# **States of Matter**

#### Chapter 5 States of Matter Exercise Solutions

Exercise: Solutions of Questions on Page Number: 152

Q1:

What will be the minimum pressure required to compress 500 dm3 of air at 1 bar to 200 dm3 at 30°C?

## Answer:

Given,

Initial pressure,  $p_1 = 1$  bar

Initial volume,  $V_1 = 500 \text{ dm}^3$ 

Final volume,  $V_2 = 200 \text{ dm}^3$ 

Since the temperature remains constant, the final pressure  $(p_2)$  can be calculated using Boyle's law.

According to Boyle's law,

$$p_1V_1 = p_2V_2$$

$$\Rightarrow p_2 = \frac{p_1V_1}{V_2}$$

$$= \frac{1 \times 500}{200} \text{ bar}$$

$$= 2.5 \text{ bar}$$

Therefore, the minimum pressure required is 2.5 bar.

## Q2:

A vessel of 120 mL capacity contains a certain amount of gas at 35 °C and 1.2 bar pressure. The gas is transferred to another vessel of volume 180 mL at 35 °C. What would be its pressure?

#### Answer:

Given,

Initial pressure,  $p_1 = 1.2$  bar

Initial volume,  $V_1 = 120 \text{ mL}$ 

Final volume,  $V_2 = 180 \text{ mL}$ 

Since the temperature remains constant, the final pressure  $(p_2)$  can be calculated using Boyle's law.

According to Boyle's law,

$$p_{1}V_{1} = p_{2}V_{2}$$

$$p_{2} = \frac{p_{1}V_{1}}{V_{2}}$$

$$= \frac{1.2 \times 120}{180} \text{ bar}$$

$$= 0.8 \text{ bar}$$

Therefore, the pressure would be 0.8 bar.

## Q3:

Using the equation of state pV = nRT; show that at a given temperature density of a gas is proportional to gas pressure p.

#### Answer:

The equation of state is given by,

$$pV = nRT$$
....(i)

Where,

p â†'Pressure of gas

Vâ†'Volume of gas

*n*â†' Number of moles of gas

R â†' Gas constant

Tâ†'Temperature of gas

From equation (i) we have,

$$\frac{n}{V} = \frac{p}{RT}$$

Replacing n with  $\dfrac{m}{M}$  , we have

$$\frac{m}{MV} = \frac{p}{RT}$$
....(ii)

Where,

m â†' Mass of gas

Mâ†' Molar mass of gas

$$\frac{m}{V} = d$$
But,  $\frac{m}{V} = d$  (d = density of gas)

Thus, from equation (ii), we have

$$\frac{d}{M} = \frac{p}{RT}$$
$$\Rightarrow d = \left(\frac{M}{RT}\right)p$$

Molar mass (M) of a gas is always constant and therefore, at constant temperature  $(T), \frac{M}{RT} = \text{constant}$ 

$$d = (\text{constant}) p$$
$$\Rightarrow d \propto p$$

Hence, at a given temperature, the density (a) of gas is proportional to its pressure (p)

#### Q4:

At 0°C, the density of a certain oxide of a gas at 2 bar is same as that of dinitrogen at 5 bar. What is the molecular mass of the oxide?

#### Answer:

Density (d) of the substance at temperature (7) can be given by the expression,

$$d = \frac{Mp}{RT}$$

Now, density of oxide  $(d_1)$  is given by,

$$d_1 = \frac{M_1 p_1}{RT}$$

Where,  $M_1$  and  $p_1$  are the mass and pressure of the oxide respectively.

Density of dinitrogen gas  $(d_2)$  is given by,

$$d_2 = \frac{M_2 p_2}{RT}$$

Where,  $M_2$  and  $p_2$  are the mass and pressure of the oxide respectively.

According to the given question,

$$d_1 = d_2$$

$$\therefore M_1 p_1 = M_2 p_2$$
Given,
$$p_1 = 2 bar$$

$$p_2 = 5 bar$$

Molecular mass of nitrogen,  $M_2 = 28 \text{ g/mol}$ 

Now, 
$$M_1 = \frac{M_2 p_2}{p_1}$$
$$= \frac{28 \times 5}{2}$$
$$= 70 \text{ g/mol}$$

Hence, the molecular mass of the oxide is 70 g/mol.

#### Q5:

Pressure of 1 g of an ideal gas A at 27 °C is found to be 2 bar. When 2 g of another ideal gas B is introduced in the same flask at same temperature the pressure becomes 3 bar. Find a relationship between their molecular masses.

#### Answer:

For ideal gas A, the ideal gas equation is given by,

$$p_{A}V = n_{A}RT \dots (i)$$

Where,  $p_A$  and  $n_A$  represent the pressure and number of moles of gas A.

For ideal gas B, the ideal gas equation is given by,

$$p_R V = n_R R T$$
 .....(ii)

Where,  $p_{B}$  and  $n_{B}$  represent the pressure and number of moles of gas B.

[V and T are constants for gases A and B]

From equation (i), we have

$$p_{\scriptscriptstyle A}V = \frac{m_{\scriptscriptstyle A}}{{\rm M}_{\scriptscriptstyle A}}{\rm R}T \Rightarrow \frac{p_{\scriptscriptstyle A}{\rm M}_{\scriptscriptstyle A}}{m_{\scriptscriptstyle A}} = \frac{{\rm R}T}{V}$$
.....(iii)

From equation (ii), we have

$$p_{\rm B}V = \frac{m_{\rm B}}{\rm M_{\rm B}}RT \Rightarrow \frac{p_{\rm B}M_{\rm B}}{m_{\rm B}} = \frac{RT}{V}$$
 .....(iv)

Where, M<sub>A</sub> and M<sub>B</sub> are the molecular masses of gases A and B respectively.

Now, from equations (iii) and (iv), we have

$$\frac{p_A \mathbf{M}_A}{m_A} = \frac{p_B \mathbf{M}_B}{m_B} \dots (v)$$

Given,

$$m_A = 1 \text{ g}$$
  
 $p_A = 2 \text{ bar}$   
 $m_B = 2 \text{ g}$   
 $p_B = (3-2) = 1 \text{ bar}$ 

(Since total pressure is 3 bar)

Substituting these values in equation (v), we have

$$\frac{2 \times M_A}{1} = \frac{1 \times M_B}{2}$$
$$\Rightarrow 4M_A = M_B$$

Thus, a relationship between the molecular masses of A and B is given by

$$4M_A = M_B$$

#### Q6:

The drain cleaner, Drainex contains small bits of aluminum which react with caustic soda to produce dihydrogen. What volume of dihydrogen at 20 °C and one bar will be released when 0.15g of aluminum reacts?

#### Answer:

The reaction of aluminium with caustic soda can be represented as:

$$2AI + 2NaOH + 2H_2O \longrightarrow 2NaAlO_2 + 3H_2$$
  
 $2 \times 27g$   $3 \times 22400 \text{ mL}$ 

At STP (273.15 K and 1 atm), 54 g (2  $\times$  27 g) of Al gives 3  $\times$  22400 mL of H<sub>2...</sub>

$$\ \, \frac{3\times22400\times0.15}{54}\,\mathrm{mL}\,\,\mathrm{of}\,\mathrm{H_2}$$
 i.e., 186.67 mL of  $\mathrm{H_2}$ 

At STP.

$$p_1 = 1$$
 atm  
 $V_1 = 186.67$  mL  
 $T_1 = 273.15$  K

Let the volume of dihydrogen be  $V_2$  at  $p_2$  = 0.987 atm (since 1 bar = 0.987 atm) and  $T_2$  = 20°C = (273.15 + 20) K = 293.15 K.

Now,  

$$\frac{p_1 V_1}{T_1} = \frac{p_2 V_2}{T_2}$$

$$\Rightarrow V_2 = \frac{p_1 V_1 T_2}{p_2 T_1}$$

$$= \frac{1 \times 186.67 \times 293.15}{0.987 \times 273.15}$$

$$= 202.98 \text{ mL}$$

= 203 mL

Therefore, 203 mL of dihydrogen will be released.

#### Q7:

What will be the pressure exerted by a mixture of 3.2 g of methane and 4.4 g of carbon dioxide contained in a 9 dm³ flask at 27 °C ?

#### Answer:

It is known that,

$$p = \frac{m}{M} \frac{RT}{V}$$

For methane (CH<sub>4</sub>),

$$p_{\text{CH}_4} = \frac{3.2}{16} \times \frac{8.314 \times 300}{9 \times 10^{-3}} \left[ \frac{\text{Since 9 dm}^3 = 9 \times 10^{-3} \text{m}^3}{27^{\circ}\text{C} = 300\text{K}} \right]$$
$$= 5.543 \times 10^4 \,\text{Pa}$$

For carbon dioxide (CO<sub>2</sub>),

$$p_{\text{CO}_2} = \frac{4.4}{44} \times \frac{8.314 \times 300}{9 \times 10^{-3}}$$
$$= 2.771 \times 10^4 \text{ Pa}$$

Total pressure exerted by the mixture can be obtained as:

$$p = p_{\text{CH}_4} + p_{\text{CO}_2}$$
  
=  $(5.543 \times 10^4 + 2.771 \times 10^4) \text{ Pa}$   
=  $8.314 \times 10^4 \text{ Pa}$ 

Hence, the total pressure exerted by the mixture is  $8.314 \times 10^4 \text{ Pa}$ .

#### Q8:

What will be the pressure of the gaseous mixture when 0.5 L of H<sub>2</sub> at 0.8 bar and 2.0 L of dioxygen at 0.7 bar are introduced in a 1L vessel at 27°C?

#### Answer:

Let the partial pressure of  $H_2$  in the vessel be  $P_{H_2}$ .

Now,

$$p_1 = 0.8 \text{ bar}$$
  $p_2 = p_{H_2} = ?$ 

$$p_2 = p_{H_2} - 2$$

$$V_1 = 0.5 \, \text{L}$$
  $V_2 = 1 \, \text{L}$ 

$$V_2 = 11$$

It is known that,

$$p_1V_1 = p_2V_2$$

$$\Rightarrow p_2 = \frac{p_1 V_1}{V_2}$$

$$\Rightarrow p_{H_2} = \frac{0.8 \times 0.5}{1}$$
$$= 0.4 \text{ bar}$$

Now, let the partial pressure of  ${\sf O_2}$  in the vessel be  ${\it p}_{{\sf O_2}}$  .

Now,

$$p_1 = 0.7 \, \text{bar}$$

$$p_1 = 0.7 \, \text{bar}$$
  $p_2 = p_{O_2} = ?$ 

$$V_1 = 2.0 \text{ L}$$

$$V_1 = 2.0 \text{ L}$$
  $V_2 = 1 \text{ L}$ 

 $p_1V_1=p_2$ 

## Q9:

Density of a gas is found to be 5.46 g/dm³ at 27 °C at 2 bar pressure. What will be its density at STP?

# Answer:

Given,

$$d_1 = 5.46 \text{ g/dm}^3$$

$$p_1 = 2 \text{ bar}$$

$$T_1 = 27^{\circ}\text{C} = (27 + 273)\text{K} = 300\text{K}$$

$$p_2 = 1 \text{ bar}$$

$$T_2 = 273 \text{ K}$$

$$d_2 = ?$$

The density  $(d_2)$  of the gas at STP can be calculated using the equation,

$$d = \frac{Mp}{RT}$$

$$\therefore \frac{d_1}{d_2} = \frac{\frac{Mp_1}{RT_1}}{\frac{Mp_2}{RT_2}}$$

$$\Rightarrow \frac{d_1}{d_2} = \frac{p_1T_2}{p_2T_1}$$

$$\Rightarrow d_2 = \frac{p_2T_1d_1}{p_1T_2}$$

$$= \frac{1 \times 300 \times 5.46}{2 \times 273}$$

$$= 3 \text{ g dm}^{-3}$$

Hence, the density of the gas at STP will be 3 g dm<sup>ae-3</sup>.

#### Q10:

 $34.05 \, \text{mL}$  of phosphorus vapour weighs  $0.0625 \, \text{g}$  at  $546 \, ^{\circ}\text{C}$  and  $0.1 \, \text{bar}$  pressure. What is the molar mass of phosphorus?

#### Answer:

Given,

p = 0.1 bar

$$V = 34.05 \text{ mL} = 34.05 \times 10^{\text{a} \cdot \text{c}} \text{ L} = 34.05 \times 10^{\text{a} \cdot \text{c}} \text{ dm}^{\text{3}}$$

 $R = 0.083 \text{ bar dm}^3 \text{ K}^{\text{a}\text{c}^{-1}} \text{ mol}^{\text{a}\text{c}^{-1}}$ 

$$T = 546$$
°C =  $(546 + 273)$  K = 819 K

The number of moles (n) can be calculated using the ideal gas equation as:

$$pV = nRT$$

$$\Rightarrow n = \frac{pV}{RT}$$

$$= \frac{0.1 \times 34.05 \times 10^{-3}}{0.083 \times 819}$$

$$= 5.01 \times 10^{-5} \text{ mol}$$

$$=\frac{0.0625}{5.01\times10^{-5}}=1247.5~\text{g mol}^{\text{ac-1}}$$
 Therefore, molar mass of phosphorus

Hence, the molar mass of phosphorus is 1247.5 g mol<sup>ae-1</sup>.

### Q11:

A student forgot to add the reaction mixture to the round bottomed flask at 27 °C but instead he/she placed the flask on the flame. After a lapse of time, he realized his mistake, and using a pyrometer he found the temperature of the flask was 477 °C. What fraction of air would have been expelled out?

## Answer:

Let the volume of the round bottomed flask be V.

Then, the volume of air inside the flask at 27° C is V.

Now,

 $V_1 = V$ 

 $T_1 = 27^{\circ}\text{C} = 300 \text{ K}$ 

 $V_2 = ?$ 

 $T_2 = 477^{\circ} \text{ C} = 750 \text{ K}$ 

According to Charles's law,

$$\frac{V_1}{T_1} = \frac{V_2}{T_2}$$

$$\Rightarrow V_2 = \frac{V_1 T_2}{T_1}$$

$$= \frac{750V}{300}$$

$$= 2.5 \text{ V}$$

Therefore, volume of air expelled out = 2.5  $V \hat{a} \in V = 1.5 V$ 

$$=\frac{1.5V}{2.5V}=\frac{3}{5}$$

Hence, fraction of air expelled out

## Q12:

Calculate the temperature of 4.0 mol of a gas occupying 5 dm<sup>3</sup> at 3.32 bar.

 $(R = 0.083 \text{ bar dm}^3 \text{ K}^{-1} \text{ mol}^{-1}).$ 

#### Answer:

Given,

n = 4.0 mol

 $V = 5 \text{ dm}^3$ 

p = 3.32 bar

 $R = 0.083 \text{ bar dm}^3 \text{ K}^{\text{a}\text{e}^{\text{u}}\text{1}} \text{ mol}^{\text{a}\text{e}^{\text{u}}\text{1}}$ 

The temperature (T) can be calculated using the ideal gas equation as:

$$pV = nRT$$

$$\Rightarrow T = \frac{pV}{nR}$$

$$= \frac{3.32 \times 5}{4 \times 0.083}$$

$$= 50 \text{ K}$$

Hence, the required temperature is 50 K.

## Q13:

Calculate the total number of electrons present in 1.4 g of dinitrogen gas.

## Answer:

Molar mass of dinitrogen (N₂) = 28 g mol<sup>â€⁻1</sup>

$$N_2 = \frac{1.4}{28} = 0.05 \ mol$$
 Thus, 1.4 g of

=  $0.05 \times 6.02 \times 10^{23}$  number of molecules

=  $3.01 \times 10^{23}$  number of molecules

Now, 1 molecule of  $N_2$  contains 14 electrons.

Therefore, 3.01  $\times$  10<sup>23</sup> molecules of N<sub>2</sub> contains = 1.4  $\times$  3.01  $\times$  10<sup>23</sup>

 $= 4.214 \times 10^{23}$  electrons

#### Q14:

How much time would it take to distribute one Avogadro number of wheat grains, if 10<sup>10</sup> grains are distributed each second?

## Answer:

Avogadro number =  $6.02 \times 10^{23}$ 

Thus, time required

$$= \frac{6.02 \times 10^{23}}{10^{10}} \text{ s}$$

$$= 6.02 \times 10^{23} \text{ s}$$

$$= \frac{6.02 \times 10^{23}}{60 \times 60 \times 24 \times 365} \text{ years}$$

$$= 1.909 \times 10^{6} \text{ years}$$

Hence, the time taken would be  $1.909 \times 10^6 \, years$ 

## Q15:

Calculate the total pressure in a mixture of 8 g of dioxygen and 4 g of dihydrogen confined in a vessel of 1  $dm^3$  at 27°C. R = 0.083 bar  $dm^3$  K<sup>-1</sup> mol<sup>-1</sup>.

## Answer:

Given,

Mass of dioxygen  $(O_2) = 8 g$ 

$$O_2 = \frac{8}{32} = 0.25$$
 mole

Thus, number of moles of

Mass of dihydrogen  $(H_2) = 4 g$ 

$$H_2 = \frac{4}{2} = 2 \text{ mole}$$

Thus, number of moles of

Therefore, total number of moles in the mixture = 0.25 + 2 = 2.25 mole

Given,

$$V = 1 \text{ dm}^3$$

$$n = 2.25 \text{ mol}$$

 $R = 0.083 \text{ bar dm}^3 \text{ K}^{\text{a}\text{e}^{\text{u}}\text{1}} \text{ mol}^{\text{a}\text{e}^{\text{u}}\text{1}}$ 

$$T = 27^{\circ}\text{C} = 300 \text{ K}$$

Total pressure (p) can be calculated as:

$$pV = nRT$$

$$\Rightarrow p = \frac{nRT}{V}$$

$$= \frac{225 \times 0.083 \times 300}{1}$$
= 56.025 bar

Hence, the total pressure of the mixture is 56.025 bar.

## Q16:

Pay load is defined as the difference between the mass of displaced air and the mass of the balloon. Calculate the pay load when a balloon of radius 10 m, mass 100 kg is filled with helium at 1.66 bar at  $27^{\circ}$ C. (Density of air = 1.2 kg m³ and R = 0.083 bar dm³ K¹ mol¹).

#### Answer:

Given,

Radius of the balloon, r = 10 m

$$\frac{1}{2} = \frac{4}{3} \pi r^2$$

$$= \frac{4}{3} \times \frac{22}{7} \times 10^{3}$$
  
= 4190.5 m<sup>3</sup> (approx)

Thus, the volume of the displaced air is 4190.5 m<sup>3</sup>.

Given,

Density of air = 1.2 kg m<sup>a∈3</sup>

Then, mass of displaced air =  $4190.5 \times 1.2 \text{ kg}$ 

$$= 5028.6 \text{ kg}$$

Now, mass of helium (m) inside the balloon is given by,

$$m = \frac{MpV}{RT}$$

Here,

$$M = 4 \times 10^{-3} \text{kg mol}^{-1}$$

$$p = 1.66 \, \text{bar}$$

$$V =$$
Volume of the balloon

$$=4190.5 \text{ m}^3$$

$$R = 0.083 \, \text{bar dm}^3 \, K^{-1} \text{mol}^{-1}$$

$$T = 27^{\circ}\text{C} = 300\text{K}$$

Then, 
$$m = \frac{4 \times 10^{-3} \times 1.66 \times 4190.5 \times 10^{3}}{0.083 \times 300}$$
  
= 1117.5 kg (approx)

Now, total mass of the balloon filled with helium = (100 + 1117.5) kg

$$= 1217.5 \text{ kg}$$

Hence, pay load = (5028.6 – 1217.5) kg = 3811.1 kg

Hence, the pay load of the balloon is 3811.1 kg.

## Q17:

Calculate the volume occupied by 8.8 g of CO<sub>2</sub> at 31.1°C and 1 bar pressure.

 $R = 0.083 \text{ bar } L \text{ K}^{-1} \text{ mol}^{-1}$ .

#### Answer:

It is known that,

$$pV = \frac{m}{M}RT$$
$$\Rightarrow V = \frac{mRT}{Mp}$$

Here,

m = 8.8 g

 $R = 0.083 \text{ bar } LK^{a \in 1} \text{ mol}^{a \in 1}$ 

$$T = 31.1$$
°C = 304.1 K

M = 44 g

p = 1 bar

Thus, volume 
$$(V) = \frac{8.8 \times 0.083 \times 304.1}{44 \times 1}$$
  
= 5.04806 L  
= 5.05 L

Hence, the volume occupied is 5.05 L.

# Q18:

2.9 g of a gas at 95  $^{\circ}$ C occupied the same volume as 0.184 g of dihydrogen at 17  $^{\circ}$ C, at the same pressure. What is the molar mass of the gas?

#### Answer:

Volume (V) occupied by dihydrogen is given by,

$$V = \frac{m}{M} \frac{RT}{p}$$
$$= \frac{0.184}{2} \times \frac{R \times 290}{p}$$

Let M be the molar mass of the unknown gas. Volume (V) occupied by the unknown gas can be calculated as:

$$V = \frac{m}{M} \frac{RT}{p}$$
$$= \frac{2.9}{M} \times \frac{R \times 368}{p}$$

According to the question,

$$\frac{0.184}{2} \times \frac{R \times 290}{p} = \frac{2.9}{M} \times \frac{R \times 368}{p}$$

$$\Rightarrow \frac{0.184 \times 290}{2} = \frac{2.9 \times 368}{M}$$

$$\Rightarrow M = \frac{2.9 \times 368 \times 2}{0.184 \times 290}$$

$$= 40 \text{ g mol}^{-1}$$

Hence, the molar mass of the gas is 40 g molac1.

#### Q19:

A mixture of dihydrogen and dioxygen at one bar pressure contains 20% by weight of dihydrogen. Calculate the partial pressure of dihydrogen.

## Answer:

Let the weight of dihydrogen be 20 g and the weight of dioxygen be 80 g.

 $n_{\rm H_2} = \frac{20}{2} = 10$  moles and the number of moles of

Then, the number of moles of dihydrogen,

 $n_{\rm O_2} = \frac{80}{32} = 2.5$  moles

Given,

Total pressure of the mixture,  $p_{total} = 1$  bar

Then, partial pressure of dihydrogen,

$$p_{\rm H_2} = \frac{n_{\rm H_2}}{n_{\rm H_2} + n_{\rm O_2}} \times P_{\rm total}$$
$$= \frac{10}{10 + 2.5} \times 1$$
$$= 0.8 \text{ bar}$$

Hence, the partial pressure of dihydrogen is  $0.8\ bar$  .

## Q20:

What would be the SI unit for the quantity  $pV^2T^2/n$ ?

## Answer:

The SI unit for pressure, p is Nm<sup>ae-2</sup>.

The SI unit for volume, V is m3.

The SI unit for temperature, T is K.

The SI unit for the number of moles, *n* is mol.

 $\frac{pV^2T^2}{n}$ 

Therefore, the SI unit for quantity n is given by,

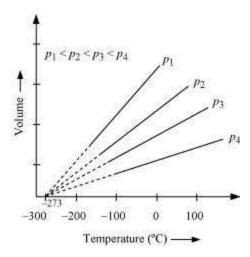
$$= \frac{\left(Nm^{-2}\right)\left(m^{3}\right)^{2}\left(K\right)^{2}}{\text{mol}}$$
$$= Nm^{4}K^{2} \text{ mol}^{-1}$$

## Q21:

In terms of Charles' law explain why -273°C is the lowest possible temperature.

#### Answer:

Charles' law states that at constant pressure, the volume of a fixed mass of gas is directly proportional to its absolute temperature.



It was found that for all gases (at any given pressure), the plots of volume vs. temperature (in °C) is a straight line. If this line is extended to zero volume, then it intersects the temperature-axis at - 273°C. In other words, the volume of any gas at -273°C is zero. This is because all gases get liquefied before reaching a temperature of - 273°C. Hence, it can be concluded that - 273°C is the lowest possible temperature.

## Q22:

Critical temperature for carbon dioxide and methane are 31.1 °C and -81.9 °C respectively. Which of these has stronger intermolecular forces and why?

## Answer:

Higher is the critical temperature of a gas, easier is its liquefaction. This means that the intermolecular forces of attraction between the molecules of a gas are directly proportional to its critical temperature. Hence, intermolecular forces of attraction are stronger in the case of CO<sub>2</sub>.

## Q23:

Explain the physical significance of Van der Waals parameters.

# Answer:

# Physical significance of 'a':

'a' is a measure of the magnitude of intermolecular attractive forces within a gas.

# Physical significance of 'b':

'b' is a measure of the volume of a gas molecule.