

chapter-23 Data Handling-II

Exercise-23.1

Solution-01:-

Ashish studies on three consecutive days are 4 hours, 5 hours, 3 hours.

$$\begin{aligned}\text{He studies daily on average} &= \frac{4 \text{ hours} + 5 \text{ hours} + 3 \text{ hours}}{3} \\ &= \frac{12 \text{ hours}}{3} \quad \left[\text{Mean} = \frac{\text{Sum of the observations}}{\text{No. of observations}} \right] \\ &= 4 \text{ hours.}\end{aligned}$$

∴ Ashish studies 4 hours daily on an average.

Solution-02:-

We have,

$$\begin{aligned}\text{mean runs scored} &= \frac{58+76+40+35+48+45+0+100}{8} \\ &= 50.25 \text{ Runs.}\end{aligned}$$

Thus, the mean runs scored in an innings is $\frac{50.25}{\text{Runs}}$

Solution-04:-

We have,

$$\begin{aligned}\text{mean enrollment} &= \frac{1555 + 1670 + 1750 + 2019 + 2540 + 2820}{6} \\ &= 2059.\end{aligned}$$

Thus, mean enrollment of the school for bus period is $\frac{2059}{\text{days}}$.

Solution-05:-

(i) Range of Rainfall = $20.5 - 0$

$$= 20.5$$

(ii) mean Rainfall = $\frac{0+12.2+2.1+0+20.5+5.3+1.0}{7}$

$$= 5.87 \text{ mm.}$$

(iii) 5 days was the rainfall less than mean rainfall

Solution-06:-

The heights of 5 persons are 140cm, 150cm, 152cm,
158cm and 161cm.

$$\text{mean height} = \frac{140\text{cm} + 150\text{cm} + 152\text{cm} + 158\text{cm} + 161\text{cm}}{5}$$
$$= 152.2\text{cm.}$$

Solution-07:-

We have,

$$\text{mean} = \frac{994 + 996 + 998 + 1002 + 1000}{5}$$
$$= 998.$$

Thus, mean is 998.

Solution-08:-

First five natural numbers are 1, 2, 3, 4, 5.

Let \bar{x} denote their arithmetic mean.

$$\text{Then, } \bar{x} = \frac{1+2+3+4+5}{5} = \frac{15}{5} = 3.$$

Thus, Mean = 3.

Solution-09:-

All factors of 10 are 1, 2, 5 and 10.

Let \bar{x} be the arithmetic mean.

$$\text{Then } \bar{x} = \frac{1+2+5+10}{4} = \frac{18}{4} = 4.5.$$

Solution-10:-

first 10 even natural numbers are 2, 4, 6, 8, 10,
12, 14, 16, 18, 20.

$$\text{mean} = \frac{2+4+6+8+10+12+14+16+18+20}{10} = \frac{110}{10} = 11.$$

\therefore Mean = $\bar{x} = 11.$

Solution-11:-

We have,

$$\text{mean} = \frac{x+x+2+x+4+x+6+x+8}{5}$$
$$= \frac{5x+20}{5}$$
$$= \frac{5(x+4)}{5}$$
$$= x+4.$$

Thus, Mean is $x+4.$

Solution -12 :-

first five multiples of '3' are - 3, 6, 9, 12, 15.

Let \bar{x} be the Mean.

$$\bar{x} = \frac{3+6+9+12+15}{5}$$

$$\bar{x} = \frac{45}{5}$$

$$\bar{x} = 9.$$

Thus, Mean is '9'

Solution -13 :-

We have,

$$\text{Mean } (\bar{x}) = \frac{3+4+3+6+4+2+4+5+3+9+4+1+3+8+4+5+4+4+3+6}{10}$$
$$= \frac{40}{10} \text{ kg} = 4 \text{ kg.}$$

Solution -14 :-

We have,

$$\text{Mean } (\bar{x}) = \frac{64+36+47+23+0+19+81+93+72+35+3+1}{12}$$
$$= 39.5.$$

Thus, Mean is 39.5.

Solution -15 :-

We have,

$$\text{Mean Number of children per family} = \frac{8+4+3+5+4+12+3+1+1+5}{10}$$
$$= \frac{30}{10}$$
$$= 3.$$

\therefore '3' children per family

Solution - 16 :-

We have,

$$n = \text{Number of observations} = 100$$

$$\text{Mean} = 40.$$

$$\therefore \text{Mean} = \frac{\text{Sum of the observations}}{\text{Number of observations}}$$

$$\Rightarrow \text{Mean} \times \text{No of observations} = \text{Sum of observations}$$
$$\Rightarrow 100 \times 40 = \text{Sum of observations}$$

$$\text{Thus, incorrect sum of observations} = 100 \times 40 \\ = 4,000.$$

$$\text{Correct sum of the observations} = \text{Incorrect sum of the observations} - \text{Incorrect observation} + \text{Correct observation.}$$

$$\Rightarrow \text{Correct sum of the observations} = 4,000 - 83 \\ + 53$$

$$= 39,970.$$

$$\therefore \text{Correct mean} = \frac{\text{Correct sum of the observations}}{\text{Number of observations}}$$

$$= \frac{39,970}{100}$$

$$= 39.97.$$

\therefore Correct mean is 39.97.

Solution - 17 :-

We have,

$$n = \text{Number of observations} = 5, \text{ Mean} = 27.$$

$$\text{Mean} = \frac{\text{Sum of the observations}}{\text{Number of observations}}$$

$$n = 5, \bar{x} = 27.$$

$$27 \times 5 = \text{Sum of the observations.}$$

$$135 = \text{Sum of the observations.}$$

When one number excluded

$$n = 4, \bar{x} = 25.$$

$$\bar{x} = \frac{\text{Sum of the observations}}{n} \Rightarrow \text{Sum} = 25 \times 4 \\ \Rightarrow \text{Sum} = 100.$$

$$\therefore \text{Excluded number} = \frac{\text{Sum of 5 numbers} - \text{Sum of 4 numbers}}{1} \\ = 135 - 100 = 35.$$

Solution - 18 :-

It is given that,

$$\text{Number of students} = 7.$$

$$\text{Mean} (\bar{x}) = 55 \text{ kg.}$$

The given numbers are 52, 54, 55, 53, 56, 54.

Let the seventh weight be 'k' then.

$$\text{Mean} = \frac{52 + 54 + 55 + 53 + 56 + 54 + k}{7}$$

$$\Rightarrow 55 \times 7 = 385 + k$$

$$\Rightarrow k = 385 - 324$$

$$\Rightarrow k = 61 \text{ kg.}$$

Seventh weight be 61 kg.

Solution-19:-

We have, Number of observations = 8.

Mean = 15kg

$$\text{We know that, Mean} = \frac{\text{Sum of the observations}}{\text{No. of observations}}$$

$$\Rightarrow 15\text{kg (8)} = \text{sum of the observations}$$
$$\Rightarrow \text{sum of the observations} = 120\text{kg.}$$

If each number is multiplied by '2'

$$\text{Then, sum of the observations} = 2(120\text{kg})$$
$$= 240\text{kg.}$$

$$\text{New Mean} = \frac{\text{Sum of observations}}{\text{No. of observations}} = \frac{240\text{kg}}{8}$$

$$\therefore \text{Mean}(\bar{x}) = 30\text{kg}$$

Solution-20:-

We have,

number of observations = 5; Mean(\bar{x}) = 18.

We know that-

$$\text{Mean} = \frac{\text{sum of observations}}{\text{No. of observations}}$$

$$18 = \frac{\text{sum of observations}}{5}$$

$$\Rightarrow \text{sum of observations} = 90.$$

If one number is excluded.

Mean(\bar{x}) = 16, number of observations = 4.

$$16 = \frac{\text{sum of observations}}{4}$$

$$\Rightarrow \text{sum of observations} = 64.$$

$$\therefore \text{excluded number} = \frac{\text{sum of five numbers} - \text{sum of four numbers}}{\text{Mean of four numbers}}$$

$$= 90 - 64$$

$$= 26.$$

\therefore excluded number is '26'.

Solution-21:-

Number of observations = 200.

Mean = 50.

$$\therefore \text{Mean} = \frac{\text{Sum of the observations}}{\text{number of observations}}$$

$$\Rightarrow \text{Sum of observations} = 50 \times 200 \\ = 10000$$

Thus, Incorrect sum of observations = 10000

$$\begin{aligned}\text{Correct sum of the observations} &= \text{Incorrect sum of the} \\ &\quad \text{observations} - \text{Incorrect observations} \\ &\quad + \text{correct observations}\end{aligned}$$

$$\begin{aligned}&= 10000 - (92+8) + 92+88 \\ &= 10000 - 100 + 88 \\ &\Rightarrow 10180\end{aligned}$$

$$\therefore \text{Mean} = \frac{\text{correct sum of the observations}}{\text{number of observations}}$$

$$\begin{aligned}&= \frac{10180}{200} = \frac{10180}{200} \\ &= 50.9\end{aligned}$$

$$\therefore \text{Mean } (\bar{x}) = 50.9.$$

Solution-22 :-

We have,

Mean = 27, Number of observations = 5.

We know that,

$$\text{Mean} = \frac{\text{sum of observations}}{\text{Number of observations}}$$

$$\Rightarrow \text{Number of observations} \times \text{Mean} = \text{sum of observations}$$

$$\Rightarrow \text{sum of observations} = 27 \times 5 = 135.$$

$$\therefore \text{sum of observations} = 135.$$

\therefore If one number is included

Mean = 25, Number of observations = 6.

$$\Rightarrow 25 = \frac{\text{sum of observations}}{6}$$

$$\Rightarrow 150 = \text{sum of observations}$$

$$\therefore \text{sum of observations} = 150.$$

Included number = sum of observation of 6 numbers

$$- \text{sum of observation of 5 numbers}$$

$$= 150 - 135$$

$$= 15$$

\therefore included number is '15'.

solution - 23 :-

We have, Number of observation = 75.

Mean = 35 kg.

We know that, mean = $\frac{\text{sum of observations}}{\text{No. of observations}}$

$$\Rightarrow 35 \times 75 = \text{sum of observations}$$

$$\Rightarrow \text{sum of observations} = 2625.$$

If each number is multiplied by '4'

$$\begin{aligned}\text{Then sum of observations} &= 4(2625) \\ &= 10500\end{aligned}$$

$$\therefore \text{New mean} = \frac{\text{sum of observations}}{\text{No. of observations}}$$

\\$

$$= \frac{10500}{75}$$

$$= 140.$$

\therefore New mean is 140

chapter-23 Data Handling-II

Exercise-23.2

Exercise-23.2.

Solution-01 :-

Score(x _i)	Frequency(f _i)	f _i x _i
1	2	2
2	5	10
3	1	3
4	4	16
5	6	30
6	2	12
	$\Sigma f_i = N$	$\Sigma f_i x_i = 73$

We have,

$$\text{Mean} = \frac{\sum f_i x_i}{\sum f_i}$$

$$= \frac{73}{20}$$

Mean Score = 3.65

Solution-02 :-

Wages(x _i)	No. of workers(f _i)	f _i x _i
130	2	260
150	4	600
180	6	1080
200	3	600
	$\Sigma f_i = 15$	$\Sigma f_i x_i = 2540$

We have,

$$\text{Mean Wage} = \frac{\Sigma f_i x_i}{\Sigma f_i} = \frac{2540}{15} = 169.33 \quad [\because \text{Mean} = \frac{\sum f_i x_i}{\sum f_i}]$$

Solution-03 :-

Weight(x _i)	Number of Workers (f _i)	f _i x _i
60	4	240
63	5	315
66	3	198
72	1	72
75	2	150
	$\Sigma f_i = 15$	$\Sigma f_i x_i = 975$

$$\text{We have, Mean weight} = \frac{\sum f_i x_i}{\sum f_i} = \frac{975}{15} = 65 \text{ kg}$$

\therefore Mean weight = 65 kg.

Solution-04:-

Age (in years)	Number of Students (f _i)	f _i x _i
14	15	140
15	14	210
16	10	160
17	8	136
18	3	54
	50	770

$$\text{Mean Age} = \frac{\sum f_i x_i}{\sum f_i} = \frac{770}{50} \\ = 15.4 \text{ years}$$

Solution-05:-

x	f	f _i x _i
5	4	20
6	8	48
7	14	98
8	11	88
9	3	27
	40	281

$$\text{Mean} = \frac{\sum f_i x_i}{\sum f_i} = \frac{281}{40} \\ = 7.025. \\ \therefore \text{Mean} = 7.025.$$

Solution-06:-

The heights of 5 persons are 140cm, 150cm, 152cm, 158cm and 161cm.

$$\text{mean height} = \frac{140\text{cm} + 150\text{cm} + 152\text{cm} + 158\text{cm} + 161\text{cm}}{5} \\ = 152.2\text{cm.}$$

Solution-07:-

We have,

$$\text{mean} = \frac{994 + 996 + 998 + 1002 + 1000}{5} \\ = 998.$$

Thus, mean is 998.

Solution-08:-

First five natural numbers are 1, 2, 3, 4, 5.

Let \bar{x} denote their arithmetic mean.

$$\text{Then, } \bar{x} = \frac{1+2+3+4+5}{5} = \frac{15}{5} = 3.$$

Thus, Mean = 3.

Solution-9:-

All factors of 10 are 1, 2, 5 and 10.

Let \bar{x} be the arithmetic mean.

$$\text{Then } \bar{x} = \frac{1+2+5+10}{4} = \frac{18}{4} = 4.5.$$

Solution-10:-

x	f	fx
5	2	10
8	5	40
10	8	80
12	22	264
P	7	7P
20	4	80
25	2	50
	$\sum f_i = 50$	$524 + 7P$

It is Given that,

$$\text{Mean} = 12.58.$$

$$\sum f_i = 50$$

$$\sum f_i x_i = 524 + 7P$$

We know that,

$$\text{Mean} = \frac{\sum f_i x_i}{\sum f_i}$$

$$\Rightarrow 12.58 = \frac{524 + 7P}{50}$$

$$\Rightarrow 629 - 524 = 7P$$

$$\Rightarrow 7P = 105$$

$$\Rightarrow P = \frac{105}{7}$$

$$\Rightarrow P = 15$$

Solution-12:-

x	f	fx
15	2	30
19	3	51
19	4	76
20+P	5P	$100P + 5P^2$
23	6	138
	$15 + 5P$	$295 + 100P + 5P^2$

It is Given that,

$$\text{Mean} = 20,$$

$$\sum f_i = 15 + 5P$$

$$\sum f_i x_i = 295 + 100P + 5P^2$$

$$\text{Mean} = \frac{\sum f_i x_i}{\sum f_i}$$

$$\Rightarrow 20 = \frac{295 + 100P + 5P^2}{15 + 5P}$$

$$\Rightarrow 100P + 300 = 295 + 100P + 5P^2$$

$$\Rightarrow 5P^2 + 100P - 100P = 300 - 295$$

$$\Rightarrow 5P^2 = 5$$

$$\Rightarrow P^2 = 1$$

$$\Rightarrow P = \pm 1$$

$$\Rightarrow P = 1.$$