Areas of Parallelograms and Triangles

IIT Foundation Material



a:b=2:31. Let a = 2x, b = 3x₽₽ M x N $a + b = 90^{\circ}$ $2x + 3x = 90^{\circ}$ \Rightarrow $5x^{\circ} = 90^{\circ}$ \Rightarrow $x^{\circ} = 18^{\circ}$ \Rightarrow $a = 36^{\circ}$ and $b = 54^{\circ}$ \Rightarrow $|b+|c=180^{\circ}$ (:: linear pair) $54^{\circ} + |c| = 180^{\circ}$ \Rightarrow $|c=180^{\circ}-54^{\circ}=136^{\circ}$ Hence (c) is the correct option.



 $\Rightarrow \qquad \frac{|b^{\circ}|}{|x_{MY}|} = 40^{\circ}$ (:: alterate angles) $\frac{|X_{MY}|}{|x_{MY}|} = a^{\circ} + b^{\circ} = 45^{\circ} + 40^{\circ} = 85^{\circ}$ Hence (d) is the correct option.

3.





$$\Delta QRS$$

$$|SQR + 85^{\circ} + 70^{\circ} = 180^{\circ}$$

$$\Rightarrow |SQR = 180^{\circ} - 155^{\circ}$$

$$= 45^{\circ}$$

$$SQ \parallel RT$$

$$\Rightarrow |SQR = |QRT = 45^{\circ}$$
(alterate angles)
Hence (a) is the correct option.



6.



$$\Rightarrow PQ \parallel XZ$$
(:: converse of Basic proportionality theorem)
 $\Delta YPQ \sim \Delta XYZ$

$$\Rightarrow Area of \Delta YPQ : Area of \Delta XYZ$$

$$\Rightarrow \frac{PQ^2}{XZ^2} = \frac{2^2}{3^2} = \frac{4}{9}$$

$$\left(\because \frac{PQ}{XZ} = \frac{2}{3} \right)$$

Hence (a) is the correct option.

7.

 \Rightarrow



Since centroid G devides the medium in the ratio 2:1 Hence (d) is the correct option.



=8cm

(:: The perpendicular drawn from the centre to a chord bisets the chord)

$$OA = 10cm$$

(:: OA is radius)
$$\Delta OAE$$
$$OE^2 = OA^2 - AE^2$$
$$= 10^2 - 8^2$$
$$= 6^2$$
$$OE = 6cm$$

Hence (d) is the correct option.









 $|\underline{A}XZ =$ $|\underline{A}XZ = 165$ Hence (d) is the correct option.

11.



 $60^{\circ}, 60^{\circ}, 120^{\circ}, 120^{\circ}$ Hence (b) is the correct option.

12.



A B C D E is a regular Pentagon. Alternative vertices are joined to make a five pointed star A B C D E. The sum of 5 vertical angles of this star is 180° Hence (b) is the correct option.



Hence (a) is the correct option.

14.

 \Rightarrow

 \Rightarrow

 \Rightarrow





Hence (d) is the correct option.









(: Basic Proportionality Theorum)

$$\frac{2}{6} = \frac{PQ}{20}$$

$$\Rightarrow PQ = \frac{2}{8} \times 20 = \frac{20}{4} = 5cm$$
Area of Trapezium P Q N M
Area of \Delta LPQ

$$= \frac{\text{Area of } \Delta LMN - \text{Area of } \Delta LPQ}{\text{Area of } \Delta LPQ}$$

$$= \frac{\text{Area of } \Delta LMN}{\text{Area of } \Delta LPQ} - 1$$

$$= \frac{20^{2}}{5^{2}} - 1$$

$$= \frac{400}{25} - 1$$

$$= 15 - 1 = 14cm$$
Hence (b) is the correct option.



Area of
$$\triangle CEO = \frac{1}{2} (\text{Area of } \triangle COB)$$

 \Rightarrow Area of
 $\triangle CEO = \frac{1}{8} (\text{Area of paralleo gram A B C D})$
 \Rightarrow Hence (a) is the correct option.

 \Rightarrow







$$\Delta ABM
AB^{2} = AM^{2} + BM^{2}
17^{2} = AM^{2} + 8^{2}
AM^{2} = 17^{2} - 8^{2}
= 289 - 64 = 225 = 15^{2}
AM = 15cm
OM = $\frac{1}{3}(15) = 5cm$
 $\Delta OBM
OB^{2} = OM^{2} + BM^{2}
= 5^{2} + 8^{2}
= 25 + 64 = 89
OB\sqrt{89}cm$
Hence (a) is the correct option.$$







Hence (b) is the correct option.

23.



- **24.** The length of the diagonal = 15 cm Hence (b) is the correct option.
- **25.** Triangle A B C the altitude through A has length h, is right angled at A. Then

 $\frac{1}{b^2} + \frac{1}{c^2} - \frac{1}{h^2} = 0$ Since Area of the triangle A B C

$$\Rightarrow \frac{1}{2}ah = \frac{1}{2}bc$$

$$\Rightarrow ah = bc$$

$$\Rightarrow \frac{1}{b^2} + \frac{1}{c^2} = \frac{b^2 + c^2}{b^2c^2}$$

$$= \frac{a^2}{(bc)^2} = \frac{a^2}{(ah)^2}$$

$$= \frac{a^2}{a^2h^2}$$

$$= \frac{1}{h^2}$$

$$\Rightarrow \frac{1}{b^2} + \frac{1}{c^2} - \frac{1}{h^2} = 0$$
Hence (b) is the correct option.

- **26.** If the height of the rectangle is 4 then the width of the rectangle $=32\sqrt{2}$ Hence (a) is the correct option.
- **27.** The radii of circle $c_1, c_2, \dots, c_{2004}$ are respectively $r_1, r_2, \dots, r_{2004}$. If $r_1 = 1, r_i = r_{n+1}$ for $i-1, 2, 3, \dots, 2004$ the $r_{2004} = 2004$ Hence (a) is the correct option.

SECTION - II Assertion - Reason Questions

28. The Digonals of a parallelogram are bisect each other The diagonals of Rhombus are perpendicular to each other. Hence (a) is the correct option. **29.** $DF \parallel BC$ $\Rightarrow DF = \frac{1}{2}BC$ $= \frac{1}{2}(15)$ = 7.5cm(\because Converse of Mid-point Theorum) Hence (a) is the correct option.

30. In a trapezium, the segment joining the Mid Points its non parallel sides is parallel to it's parallel sides and half the sum of parallelsides.

and

The figure formed by joining the Mid-Points of the sides of a rectangle in order is a rhombus. Hence (b) is the correct option.

31. If 'O' is the Mid point of AC then 0 is circumcentre of $\triangle ABC$

$$\Rightarrow \qquad OA = OB = OC =$$

The figure formed by joining the Mid Points of the sides of a square in order another square.

Hence (b) is the correct option.

 $\frac{AC}{2}$

- 32. The area of a parallelogram is product of any of its side and corresponding altitudes.Area of triangle is half the product of any its sides and the corresponding altitudes.Hence (b) is the correct option.
- **33.** AD is the Median and E is the Mid Point of AD. Area of $\triangle AED$

 $=\frac{1}{2}$ Area of $\triangle ABC$

(:: The Median AD devides $\triangle ABC$ in to two triangles which are equal in Area)

Area of $\triangle AED$

$$= \frac{1}{2} (\text{Area of } \Delta \text{ABD})$$
$$= \frac{1}{2} = \left(\frac{1}{2} \text{Area of } \Delta \text{ABC}\right)$$
$$= \frac{1}{4} \text{Area of } \Delta \text{ABC}$$

Hence (a) is the correct option.

$$34. \qquad \underline{AOB} = 180^{\circ}$$

$$\underline{|APB|} = \frac{1}{2} (180^\circ)$$
$$= 90^\circ'$$

The angle at a semi circle is 90° .

In equal circles if two are equal. They subtend equal angles at their correspondingly centres.

Hence (b) is the correct option.

- **35.** The angle in the semi circle is 90°. Hence (a) is the correct option.
- **36.** Angle in a semi circle is 90°. Since angle subtended by an arc at the centre is double to the angle subtended by the same arc at any point on the circumference of the circle. Hence (b) is the correct option.

SECTION - III Linked Comprehension Type

- **37.** $AB = 2 \times EF$ = 2×4=8 $BC = 2 \times DE$ = 2×3=6 $AC = 2 \times DF$ = 2×3.5=7 \Rightarrow Lengths of AB, AC and BC are 8, 7, 6 Hence (b) is the correct option.
- **38.** The perimeter of $\triangle ABC$ =8+7+6=21*cm* Hence (a) is the correct option.
- **39.** Area of $\triangle ABC$ = 4 Area of $\triangle DEF$ Hence (d) is the correct option.

40. DE = EF
Since
$$\frac{AB}{BC} = \frac{DE}{EF}$$

 $\frac{AB}{AB} = \frac{DE}{EF}$
($\because AB = BC$)
 $\Rightarrow DE = EF$
Hence (a) is the correct option.

41.
$$BX = \frac{1}{2}AD$$

Hence (b) is the correct option.

$$42. \qquad BE = \frac{1}{2} (AD + CF)$$

$$\Rightarrow AD + CF = 2BE$$

Hence (d) is the correct option.

43.
$$BG = 6cm$$

 $BG = \frac{2}{3}BE$
 $\Rightarrow \qquad 6 = \frac{2}{3}BE$
 $\Rightarrow \qquad B = \frac{18}{2} = 9cm$
 $GE = BE - BG = 9 - 6 = 3cm$
Hence (a) is the correct option

44.
$$FG = \frac{1}{3}CF$$

 $\Rightarrow 4 = \frac{1}{3}CF$

$$\Rightarrow CF = 12cm$$

$$CG = CF - FG = 12 - 4 = 8cm$$
Hence (b) is the correct option.

45.
$$AD = 7.5cm$$

 $\Rightarrow \quad GD = \frac{1}{3}AD$
 $= \frac{1}{3}(7.5)$
 $= 2.5cm$
Hence (c) is the correct option.

46. Area of $\triangle ABC$ = $\frac{1}{2} \times 8 \times 4$ = $16cm^2$ Hence (a) is the correct option.

47. Area of
$$\triangle ABC$$

 $16 = \frac{1}{2} \times 5 \times BC$
 $\Rightarrow \frac{16 \times 2}{5} = BC$
 $\Rightarrow BC = 6.4cm$
Hence (b) is the correct option.
48. $\triangle ABE$
 $BE^2 = AB^2 - AE^2$
 $= 8^2 - 5^2$
 $= 64 - 25$
 $= 39$
 $BE = \sqrt{39}cm$
Hence (b) is the correct option.

- **49.** $|\underline{R}PB = 30^{\circ}$ Hence (a) is the correct option.
- **50.** $|PBR| = 115^{\circ}$ Hence (b) is the correct option.
- **51.** $|BRP = 35^{\circ}$ Hence (c) is the correct option.
- **52.** Area of $\Delta(AQR)$ = Area of $\Delta(BPQ)$ ($\because PR = BC$) Hence (a) is the correct option. **53.** Area of ΔCPR = Area of ΔCAR Hence (b) is the correct option.

54. Area of $\triangle PQC$ = Area of $\triangle AQR$ Hence (c) is the correct option.

