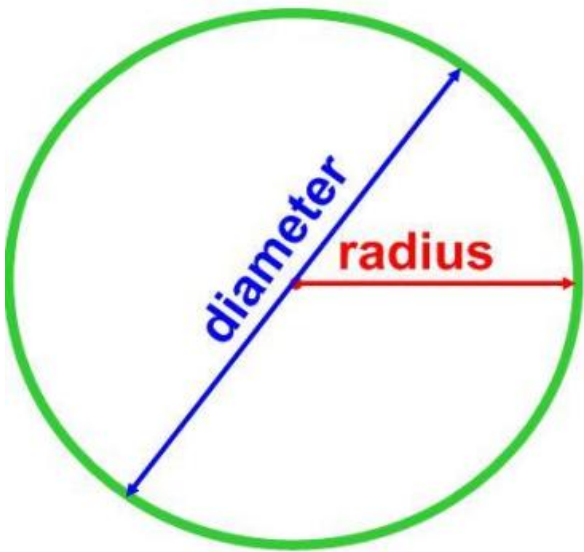


Areas Of Circle, Sector & Segment

Exercise 18



Area of a circle
 $= \pi \times \text{radius}^2$

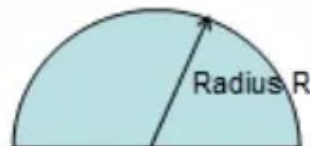
Circumference of a
circle $= \pi \times \text{diameter}$

remember that the
diameter $= 2 \times \text{radius}$

AREA OF A SEMICIRCLE

- A semicircle is just **half of a circle**. To find the area of a semicircle we just take **half of the area of a circle**.
- So, the formula for the area of a semicircle is:

$$\text{Area} = \frac{1}{2} \pi r^2$$



AREA OF A SECTOR

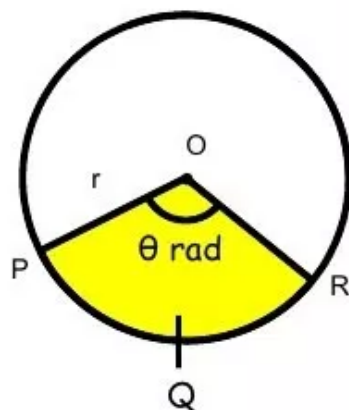
The area of a sector, A is proportional to the angle subtended at the centre of the circle.

$$\frac{\text{Area of sector OPQR}}{\text{Area of circle}} = \frac{\theta}{2\pi}$$

$$\frac{A}{\pi r^2} = \frac{\theta}{2\pi}$$

$$A = \frac{\theta}{2\pi} \times \pi r^2$$

$$A = \frac{1}{2} r^2 \theta$$



Measurement of area of sector of a circle in Radian

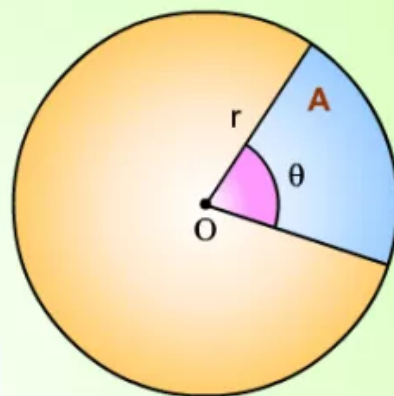
In general, if the angle of a sector, θ , is measured in degree,

then the **area of the sector**, $A = \frac{\theta}{360} \times \pi r^2$

If θ is measured in **radians**,

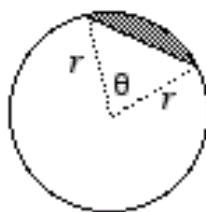
then the area of the sector, $A = \frac{\theta}{2\pi} \times \pi r^2$ $2\pi \text{ rad} = 360^\circ$

$$\therefore A = \frac{1}{2} r^2 \theta$$



Segment of a Circle
(shaded)

$$\begin{aligned} \text{Area} &= \frac{1}{2} r^2 (\theta - \sin \theta) \quad (\text{radians}) \\ &= \frac{1}{2} r^2 \left(\frac{\pi}{180} \theta - \sin \theta \right) \quad (\text{degrees}) \end{aligned}$$



Question 1:

$$\text{Radius} = \frac{\text{Diameter}}{2} = \frac{35}{2} \text{ cm}$$

$$\text{Circumference of circle} = 2\pi r = \left(2 \times \frac{22}{7} \times \frac{35}{2}\right) \text{ cm} = 110 \text{ cm}$$

$$\begin{aligned} \therefore \text{Area of circle} &= \pi r^2 = \left(\frac{22}{7} \times \frac{35}{2} \times \frac{35}{2}\right) \text{ cm}^2 \\ &= 962.5 \text{ cm}^2 \end{aligned}$$

Question 2:

$$\text{Circumference of circle} = 2\pi r = 39.6 \text{ cm}$$

$$\Rightarrow 2 \times \frac{22}{7} \times r = 39.6$$

$$r = \left(39.6 \times \frac{7}{44}\right) \text{ cm} = 6.3$$

$$r = 6.3 \text{ cm}$$

$$\begin{aligned} \text{Area of circle} &= \pi r^2 = \left(\frac{22}{7} \times 6.3 \times 6.3\right) \text{ cm}^2 \\ &= 124.74 \text{ cm}^2 \end{aligned}$$

Question 3:

$$\text{Area of circle} = \pi r^2 = 301.84$$

$$\Rightarrow r^2 = 301.84 \times \frac{7}{22} = 96.04$$

$$r = \sqrt{96.04} \text{ cm} = 9.8 \text{ cm}$$

$$\text{Circumference of circle} = 2\pi r = \left(2 \times \frac{22}{7} \times 9.8\right) = 61.6 \text{ cm}$$

Question 4:

Let radius of circle be r

Then, diameter = $2r$

circumference - Diameter = 16.8

$$\Rightarrow 2\pi r - 2r = 16.8$$

$$\Rightarrow \frac{44}{7}r - 2r = 16.8$$

$$\Rightarrow \frac{30r}{7} = 16.8 \Rightarrow r = \frac{16.8 \times 7}{30} = 3.92 \text{ cm}$$

$$\text{Circumference of circle} = 2\pi r = \left(2 \times \frac{22}{7} \times 3.92\right) \text{ cm} = 24.64 \text{ cm}$$

Question 5:

Let the radius of circle be r cm

Then, circumference - radius = 37 cm

$$2\pi r = 37$$

$$\frac{44r}{7} = 37$$

$$\frac{37r}{7} = 37 \Rightarrow r = \frac{37 \times 7}{37} = 7 \text{ cm}$$

$$\text{Area of circle} = \pi r^2 = \frac{22}{7} \times 7 \times 7 = 154 \text{ cm}^2$$

Question 6:

$$\text{Area of square} = (\text{side})^2 = 484 \text{ cm}^2$$

$$\Rightarrow \text{side} = \sqrt{484} \text{ cm} = 22 \text{ cm}$$

$$\text{Perimeter of square} = 4 \times \text{side} = 4 \times 22 = 88 \text{ cm}$$

$$\text{Circumference of circle} = \text{Perimeter of square}$$

$$2\pi r = 88 \text{ cm} \Rightarrow r = \frac{88 \times 7}{2 \times 22} = 14 \text{ cm}$$

$$\text{Area of circle} = \pi r^2 = \left(\frac{22}{7} \times 14 \times 14 \right) \text{ cm}^2 = 616 \text{ cm}^2$$

Question 7:

$$\text{Area of equilateral} = \frac{\sqrt{3}}{4} a^2 = 121\sqrt{3}$$

$$a^2 = 121 \times \frac{\sqrt{3}}{\sqrt{3}} \times 4$$

$$a^2 = 484 \Rightarrow a = \sqrt{484}$$

$$a = 22 \text{ cm}$$

$$\text{Perimeter of equilateral triangle} = 3a = (3 \times 22) \text{ cm} = 66 \text{ cm}$$

$$\text{Circumference of circle} = \text{Perimeter of circle}$$

$$2\pi r = 66$$

$$\Rightarrow \left(2 \times \frac{22}{7} \times r \right) \text{ cm} = 66$$

$$\Rightarrow r = 10.5 \text{ cm}$$

$$\begin{aligned} \text{Area of circle} &= \pi r^2 = \left(\frac{22}{7} \times 10.5 \times 10.5 \right) \text{ cm}^2 \\ &= 346.5 \text{ cm}^2 \end{aligned}$$

Question 8:

Let the radius of park be r meter

$$\text{Thus, } \pi r + 2r = 90 \Rightarrow \frac{22r}{7} + 2r = 90$$

$$\Rightarrow \frac{36r}{7} = 90 \Rightarrow r = \frac{90 \times 7}{36}$$

$$r = 17.5 \text{ cm}$$

$$\begin{aligned} \text{Area of semicircle} &= \frac{1}{2} \pi r^2 = \left(\frac{1}{2} \times \frac{22}{7} \times 17.5 \times 17.5 \right) \text{m}^2 \\ &= 481.25 \text{ m}^2 \end{aligned}$$

Question 9:

Let the radii of circles be x cm and $(7 - x)$ cm

Then,

$$2\pi x - [2\pi(7 - x)] = 8$$

$$2\pi x - [14\pi - 2\pi x] = 8$$

$$2\pi x - 14\pi + 2\pi x = 8$$

$$4\pi x - 14\pi = 8$$

$$2\pi x = 4 + 7\pi$$

$$2\pi x = 4 + 22$$

$$2\pi x = 26$$

Substitute the value of $2\pi x$ in $2\pi(7 - x)$

$$= 14\pi - 2\pi x = 14 \times \frac{22}{7} - 26$$

$$= 44 - 26 = 18 \text{ cm}$$

Circumference of the circles are 26 cm and 18 cm

Question 10:

Area of first circle = $\pi r^2 = 962.5 \text{ cm}^2$

$$r^2 = \left(962.5 \times \frac{7}{22} \right) \text{cm}$$

$$r^2 = 306.25$$

$$r = 17.5 \text{ cm}$$

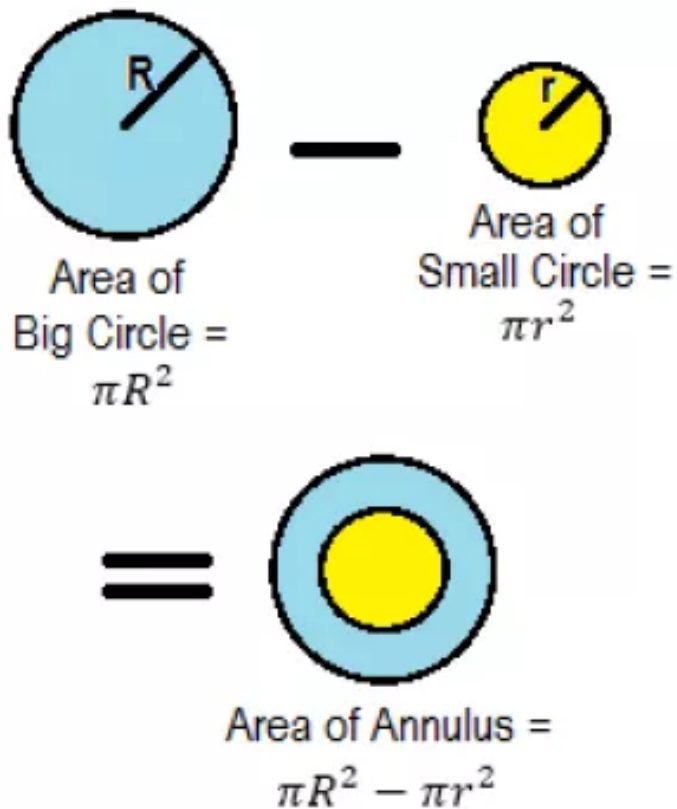
Area of second circle = $\pi R^2 = 1386 \text{ cm}^2$

$$R^2 = \left(1386 \times \frac{7}{22} \right) \text{cm}$$

$$R^2 = 441$$

$$\Rightarrow R = 21 \text{ cm}$$

Width of ring $R - r = (21 - 17.5) \text{ cm} = 3.5 \text{ cm}$



Question 11:

$$\text{Area of outer circle} = \pi r_1^2 = \left(\frac{22}{7} \times 23 \times 23\right) \text{ cm}^2 = 1662.5$$

$$\text{Area of inner circle} = \pi r_2^2 = \left(\frac{22}{7} \times 12 \times 12\right) \text{ cm}^2 = 452.2 \text{ cm}^2$$

$$\begin{aligned} \text{Area of ring} &= \text{Outer area} - \text{inner area} \\ &= (1662.5 - 452.5) \text{ cm}^2 = 1210 \text{ cm}^2 \end{aligned}$$

Question 12:

Inner radius of the circular park = 17 m

Width of the path = 8 m

Outer radius of the circular park = $(17 + 8)\text{m} = 25 \text{ m}$

$$\text{Area of path} = \pi[(25)^2 - (17)^2] = \text{cm}^2$$

$$= \pi(25 + 17)(25 - 17) \text{ m}^2$$

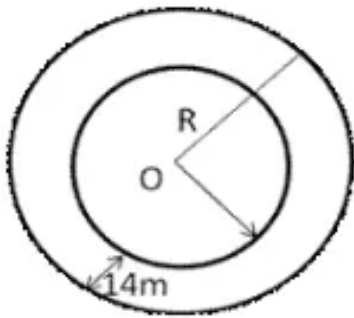
$$= \left[\frac{22}{7} \times 42 \times 8\right] \text{ m}^2$$

$$\text{Area} = 1056 \text{ m}^2$$

Question 13:

Let the inner and outer radii of the circular tracks be r meter and R meter respectively. Then

Inner circumference = 440 meter



$$\Rightarrow 2\pi r = 440$$

$$2 \times \frac{22}{7} \times r = 440$$

$$\Rightarrow r = 70 \text{ m}$$

Since the track is 14 m wide every where.

Therefore,

$$\text{Outer radius } R = r + 14\text{m} = (70 + 14) \text{ m} = 84 \text{ m}$$

$$\text{Outer circumference} = 2\pi R$$

$$= \left(2 \times \frac{22}{7} \times 84\right) \text{ m} = 528 \text{ m}$$

$$\text{Rate of fencing} = \text{Rs. 5 per meter}$$

$$\text{Total cost of fencing} = \text{Rs. } (528 \times 5) = \text{Rs. 2640}$$

$$\text{Area of circular ring} = \pi R^2 - \pi r^2$$

$$= \pi (84^2 - 70^2) = \frac{22}{7} \times 2156 = 6776 \text{ m}^2$$

$$\text{Cost of levelling} = \text{Rs 0.25 per m}^2$$

$$\text{Cost of levelling the track} = \text{Rs}(6776 \times 0.25) = \text{Rs. 1694}$$

Question 14:

Let r m and R m be the radii of inner circle and outer boundaries respectively.

Then, $2r = 352$ and $2R = 396$

$$r = \frac{352}{2\pi}, R = \frac{396}{2\pi}$$

$$\text{Width of the track} = (R - r) \text{ m}$$

$$= \left(\frac{396}{2\pi} - \frac{352}{2\pi}\right) \text{ m} = \left(\frac{44}{2\pi}\right) \text{ m}$$

$$= \left(\frac{44}{2} \times \frac{7}{22}\right) \text{ m} = 7 \text{ m}$$

$$\begin{aligned}
 \text{Area the track} &= \pi(R^2 - r^2) = \pi(R+r)(R-r) \\
 &= \left[\pi \left(\frac{352}{2\pi} + \frac{396}{2\pi} \right) \times 7 \right] \text{m}^2 \\
 &= \left[\left(\pi \times \frac{748}{2\pi} \right) \times 7 \right] \text{m}^2 = (374 \times 7) \text{m}^2 \\
 &= 2618 \text{ m}^2
 \end{aligned}$$

Question 15:

$$\text{Area of rectangle} = (120 \times 90)$$

$$= 10800 \text{ m}^2$$

$$\text{Area of circular lawn} = [\text{Area of rectangle} - \text{Area of park excluding circular lawn}]$$

$$= [10800 - 2950] \text{ m}^2 = 7850 \text{ m}^2$$

$$\text{Area of circular lawn} = 7850 \text{ m}^2$$

$$\Rightarrow \pi r^2 = 7850 \text{ m}^2$$

$$3.14 \times r^2 = 7850 \text{ m}^2$$

$$r^2 = \left(\frac{7850}{3.14} \right) \text{m}^2$$

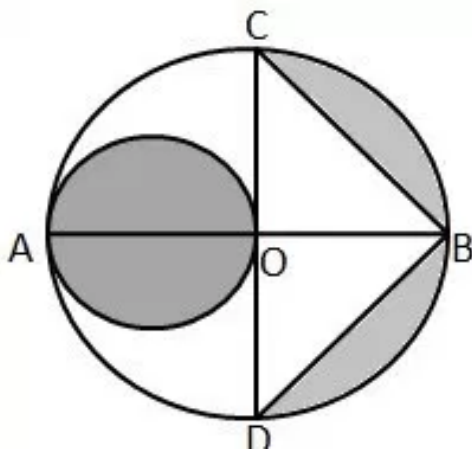
$$= 2500 \text{ m}^2$$

$$r = \sqrt{2500} \text{ m}$$

$$\text{or } r = 50 \text{ m}$$

Hence, radius of the circular lawn = 50 m

Question 16:



Area of the shaded region = (area of circle with OA as diameter) + (area of semicircle $\triangle DBC$) - (area of $\triangle BCD$)

$$\text{Area of circle with OA as diameter} = \pi r^2$$

$$= \left(\frac{22}{7} \times \frac{7}{2} \times \frac{7}{2} \right) \text{cm}^2$$

$$= 38.5 \text{ m}^2$$

OB = 7 cm, CD = AB = 14 cm

$$\text{Area of semicircle } \triangle DBC = \frac{1}{2}\pi r^2 - \left(\frac{1}{2} \times \frac{22}{7} \times 7 \times 7\right) \text{ cm}^2$$

$$= 72$$

$$\text{Area of } \triangle BCD = \frac{1}{2} \times DC \times OB$$

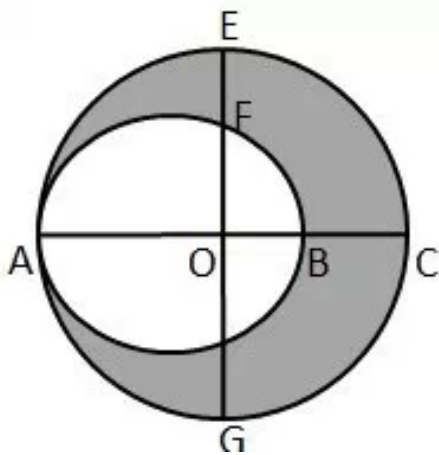
$$= \frac{1}{2} \times 14 \times 7$$

$$= 49 \text{ cm}^2$$

$$\text{Area of shaded region} = (38.5 + 77 - 49)$$

$$= 66.5 \text{ cm}^2$$

Question 17:



Diameter of bigger circle = AC = 54 cm

$$\text{Radius of bigger circle} = \frac{AC}{2}$$

$$= \left(\frac{54}{2}\right) \text{ cm} = 27 \text{ cm}$$

Diameter AB of smaller circle = AC - BC = 54 - 10 = 44 cm

$$\text{Radius of smaller circle} = \frac{44}{2} \text{ cm} = 22 \text{ cm}$$

$$\text{Area of bigger circle} = \pi R^2 = \left(\frac{22}{7} \times 27 \times 27\right) \text{ cm}^2$$

$$= 2291.14 \text{ cm}^2$$

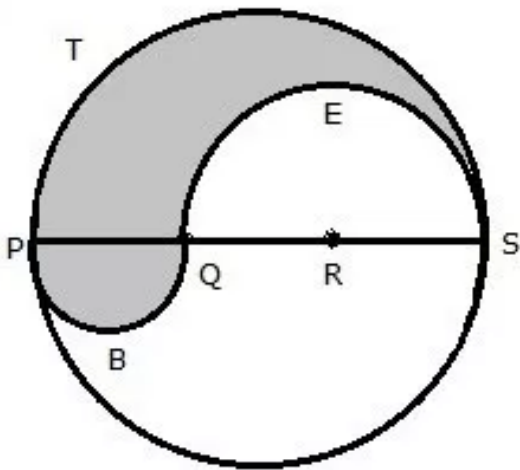
$$\text{Area of smaller circle} = \pi r^2 = \left(\frac{22}{7} \times 22 \times 22\right) \text{ cm}^2$$

$$= 1521.11 \text{ cm}^2$$

$$\text{Area of shaded region} = \text{area of bigger circle} - \text{area of smaller circle}$$

$$= (2291.14 - 1521.11) \text{ cm}^2 = 770 \text{ cm}^2$$

Question 18:



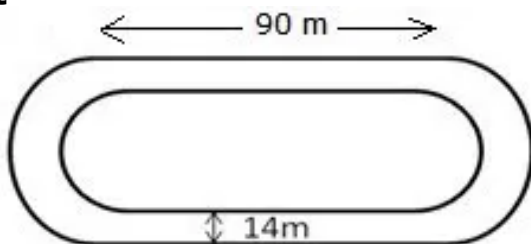
$PS = 12 \text{ cm}$
 $PQ = QR = RS = 4 \text{ cm}, QS = 8 \text{ cm}$
 Perimeter = arc PTS + arc PBQ + arc QES

$$\begin{aligned}
 &= (\pi \times 6 + \pi \times 2 + \pi \times 4) \text{ cm} \\
 &= 12\pi \text{ cm} \\
 &= 12\pi = 12 \times 3.14 \text{ cm} \\
 &= 37.68 \text{ cm}
 \end{aligned}$$

Area of shaded region = (area of the semicircle PBQ) + (area of semicircle PTS) - (Area of semicircle QES)

$$\begin{aligned}
 &= \left[\frac{1}{2} \pi \times (2)^2 + \frac{1}{2} \times \pi \times (6)^2 - \frac{1}{2} \times \pi \times (4)^2 \right] \text{ cm}^2 \\
 &= [2\pi + 18\pi - 8\pi] = 12\pi \text{ cm}^2 = (12 \times 3.14) \text{ cm}^2 \\
 &= 37.68 \text{ cm}^2
 \end{aligned}$$

Question 19:



Length of the inner curved portion
 $= (400 - 2 \times 90) \text{ m}$
 $= 220 \text{ m}$
 Let the radius of each inner curved part be r

Then, $\frac{22}{7} \times r = 110 \text{ m}$

$$r = \left(110 \times \frac{7}{22}\right) \text{ m} = 35 \text{ m}$$

Inner radius = 35 m, outer radius = (35 + 14) = 49 m

Area of the track = (area of 2 rectangles each 90 m × 14 m) + (area of circular ring with R = 49 m, r = 35 m)

$$= \left[2 \times 90 \times 14 + \frac{22}{7} \{(49)^2 - (35)^2\}\right] \text{ m}^2$$

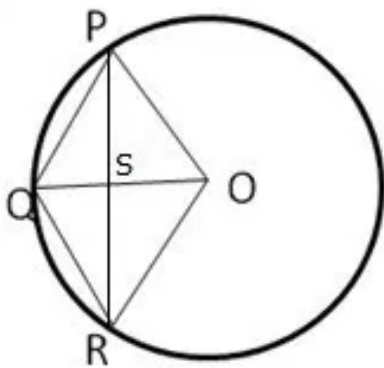
$$= \left[2520 + \frac{22}{7} (49 + 35)(49 - 35)\right] \text{ m}^2$$

$$= [2520 + 3696] \text{ m}^2 = 6216 \text{ m}^2$$

Length of outer boundary of the track

$$= \left[2 \times 90 + 2 \times \frac{22}{7} \times 49\right] \text{ m} = 488 \text{ m}$$

Question 20:



$$OP = OR = OQ = r$$

Let OQ and PR intersect at S

We know the diagonals of a rhombus bisect each other at right angle.

Therefore we have

$$OS = \frac{1}{2}r \text{ and } \angle OSR = 90^\circ$$

$$\therefore SR = \sqrt{OR^2 - OS^2}$$

$$= \sqrt{r^2 - \frac{r^2}{4}} = \frac{\sqrt{3}r}{2}$$

$$\therefore PR = 2 \times SR = \sqrt{3}r$$

$$\text{Area of rhombus} = \frac{1}{2} \times OQ \times PR$$

$$= \frac{1}{2} \times r \times \sqrt{3}r = \frac{\sqrt{3}r^2}{2}$$

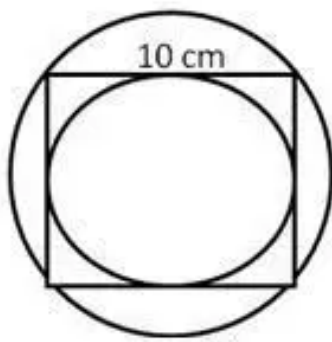
$$\therefore \frac{\sqrt{3}r^2}{2} = 32\sqrt{3} \Rightarrow r^2 = \frac{32\sqrt{3}}{\sqrt{3}} \times 2 = 64 \text{ cm}$$

$$r = 8 \text{ cm}$$

Question 21:

Diameter of the inscribed circle = Side of the square = 10 cm

Radius of the inscribed circle = 5 cm



Diameter of the circumscribed circle

= Diagonal of the square

= $(\sqrt{2} \times 10)$ cm

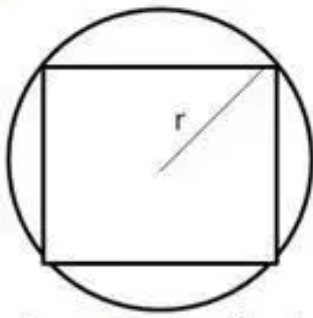
Radius of circumscribed circle = $5\sqrt{2}$ cm

(i) Area of inscribed circle = $\left(\frac{22}{7} \times 5 \times 5\right) = 78.57 \text{ cm}^2$

(ii) Area of the circumscribed circle = $\left(\frac{22}{7} \times 5\sqrt{2} \times 5\sqrt{2}\right) = 157.14 \text{ cm}^2$

Question 22:

Let the radius of circle be r cm



Then diagonal of square = diameter of circle = $2r$ cm

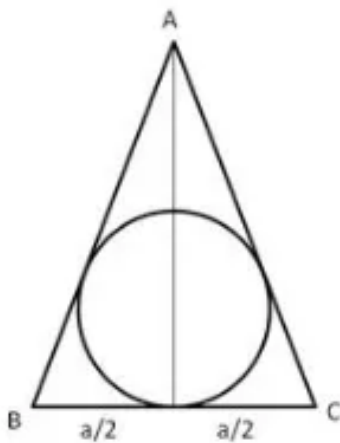
Area of the circle = πr^2 cm²

$$\begin{aligned}\text{Area of square} &= \frac{1}{2} \times (\text{diagonal})^2 \\ &= \frac{1}{2} \times (2r)^2 = 2r^2 \text{ cm}^2\end{aligned}$$

$$\text{Ratio} = \frac{\text{Area of circle}}{\text{Area of square}} = \frac{\pi r^2}{2r^2} = \frac{\pi}{2} = (\pi : 2)$$

Question 23:

Let the radius of circle be r cm



$$\text{Then, } \pi r^2 = 154$$

$$\Rightarrow r^2 = \left(154 \times \frac{7}{22}\right)$$

$$\Rightarrow r = 7 \text{ cm}$$

Let each side of the triangle be a cm

And height be h cm

$$\text{Then, } r = \frac{h}{3}$$

$$\Rightarrow h = 3r = 21 \text{ cm}$$

$$h = \sqrt{a^2 - \frac{a^2}{4}} = \frac{\sqrt{3a^2}}{2} = \frac{\sqrt{3}a}{2} = 21$$

$$a = \frac{42}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} = 14\sqrt{3} \text{ cm}$$

$$\begin{aligned}\text{Perimeter} &= 3a = (3 \times 14 \times \sqrt{3}) = (42 \times 1.73) \text{ cm} \\ &= 72.66 \text{ cm}\end{aligned}$$

Question 24:

Radius of the wheel = 42 cm

$$\text{Circumference of wheel} = 2\pi r = \left(2 \times \frac{22}{7} \times 42\right) = 264 \text{ cm}$$

$$\text{Distance travelled} = 19.8 \text{ km} = 1980000 \text{ cm}$$

$$\text{Number of revolutions} = \frac{1980000}{264} = 7500$$

Question 25:

Radius of wheel = 2.1 m

$$\text{Circumference of wheel} = 2\pi r = \left(2 \times \frac{22}{7} \times 2.1\right) = 13.2 \text{ m}$$

$$\text{Distance covered in one revolution} = 13.2 \text{ m}$$

$$\begin{aligned}\text{Distance covered in 75 revolutions} &= (13.2 \times 75) \text{ m} = 990 \text{ m} \\ &= \frac{990}{1000} \text{ km}\end{aligned}$$

$$\text{Distance a covered in 1 minute} = \frac{99}{100} \text{ km}$$

$$\text{Distance covered in 1 hour} = \frac{99}{100} \times 60 \text{ km} = 59.4 \text{ km}$$

Question 26:

Distance covered by the wheel in 1 revolution

$$= \left(\frac{4.95 \times 1000 \times 100}{2500} \right) \text{ cm} = 198 \text{ cm}$$

The circumference of the wheel = 198 cm

Let the diameter of the wheel be d cm

$$\text{Then, } \pi d = 198 \Rightarrow \frac{22}{7} \times d = 198$$

$$\Rightarrow d = \frac{198 \times 7}{22} = 63 \text{ cm}$$

Hence diameter of the wheel is 63 cm

Question 27:

$$\text{Radius of the wheel} = r = \frac{60}{2} = 30 \text{ cm}$$

$$\text{Circumference of the wheel} = 2\pi r = \left(2 \times \frac{22}{7} \times 30\right) = \frac{1320}{7} \text{ cm}$$

Distance covered in 140 revolution

$$= \left(\frac{1320}{7} \times 140 \right) \text{ cm} = (1320 \times 20) \text{ cm}$$

$$= 26400 \text{ cm} = \frac{26400}{100} \text{ m} = 264 \text{ m} = \frac{264}{1000} \text{ km}$$

Distance covered in one hour = $\frac{264}{1000} \times 60 = 15.84 \text{ km}$

Question 28:

Distance covered by a wheel in 1 minute

$$= \left(\frac{72.6 \times 1000 \times 100}{60} \right) \text{ cm} = 121000 \text{ cm}$$

Circumference of a wheel = $2\pi r = \left(2 \times \frac{22}{7} \times 70 \right) = 440 \text{ cm}$

Number of revolution in 1 min = $\frac{121000}{440} = 275$

Question 29:

Area of quadrant = $\frac{1}{4} \pi r^2$

Circumference of circle = $2\pi r = 22$

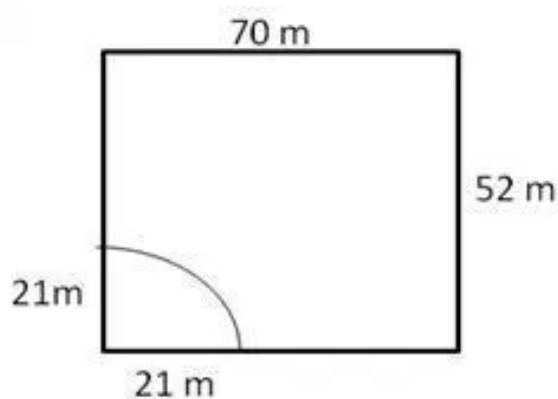
$$2 \times \frac{22}{7} \times r = 22$$

$$\Rightarrow r = \frac{22 \times 7}{2 \times 22} = 3.5 \text{ cm}$$

$$\text{Area of quadrant} = \frac{1}{4} \pi r^2 = \left(\frac{1}{4} \times \frac{22}{7} \times 3.5 \times 3.5 \right) \text{ cm}^2$$

$$= 9.625 \text{ cm}^2$$

Question 30:



Area which the horse can graze = Area of the quadrant of radius 21 m

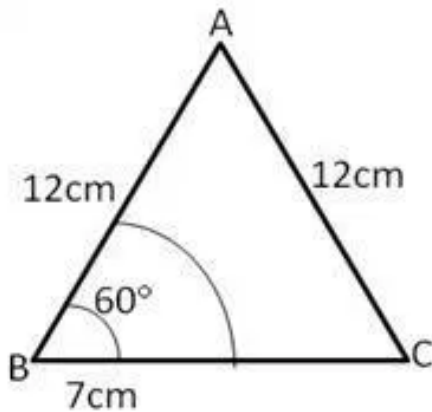
$$= \left(\frac{1}{4} \times \frac{22}{7} \times 21 \times 21 \right) \text{ m}^2$$

$$= 346.5 \text{ m}^2$$

$$\begin{aligned}\text{Area ungrazed} &= [(70 \times 52) - 346.5] \text{ m}^2 \\ &= 3293.5 \text{ m}^2\end{aligned}$$

Question 31:

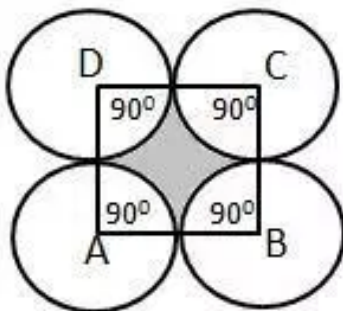
Each angle of equilateral triangle is 60°



$$\begin{aligned}\text{Area which cannot be grazed} &= (\text{area of equilateral } \triangle ABC) \\ &\quad - (\text{area of the sector with } r = 7\text{m}, \theta = 60^\circ) \\ &= \left[\frac{\sqrt{3}}{4} \times (12)^2 - \frac{22}{7} \times (7)^2 \times \frac{60}{360} \right] \text{ m}^2 \\ &= \left[(\sqrt{3} \times 12 \times 3) - \frac{(22 \times 7)}{6} \right] \\ &= 62.35 - 25.66 \text{ m}^2 \\ &= 36.68 \text{ m}^2\end{aligned}$$

Area that the horse cannot graze is 36.68 m^2

Question 32:



Each side of the square is 14 cm

$$\begin{aligned}\text{Then, area of square} &= (14 \times 14) \text{ cm}^2 \\ &= 196 \text{ cm}^2\end{aligned}$$

Thus, radius of each circle 7 cm

$$\text{Required area} = \text{area of square ABCD} - 4 (\text{area of sector with } r = 7 \text{ cm}, \theta = 90^\circ)$$

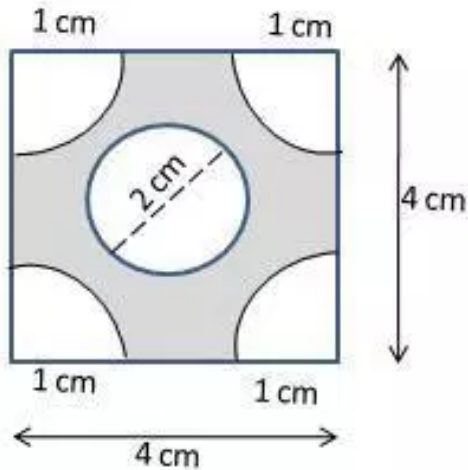
$$= \left[196 - 4 \times \frac{22}{7} \times 7 \times 7 \times \frac{90}{360} \right] \text{cm}^2$$

$$= [196 - 154] \text{cm}^2$$

$$= 42 \text{ cm}^2$$

Area of the shaded region = 42 cm^2

Question 33:



$$\text{Area of square} = (4 \times 4) \text{ cm}^2$$

$$= 16 \text{ cm}^2$$

Area of four quadrant corners

$$= 4 \left[\frac{1}{4} \pi^2 \right]$$

$$= \pi^2$$

$$= (\pi \times 1 \times 1) \text{ cm}^2$$

$$= 3.14 \text{ cm}^2$$

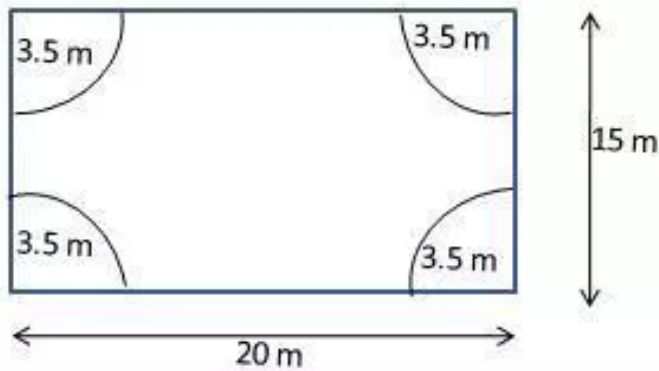
$$\text{Radius of inner circle} = 2/2 = 1 \text{ cm}$$

$$\text{Area of circle at the center} = \pi r^2 = (3.14 \times 1 \times 1) \text{ cm}^2$$

$$= 3.14 \text{ cm}^2$$

Area of shaded region = [area of square – area of four corner quadrants – area of circle at the centre]

$$= [16 - 3.14 - 3.14] \text{ cm}^2 = 9.72 \text{ cm}^2$$

Question 34:

Area of rectangle = $(20 \times 15) \text{ m}^2 = 300 \text{ m}^2$

Area of 4 corners as quadrants of circle

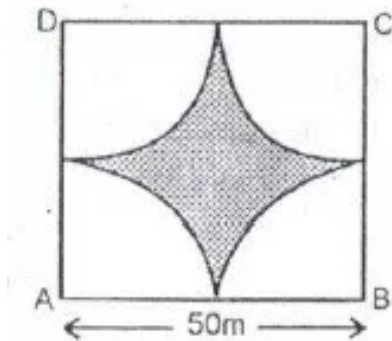
$$= 4 \times \left(\frac{1}{4} \pi r^2 \right)$$

$$= \left[\frac{22}{7} \times 3.5 \times 3.5 \right] \text{m}^2$$

$$= 38.5 \text{ m}^2$$

Area of remaining part = (area of rectangle – area of four quadrants of circles)

$$= (300 - 38.5) \text{ m}^2 = 261.5 \text{ m}^2$$

Question 35:

Ungrazed area

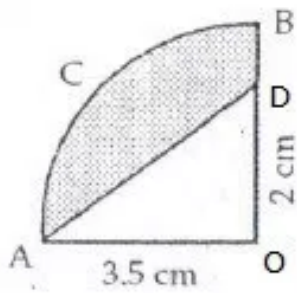
= shaded area

$$= \left[(50 \times 50) - \frac{4 \times \pi \times (25)^2 \times 90}{360} \right] \text{m}^2$$

$$= [2500 - 3.14 \times 25 \times 25] \text{m}^2$$

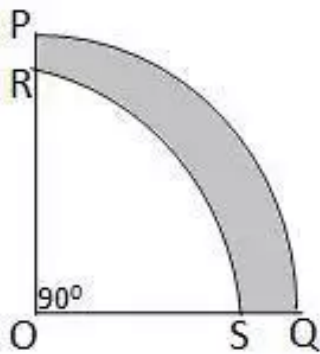
$$= [2500 - 1962.5] \text{m}^2$$

$$= 537.5 \text{ m}^2$$

Question 36:

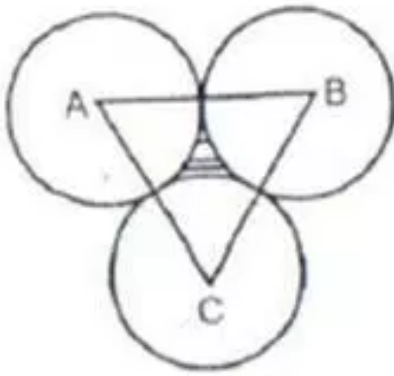
Shaded area = (area of quadrant) – (area of DAOD)

$$\begin{aligned}
 &= \left[\frac{1}{4} \pi^2 - \frac{1}{2} \times h \times b \right] \\
 &= \left[\frac{1}{4} \times \frac{22}{7} \times 3.5 \times 3.5 - \frac{1}{2} \times 2 \times 3.5 \right] \text{cm}^2 \\
 &= (9.625 - 3.5) \text{cm}^2 = 6.125 \text{cm}^2
 \end{aligned}$$

Question 37:

Area of flower bed = (area of quadrant OPQ) – (area of the quadrant ORS)

$$\begin{aligned}
 &= \left[\frac{1}{4} \pi_1^2 - \frac{1}{4} \pi_2^2 \right] \\
 &= \left[\frac{1}{4} \times \frac{22}{7} \times 21 \times 21 - \frac{1}{4} \times \frac{22}{7} \times 14 \times 14 \right] \text{m}^2 \\
 &= [346.5 - 154] \text{m}^2 = 192.5 \text{m}^2
 \end{aligned}$$

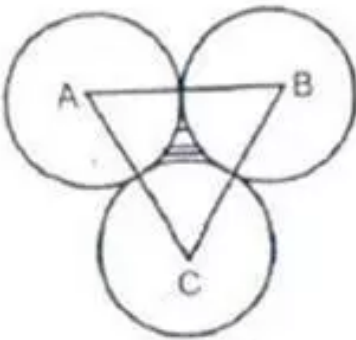
Question 38:

Let A, B, C be the centres of these circles. Join AB, BC, CA

Required area = (area of $\triangle ABC$ with each side $a = 12$ cm) $- 3$ (area of sector with $r = 6$, $\theta = 60^\circ$)

$$\begin{aligned}
 &= \left[\frac{\sqrt{3}}{4} \times (12)^2 - 3 \times \left(3.14 \times (6)^2 \times \frac{60}{360} \right) \right] \\
 &= \left[\frac{\sqrt{3}}{4} \times 12 \times 12 - 3 \times 3.14 \times 6 \right] \text{ cm}^2 \\
 &= (36 \times 1.73 - 56.52) \text{ cm}^2 \\
 &= (62.28 - 56.52) \text{ cm}^2 \\
 &= 5.76 \text{ cm}^2
 \end{aligned}$$

The area enclosed = 5.76 cm^2

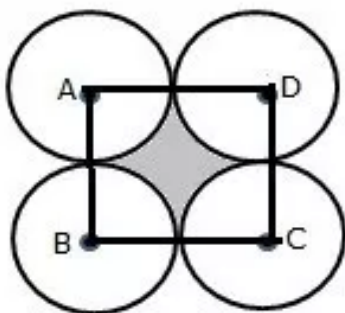
Question 39:

Let A, B, C be the centers of these circles. Join AB, BC, CA

Required area = (area of $\triangle ABC$ with each side 2) $- 3$ [area of sector with $r = a$ cm, $\theta = 60^\circ$]

$$\begin{aligned}
&= \left[\frac{\sqrt{3}}{4} \times (2a)^2 - \frac{3\pi a^2 \times 60}{360} \right] \\
&= (1.73a^2 - 1.57a^2) \\
&= 0.16a^2 \\
&= \frac{16}{100}a^2 \\
&= \left(\frac{4}{25}a^2 \right) \text{sq unit}
\end{aligned}$$

Question 40:



Let A, B, C, D be the centres of these circles

Join AB, BC, CD and DA

Side of square = 10 cm

Area of square ABCD

$$= (10 \times 10) \text{ cm}^2$$

$$= 100 \text{ cm}^2$$

$$\text{Area of each sector} = \left(\pi^2 \times \frac{\theta}{360} \right) = 3.14 \times 5 \times 5 \times \frac{90}{360}$$

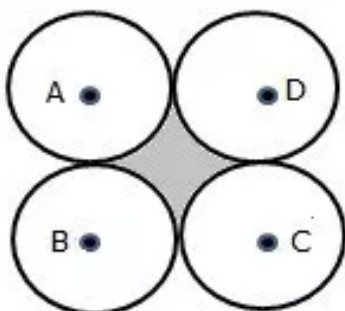
$$= 19.625 \text{ cm}^2$$

Required area = [area of sq. ABCD - 4(area of each sector)]

$$= (100 - 4 \times 19.625) \text{ cm}^2$$

$$= (100 - 78.5) = 21.5 \text{ cm}^2$$

Question 41:



Required area = [area of square - areas of quadrants of circles]

Let the side = 2a unit and radius = a units

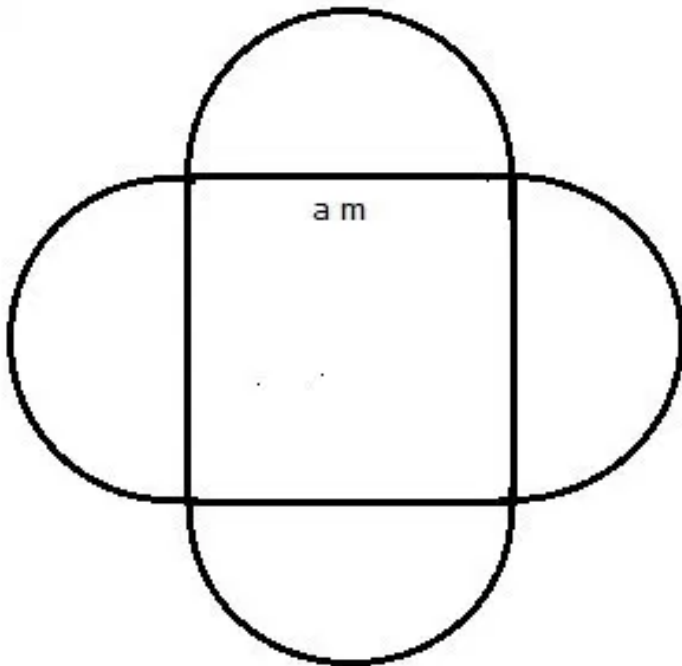
Area of square = (side \times side) = $(2a \times 2a)$ sq. units = $4a^2$ sq.units

Area of quadrant = $\frac{1}{4} \pi r^2$

Area of 4 quadrants = $4 \times \frac{1}{4} \pi r^2 = \pi r^2 = \frac{22}{7} \times a \times a = \frac{22}{7} a^2$ sq.unit

Required area = $\left(4a^2 - \frac{22}{7} a^2\right)$ sq unit = $\frac{6a^2}{7}$

Question 42:



Let the side of square = a m

Area of square = $(a \times a)$ cm = $a^2 m^2$

$$\therefore a^2 = 1600$$

$$a = \sqrt{1600} \text{ m}$$

$$a = 40 \text{ m}$$

Side of square = 40 m

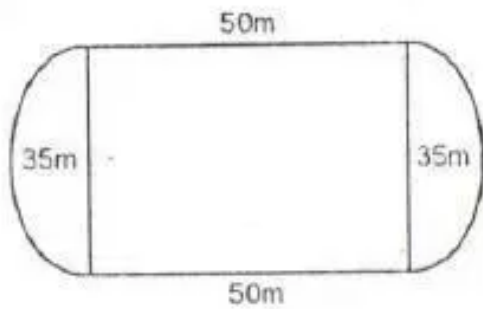
Therefore, radius of semi circle = 20 m

$$\begin{aligned} \text{Area of semi circle} &= \frac{1}{2} \pi r^2 = \left(\frac{1}{2} \times 3.14 \times 20 \times 20 \right) m^2 \\ &= 628 m^2 \end{aligned}$$

$$\text{Area of four semi circles} = (4 \times 628) m^2 = 2512 m^2$$

Cost of turfing the plot of area $1 m^2$ = Rs. 1.25

Cost of turfing the plot of area $2512 m^2$ = Rs. (1.25×2512)
= Rs. 3140

Question 43:

Area of rectangular lawn in the middle

$$= (50 \times 35) = 1750 \text{ m}^2$$

$$\text{Radius of semi circles} = \frac{35}{2} = 17.5 \text{ m}$$

Area of two semicircles = 2(area of semi circle)

$$\begin{aligned}
 &= \left[2 \left(\frac{1}{2} \pi r^2 \right) \right] \text{m}^2 \\
 &= \left(2 \times \frac{1}{2} \times \frac{22}{7} \times 17.5 \times 17.5 \right) \text{m}^2 \\
 &= 962.5 \text{ m}^2
 \end{aligned}$$

Area of lawn = (area of rectangle + area of semi circle)

$$= (1750 + 962.5) \text{ m}^2 = 2712.5 \text{ m}^2$$

Question 44:

Area of plot which cow can graze when $r = 16 \text{ m}$ is πr^2

$$= \left(\frac{22}{7} \times 10.5 \times 10.5 \right)$$

$$= 804.5 \text{ m}^2$$

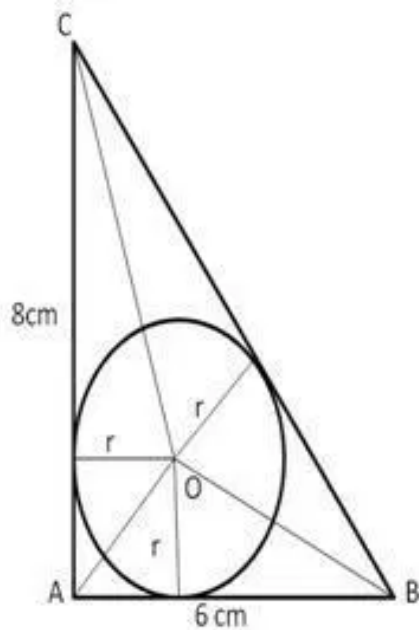
Area of plot which cow can graze when radius is increased to 23 m

$$= \left(\frac{22}{7} \times 10.5 \times 10.5 \right)$$

$$= 1662.57 \text{ m}^2$$

Additional ground = Area covered by increased rope – old area

$$= (1662.57 - 804.5) \text{ m}^2 = 858 \text{ m}^2$$

Question 45:

Given: ABC is right angled at A with AB = 6 cm and AC = 8 cm

$$BC = \sqrt{AB^2 + AC^2} = \sqrt{(6)^2 + (8)^2} \text{ cm}$$

$$= \sqrt{36 + 64} \text{ cm}$$

$$BC = \sqrt{100} \text{ cm} = 10 \text{ cm}$$

Let us join OA, OB and OC

$$\text{ar}(\triangle AOC) + \text{ar}(\triangle OAB) + \text{ar}(\triangle BOC) = \text{ar}(\triangle ABC)$$

$$\Rightarrow \left(\frac{1}{2} \times 8 \times r\right) + \left(\frac{1}{2} \times 6 \times r\right) + \left(\frac{1}{2} \times 10 \times r\right)$$

$$= \frac{1}{2} \times 6 \times 8$$

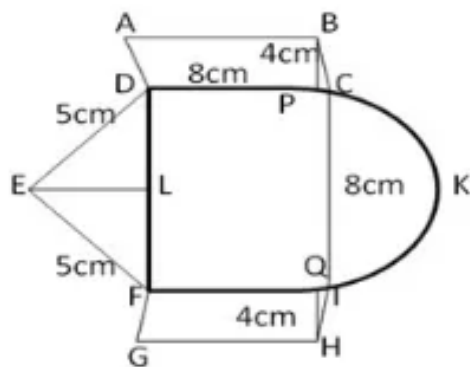
$$4r + 3r + 5r = 24$$

$$12r = 24$$

$$\Rightarrow r = \frac{24}{12} = 2$$

$$\text{Radius} = 2 \text{ cm}$$

Question 46:



Given $BP \perp CD$, $HQ \perp FI$ and $EL \perp DF$,
 $DC=8$ cm, $BP = HQ = 4$ cm and $DE = EF = 5$ cm
 Area of parallelogram ABCD = $BP \times DC$

$$= 4 \times 8 = 32 \text{ cm}^2$$

Area of parallelogram FGHI = $FI \times HQ$

$$= 8 \times 4 = 32 \text{ cm}^2$$

Area of semicircle CKI = $\frac{1}{2} \pi r^2$

$$= \frac{1}{2} \times 3.14 \times (4)^2 = 25.12 \text{ cm}^2$$

Area of isosceles $\triangle DEF = \frac{1}{4} b \sqrt{4a^2 - b^2}$

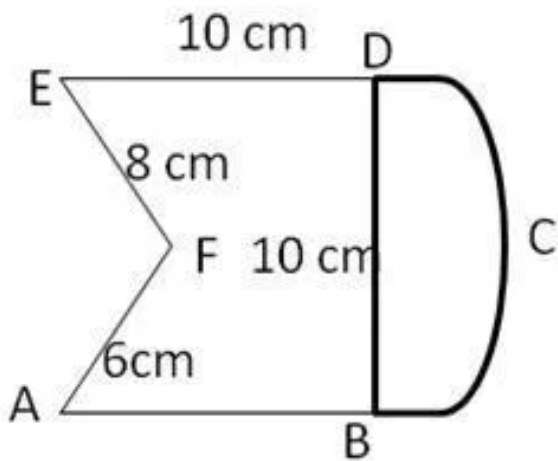
$$= \frac{1}{4} (8) \sqrt{4(5)^2 - (8)^2} = 2\sqrt{100 - 64}$$

$$= 2\sqrt{36} = 12 \text{ cm}^2$$

Area of square CDFI = $(\text{side})^2 = (8)^2 = 64 \text{ cm}^2$

Area of whole figure = area of \parallel^{gm} ABCD + area of \parallel^{gm} FGHI
 + area of semi-circle CKI + area of $\triangle DEF$
 + area of square CDFI
 $= (32+32+25.12+12+64) \text{ cm}^2$
 $= 165.12 \text{ cm}^2$

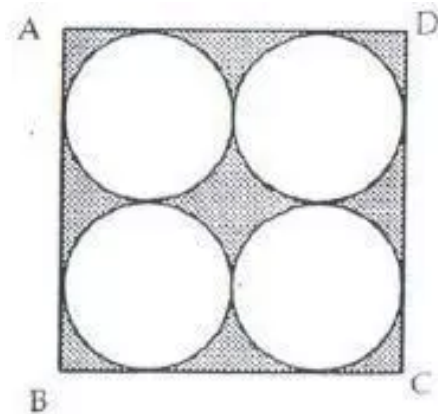
Question 47:



Area of region ABCDEFA = area of square ABDE + area of semi circle BCD – area of $\triangle AFE$

$$= \left[10 \times 10 + \frac{1}{2} \times 3.14 \times 5 \times 5 - \frac{1}{2} \times 6 \times 8 \right] \text{cm}^2$$
$$= [100 + 39.25 - 24] \text{cm}^2 = 115.25 \text{ cm}^2$$

Question 48:



Side of the square ABCD = 14 cm

Area of square ABCD = $14 \times 14 = 196 \text{ cm}^2$

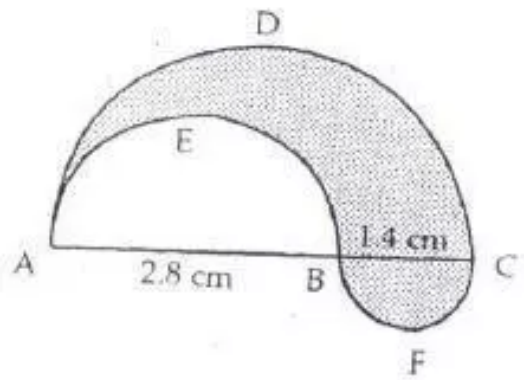
Radius of each circle = $\frac{14}{4} = 3.5 \text{ cm}$

Area of the circles = $4 \times \text{area of one circle}$

$$= 4 \times \pi (3.5)^2$$
$$= 4 \times \frac{22}{7} \times 3.5 \times 3.5$$
$$= 154 \text{ cm}^2$$

Area of shaded region = Area of square – area of 4 circles
 $= 196 - 154 = 42 \text{ cm}^2$

Question 49:



$$\text{Diameter } AC = 2.8 + 1.4 \\ = 4.2 \text{ cm}$$

$$\text{Radius } r_1 = \frac{4.2}{2} = 2.1 \text{ cm}$$

$$\text{Length of semi-circle } ADC = \pi r_1 = \pi \times 2.1 = 2.1 \pi \text{ cm}$$

$$\text{Diameter } AB = 2.8 \text{ cm}$$

$$\text{Radius } r_2 = 1.4 \text{ cm}$$

$$\text{Length of semi-circle } AEB = \pi r_2 = \pi \times 1.4 = 1.4 \pi \text{ cm}$$

$$\text{Diameter } BC = 1.4 \text{ cm}$$

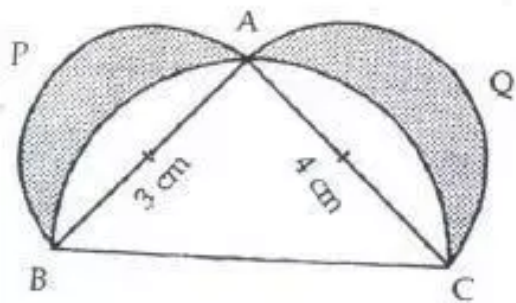
$$\text{Radius } r_3 = \frac{1.4}{2} = 0.7 \text{ cm}$$

$$\text{Length of semi-circle } BFC = \pi \times 0.7 = 0.7 \pi \text{ cm}$$

$$\text{Perimeter of shaded region} = 2.1 + 1.4 + 0.7 = 4.2 \pi \text{ cm}$$

$$= 4.2 \times \frac{22}{7} = 13.2 \text{ cm}$$

Question 50:



$$\text{Area of shaded region} = \text{Area of } \triangle ABC + \text{Area of semi-circle } APB + \text{Area of semi-circle } AQC - \text{Area of semicircle } BAC$$

$$\text{Now, Area of } \triangle ABC = \frac{1}{2} \times 3 \times 4 = 6 \text{ cm}^2 \text{ --- (1)}$$

$$\text{Area of semi-circle } APB = \frac{1}{2} \pi r^2 = \frac{1}{2} \pi \times \left(\frac{3}{2}\right)^2 = \frac{9}{8} \pi \text{ --- (2)}$$

$$\begin{aligned} \text{Area of semi-circle } AQC &= \frac{1}{2} \pi r^2 \\ &= \frac{1}{2} \pi \left(\frac{4}{2}\right)^2 = 2\pi \text{ cm}^2 \text{ --- (3)} \end{aligned}$$

Further in $\triangle ABC$, $\angle A = 90^\circ$

$$\therefore BC^2 = AB^2 + AC^2 = 9 + 16 = 25$$

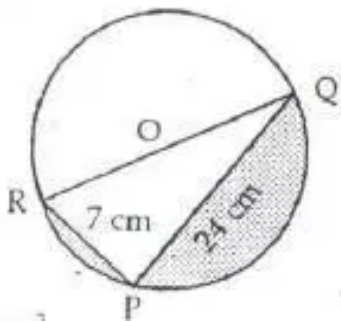
$$\therefore BC = 5$$

$$\text{Area of semi-circle BAC} = \frac{1}{2} \pi \left(\frac{5}{2}\right)^2 = \frac{25}{8} \pi \quad \text{--- (4)}$$

Adding (1), (2), (3) and subtracting (4)

$$\begin{aligned} \therefore \text{Area of shaded region} &= 6 + \frac{9}{8} \pi + 2\pi - \frac{25}{8} \pi \\ &= 6 + \frac{25}{8} \pi - \frac{25}{8} \pi = 6 \text{ cm}^2 \end{aligned}$$

Question 51:



In $\triangle PQR$, $\angle P = 90^\circ$, $PQ = 24 \text{ cm}$, $PR = 7 \text{ cm}$

$$\begin{aligned} \therefore QR^2 &= RP^2 + PQ^2 = 7^2 + 24^2 \\ &= 49 + 576 = 625 \end{aligned}$$

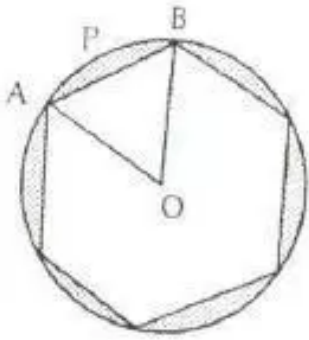
$$\therefore QR = 25 \text{ cm}$$

Area of semicircle

$$\begin{aligned} &= \frac{1}{2} \times \pi \times \left(\frac{25}{2}\right)^2 \\ &= \frac{1}{2} \times 3.14 \times \frac{25 \times 25}{4} \text{ cm}^2 \\ &= \frac{625 \times 3.14}{8} = 245.31 \text{ cm}^2 \end{aligned}$$

$$\text{Area of } \triangle PQR = \frac{1}{2} \times 7 \times 24 \text{ cm}^2 = 84 \text{ cm}^2$$

$$\text{Shaded area} = 245.31 - 84 = 161.31 \text{ cm}^2$$

Question 52:

ABCDEF is a hexagon.

$\angle AOB = 60^\circ$, Radius = 35 cm

Area of sector AOB

$$= \pi r^2 \times \frac{60^\circ}{360^\circ} = \frac{\pi \times 35 \times 35}{6} \text{ cm}^2$$

$$= \frac{3.14 \times 35 \times 35}{6} \text{ cm}^2$$

$$= 641.083 \text{ cm}^2$$

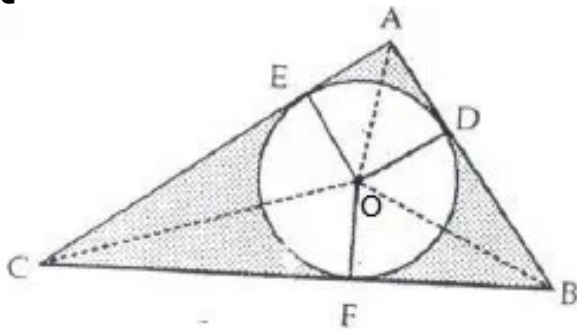
Area of $\triangle AOB = \frac{\sqrt{3}}{4} \times r^2 = \frac{\sqrt{3}}{4} \times 35 \times 35 \text{ cm}^2$

$$= 530.425 \text{ cm}^2$$

Area of segment APB = $(641.083 - 530.425) \text{ cm}^2 = 110.658 \text{ cm}^2$

Area of design (shaded area) = $6 \times 110.658 \text{ cm}^2 = 663.948 \text{ cm}^2$

$$= 663.95 \text{ cm}^2$$

Question 53:

In $\triangle ABC$, $\angle A = 90^\circ$, AB = 6 cm, BC = 10 cm

$$BC^2 = AC^2 + AB^2$$

$$\therefore AC^2 = BC^2 - AB^2 = 10^2 - 6^2 = 100 - 36 = 64$$

$$\therefore AC = 8 \text{ cm}$$

Area of $\triangle ABC = \frac{1}{2} \times AC \times AB = \frac{1}{2} \times 8 \times 6 \text{ cm}^2 = 24 \text{ cm}^2$

Let r be the radius of circle of centre O

$$\text{Area of } \triangle OCB = \frac{1}{2} \times 10 \times r \text{ cm}^2 = 5r \text{ cm}^2$$

$$\text{Area of } \triangle OAB = \frac{1}{2} \times 6 \times r \text{ cm}^2 = 3r \text{ cm}^2$$

$$\text{Area of } \triangle OCA = \frac{1}{2} \times 8 \times r \text{ cm}^2 = 4r \text{ cm}^2$$

$$\text{Area of } (\triangle OCB + \triangle OAB + \triangle OCA) = \text{Area of } \triangle ABC$$

$$\therefore 5r + 3r + 4r = 24$$

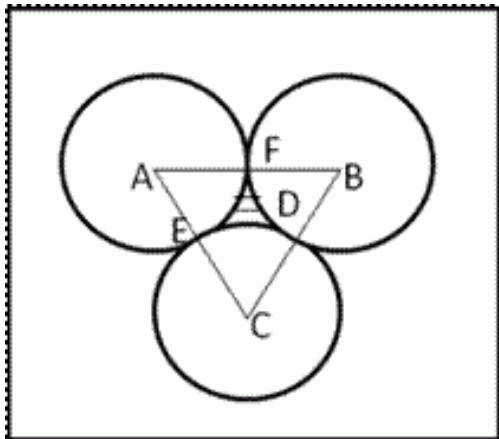
$$\text{or } 12r = 24 \quad \therefore r = 2 \text{ cm}$$

$$\begin{aligned} \therefore \text{Area of incircle} &= \pi r^2 = 3.14 \times 2 \times 2 \text{ cm}^2 \\ &= 12.56 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \Rightarrow \text{Shaded area} &= \text{Area of } \triangle ABC - \text{Area of incircle} \\ &= (24 - 12.56) \text{ cm}^2 = 11.44 \text{ cm}^2 \end{aligned}$$

Question 54:

Area of equilateral triangle $ABC = 49\sqrt{3} \text{ cm}^2$



Let a be its side

$$\therefore \frac{\sqrt{3}}{4} a^2 = 49\sqrt{3}$$

$$\text{or } a^2 = 49 \times 4$$

$$\therefore a = 7 \times 2$$

$$\Rightarrow a = 14 \text{ cm}$$

$$\text{Area of sector BDF} = \pi r^2 \times \frac{\theta}{360^\circ}$$

$$= \frac{22}{7} \times 7 \times 7 \times \frac{60}{360} \text{ cm}^2$$

$$= \frac{11 \times 7}{3} \text{ cm}^2 = \frac{77}{3} \text{ cm}^2$$

Area of sector BDF = Area of sector CDE = Area of sector AEF
Sum of area of all the sectors

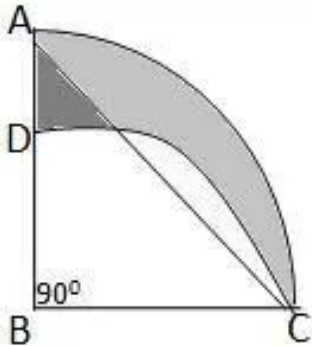
$$= \frac{77}{3} \times 3 \text{ cm}^2 = 77 \text{ cm}^2$$

Shaded area = Area of ΔABC – sum of area of all sectors

$$= 49\sqrt{3} - 77 = (84.77 - 77.00) \text{ cm}^2$$

$$= 7.77 \text{ cm}^2$$

Question 55:



In ΔABC , $\angle B = 90^\circ$, $AB = 48 \text{ cm}$, $BC = 14 \text{ cm}$

$$\therefore AC^2 = AB^2 + BC^2 = 48^2 + 14^2$$

$$= 2304 + 196 = 2500$$

$$\therefore AC = 50 \text{ cm}$$

$$\text{Area of } \Delta ABC = \frac{1}{2} \times 48 \times 14 \text{ cm}^2 = 336 \text{ cm}^2$$

Area of semi-circle APC

$$= \frac{1}{2} \pi r^2 = \frac{1}{2} \times \frac{22}{7} \times 25 \times 25 \text{ cm}^2$$

$$= \frac{11 \times 625}{7} \text{ cm}^2 = \frac{6875}{7} \text{ cm}^2$$

$$= 982.14 \text{ cm}^2$$

Area of quadrant BDC with radius 14 cm

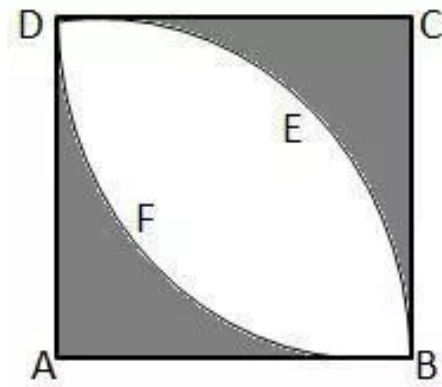
$$= \frac{1}{4} \times \frac{22}{7} \times 14 \times 14 \text{ cm}^2 = 154 \text{ cm}^2$$

Shaded area = Area of ΔABC + Area of semi-circle APC – Area of quadrant BDC

$$= (336 + 982.14 - 154) \text{ cm}^2$$

$$= (1164.14 - 154) \text{ cm}^2 = 1010.14 \text{ cm}^2$$

Question 56:



Radius of quadrant ABED = 16 cm

$$\text{Its area} = \frac{1}{4} \times \frac{22}{7} \times 16 \times 16 \text{ cm}^2$$

$$\begin{aligned}\text{Area of } \triangle ABD &= \left(\frac{1}{2} \times 16 \times 16\right) \text{ cm}^2 \\ &= 128 \text{ cm}^2\end{aligned}$$

Area of segment DEB

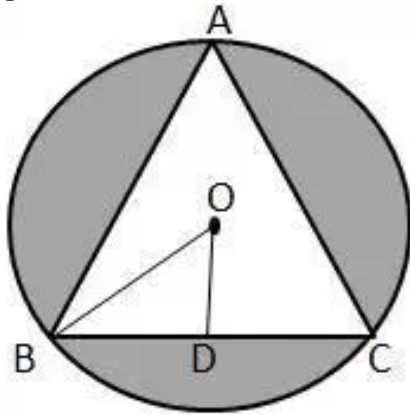
$$\begin{aligned}&= \frac{11 \times 128}{7} - 128 \\ &= 128 \left(\frac{11-7}{7} \right) \text{ cm}^2 = \frac{128 \times 4}{7} \text{ cm}^2 = \frac{512}{7} \text{ cm}^2\end{aligned}$$

$$\text{Area of segment DFB} = \frac{512}{7} \text{ cm}^2$$

$$\text{Total area of segments} = 2 \times \frac{512}{7} \text{ cm}^2 = \frac{1024}{7} \text{ cm}^2$$

Shaded area = Area of square ABCD - Total area of segments

$$\begin{aligned}&= \left(16 \times 16 - \frac{1024}{7} \right) \text{ cm}^2 \\ &= \left(256 - \frac{1024}{7} \right) \text{ cm}^2 = \frac{1792 - 1024}{7} \text{ cm}^2 \\ &= \frac{768}{7} \text{ cm}^2 = 109.7 \text{ cm}^2\end{aligned}$$

Question 57:

Radius of circular table cover = 70 cm

$$\text{Area of the circular cover} = \pi r^2 = \frac{22}{7} \times 70 \times 70 \text{ cm}^2 = 15400 \text{ cm}^2$$

In ΔBOD , $\angle D = 90^\circ$, $\angle OBD = 30^\circ$

$$\therefore \frac{BD}{OB} = \cos 30^\circ = \frac{\sqrt{3}}{2}$$

$$\Rightarrow BD = OB \cos 30^\circ$$

$$= 70 \times \frac{\sqrt{3}}{2} \text{ cm}$$

$$= 35\sqrt{3} \text{ cm}$$

$$\Rightarrow BC = 2BD = 2 \times 35\sqrt{3} = 70\sqrt{3}$$

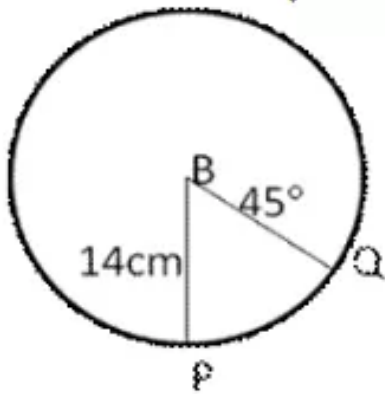
$$\begin{aligned} \text{Area of } \Delta ABC &= \frac{\sqrt{3}}{4} \times a^2 = \frac{\sqrt{3}}{4} \times 70\sqrt{3} \times 70\sqrt{3} \\ &\quad [\because \Delta ABC \text{ is equilateral}] \\ &= \frac{4900 \times 3 \times \sqrt{3}}{4} \text{ cm}^2 = 1225 \times 3 \times \sqrt{3} \\ &= 3675\sqrt{3} \text{ cm}^2 = 6365.1 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Shaded area} &= \text{Area of circle} - \text{Area of } \Delta ABC \\ &= (15400 - 6365.1) \end{aligned}$$

Question 58:

$$\text{Area of the sector of circle} = \frac{\pi r^2 \theta}{360^\circ}$$

$r = 14 \text{ cm}$ and $\theta = 45^\circ$



$$\begin{aligned}\therefore \text{Area of sector} &= \left(\frac{\pi \times 14 \times 14 \times 45}{360} \right) \text{cm}^2 \\ &= (24.5\pi) \text{cm}^2 \\ &= \left(24.5 \times \frac{22}{7} \right) \text{cm}^2 = 77 \text{ cm}^2\end{aligned}$$

Question 59:

Length of the arc = $\frac{2\pi r\theta}{360}$, $r = 21 \text{ cm}$, $\theta = 150^\circ$

$$= \left(\frac{2\pi \times 21 \times 150}{360} \right) \text{cm} = (17.5\pi) \text{cm}$$

Length of arc = $(17.5 \times \frac{22}{7}) \text{ cm} = 55 \text{ cm}$

$$\text{Area of the sector} = \frac{\pi r^2 \theta}{360} = \left(\frac{\pi \times 21 \times 21 \times 150}{360} \right) \text{cm}^2$$

$$= \left(\frac{22}{7} \times 183.75 \right) \text{cm}^2 = 577.5 \text{ cm}^2$$

Question 60:

Length of arc of circle = 44 cm

Radius of circle = 17.5 cm

$$\text{Area of sector} = \frac{1}{2}lr = \left(\frac{1}{2} \times 44 \times 17.5 \right) \text{cm}^2$$

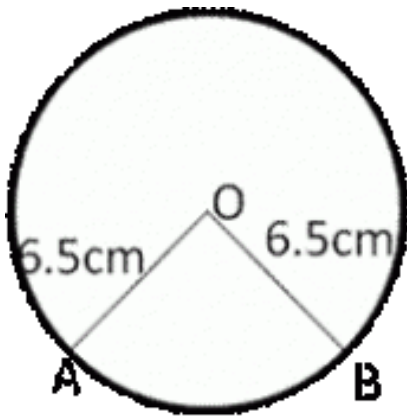
$$= (22 \times 17.5) \text{cm}^2 = 385 \text{ cm}^2$$

Question 61:

Let sector of circle is OAB

Perimeter of a sector of circle = 31 cm

OA + OB + length of arc AB = 31 cm



$$6.5 + 6.5 + \text{arc AB} = 31 \text{ cm}$$

$$\text{arc AB} = 31 - 13$$

$$= 18 \text{ cm}$$

$$\text{Area of circle} = \frac{1}{2}lr$$

$$= \frac{1}{2} \times 18 \times 6.5 = 58.5 \text{ cm}^2$$

Question 62:

$$\text{Area of the sector of circle} = \frac{\pi r^2 \theta}{360} = 69.3$$

$$\text{Radius} = 10.5 \text{ cm}$$

$$\Rightarrow \frac{\pi \times (10.5)^2 \times \theta}{360} = 69.3$$

$$\Rightarrow \theta = \frac{69.3 \times 360 \times 7}{10.5 \times 10.5 \times 22} = 72^\circ$$

Question 63:

$$\text{Length of the pendulum} = \text{radius of sector} = r \text{ cm}$$

$$\text{Arc length} = 8.8 \Rightarrow 2 \times \frac{22}{7} \times r \times \frac{30}{360} = 8.8$$

$$\Rightarrow r = \frac{8.8 \times 7 \times 360}{2 \times 22 \times 30} = 16.8 \text{ cm}$$

Question 64:

$$\text{Length of arc} = \frac{2\pi r \theta}{360} = 16.5 \text{ cm}$$

$$2 \times \frac{22}{7} \times r \times \frac{54}{360} = 16.5$$

$$r = \frac{16.5 \times 7 \times 360}{2 \times 22 \times 54} = 17.5 \text{ cm}$$

Circumference of circle = $2\pi r$

$$\left(2 \times \frac{22}{7} \times 17.5\right) = 110 \text{ cm}$$

Area of circle =

$$\pi r^2 = \left(\frac{22}{7} \times 17.5 \times 17.5\right) \text{ cm}^2$$
$$= 962.5 \text{ cm}^2$$

Question 65:

Circumference of circle = $2\pi r$

$$2\pi r = 88 \Rightarrow r = \frac{88 \times 7}{2 \times 22} = 14 \text{ cm}$$

$$\text{Area of sector} = \frac{\pi^2 \theta}{360}$$
$$= \left(\frac{22}{7} \times 14 \times 14 \times \frac{72}{360}\right) \text{ cm}^2 = 123.2 \text{ cm}^2$$

Question 66:

Angle described by the minute hand in 60 minutes $\theta = 360^\circ$

Angle described by minute hand in 20 minutes

$$= \left(\frac{360}{60} \times 20\right) = 120^\circ$$

Required area swept by the minute hand in 20 minutes

= Area of the sector (with $r = 15 \text{ cm}$ and $\theta = 120^\circ$)

$$= \left(\frac{\pi^2 \theta}{360^\circ}\right) \text{ cm}^2 = \left(3.14 \times 15 \times 15 \times \frac{120^\circ}{360^\circ}\right)$$
$$= 235.5 \text{ cm}^2$$

Question 67:

$\theta = 56^\circ$ and let radius is $r \text{ cm}$

$$\text{Area of sector} = \frac{\pi^2 \theta}{360^\circ} = 17.6 \text{ cm}^2$$

$$\Rightarrow \frac{22}{7} \times r^2 \times \frac{56^\circ}{360^\circ} = 17.6$$

$$r^2 = \left(\frac{17.6 \times 360 \times 7}{22 \times 56} \right) \text{cm}^2$$

$$r^2 = 36 \text{ cm}^2 \Rightarrow r = \sqrt{36} \text{ cm} = 6 \text{ cm}$$

Hence radius = 6cm

Question 68:

$$\frac{\text{Area of sector with } \theta = 150^\circ}{\text{Area of the circle}} = \frac{\pi \times (6)^2 \times \frac{150}{360}}{\pi \times (6)^2}$$

$$= \frac{150}{360} = \frac{5}{12}$$

$$\text{Required ratio} = \left(36\pi \times \frac{90}{360} \right) : \left(36\pi \times \frac{120}{360} \right) : \left(36\pi \times \frac{150}{360} \right)$$

$$= \frac{1}{4} : \frac{1}{3} : \frac{5}{12} = 3 : 4 : 5$$

Question 69:

In 2 days, the short hand will complete 4 rounds

\therefore Distance travelled by its tip in 2 days

= 4(circumference of the circle with $r = 4$ cm)

= $(4 \times 2 \times 4)$ cm = 32 cm

In 2 days, the long hand will complete 48 rounds

\therefore length moved by its tip

= 48(circumference of the circle with $r = 6$ cm)

= $(48 \times 2 \times 6)$ cm = 576 cm

\therefore Sum of the lengths moved

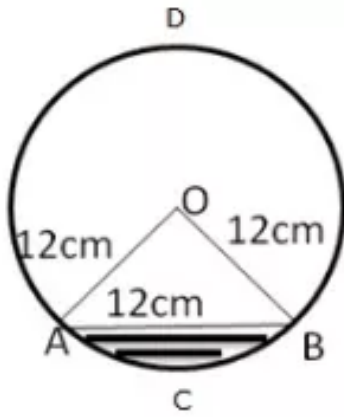
= $(32 + 576)$ = 608 cm

= (608×3.14) cm = 1909.12 cm

Question 70:

ΔOAB is equilateral.

So, $\angle AOB = 60^\circ$



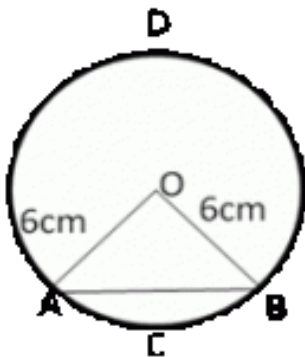
$$\begin{aligned}\text{arc ACB} &= \left(2\pi \times 12 \times \frac{60}{360} \right) \text{cm} \\ &= 4\pi \text{ cm} \\ &= (4 \times 3.14) \text{cm} \\ &= 12.56 \text{ cm}\end{aligned}$$

Length of arc BDA = $(2\pi \times 12 - \text{arc ACB})$ cm
 $= (24\pi - 4\pi)$ cm = (20π) cm
 $= (20 \times 3.14)$ cm = 62.8 cm
 Area of the minor segment ACBA

$$\begin{aligned}&= \left[\pi \times (12)^2 \times \frac{60}{360} - \frac{\sqrt{3}}{4} \times (12)^2 \right] \text{cm}^2 \\ &= \left(3.14 \times 12 \times 12 \times \frac{60}{360} - \frac{1.73}{4} \times 12 \times 12 \right) \text{cm}^2 \\ &= (75.36 - 62.28) \text{cm}^2 = 13.08 \text{ cm}^2\end{aligned}$$

Question 71:

Let AB be the chord of circle of centre O and radius = 6 cm such that $\angle AOB = 90^\circ$



Area of sector = OACBO

$$= \frac{\pi r^2 \theta}{360} \text{ cm}^2$$

$$= \left(\frac{22}{7} \times 6 \times 6 \times \frac{90}{360} \right) \text{ cm}^2$$

$$= 28.29 \text{ cm}^2$$

$$\text{Area of } \triangle AOB = \frac{1}{2} r^2 \sin \theta = \left(\frac{1}{2} \times 6 \times 6 \times \sin 90^\circ \right) = 18 \text{ cm}^2$$

Area of minor segment ACBA

= (area of sector OACBO) - (area of $\triangle OAB$)

$$= (28.29 - 18) \text{ cm}^2 = 10.29 \text{ cm}^2$$

Area of major segment BDAB

= (area of circle) - (area of minor segment)

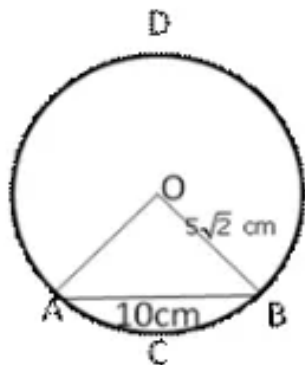
$$= \left[\left(\frac{22}{7} \times 6 \times 6 \right) - 10.29 \right] \text{ cm}^2$$

$$= (113.14 - 10.29) \text{ cm}^2 = 102.85 \text{ cm}^2$$

Question 72:

Let $OA = 5\sqrt{2} \text{ cm}$, $OB = 5\sqrt{2} \text{ cm}$

And $AB = 10 \text{ cm}$



$$\text{Then, } OA^2 + OB^2 = AB^2$$

$$\Rightarrow \angle AOB = 90^\circ$$

Area of the sector OACBO

$$= \frac{\pi r^2 \theta}{360} \text{ cm}^2$$

$$= \left(3.14 \times (5\sqrt{2}) \times (5\sqrt{2}) \times \frac{90}{360} \right) \text{ cm}^2$$

$$= 39.25 \text{ cm}^2$$

$$\text{Area of } \triangle AOB = \frac{1}{2} r^2 \sin \theta = \left(\frac{1}{2} \times 5\sqrt{2} \times 5\sqrt{2} \times \sin 90^\circ \right)$$

$$= 25 \text{ cm}^2$$

Area of minor segment = (area of sector OACBO) – (area of ΔOAB)

$$= (39.25 - 25) \text{ cm}^2 = 14.25 \text{ cm}^2$$

Area of the major segment BDAB

= area of circle – area of minor segment

$$= \left(\frac{22}{7} \times 5\sqrt{2} \times 5\sqrt{2} - 14.25 \right) \text{ cm}^2$$

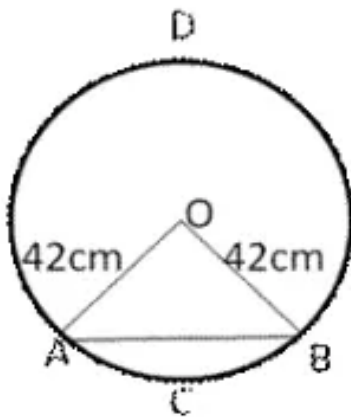
$$= \left(\frac{1100}{7} - 14.25 \right) \text{ cm}^2 = (157 - 14.25) \text{ cm}^2$$

$$= 142.75 \text{ cm}^2$$

Question 73:

Area of sector OACBO

$$= \frac{\pi r^2 \theta}{360} \text{ cm}^2 = \left(\frac{22}{7} \times 42 \times 42 \times \frac{120}{360} \right) \text{ cm}^2 = 1848 \text{ cm}^2$$



$$\text{Area of } \Delta OAB = \frac{1}{2} r^2 \sin \theta$$

$$= \left(\frac{1}{2} \times 42 \times 42 \times \sin 120^\circ \right)$$

$$= \left(21 \times 42 \times \frac{\sqrt{3}}{2} \right) \text{ cm}^2$$

$$= (21 \times 21 \times 1.73) \text{ cm}^2 = 762.93 \text{ cm}^2$$

Area of minor segment ACBA

$$= (\text{area of sector OACBO}) - (\text{area of the } \Delta OAB)$$

$$= (1848 - 762.93) \text{ cm}^2 = 1085.07 \text{ cm}^2$$

Area of major segment BADB

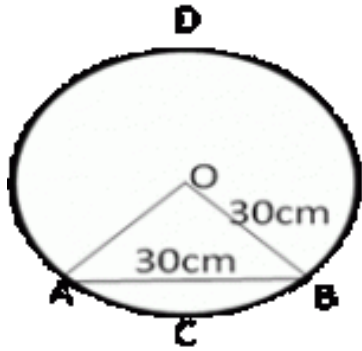
$$= (\text{area of the circle}) - (\text{area of minor segment})$$

$$= \frac{22}{7} \times 42 \times 42 - 1085.07$$

$$= (5544 - 1085.07) \text{ cm}^2 = 4458.93 \text{ cm}^2$$

Question 74:

Let AB be the chord of circle of centre O and radius = 30 cm such that $\angle AOB = 60^\circ$



Area of the sector OACBO

$$= \frac{\pi^2 \theta}{360} \text{ cm}^2$$

$$= \left(3.14 \times 30 \times 30 \times \frac{60}{360} \right) \text{ cm}^2$$

$$= 471 \text{ cm}^2$$

$$\text{Area of } \triangle OAB = \frac{1}{2} r^2 \sin \theta = \left(\frac{1}{2} \times 30 \times 30 \times \sin 60^\circ \right) \text{ cm}^2$$

$$= \left(\frac{1}{2} \times 30 \times 30 \times \frac{\sqrt{3}}{2} \right) \text{ cm}^2 = (225\sqrt{3}) \text{ cm}^2$$

$$= (225 \times 1.73) \text{ cm}^2 = 389.25 \text{ cm}^2$$

Area of the minor segment ACBA

$$= (\text{area of the sector OACBO}) - (\text{area of the } \triangle OAB)$$

$$= (471 - 389.25) \text{ cm}^2 = 81.75 \text{ cm}^2$$

Area of the major segment BADB

$$= (\text{area of circle}) - (\text{area of the minor segment})$$

$$= [(3.14 \times 30 \times 30) - 81.75] \text{ cm}^2 = 2744.25 \text{ cm}^2$$

Question 75:

Let the major arc be x cm long

Then, length of the minor arc = $\frac{1}{5}x$ cm

$$\text{Circumference} = \left(x + \frac{1}{5}x \right) \text{ cm} = \frac{6x}{5} \text{ cm}$$

$$\frac{6x}{5} = 2 \times \frac{22}{7} \times \frac{21}{2} \Rightarrow x = 55 \text{ cm}$$

$$\text{Required area} = \left(\frac{1}{2} \times 55 \times \frac{21}{2} \right) \text{ cm}^2$$

$$\left[\text{Area} = \frac{1}{2} r l \right]$$

$$= 288.75 \text{ cm}^2$$

Question 76:

$$\text{Radius of the front wheel} = 40 \text{ cm} = \frac{2}{5} \text{ m}$$

$$\text{Circumference of the front wheel} = \left(2\pi \times \frac{2}{5} \right) \text{ m} = \frac{4\pi}{5} \text{ m}$$

Distance moved by it in 800 revolution

$$= \left(\frac{4\pi}{5} \times 800 \right) \text{ m} = (640\pi) \text{ m}$$

$$\text{Circumference of rear wheel} = (2\pi \times 1) \text{ m} = (2\pi) \text{ m}$$

$$\text{Required number of revolutions} = \left(\frac{640\pi}{2\pi} \right) = 320$$