mean} = \frac{1}{\sqrt{2} \pi d^2 n}$$

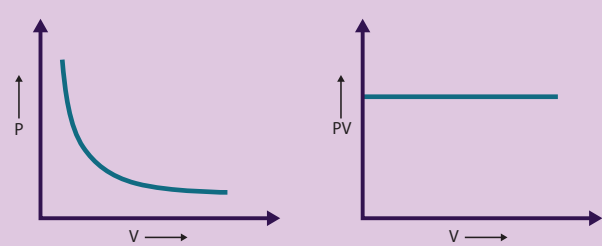
d = diameter of molecules.

n = No. of molecules per unit volume



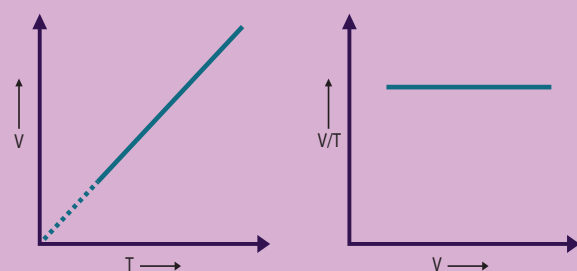
DALTON'S LAW OF PARTIAL PRESSURE

Boyle's Law



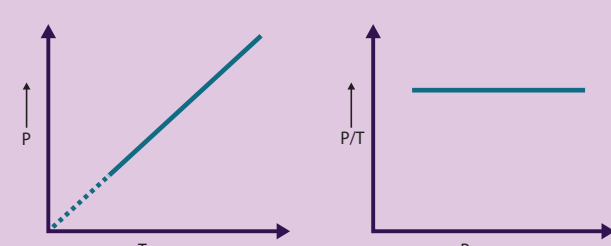
- For fixed mass, pressure of gas is inversely proportional to volume.
- $PV = \text{constant}$, if $T = \text{constant}$
- $P_1 V_1 = P_2 V_2$ when gas changes its state under constant temperature.

Charles's Law



- For a fixed mass, volume of gas is directly proportional to temperature.
- $V \propto T$; = constant; $P = \text{constant}$.
- $\frac{3}{2} PV$, when gas change its state under constant pressure.

Gay Lussac's Law



- For a fixed mass, pressure of a gas is directly proportional to its temperature.
- $P \propto T$; = constant; $V = \text{constant}$.
- When gas change its state under constant volume.

LAW OF EQUIPARTITION OF ENERGY

- The total kinetic energy of a gas molecule is equally distributed among its all degrees of freedom.

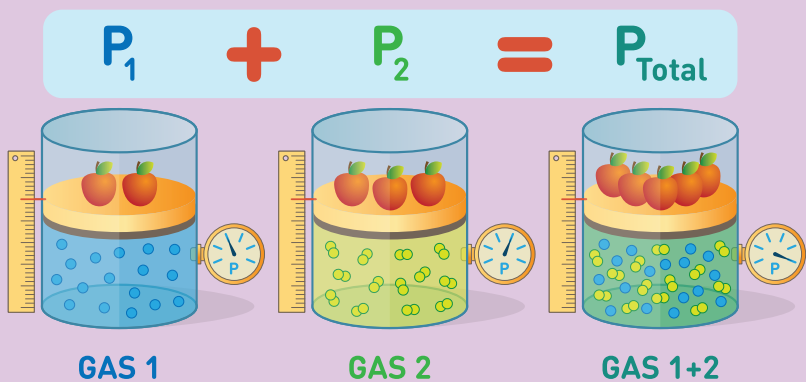
$$U = \frac{f}{2} K_B T$$

f = degrees of freedom.

K_B = Boltzmann Constant.

$$\text{For monoatomic gas, } U = \frac{3}{2} K_B T$$

$$\text{For diatomic gas, } U = \frac{5}{2} K_B T$$



Total pressure of a mixture of non-reacting gas is equal to summation of pressure of individual gases.

$$P = P_1 + P_2 + P_3 + \dots + P_n$$

