

**Importance :** 1 or 2 questions based on simplification are essential part of almost every competitive exams. The difficulty level varies based on examination level.

**Scope of questions :** The mostly asked questions are based on complex, fractions, decimal, squares, cubes, square roots and cuberoots. Questions are completely numerical kind with no alongways.

**Way to success:** Note that BODMAS rule and other simplification TRICKS & RULES are completely followed. Your concentration and 'Mental calculation' will help most in these questions.

**Rule 1 :** An expression must be simplified by following defined order/sequence known as VBODMAS, which is given by:

1st step, V – Vineculum (line brackets)/Bar

B – Brackets

O – Of

D – Division

M – Multiplication

A – Addition

Last step, S – Subtraction

There are four types of brackets given below.

(i) – → Line/Bar

(ii) ( ) → Simple or Small Bracket/open brackets

(iii) { } → Curly Brackets/Braces

(iv) [ ] → Square Brackets/Closed brackets

These brackets must be solved in given order only.

**Rule 2 :**

$$\frac{1}{n(n+1)} + \frac{1}{(n+1)(n+2)} + \frac{1}{(n+2)(n+3)} + \dots + \frac{1}{(n+r-1)(n+r)}$$

$$= \left( \frac{1}{n} - \frac{1}{n+1} \right) + \left( \frac{1}{n+1} - \frac{1}{n+2} \right) + \left( \frac{1}{n+2} - \frac{1}{n+3} \right)$$

$$+ \dots + \left( \frac{1}{n+r-1} - \frac{1}{n+r} \right) = \left( \frac{1}{n} - \frac{1}{n+r} \right)$$

$$\text{Rule 3 : } \frac{1}{n(n+2)} + \frac{1}{(n+2)(n+4)} + \frac{1}{(n+4)(n+6)}$$

$$+ \dots + \frac{1}{(n+2r-2)(n+2r)} = \frac{1}{2} \left( \frac{1}{n} - \frac{1}{n+2r} \right)$$

$$\text{Rule 4 : FORMULA} \rightarrow \frac{a^3+b^3}{a^2-ab+b^2} = (a+b)$$

$$\text{Rule 5 : FORMULA} \rightarrow \frac{a^3-b^3}{a^2+ab+b^2} = (a-b)$$

$$\text{Rule 6 : FORMULA} \rightarrow \frac{(a+b)^2+(a-b)^2}{(a^2+b^2)} = 2$$

$$\text{Rule 7 : FORMULA} \rightarrow a^2 + 2ab + b^2 = (a+b)^2$$

$$\text{Rule 8 : } \frac{a^2-b^2}{a-b} = a+b \text{ or, } \frac{a^2-b^2}{a+b} = a-b$$

### Basic formulae

$$(i) (a+b)^2 = a^2 + 2ab + b^2$$

$$(ii) (a-b)^2 = a^2 - 2ab + b^2$$

$$(iii) (a^2 - b^2) = (a+b)(a-b)$$

$$(iv) (a+b)^2 + (a-b)^2 = 2(a^2 + b^2)$$

$$(v) (a+b)^2 - (a-b)^2 = 4ab$$

$$(vi) (a+b)^3 = a^3 + b^3 + 3ab(a+b)$$

$$(vii) (a-b)^3 = a^3 - b^3 - 3ab(a-b)$$

$$(viii) a^3 + b^3 = (a+b)(a^2 - ab + b^2)$$

$$(ix) a^3 - b^3 = (a-b)(a^2 + ab + b^2)$$

$$(x) a^3 + b^3 + c^3 - 3abc = (a+b+c)(a^2 + b^2 + c^2 - ab - bc - ca)$$

$$\text{If } a+b+c=0$$

$$\Rightarrow a^3 + b^3 + c^3 = 3abc$$

$$(xi) a^2 + \frac{1}{a^2} = \left( a + \frac{1}{a} \right)^2 - 2 = \left( a - \frac{1}{a} \right)^2 + 2$$

$$(xii) \left( a + \frac{1}{a} \right)^3 = a^3 + \frac{1}{a^3} + 3 \times \left( a + \frac{1}{a} \right)$$

$$(xiii) \left( a - \frac{1}{a} \right)^3 = a^3 - \frac{1}{a^3} - 3 \times \left( a - \frac{1}{a} \right)$$



# QUESTIONS ASKED IN PREVIOUS SSC EXAMS

## TYPE-I

**1.** Simplify :  $1 + \frac{1}{1 + \frac{2}{2 + \frac{3}{1 + \frac{4}{5}}}}$

- (1)  $1\frac{11}{17}$       (2)  $1\frac{5}{7}$

- (3)  $1\frac{6}{17}$       (4)  $1\frac{21}{17}$

(SSC CGL Prelim Exam. 04.07.1999  
(First Sitting)

**2.** Simplify :  $1 + \frac{2}{1 + \frac{3}{1 + \frac{4}{1 + \frac{5}{5}}}}$

- (1)  $\frac{7}{4}$       (2)  $\frac{4}{7}$

- (3)  $\frac{7}{5}$       (4)  $\frac{3}{7}$

(SSC CGL Prelim Exam. 04.07.1999  
(First Sitting)

**3.** The value of

$$\frac{1}{3 + \frac{1}{2 - \frac{1}{2 - \frac{1}{9}}}} + \frac{17}{22} \text{ is :}$$

- (1)  $\frac{12}{22}$       (2)  $\frac{22}{5}$

- (3)  $\frac{5}{22}$       (4) 1

(SSC CGL Prelim Exam. 24.02.2002  
(First Sitting)

**4.** If  $x = 1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{2}}}}$

then, the value of  $2x + \frac{7}{4}$  is :

- (1) 3      (2) 4

- (3) 5      (4) 6

(SSC CGL Prelim Exam. 24.02.2002  
(Second Sitting)

**5.** Simplify :

$$\frac{19}{43} \div \frac{1}{2 + \frac{1}{3 + \frac{1}{1 + \frac{1}{4}}}}$$

- (1) 1      (2)  $\frac{19}{43}$

- (3)  $\frac{43}{19}$       (4)  $\frac{38}{43}$

(SSC CGL Prelim Exam. 24.02.2002  
(Middle Zone)

**6.** The simplification of  $\frac{5}{3 + \frac{3}{1 - \frac{2}{3}}}$

gives

- (1) 5      (2)  $\frac{5}{3}$

- (3)  $\frac{5}{12}$       (4)  $\frac{3}{5}$

(SSC CPO S.I. Exam. 2.01.2003)

**7.** If  $2 = x + \frac{1}{1 + \frac{1}{3 + \frac{1}{4}}}$ , then the

value of  $x$  is :

- (1)  $\frac{18}{17}$       (2)  $\frac{21}{17}$

- (3)  $\frac{13}{17}$       (4)  $\frac{12}{17}$

(SSC CGL Prelim Exam. 11.05.2003  
(First Sitting)

**8.** Find the value of

$$\frac{2}{1 + \frac{1}{1 - \frac{1}{2}}} \times \frac{3}{\frac{5}{6} \text{ of } \frac{3}{2} \div 1\frac{1}{4}}$$

- (1) 6      (2) 8

- (3) 4      (4) 2

(SSC CGL Prelim Exam. 11.05.2003  
(Second Sitting)

**9.** Simplify :

$$1 + \frac{4}{2 + \frac{3}{5 - \frac{1}{2}}} (10 \div 2)$$

- (1) 1      (2) 0

- (3)  $-\frac{15}{2}$       (4)  $-\frac{1}{2}$

(SSC CGL Prelim Exam. 11.05.2003  
(Second Sitting)

**10.**

$$\left[ \left( 1 + \frac{1}{10 + \frac{1}{10}} \right) \times \left( 1 + \frac{1}{10 + \frac{1}{10}} \right) - \left( 1 - \frac{1}{10 + \frac{1}{10}} \right) \times \right]$$

$$\left[ 1 - \frac{1}{10 + \frac{1}{10}} \right] \div$$

$$\left[ \left( 1 + \frac{1}{10 + \frac{1}{10}} \right) + \left( 1 - \frac{1}{10 + \frac{1}{10}} \right) \right]$$

simplifies to

- (1)  $\frac{100}{101}$       (2)  $\frac{90}{101}$

- (3)  $\frac{20}{101}$       (4)  $\frac{101}{100}$

(SSC CPO S.I. Exam. 07.09.2003)

**11.**  $\frac{5\frac{9}{14}}{5 + \frac{1}{3 + \frac{1}{5}}}$  is equal to

- (1) 1      (2) 1.5

- (3) 2      (4) 2.5

(SSC CGL Prelim Exam. 08.02.2004  
(First Sitting)

**12.**  $\frac{2}{2 + \frac{2}{3 + \frac{2}{3 + \frac{2}{3}}}} \times 0.39$  is simplified to

- (1)  $\frac{1}{3}$       (2) 2

- (3) 6      (4) None of these

(SSC CGL Prelim Exam. 08.02.2004  
(Second Sitting))

## SIMPLIFICATION

**13.**  $1 + \frac{1}{1 + \frac{1}{2}}$  is equal to

- (1) 3      (2)  $\frac{3}{2}$

- (3)  $\frac{2}{3}$       (4)  $\frac{5}{3}$

(SSC CPO S.I. Exam. 05.09.2004)

**14.**  $\frac{13}{48}$  is equal to

- (1)  $\frac{1}{3 + \frac{1}{1 + \frac{1}{16}}}$

- (2)  $\frac{1}{2 + \frac{1}{1 + \frac{1}{8}}}$

- (3)  $\frac{1}{3 + \frac{1}{1 + \frac{1}{1 + \frac{1}{8}}}}$

- (4)  $\frac{1}{3 + \frac{1}{1 + \frac{1}{2 + \frac{1}{4}}}}$

(SSC CPO S.I. Exam. 03.09.2006)

**15.** The value of

- $1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{2}{3}}}}}$  is

- (1)  $\frac{21}{13}$       (2)  $\frac{17}{3}$

- (3)  $\frac{34}{21}$       (4)  $\frac{8}{5}$

(SSC CGL Tier-1 Exam. 19.06.2011  
(First Sitting)

**16.** The value of  $\frac{2\frac{1}{3} - 1\frac{2}{11}}{3 + \frac{1}{3 + \frac{1}{3 + \frac{1}{3}}}}$  is

- (1)  $\frac{38}{109}$       (2)  $\frac{109}{38}$

- (3) 1      (4)  $\frac{116}{109}$

(SSC CGL Tier-1 Exam 26.06.2011  
(First Sitting)

**17.** The value of  $3 + \frac{3}{3 + \frac{1}{3 + \frac{1}{3}}}$  is

- (1)  $\frac{40}{11}$       (2)  $\frac{43}{11}$

- (3)  $\frac{46}{11}$       (4)  $\frac{41}{11}$

(SSC CGL Tier-1 Exam. 26.06.2011  
(Second Sitting)

**18.**  $1 + \frac{1}{1 + \frac{1}{5}} = ?$

- (1)  $\frac{11}{6}$       (2)  $\frac{13}{6}$

- (3)  $\frac{15}{6}$

(4) None of the above  
(SSC CISF Constable (GD)  
Exam. 05.06.2011)

**19.**  $\frac{4\frac{2}{7} - \frac{1}{2}}{3\frac{1}{2} + 1\frac{1}{7}} \div \frac{1}{2 + \frac{1}{2 + \frac{1}{5 - \frac{1}{5}}}}$

is equal to

- (1) 1      (2)  $\frac{1}{2}$

- (3) 2      (4)  $\frac{1}{3}$

(SSC CHSL DEO & LDC Exam.  
27.10.2013 IIInd Sitting)

**20.** If  $\left[ 4 - \frac{5}{1 + \frac{1}{3 + \frac{1}{2 + \frac{1}{4}}}} \right]^{\text{th}}$

part of a journey takes 10 minutes, then to complete  $\frac{3}{5}$  th of that journey, it will take

(1) 40 minutes (2) 45 minutes  
(3) 48 minutes (4) 36 minutes  
(SSC CHSL DEO & LDC Exam.  
10.11.2013, 1st Sitting)

**21.**

$$\frac{4\frac{1}{7} - 2\frac{1}{4}}{3\frac{1}{2} + 1\frac{1}{7}} \div \frac{2 + \frac{1}{2 + \frac{1}{5 - \frac{1}{5}}}}{2 + \frac{1}{5 - \frac{1}{5}}}$$

is equal to

- (1) 1      (2) 4

- (3) 3      (4) 2

(SSC CHSL DEO & LDC Exam.  
10.11.2013, IIInd Sitting)

**22.** The value of  $1 + \frac{1}{1 + \frac{2}{3 + \frac{4}{5}}}$  is :

- (1)  $\frac{12}{29}$       (2)  $\frac{8}{19}$

- (3)  $\frac{48}{29}$       (4)  $\frac{2}{19}$

(SSC CAPFs SI & CISF ASI  
Exam. 23.06.2013)

**23.** The value of  $1 - \frac{a}{1 - \frac{1}{1 + \frac{a}{1 - a}}}$  is

- (1)  $a$       (2)  $1 - a$

- (3) 1      (4) 0

(SSC CGL Tier-I Exam. 26.10.2014)

**24.** On simplification, the expression

$$\frac{4\frac{1}{7} - 2\frac{1}{7}}{3\frac{1}{2} + 1\frac{1}{7}} \div \frac{1}{2 + \frac{1}{2 + \frac{1}{5 - \frac{1}{5}}}}$$

is equal to

- (1)  $\frac{28}{65}$       (2)  $\frac{24}{53}$

- (3)  $\frac{56}{53}$       (4)  $\frac{14}{65}$

(SSC CGL Tier-II Exam. 2014 12.04.2015  
(Kolkata Region) TF No. 789 TH 7)

**25.** The simplified value of :

$$\left\{ \left( 1 + \frac{1}{10 + \frac{1}{10}} \right) \left( 1 + \frac{1}{10 + \frac{1}{10}} \right) - \right\} \div \left\{ \left( 1 - \frac{1}{10 + \frac{1}{10}} \right) \left( 1 - \frac{1}{10 + \frac{1}{10}} \right) \right\}$$

- (1)  $\frac{20}{101}$       (2)  $\frac{100}{101}$

- (3) 2      (4)  $\frac{90}{101}$

(SSC CGL Tier-I Exam, 16.08.2015  
(IInd Sitting) TF No. 2176783)

**26.** The value of

$$4 - \frac{1}{1 + \frac{1}{3 + \frac{1}{2 + \frac{1}{4}}}} \text{ is}$$

- (1)  $\frac{1}{8}$       (2)  $\frac{1}{64}$   
(3)  $\frac{1}{16}$       (4)  $\frac{1}{32}$

(SSC CGL Tier-II Exam,  
25.10.2015, TF No. 1099685)

**TYPE-II**

**1.** Evaluate :  $\frac{9|3-5|-5|4|+10}{-3(5)-2 \times 4 \div 2}$

- (1)  $\frac{9}{10}$       (2)  $-\frac{8}{17}$   
(3)  $-\frac{16}{19}$       (4)  $\frac{4}{7}$

(SSC CGL Prelim Exam. 04.07.1999  
(First Sitting)

**2.**  $5-[4-(3-(3-3-6))]$  is equal to :

- (1) 10      (2) 6  
(3) 4      (4) 0

(SSC CGL Prelim Exam. 04.07.1999  
(First Sitting)

**3. Evaluate :**

$$\frac{-(4-6)^2 - 3(-2) + |-6|}{18 - 9 \div 3 \times 5}$$

- (1)  $\frac{3}{8}$       (2)  $\frac{4}{7}$   
(3)  $\frac{8}{3}$       (4)  $\frac{7}{4}$

(SSC CGL Prelim Exam. 04.07.1999  
(Second Sitting)

**4. Simplify :**  $\frac{\frac{5}{3} \times \frac{7}{51} \text{ of } \frac{17}{5} - \frac{1}{3}}{\frac{2}{9} \times \frac{5}{7} \text{ of } \frac{28}{5} - \frac{2}{3}}$

- (1)  $\frac{1}{2}$       (2) 4  
(3) 2      (4)  $\frac{1}{4}$

(SSC CGL Prelim Exam. 04.07.1999  
(Second Sitting)

**5.**  $1 - [5 - \{2 + (-5 + 6 - 2) 2\}]$  is equal to :

- (1) -4      (2) 2  
(3) 0      (4) -2

(SSC CGL Prelim Exam. 04.07.1999  
(Second Sitting)

**6.** On simplification  $3034 - (1002 \div 20.04)$  is equal to

- (1) 3029      (2) 2984  
(3) 2993      (4) 2543

(SSC CGL Prelim Exam. 27.02.2000  
(First Sitting)

**7.** When simplified, the expression

$$(100)\frac{1}{2} \times (0.001)\frac{1}{3} -$$

$(0.0016)\frac{1}{4} \times 3^0 + \left(\frac{5}{4}\right)^{-1}$  is equal to:

- (1) 1.6      (2) 0.8  
(3) 1.0      (4) 0

(SSC CGL Prelim Exam. 27.02.2000  
(First Sitting)

**8.** When  $\left(\frac{1}{2} - \frac{1}{4} + \frac{1}{5} - \frac{1}{6}\right)$  is

divided by  $\left(\frac{2}{5} - \frac{5}{9} + \frac{3}{5} - \frac{7}{18}\right)$ ,

the result is :

- (1)  $5\frac{1}{10}$       (2)  $2\frac{1}{18}$   
(3)  $3\frac{1}{6}$       (4)  $3\frac{3}{10}$

(SSC CGL Prelim Exam. 27.02.2000  
(Second Sitting)

**9. Simplify :**

$$8\frac{1}{2} - \left[ 3\frac{1}{4} \div \left\{ 1\frac{1}{4} - \frac{1}{2} \left( 1\frac{1}{2} - \frac{1}{3} - \frac{1}{6} \right) \right\} \right]$$

- (1)  $4\frac{1}{2}$       (2)  $4\frac{1}{6}$   
(3)  $9\frac{1}{2}$       (4)  $\frac{2}{9}$

(SSC CGL Prelim Exam. 24.02.2002  
(First Sitting)

**10.** If  $\frac{50}{*} = \frac{*}{12\frac{1}{2}}$ , then the value of \*

- is :  
(1)  $\frac{25}{2}$       (2)  $\frac{4}{25}$   
(3) 4      (4) 25

(SSC CGL Prelim Exam. 24.02.2002  
(First Sitting)

**11.** The value of  $0.008 \times 0.01 \times 0.072 \div (0.12 \times 0.0004)$  is :

- (1) 1.2      (2) 0.12  
(3) 0.012      (4) 1.02

(SSC CGL Prelim Exam. 24.02.2002  
(First Sitting)

**12.** The value of

$$\frac{2}{3} \times \frac{3}{\frac{5}{6} \div \frac{2}{3} \text{ of } 1\frac{1}{4}}$$

- (1) 2      (2) 1  
(3)  $\frac{1}{2}$       (4)  $\frac{2}{3}$

(SSC CGL Prelim Exam. 24.02.2002  
(1st Sitting) & (SSC CGL Prelim Exam. 13.11.2005 (IInd Sitting)

**13.** Find the sum of the following :

$$\frac{1}{9} + \frac{1}{6} + \frac{1}{12} + \frac{1}{20} + \frac{1}{30} + \frac{1}{42} + \frac{1}{56} + \frac{1}{72}$$

- (1)  $\frac{1}{2}$       (2) 0

- (3)  $\frac{1}{9}$       (4)  $\frac{1}{2520}$

(SSC CGL Prelim Exam. 24.02.2002  
(First Sitting)

**14.** The value of  $25 - 5 [2 + 3 (2 - 2(5-3) + 5) - 10] \div 4$  is :

- (1) 5      (2) 23.25  
(3) 23.75      (4) 25

(SSC CGL Prelim Exam. 24.02.2002  
(Second Sitting)

## SIMPLIFICATION

**15.** Find the value of \* in the following

$$1\frac{2}{3} \div \frac{2}{7} \times \frac{*}{7} = 1\frac{1}{4} \times \frac{2}{3} \div \frac{1}{6}$$

- (1)  $\frac{1}{6}$  (2) 0.6

- (3) 0.006 (4) 6

(SSC CGL Prelim Exam. 24.02.2002  
(Second Sitting)

**16.**  $9 - 1\frac{2}{9}$  of  $3\frac{3}{11} \div 5\frac{1}{7}$  of  $\frac{7}{9}$  is equal to :

- (1) 8 (2) 9

- (3)  $8\frac{32}{81}$  (4)  $\frac{3}{4}$

(SSC CGL Prelim Exam. 24.02.2002  
(Second Sitting)

**17.** The value of

$$\frac{5}{1\frac{7}{8} \text{ of } 1\frac{1}{3}} \times \frac{2\frac{1}{10}}{3\frac{1}{2}} \text{ of } 1\frac{1}{4}$$

- (1)  $1\frac{1}{2}$  (2) 0.05

- (3) 1 (4) 2

(SSC CGL Prelim Exam. 24.02.2002  
(Middle Zone)

$$18. \frac{9}{20} - \left[ \frac{1}{5} + \left\{ \frac{1}{4} + \left( \frac{5}{6} - \frac{1}{3} + \frac{1}{2} \right) \right\} \right]$$

is equal to

- (1) 0 (2) 1

- (3)  $\frac{9}{20}$  (4)  $\frac{9}{10}$

(SSC CGL Prelim Exam. 24.02.2002  
(Middle Zone)

$$19. \frac{0.83 \div 7.5}{2.321 - 0.098} \text{ is equal to}$$

- (1) 0.6 (2) 0.1

- (3) 0.06 (4) 0.05

(SSC CGL Prelim Exam. 24.02.2002  
(Middle Zone)

**20.** For what value of \*, statement

$$\left[ \frac{(*)}{21} \times \frac{(*)}{189} \right] = 1 \text{ is correct ?}$$

- (1) 3969 (2) 147

- (3) 63 (4) 21

(SSC CGL Prelim Exam. 24.02.2002  
(Middle Zone)

**21.** If  $\frac{1120}{\sqrt{P}} = 80$ , then P is equal to

- (1) 14 (2) 140  
(3) 196 (4) 225

(SSC CPO S.I. Exam. 12.01.2003)

$$22. \frac{3\frac{1}{4} - \frac{4}{5} \text{ of } \frac{5}{6}}{4\frac{1}{3} \div \frac{1}{5} - \left( \frac{3}{10} + 21\frac{1}{5} \right)} - \left( \frac{2}{3} \text{ of } 1\frac{1}{2} \right)$$

is equal to

- (1) 9 (2)  $11\frac{1}{2}$

- (3) 13 (4)  $15\frac{1}{2}$

(SSC CPO S.I. Exam. 12.01.2003)

**23.** Simplify

$$\left[ \frac{3\frac{1}{4} \div \left\{ 1\frac{1}{4} - \frac{1}{2} \left( 2\frac{1}{2} - \frac{1}{4} - \frac{1}{6} \right) \right\}}{\frac{1}{2} \text{ of } 4\frac{1}{3}} \right]$$

- (1) 18 (2) 36  
(3) 39 (4) 78

(SSC CPO S.I. Exam. 12.01.2003)

**24.** The value of

$$\frac{0.1 \times 0.1 \times 0.1 + 0.2 \times 0.2 \times 0.2 + 0.3 \times 0.3 \times 0.3 - 3 \times 0.1 \times 0.2 \times 0.3}{0.1 \times 0.1 + 0.2 \times 0.2 + 0.3 \times 0.3 - 0.1 \times 0.2 - 0.2 \times 0.3 - 0.3 \times 0.1}$$

- is  
(1) 0.006 (2) 0.6  
(3) 0 (4) 0.2

(SSC CPO S.I. Exam. 12.01.2003)

**25.**

$$\frac{1}{30} + \frac{1}{42} + \frac{1}{56} + \frac{1}{72} + \frac{1}{90} + \frac{1}{110} = ?$$

- (1)  $\sqrt{2}\frac{2}{27}$  (2)  $\frac{1}{9}$

- (3)  $\frac{5}{27}$  (4)  $\frac{6}{55}$

(SSC CPO S.I. Exam. 12.01.2003)

**26.** If  $I = \frac{3}{4} \div \frac{5}{6}$ ,  $II = 3 \div [(4 \div 5) \div 6]$ ,

$III = [3 \div (4 \div 5)] \div 6$ ,  $IV = 3 \div 4$   
(5  $\div$  6) then

- (1) I and II are equal  
(2) I and IV are equal  
(3) I and III are equal  
(4) All are equal

(SSC CPO S.I. Exam. 12.01.2003)

**27.** The value of  $1 \div [1 + 1 \div \{1 + 1 \div (1 + 1 \div 2)\}]$  is

- (1) 1 (2)  $\frac{5}{8}$

- (3) 2 (4)  $\frac{1}{2}$

(SSC CGL Prelim Exam. 11.05.2003  
(First Sitting))

**28.** The simplified value of

$$\frac{\frac{1}{3} \div \frac{1}{3} \times \frac{1}{3}}{\frac{1}{3} \div \frac{1}{3} \text{ of } \frac{1}{3}} - \frac{1}{9} \text{ is}$$

- (1) 0 (2) 1

- (3)  $\frac{1}{3}$  (4)  $\frac{1}{9}$

(SSC CGL Prelim Exam. 11.05.2003  
(First Sitting))

**29.** Simplify :

$$\frac{\frac{2}{4} \div \frac{7}{8} \times \left( \frac{1}{3} + \frac{1}{4} \right) + \frac{5}{7} \div \frac{3}{4} \text{ of } \frac{3}{7}}{\frac{1}{5} \div \frac{6}{6}}$$

- (1)  $\frac{56}{77}$  (2)  $\frac{49}{80}$

- (3)  $\frac{2}{3}$  (4)  $3\frac{2}{9}$

(SSC CGL Prelim Exam. 11.05.2003  
(First Sitting))

**30.** The simplification of

$$3.\overline{36} - 2.\overline{05} + 1.\overline{33} \text{ equals :}$$

- (1) 2.60 (2) 2.61

- (3) 2.64 (4) 2.64

(SSC CGL Prelim Exam. 11.05.2003  
(First Sitting))

**31.** The value of

$$0.9 \times 0.9 \times 0.9 + 0.2 \times 0.2 \times 0.2 + 0.3 \times 0.3$$

$$\times 0.3 - 3 \times 0.9 \times 0.2 \times 0.3$$

$$\frac{0.9 \times 0.9 + 0.2 \times 0.2 + 0.3 \times 0.3 - 0.9}{0.9 \times 0.9 + 0.2 \times 0.2 + 0.3 \times 0.3 - 0.9}$$

$$\times 0.2 - 0.2 \times 0.3 - 0.3 \times 0.9$$

is

- (1) 1.4 (2) 0.054

- (3) 0.8 (4) 1.0

(SSC CGL Prelim Exam. 11.05.2003  
(Second Sitting))

## SIMPLIFICATION

**32.** Simplify :

$$(0.\overline{1})^2 \left\{ 1 - 9 (0.1\overline{6})^2 \right\}$$

$$(1) -\frac{1}{162} \quad (2) \frac{1}{108}$$

$$(3) \frac{7696}{10^6} \quad (4) \frac{1}{109}$$

(SSC CGL Prelim Exam. 11.05.2003  
(Second Sitting)

**33.** Simplify :

$$\frac{1 + \frac{1}{2}}{1 - \frac{1}{2}} \div \frac{4}{7} \left( \frac{2}{5} + \frac{3}{10} \right) \text{ of } \frac{\frac{1}{2} + \frac{1}{3}}{\frac{1}{2} - \frac{1}{3}}$$

$$(1) \frac{2}{3} \quad (2) 37\frac{1}{2}$$

$$(3) \frac{3}{2} \quad (4) 18\frac{3}{8}$$

(SSC CGL Prelim Exam. 11.05.2003  
(Second Sitting)

**34.** Simplify :

$$[0.9 - \{2.3 - 3.2 - (7.1 - 5.4 - 3.5)\}]$$

$$(1) 0.18 \quad (2) 1.8 \\ (3) 0 \quad (4) 2.6$$

(SSC CGL Prelim Exam. 11.05.2003  
(Second Sitting)

**35.**  $(32)^3 + (79)^3 - (111)^3 + 3 \times 32 \times 79 \times 111$  is equal to

$$(1) 10000 \quad (2) 0 \\ (3) 30007 \quad (4) 1$$

(SSC CPO S.I. Exam. 07.09.2003)

**36.**  $\left(\frac{5}{2} + \frac{3}{2}\right) \left(\frac{25}{4} - \frac{15}{4} + \frac{9}{4}\right)$  is equal to

$$(1) 38 \quad (2) 19 \\ (3) 37 \quad (4) 36$$

(SSC CPO S.I. Exam. 07.09.2003)

**37.**  $(0.2 \times 0.2 + 0.01) (0.1 \times 0.1 + 0.02)^{-1}$  is equal to

$$(1) \frac{5}{3} \quad (2) \frac{41}{12} \\ (3) \frac{41}{4} \quad (4) \frac{9}{5}$$

(SSC Section Officer (Commercial Audit)  
Exam. 16.11.2003)

**38.**  $\frac{1}{2} + \left\{ 4 \frac{3}{4} - \left( 3 \frac{1}{6} - 2 \frac{1}{3} \right) \right\}$  is equal to

$$(1) 3\frac{2}{3} \quad (2) 1\frac{1}{4}$$

$$(3) 4\frac{5}{12} \quad (4) 1\frac{2}{3}$$

(SSC Section Officer (Commercial Audit)  
Exam. 16.11.2003)

**39.** The simplification of

$$\frac{1}{8} + \frac{1}{8^2} + \frac{1}{8^3} + \frac{1}{8^4} + \frac{1}{8^5} \text{ upto}$$

three-places of decimals yields

$$(1) 0.143 \quad (2) 0.163 \\ (3) 0.215 \quad (4) 0.715$$

(SSC Section Officer (Commercial Audit)  
Exam. 16.11.2003)

**40.**  $8.7 - [7.6 - \{6.5 - (5.4 - 4.3 - 2)\}]$  is

simplified to :

$$(1) 2.5 \quad (2) 3.5 \\ (3) 4.5 \quad (4) 5.5$$

(SSC CGL Prelim Exam. 08.02.2004  
(Second Sitting)

**41.** The simplified value of

$$[(0.111)^3 + (0.222)^3 - (0.333)^3 + (0.333)^2 (0.222)]^3 \text{ is :}$$

$$(1) 0.999 \quad (2) 0 \\ (3) 0.888 \quad (4) 0.111$$

(SSC CGL Prelim Exam. 08.02.2004  
(Second Sitting)

**42.**  $\frac{1\frac{1}{4} \div 1\frac{1}{2}}{\left(\frac{1}{15} + 1 - \frac{9}{10}\right)}$  is equal to :

$$(1) 3 \quad (2) 6 \\ (3) \frac{2}{5} \quad (4) 5$$

(SSC CGL Prelim Exam. 08.02.2004  
(Second Sitting)

**43.**  $-\frac{1}{2} - \frac{2}{3} + \frac{4}{5} - \frac{1}{3} + \frac{1}{5} + \frac{3}{4}$  is sim-

$$\frac{1}{2} + \frac{2}{3} - \frac{4}{3} + \frac{1}{3} - \frac{1}{5} - \frac{4}{5}$$

plified to

$$(1) -\frac{10}{3} \quad (2) -\frac{3}{10}$$

$$(3) 1 \quad (4) -2$$

(SSC CGL Prelim Exam. 08.02.2004  
(Second Sitting)

**44.** The simplification of

$$(0.\overline{63} + 0.\overline{37} + 0.\overline{80}) \text{ yields the result}$$

$$(1) 1.\overline{80} \quad (2) 1.\overline{81}$$

$$(3) 1.\overline{79} \quad (4) 1.80$$

(SSC CGL Prelim Exam. 08.02.2004  
(Second Sitting)

$$45. \frac{(4.53 - 3.07)^2}{(3.07 - 2.15)(2.15 - 4.53)} +$$

$$\frac{(3.07 - 2.15)^2}{(2.15 - 4.53)(4.53 - 3.07)} +$$

$$\frac{(2.15 - 4.53)^2}{(4.53 - 3.07)(3.07 - 2.15)} \text{ is}$$

$$(1) 0 \quad (2) 1 \\ (3) 2 \quad (4) 3$$

(SSC CPO S.I. Exam. 05.09.2004)

$$46. \frac{17}{15} \times \frac{17}{15} + \frac{2}{15} \times \frac{2}{15} - \frac{17}{15} \times \frac{4}{15} \text{ is equal to}$$

$$(1) 0 \quad (2) 1 \\ (3) 10 \quad (4) 11$$

(SSC CPO S.I. Exam. 05.09.2004)

$$47. \left(4\frac{11}{15} + \frac{15}{71}\right)^2$$

$$-\left(4\frac{11}{15} - \frac{15}{71}\right)^2 \text{ is equal to :}$$

$$(1) 1 \quad (2) 2 \\ (3) 3 \quad (4) 4$$

(SSC CPO S.I. Exam. 26.05.2005)

**48.** The value of

$$\frac{0.1 \times 0.1 \times 0.1 + 0.02 \times 0.02 \times 0.02}{0.2 \times 0.2 \times 0.2 + 0.04 \times 0.04 \times 0.04} \text{ is :}$$

$$(1) 0.0125 \quad (2) 0.125 \\ (3) 0.25 \quad (4) 0.5$$

(SSC CGL Prelim Exam. 13.11.2005  
(First Sitting)

**49.** If \* represents a number, then the value of \* in  $5\frac{3}{*} \times 3\frac{1}{2} = 19$  is :

$$(1) 7 \quad (2) 4 \\ (3) 6 \quad (4) 2$$

(SSC CGL Prelim Exam. 13.11.2005  
(First Sitting)

$$50. \left(\sqrt{2} + \frac{1}{\sqrt{2}}\right)^2 \text{ is equal to :}$$

$$(1) 2\frac{1}{2} \quad (2) 3\frac{1}{2} \\ (3) 4\frac{1}{2} \quad (4) 5\frac{1}{2}$$

(SSC CGL Prelim Exam. 13.11.2005  
(1st Sitting) & (SSC CISF ASI  
Exam. 29.08.2010)

**51.** The value of  $(0.98)^3 + (0.02)^3 + 3 \times 0.98 \times 0.02 - 1$  is :

- (1) 1.98      (2) 1.09  
 (3) 1      (4) 0

(SSC CGL Prelim Exam. 13.11.2005  
 (First Sitting)

**52.**  $(71 \times 29 + 27 \times 15 + 8 \times 4)$  equals

- (1) 3450      (2) 3458  
 (3) 2496      (4) None of these

(SSC CGL Prelim Exam. 13.11.2005  
 (Second Sitting)

**53.**  $(0.05 \times 5 - 0.005 \times 5)$  equals

- (1) 2.250      (2) 0.225  
 (3) 0.0225      (4) 0.275

(SSC CGL Prelim Exam. 13.11.2005  
 (Second Sitting)

**54.** The value of

$$\frac{0.2 \times 0.2 \times 0.2 + 0.04 \times 0.04 \times 0.04}{0.4 \times 0.4 \times 0.4 + 0.08 \times 0.08 \times 0.08}$$

is

- (1) 0.5      (2) 0.25  
 (3) 0.75      (4) 0.125

(SSC CGL Prelim Exam. 13.11.2005  
 (Second Sitting)

**55.**  $(256)^{0.16} \times (16)^{0.18}$  is equal to

- (1) 4      (2) 16  
 (3) 64      (4) 256.25

(SSC CGL Prelim Exam. 04.02.2007  
 (First Sitting)

**56.**

$$\left( \frac{1}{3.5} + \frac{1}{5.7} + \frac{1}{7.9} + \frac{1}{9.11} + \frac{1}{11.13} + \frac{1}{13.15} \right)$$

is equal to

- (1)  $\frac{2}{45}$       (2)  $\frac{4}{45}$   
 (3)  $\frac{7}{45}$       (4)  $\frac{2}{15}$

(SSC CGL Prelim Exam. 04.02.2007  
 (Second Sitting)

**57.**  $(53 \times 87 + 159 \times 21 + 106 \times 25)$  is equal to

- (1) 16000      (2) 1060  
 (3) 10600      (4) 60100

(SSC CGL Prelim Exam. 04.02.2007  
 (Second Sitting)

**58.** The value of  $\frac{0.125 + 0.027}{0.25 - 0.15 + 0.09}$  is

- (1) 0.2      (2) 0.25  
 (3) 0.3      (4) 0.8

(SSC CGL Prelim Exam. 27.07.2008 (IInd Sitting) & (SSC CGL Tier-I Exam. 16.05.2010 (Ist Sitting)

**59.**  $\frac{8(3.75)^3 + 1}{(7.5)^2 - 6.5}$  is equal to

- (1) 2.75      (2)  $\frac{9}{5}$

- (3) 4.75      (4) 8.5

(SSC CGL Prelim Exam. 27.07.2008  
 (Second Sitting)

**60.** The value of

$$\frac{(2.697 - 0.498)^2 + (2.697 + 0.498)^2}{2.697 \times 2.697 + 0.498 \times 0.498}$$

- (1) 4      (2) 2

- (3) 2.199      (4) 3.195

(SSC CGL Prelim Exam. 27.07.2008  
 (Second Sitting)

**61.** The least fraction to be subtracted from the expression

$$\frac{3\frac{1}{4} - \frac{4}{5} \text{ of } \frac{5}{6}}{4\frac{1}{3} \div \frac{1}{5} - \left( \frac{3}{10} + 21\frac{1}{5} \right)}$$

to make

it an integer.

- (1)  $\frac{1}{2}$       (2)  $\frac{5}{6}$

- (3)  $\frac{1}{4}$       (4)  $\frac{3}{10}$

(SSC CPO S.I. Exam. 06.09.2009)

**62.** If  $\sqrt[2]{0.014 \times 0.14x} = 0.014 \times$

$0.14 \sqrt[2]{y}$ , find the value of  $\frac{x}{y}$ .

- (1) 0.000196      (2) 0.00196  
 (3) 0.0196      (4) 0.196

(SSC CPO S.I. Exam. 06.09.2009)

**63.**  $\frac{4.41 \times 0.16}{2.1 \times 1.6 \times 0.21}$  is simplified to

- (1) 1      (2) 0.1  
 (3) 0.01      (4) 10

(SSC CGL Tier-I Exam. 16.05.2010  
 (First Sitting)

**64.**  $(0.1 \times 0.01 \times 0.001 \times 10^7)$  is equal to

- (1) 100      (2)  $\frac{1}{10}$

- (3)  $\frac{1}{100}$       (4) 10

(SSC CGL Tier-I Exam. 16.05.2010  
 (Second Sitting)

**65.**  $\frac{3.25 \times 3.20 - 3.20 \times 3.05}{0.064}$  is equal to :

- (1) 1      (2)  $\frac{1}{2}$

- (3)  $\frac{1}{10}$       (4) 10

(SSC CGL Tier-I Exam. 16.05.2010  
 (Second Sitting)

**66.**  $\left\{ \frac{(0.1)^2 - (0.01)^2}{0.0001} + 1 \right\}$  is equal to

- (1) 1010      (2) 110  
 (3) 101      (4) 100

(SSC CGL Tier-I Exam. 16.05.2010  
 (Second Sitting)

**67.**  $(0.5 \times 5 + 0.25 \times 0.5 + 0.5 \times 4 + 0.5 \times 0.75)$  is equal to

- (1) 5      (2) 10  
 (3) 15      (4) 20

(SSC CISF ASI Exam. 29.08.2010  
 (Paper-1))

**68.**  $\frac{(5+5+5+5) \div 5}{3+3+3+3 \div 3}$  is equal to

- (1) 1      (2)  $\frac{3}{10}$

- (3)  $\frac{4}{9}$       (4)  $\frac{2}{5}$

(SSC (South Zone) Investigator Exam. 12.09.2010)

**69.**

$\frac{(100-1)(100-2)(100-3)\dots(100-200)}{100 \times 99 \times 98 \times \dots \times 3 \times 2 \times 1}$

is equal to

- (1)  $\frac{100}{99 \times 98 \times 97 \times \dots \times 3 \times 2 \times 1}$

- (2)  $-\frac{1}{99 \times 98 \times 97 \times \dots \times 3 \times 2 \times 1}$

- (3) 0

- (4)  $-\frac{2}{99 \times 98 \times 97 \times \dots \times 3 \times 2 \times 1}$

(SSC CPO S.I. Exam. 12.12.2010  
 (Paper-I))

**70.**  $(0.9 \times 0.9 \times 0.9 + 0.1 \times 0.1 \times 0.1)$  is equal to

- (1) 0.73      (2) 0.82  
 (3) 0.91      (4) 1.00

(SSC CPO S.I. Exam. 12.12.2010  
 (Paper-I))

## SIMPLIFICATION

**71.** Simplify:

$$\frac{0.0347 \times 0.0347 \times 0.0347 + (0.9653)^3}{(0.0347)^2 - (0.347)(0.09653) + (0.9653)^2}$$

- (1) 0.9306      (2) 1.0009  
 (3) 1.0050      (4) 1

(SSC CGL Tier-I Exam. 19.06.2011  
 (First Sitting)

$$72. \text{ The value of } \frac{(3.2)^3 - 0.008}{(3.2)^2 + 0.64 + 0.04}$$

is

- (1) 0      (2) 2.994  
 (3) 3.208      (4) 3

(SSC CGL Tier-I Exam. 26.06.2011  
 (Second Sitting)

**73.** Simplify:

$$\frac{\frac{1}{3} + \frac{1}{4} \left[ \frac{2}{5} - \frac{1}{2} \right]}{1 \frac{2}{3} \text{ of } \frac{3}{4} - \frac{3}{4} \text{ of } \frac{4}{5}}$$

- (1)  $\frac{37}{78}$       (2)  $\frac{37}{13}$

- (3)  $\frac{74}{78}$       (4)  $\frac{74}{13}$

(SSC Multi-Tasking (Non-Technical)  
 Staff Exam. 20.02.2011)

$$74. \frac{0.04}{0.03} \text{ of } \frac{\left(3 \frac{1}{3} - 2 \frac{1}{2}\right) \div \frac{1}{2} \text{ of } 1 \frac{1}{4}}{\frac{1}{3} + \frac{1}{5} \text{ of } \frac{1}{9}}$$

- (1) 1      (2) 5  
 (3)  $\frac{1}{5}$       (4)  $\frac{1}{2}$

(SSC Multi-Tasking (Non-Technical)  
 Staff Exam. 27.02.2011)

$$75. \frac{0.3555 \times 0.5555 \times 2.025}{0.225 \times 1.7775 \times 0.2222} \text{ is equal}$$

- to :  
 (1) 5.4      (2) 4.58  
 (3) 4.5      (4) 5.45

(SSC CHSL DEO & LDC Exam.  
 04.11.2012 (IIInd Sitting)

$$76. 100 \times 10 - 100 + 2000 \div 100 = ?$$

- (1) 29      (2) 920  
 (3) 980      (4) 1000

(SSC Graduate Level Tier-I Exam.  
 11.11.2012 (Ist Sitting)

$$77. \text{ If } \frac{547.527}{0.0082} = x, \text{ then the}$$

value of  $\frac{547527}{82}$  is

- (1)  $10x$       (2)  $100x$

- (3)  $\frac{x}{100}$       (4)  $\frac{x}{10}$

(SSC CHSL DEO & LDC Exam.  
 04.11.2012 Ist Sitting)

$$78. \frac{1}{1+2^{a-b}} + \frac{1}{1+2^{b-a}} \text{ is}$$

- (1)  $a - b$       (2)  $b - a$   
 (3) 1      (4) 0

(SSC Graduate Level Tier-I  
 Exam. 21.04.2013 IIInd Sitting)

**79.** The value of

$$3 \frac{1}{2} - \left[ 2 \frac{1}{4} \div \left\{ 1 \frac{1}{4} - \frac{1}{2} \left( 1 \frac{1}{2} - \frac{1}{3} - \frac{1}{6} \right) \right\} \right]$$

is

- (1)  $\frac{1}{2}$       (2)  $2 \frac{1}{2}$

- (3)  $3 \frac{1}{2}$       (4)  $9 \frac{1}{2}$

(SSC CHSL DEO & LDC Exam.  
 27.10.2013 IIInd Sitting)

$$80. 3 \frac{3}{5} \times 3 \frac{3}{5} + 2 \times 3 \frac{3}{5} \times \frac{2}{5} + \frac{2}{5} \times \frac{2}{5} = ?$$

- (1) 15      (2) 16  
 (3) 17      (4) 18

(SSC Constable (GD)  
 Exam. 12.05.2013)

**81.** Find the sum of

$$\left(1 - \frac{1}{n+1}\right) + \left(1 - \frac{2}{n+1}\right) +$$

$$\left(1 - \frac{3}{n+1}\right) + \dots \dots \left(1 - \frac{n}{n+1}\right)$$

- (1)  $n$       (2)  $\frac{1}{2}n$

- (3)  $(n+1)$       (4)  $\frac{1}{2}(n+1)$

(SSC Graduate Level Tier-II  
 Exam. 29.09.2013)

**82.** The value of

$$5 \frac{1}{3} \div 1 \frac{2}{9} \times \frac{1}{4} \left( 10 + \frac{3}{1 - \frac{1}{5}} \right) \text{ is}$$

- (1) 15      (2)  $\frac{67}{25}$

- (3)  $\frac{128}{11}$       (4)  $\frac{128}{99}$

(SSC CGL Tier-I Re-Exam. (2013)  
 20.07.2014 (Ist Sitting)

**83.** If  $x [-2 \{-4 (-a)\}] + 5 [-2 \{-2 (-a)\}] = 4a$ , then  $x =$   
 (1) -2      (2) -3  
 (3) -4      (4) -5

(SSC CGL Tier-I Exam.  
 19.10.2014 (Ist Sitting)

**84.** The value of

$$3 \div \left[ (8 - 5) \div \left\{ (4 - 2) + \left( 2 + \frac{8}{13} \right) \right\} \right] \text{ is}$$

- (1)  $\frac{15}{17}$       (2)  $\frac{13}{17}$

- (3)  $\frac{15}{19}$       (4)  $\frac{13}{19}$

(SSC CAPFs SI, CISF ASI & Delhi  
 Police SI Exam. 22.06.2014  
 TF No. 999 KPO)

**85.** If '+' means ' $\div$ ', ' $\times$ ' means ' $-$ ',  
 ' $\div$ ' means ' $\times$ ' and ' $-$ ' means ' $+$ ',  
 what will be the value of the  
 following expression ?

$$9 + 3 \div 4 - 8 \times 2 = ?$$

- (1)  $6 \frac{1}{4}$       (2)  $6 \frac{3}{4}$

- (3)  $-1 \frac{3}{4}$       (4) 18

(SSC CAPFs SI, CISF ASI & Delhi  
 Police SI Exam. 22.06.2014  
 TF No. 999 KPO)

**86.** The simplified value of

$$\frac{4}{15} \text{ of } \frac{5}{8} \times 6 + 15 - 10 \text{ is}$$

- (1) 6      (2) 3  
 (3) 5      (4) 4

(SSC CAPFs SI, CISF ASI & Delhi  
 Police SI Exam. 21.06.2015  
 IIInd Sitting)

**87.** The value of the following is :

$$\frac{0.2 \times 0.02 \times 0.002 \times 32}{0.4 \times 0.04 \times 0.004 \times 16}$$

- (1) 0.20      (2) 0.50  
 (3) 0.40      (4) 0.25

(SSC CAPFs (CPO) SI & ASI,  
 Delhi Police Exam. 20.03.2016)  
 (IIInd Sitting)

**88.**  $(113^2 + 115^2 + 117^2 - 113 \times 115 - 115 \times 117 - 117 \times 113)$  is equal to

- (1) 0      (2) 4  
 (3) 8      (4) 12

(SSC CGL Tier-I (CBE)  
 Exam. 31.08.2016) (IIInd Sitting)

### TYPE-III

**1.** Assume that

$$\sqrt{13} = 3.605 \text{ (approximately)}$$

$$\sqrt{1300} = 11.40 \text{ (approximately)}$$

Find the value of :

$$\sqrt{1.3} + \sqrt{1300} + \sqrt{0.013}$$

- (1) 36.164      (2) 36.304  
 (3) 37.304      (4) 37.164

(SSC CGL Prelim Exam. 04.07.1999)  
 (First Sitting)

**2.** On simplification of

$$\frac{(2.644)^2 - (2.356)^2}{0.288}$$

we get :

- (1) 1      (2) 4  
 (3) 5      (4) 6

(SSC CGL Prelim Exam. 04.07.1999)  
 (First Sitting)

**3.** Simplification of

$$\frac{(3.4567)^2 - (3.4533)^2}{0.0034}$$

yields the result :

- (1) 6.91      (2) 7  
 (3) 6.81      (4) 7.1

(SSC CGL Prelim Exam. 04.07.1999)  
 (Second Sitting)

**4.** The value of  $\frac{(0.03)^2 - (0.01)^2}{0.03 - 0.01}$  is:

- (1) 0.02      (2) 0.004  
 (3) 0.4      (4) 0.04

(SSC CGL Prelim Exam.  
 04.07.1999 (Second Sitting)

**5.**  $(\sqrt{72} - \sqrt{18}) \div \sqrt{12}$  is equal to:

- (1)  $\sqrt{6}$       (2)  $\sqrt{3}/2$   
 (3)  $\sqrt{2}/3$       (4)  $\sqrt{6}/2$

(SSC CGL Prelim Exam. 27.02.2000)  
 (First Sitting)

**6.** The value of  $\frac{\sqrt{80} - \sqrt{112}}{\sqrt{45} - \sqrt{63}}$  is :

- (1)  $\frac{3}{4}$       (2)  $1\frac{3}{4}$   
 (3)  $1\frac{1}{3}$       (4)  $1\frac{7}{9}$

(SSC CGL Prelim Exam. 27.02.2000)  
 (First Sitting)

**7.** The value of

$$\sqrt{\frac{(0.1)^2 + (0.01)^2 + (0.009)^2}{(0.01)^2 + (0.001)^2 + (0.0009)^2}}$$

is :

- (1)  $10^2$       (2) 10  
 (3) 0.1      (4) 0.01

(SSC CGL Prelim Exam. 24.02.2002)  
 (First Sitting)

**8.** The value of

$$\sqrt{\frac{(0.03)^2 + (0.21)^2 + (0.065)^2}{(0.003)^2 + (0.021)^2 + (0.0065)^2}}$$

is :

- (1) 0.1      (2) 10  
 (3)  $10^2$       (4)  $10^3$

(SSC CGL Prelim Exam. 24.02.2002)  
 (Second Sitting)

**9.** The sum of

$$\sqrt{0.01} + \sqrt{0.81} + \sqrt{1.21} + \sqrt{0.0009}$$

is :

- (1) 2.1      (2) 2.13  
 (3) 2.03      (4) 2.11

(SSC CGL Prelim Exam. 24.02.2002)  
 (Second Sitting)

**10.** The value of

$$\sqrt{\frac{(6.1)^2 + (61.1)^2 + (611.1)^2}{(0.61)^2 + (6.11)^2 + (61.11)^2}}$$

- (1) 0.1      (2) 1.1  
 (3) 10      (4) 100

(SSC CGL Prelim Exam. 24.02.2002)  
 (Middle Zone)

**11.** Simplify

$$\sqrt{[(12.1)^2 - (8.1)^2] + [(0.25)^2 + (0.25)(19.95)]}$$

- (1) 1      (2) 2  
 (3) 3      (4) 4

(SSC CPO S.I. Exam. 12.01.2003)

**12.** The value of

$$\frac{0.051 \times 0.051 \times 0.051 + 0.041 \times 0.041 \times 0.041}{0.051 \times 0.051 - 0.051 \times 0.041 + 0.041 \times 0.041}$$

- is :  
 (1) 0.92      (2) 0.092  
 (3) 0.0092      (4) 0.00092

(SSC CGL Prelim Exam. 11.05.2003)  
 (First Sitting)

**13.** The value of

$$\sqrt{5 + \sqrt{11 + \sqrt{19 + \sqrt{29 + \sqrt{49}}}}}$$

- (1) 3      (2) 9  
 (3) 7      (4) 5

(SSC CGL Prelim Exam. 11.05.2003)  
 (Second Sitting)

**14.** The value of  $\frac{(75.8)^2 - (55.8)^2}{20}$  is

- (1) 20      (2) 40  
 (3) 121.6      (4) 131.6

(SSC CPO S.I. Exam. 07.09.2003)

**15.**  $\sqrt{\frac{0.25}{0.0009}} \times \sqrt{\frac{0.09}{0.36}}$  is equal to :

- (1)  $\frac{5}{6}$       (2)  $7\frac{1}{6}$   
 (3)  $7\frac{1}{3}$       (4)  $8\frac{1}{3}$

(SSC CGL Prelim Exam. 08.02.2004)  
 (First Sitting)

**16.**  $\frac{(3.63)^2 - (2.37)^2}{3.63 + 2.37}$  is simplified to

- (1) 6      (2) 1.36  
 (3) 2.26      (4) 1.26

(SSC CPO S.I. Exam. 03.09.2006)

**17.**  $\sqrt{\frac{0.081 \times 0.484}{0.0064 \times 6.25}}$  is equal to

- (1) 9      (2) 0.9  
 (3) 99      (4) 0.99

(SSC CPO S.I. Exam. 09.11.2008)

**18.** The simplified value of

$$\sqrt{900} + \sqrt{0.09} - \sqrt{0.000009}$$

- (1) 30.27      (2) 30.297  
 (3) 30.097      (4) 30.197

(SSC CPO S.I. Exam. 06.09.2009)

**19.**  $\sqrt{\frac{0.009 \times 0.036 \times 0.016 \times 0.08}{0.002 \times 0.0008 \times 0.0002}}$

is equal to

- (1) 34      (2) 36  
(3) 38      (4) 39

(SSC CGL Tier-I Exam. 16.05.2010  
(First Sitting)

**20.**  $\sqrt{1\frac{1}{4} \times \frac{64}{125} \times 1.44}$  is equal to

- (1)  $1\frac{1}{25}$       (2)  $\frac{24}{25}$   
(3)  $\frac{23}{25}$       (4)  $\frac{21}{25}$

(SSC CISF ASI Exam. 29.08.2010  
(Paper-1)

**21.**  $\left[ 2\sqrt{54} - 6\sqrt{\frac{2}{3}} - \sqrt{96} \right]$  is equal to

- (1) 0      (2) 1  
(3) 2      (4)  $\sqrt{6}$

(SSC CISF ASI Exam. 29.08.2010  
(Paper-1)

**22.**  $\frac{\sqrt{24} + \sqrt{216}}{\sqrt{96}}$  is equal to

- (1)  $\frac{2}{\sqrt{6}}$       (2)  $2\sqrt{6}$   
(3)  $4\sqrt{6}$       (4) 2

(SSC CPO Sub-Inspector  
Exam. 12.12.2010 (Paper-1)

**23.** The value of  $\frac{4 - \sqrt{0.04}}{4 + \sqrt{0.4}}$  is close to

- (1) 0.4      (2) 0.8  
(3) 1.0      (4) 1.4

(SSC CPO S.I. Exam. 12.01.2003)

**24.** The value of

$$(3 + \sqrt{8}) + \frac{1}{3 - \sqrt{8}} - (6 + 4\sqrt{2})$$

- (1) 8      (2) 1  
(3)  $\sqrt{2}$       (4) 0

(SSC FCI Assistant Grade-III Main  
Exam. 07.04.2013)

**25.** What is the square root of 0.09?  
(1) 0.3      (2) 0.03  
(3) 0.003      (4) 3.0  
(SSC CGL Prelim Exam. 04.07.1999  
(First Sitting)

**26.** The square root of :

$$\frac{(0.75)^3}{1 - 0.75} + \left[ 0.75 + (0.75)^2 + 1 \right]$$

is :

- (1) 4      (2) 3  
(3) 2      (4) 1

(SSC CGL Prelim Exam. 04.07.1999  
(Second Sitting)

**27.** The square root of  $(272^2 - 128^2)$  is :

- (1) 256      (2) 200  
(3) 240      (4) 144

(SSC CGL Prelim Exam. 27.02.2000  
(Second Sitting)

**28.** The value of  $\sqrt{0.000441}$  is equal

to :  
(1) 0.21      (2) 0.0021  
(3) 0.021      (4) 0.00021

(SSC CGL Prelim Exam. 24.02.2002  
(First Sitting)

**29.** The value of  $\frac{\sqrt{0.441}}{\sqrt{0.625}}$  is equal

to :  
(1) 0.048      (2) 0.84  
(3) 0.48      (4) 0.084

(SSC CGL Prelim Exam. 24.02.2002  
(Second Sitting)

**30.** The square root of

$$\frac{0.342 \times 0.684}{0.000342 \times 0.000171}$$

is :  
(1) 250      (2) 2500  
(3) 2000      (4) 4000

(SSC CGL Prelim Exam. 24.02.2002  
(Second Sitting)

**31.**  $\sqrt{0.00060516}$  is equal to

- (1) 0.0246      (2) 0.00246  
(3) 0.246      (4) 0.000246

(SSC CGL Prelim Exam. 24.02.2002

(Middle Zone)

**32.** The Square root of

$$\frac{9.5 \times 0.085}{0.017 \times 0.019}$$

is  
(1) 0.5      (2) 5  
(3) 50      (4) 500

(SSC CGL Prelim Exam. 24.02.2002  
(Middle Zone) & SSC MTS Exam.  
17.03.2013 (IIInd Sitting)

**33.** Find the value of

$$\sqrt{248 + \sqrt{52 + \sqrt{144}}}$$

- (1) -16      (2)  $\pm 16$   
(3) 16      (4) 16.2

(SSC CGL Prelim Exam. 24.02.2002  
(Middle Zone) & SSC CGL Exam.  
08.02.2004 (IIInd Sitting)

**34.** If  $(102)^2 = 10404$  then, the value of

$$\sqrt{104.04} + \sqrt{1.0404} + \sqrt{0.010404}$$

is equal to

- (1) 0.306      (2) 0.0306  
(3) 11.122      (4) 11.322

(SSC CGL Prelim Exam. 24.02.2002  
(Middle Zone)

**35.**  $\sqrt{0.00004761}$  equals

- (1) 0.069      (2) 0.0069  
(3) 0.00069      (4) 0.0609

(SSC CPO S.I. Exam. 12.01.2003)

**36.** If  $\sqrt{2} = 1.414$ , the square root

of  $\frac{\sqrt{2} - 1}{\sqrt{2} + 1}$  is nearest to

- (1) 0.172      (2) 0.414  
(3) 0.586      (4) 1.414

(SSC CPO S.I. Exam. 12.01.2003)

**37.**  $\sqrt{\frac{0.00001225}{0.00005392}}$  is equal to :

$$\frac{25}{77} \quad \frac{35}{73}$$

$$\frac{35}{77} \quad \frac{25}{73}$$

(SSC CGL Prelim Exam. 11.05.2003  
(First Sitting)

**38.** The square root of  $0.\bar{4}$  is :

- (1)  $0.\bar{8}$       (2)  $0.\bar{6}$   
(3)  $0.\bar{7}$       (4)  $0.\bar{9}$

(SSC CGL Prelim Exam. 08.02.2004  
(First Sitting)

**39.** The square root of

$$\frac{\left(3\frac{1}{4}\right)^4 - \left(4\frac{1}{3}\right)^4}{\left(3\frac{1}{4}\right)^2 - \left(4\frac{1}{3}\right)^2}$$

$$\left(1\frac{1}{12}\right)^2 \quad \left(5\frac{5}{12}\right)^2$$

$$\left(3\frac{1}{12}\right)^2 \quad \left(1\frac{7}{12}\right)^2$$

(SSC CPO S.I. Exam. 26.05.2005)

**40.** The positive square root of

$$[0.6 \times 0.6 \times 0.6 + 0.4 \times 0.4 \times 0.4 + 3 \times 0.6 \times 0.4]$$

is equal to

- (1) 2.1736      (2) 1  
(3) 0.21736      (4) 0.072

(SSC SAS Exam. 26.06.2010 (Paper-1))

## SIMPLIFICATION

**41.**  $\sqrt{\frac{0.49}{0.25}} + \sqrt{\frac{0.81}{0.36}}$  is equal to :

- (1)  $7\frac{9}{10}$       (2)  $2\frac{9}{10}$

- (3)  $\frac{9}{10}$       (4)  $9\frac{9}{10}$

(SSC CGL Prelim Exam. 04.07.1999  
(First Sitting)

**42.** If  $\sqrt{x} \div \sqrt{441} = 0.02$ , then value of x is :

- (1) 1.64      (2) 2.64  
(3) 1.764      (4) 0.1764

(SSC CGL Prelim Exam. 04.07.1999  
(Second Sitting)

**43.** Find the value of

$$\sqrt{4 + \sqrt{44 + \sqrt{10000}}}$$

- (1) 12      (2) 8  
(3) 4      (4) -4

(SSC CGL Prelim Exam. 04.07.1999  
(Second Sitting)

**44.** Given that

$$\sqrt{574.6} = 23.97$$

$$\sqrt{5746} = 75.8$$

then  $\sqrt{0.00005746}$  equals

- (1) 0.002397      (2) 0.0002397  
(3) 0.007580      (4) 0.00758  
(SSC CPO S.I. Exam. 12.01.2003)

**45.**

$$\sqrt{(0.798)^2 + 0.404 \times 0.798 + (0.202)^2}$$

$$+1 = 2 ?$$

- (1) 0      (2) 2  
(3) 1.596      (4) 0.404

(SSC CGL Prelim Exam. 11.05.2003  
(First Sitting)

**46.** The value of

$$\sqrt{11.981 + 7\sqrt{1.2996}}$$
 is closest to

- (1) 5.1      (2) 4.9  
(3) 4.5      (4) 4.1

(SSC Section Officer (Commercial Audit)  
Exam. 16.11.2003)

**47.** The value of

$$\sqrt{32} - \sqrt{128} + \sqrt{50}$$
 correct to 3

places of decimal is :

- (1) 1.732      (2) 1.141  
(3) 1.414      (4) 1.441

(SSC CGL Prelim Exam. 08.02.2004  
(First Sitting)

**48.** The square root of

$$(7 + 3\sqrt{5})(7 - 3\sqrt{5})$$
 is :

- (1) 4      (2)  $\sqrt{5}$   
(3)  $3\sqrt{5}$       (4) 2

(SSC CGL Prelim Exam. 08.02.2004  
(First Sitting)

**49.** The value of

$$\sqrt{400} + \sqrt{0.0400} + \sqrt{0.000004}$$
 is

- (1) 0.222      (2) 20.22  
(3) 20.202      (4) 2.022

(SSC CGL Prelim Exam. 08.02.2004  
(Second Sitting)

**50.** If  $\sqrt{3} = 1.7321$ , the value of

$$\sqrt{192} - \frac{1}{2}\sqrt{48} - \sqrt{75},$$
 correct to 3

places of decimal, is

- (1) 8.661      (2) 4.331  
(3) 1.7321      (4) -1.732

(SSC CGL Prelim Exam. 08.02.2004  
(Second Sitting)

**51.**  $\sqrt{\frac{48.4}{0.289}}$  is equal to

- (1)  $129\frac{7}{17}$       (2)  $1\frac{5}{17}$

- (3)  $12\frac{16}{17}$       (4)  $12\frac{1}{17}$

(SSC CGL Prelim Exam. 08.02.2004  
(Second Sitting)

**52.** The sum of the squares of 3 consecutive positive numbers is

365. The sum of the numbers is

- (1) 30      (2) 33  
(3) 36      (4) 45

(SSC Multi-Tasking (Non-Technical)  
Staff Exam. 20.02.2011)

**53.** If  $\sqrt{4096} = 64$ , then the value of

$$\sqrt{40.96} + \sqrt{0.4096}$$

$$+\sqrt{0.004096} + \sqrt{0.00004096}$$

up to two places of decimals is :

- (1) 7.09      (2) 7.10  
(3) 7.11      (4) 7.12

(SSC CGL Prelim Exam. 24.02.2002 (Ist  
Sitting) & SSC CGL Prelim Exam.  
13.11.2005 (Ist Sitting) & FCI Assistant  
Grade III Exam. 25.02.2012 (Paper-I)  
North Zone (Ist Sitting)

**54.** Given that  $\sqrt{13} = 3.6$  and

$$\sqrt{130} = 11.4,$$
 then the value of

$$\sqrt{13} + \sqrt{1300} + \sqrt{0.013}$$
 is equal

to  
(1) 36.164      (2) 37.254

- (3) 36.254      (4) 37.154

(SSC CGL Prelim Exam. 27.07.2008  
(Second Sitting)

**55.** The simplified value of

$$\sqrt{5 + \sqrt{11 + \sqrt{19 + \sqrt{29 + \sqrt{49}}}}}$$
 is

- (1) 3      (2) 2  
(3) 4      (4) 6

(SSC CPO S.I. Exam. 06.09.2009)

**56.**  $\sqrt{110\frac{1}{4}}$  is equal to

- (1) 12.0      (2) 11.5  
(3) 11.0      (4) 10.5

(SSC CPO Sub-Inspector  
Exam 12.12.2010 (Paper-I))

**57.**  $\sqrt{8 + \sqrt{57 + \sqrt{38 + \sqrt{108 + \sqrt{169}}}}} = ?$

- (1) 4      (2) 6  
(3) 8      (4) 10

(SSC CGL Tier-1 Exam 19.06.2011  
(First Sitting))

**58.** If  $(10.15)^2 = 103.0225$ , then the  
value of  $\sqrt{1.030225} +$

$$\sqrt{10302.25}$$
 is

- (1) 1025.15      (2) 103.515  
(3) 102.515      (4) 102.0515

(SSC CPO (SI, ASI & Intelligence Officer)  
Exam 28.08.2011 (Paper-I))

**59.** The number of digits in the  
square root of 625686734489 is

- (1) 4      (2) 5

- (3) 6      (4) 7

(SSC CGL Prelim Exam. 04.02.2007  
(First Sitting))

**60.** If the square root of 841 is 29,  
then 0.00000841 is equal to :

- (1) 0.029      (2) 0.0029

- (3) 0.00029      (4) 0.29

(SSC CGL Prelim Exam. 04.07.1999  
(First Sitting) & Tier-1 Exam, 16.05.2010  
(First Sitting))

**61.** The square root of

$$\frac{0.324 \times 0.081 \times 4.624}{1.5625 \times 0.0289 \times 72.9 \times 64}$$
 is

- (1) 24      (2) 2.4

- (3) 0.024      (4) 1.2

(SSC Constable (GD) & Rifleman  
(GD) Exam. 22.04.2012 (Ist Sitting))

## SIMPLIFICATION

**62.** The simplified value of

$$\sqrt{0.25 \times 2.25} \text{ is}$$

- (1) 0.075      (2) 0.705  
 (3) 0.750      (4) 7.500

(SSC Constable (GD) & Rifleman (GD) Exam. 22.04.2012 (IInd Sitting)

**63.**  $\sqrt{64} - \sqrt{36}$  is equal to

- (1) -2      (2) 2  
 (3) 0      (4) 1

(SSC CISF Constable (GD) Exam.

**64.** If  $\sqrt{18225} = 135$ , then the value of

$$\sqrt{18225} + \sqrt{182.25} + \sqrt{1.8225}$$

+  $\sqrt{0.018225}$  is

- (1) 14.9985      (2) 149.985  
 (3) 1499.85      (4) 1.49985  
 (SSC CHSL DEO & LDC Exam. 21.10.2012 (IInd Sitting))

**65.** The square root of  $21\frac{51}{169}$  is

- (1)  $5\frac{8}{13}$       (2)  $4\frac{8}{13}$

- (3)  $4\frac{3}{13}$       (4)  $5\frac{5}{13}$

(SSC CHSL DEO & LDC Exam. 28.10.2012 (Ist Sitting))

**66.** If  $(1101)^2 = 1212201$ , find the value of  $\sqrt{121.2201}$ .

- (1) 110.1      (2) 11.01  
 (3) 1.101      (4) 11.001

(SSC CGL Tier-I Exam. 11.11.2012 (Ist Sitting))

**67.** The value of

$$\sqrt{\frac{0.064 \times 0.256 \times 15.625}{0.025 \times 0.625 \times 4.096}} \text{ is}$$

- (1) 2      (2) 2.4  
 (3) 0.24      (4) 4.2

(SSC Delhi Police Sub-Inspector (SI) Exam. 19.08.2012)

**68.** The value of

$$\sqrt{19.36} + \sqrt{0.1936} + \sqrt{0.001936}$$

+  $\sqrt{0.00001936}$  is :

- (1) 4.8484      (2) 4.8694

- (3) 4.8884      (4) 4.8234

(SSC CAPFs SI & CISF ASI Exam. 23.06.2013)

**69.** The number of pairs of natural numbers, the difference of whose squares is 45 will be

- (1) 2      (2) 3  
 (3) 6      (4) 5

(SSC CHSL DEO & LDC Exam. 04.11.2012, IInd Sitting)

**70.** What is the value of

$$\frac{\sqrt{24} + \sqrt{216}}{\sqrt{96}} ?$$

- (1)  $2\sqrt{6}$       (2)  $4\sqrt{6}$   
 (3) 2      (4) 4

(SSC Multi-Tasking Staff Exam. 10.03.2013)

**71.** Simplify :

$$\sqrt{3\frac{33}{64}} \div \sqrt{9\frac{1}{7}} \times 2\sqrt{3\frac{1}{9}}$$

- (1)  $\frac{45}{256}$       (2)  $1\frac{17}{28}$

- (3)  $4\frac{3}{8}$       (4)  $2\frac{3}{16}$

(SSC Multi-Tasking Staff Exam. 17.03.2013, Ist Sitting)

**72.** The simplified value of

$$\frac{\sqrt{32} + \sqrt{48}}{\sqrt{8} + \sqrt{12}} \text{ is}$$

- (1) 3      (2) 2  
 (3) 6      (4) 4

(SSC Multi-Tasking Staff Exam. 17.03.2013, IInd Sitting)

**73.** Number of digits in the square root of 62478078 is:

- (1) 4      (2) 5  
 (3) 6      (4) 3

(SSC CGL Tier-I Exam. 21.04.2013, Ist Sitting)

**74.** If  $\left(n^r - t n + \frac{1}{4}\right)$  be a perfect

square, then the values of t are:

- (1)  $\pm 2$       (2) 1, 2  
 (3) 2, 3      (4)  $\pm 1$

(SSC CGL Tier-I Exam. 21.04.2013, Ist Sitting)

**75.** The square root of  $33 - 4\sqrt{35}$

is :

$$(1) \pm(2\sqrt{7} + \sqrt{5})$$

$$(2) \pm(\sqrt{7} + 2\sqrt{5})$$

$$(3) \pm(\sqrt{7} - 2\sqrt{5})$$

$$(4) \pm(2\sqrt{7} - \sqrt{5})$$

(SSC CGL Tier-I Exam. 21.04.2013)

**76.** Find the value of

$$\sqrt{156.25} + \sqrt{0.0081} - \sqrt{0.0361}$$

- (1) 13.4      (2) 15.4

- (3) 12.4      (4) 17.4

(SSC Constable (GD) Exam. 12.05.2013)

**77.** The fourth root of 24010000 is

- (1) 7      (2) 49

- (3) 490      (4) 70

(SSC CGL Tier-I Exam. 19.05.2013)

**78.** The digit at the unit's place in the square-root of 15876 is :

- (1) 8      (2) 6

- (3) 4      (4) 2

(SSC CGL Prelim Exam. 27.02.2000 (First Sitting))

**79.** The digit at unit's place of the number  $(1570)^2 + (1571)^2 + (1572)^2 + (1573)^2$  is :

- (1) 4      (2) 1

- (3) 2      (4) 3

(SSC CHSL DEO & LDC Exam. 21.10.2012 (IInd Sitting))

**80.** The smallest 4-digit number, which is a perfect square, is

- (1) 1009      (2) 1016

- (3) 1024      (4) 1025

(SSC CPO Sub-Inspector Exam. 05.09.2004 & SAS Exam. 26.06.2010)

**81.** The smallest number added to 680621 to make the sum a perfect square is :

- (1) 4      (2) 5

- (3) 6      (4) 8

(SSC CGL Prelim Exam. 13.11.2005 (First Sitting))

**82.** The smallest positive integer, when multiplied by 392, the product is a perfect square, is

- (1) 6      (2) 5

- (3) 3      (4) 2

(SSC CGL Prelim Exam. 13.11.2005 (Second Sitting))

**83.** Which smallest number must be added to 2203 so that we get a perfect square?

- (1) 1      (2) 3

- (3) 6      (4) 8

(SSC CGL Prelim Exam. 13.11.2005 (Second Sitting))

**84.** The number of perfect square numbers between 50 and 1000 is

- (1) 21      (2) 22

- (3) 23      (4) 24

(SSC Section Officer (Commercial Audit) Exam. 26.11.2006 (Second Sitting))

**85.** The smallest number which should be added to the number 8958 so that the result is a perfect square is

- (1) 69      (2) 67  
 (3) 77      (4) 79

(SSC CGL Prelim Exam. 04.02.2007  
 (Second Sitting)

**86.** The largest number of five digits, which is a perfect square is

- (1) 99999      (2) 99976  
 (3) 99856      (4) 99764

(SSC CGL Prelim Exam. 27.07.2008  
 (First Sitting)

**87.** How many perfect squares lie between 120 and 300 ?

- (1) 5      (2) 6  
 (3) 7      (4) 8

(SSC CGL Tier-I Exam. 16.05.2010  
 (Second Sitting)

**88.** The smallest number that must be subtracted from 1000 to make the resulting number a perfect square is

- (1) 37      (2) 38  
 (3) 39      (4) 40

(SSC Data Entry Operator Exam. 02.08.2009)

**89.** The least integer which should be added to 1000 so as to make it a perfect square is

- (1) 10      (2) 18  
 (3) 24      (4) 89

(SSC Constable (GD) & Rifleman (GD) Exam. 22.04.2012 (Ist Sitting)

**90.** The greatest 4 digit number which is a perfect square, is

- (1) 9999      (2) 9909  
 (3) 9801      (4) 9081

(SSC CGL Tier-I Exam. 19.05.2013)

**91.** What number must be added to the expression  $16a^2 - 12a$  to make it a perfect square ?

- (1)  $\frac{9}{4}$       (2)  $\frac{11}{2}$

- (3)  $\frac{13}{2}$       (4) 16

(SSC CGL Tier-I Exam. 19.05.2013)

**92.** If the number p is 5 more than q and the sum of the squares of p and q is 55, then the product of p and q is

- (1) 10      (2) -10  
 (3) 15      (4) -15

(SSC Multi-Tasking (Non-Technical) Staff Exam. 20.02.2011)

**93.** The square root of a positive number less than 100 lies between :

- (1) 0 and 1000  
 (2) 0 and 10  
 (3) -10 and 10  
 (4) -100 and 100

(SSC CGL Prelim Exam. 04.07.1999  
 (First Sitting)

**94.** If the sum of two numbers is 22 and the sum of their squares is 404, then the product of the numbers is :

- (1) 40      (2) 44  
 (3) 80      (4) 88

(SSC CGL Prelim Exam. 27.02.2000  
 (First Sitting)

**95.** One-third of the square root of which number is 0.001?

- (1) 0.0009      (2) 0.000001  
 (3) 0.00009      (4) None of the above

(SSC CGL Prelim Exam. 27.02.2000  
 (Second Sitting)

**96.** Three fifth of the square of a certain number is 126.15. What is the number?

- (1) 210.25      (2) 75.69  
 (3) 14.5      (4) 145

(SSC CGL Prelim Exam. 24.02.2002  
 (First Sitting) & SSC CGL Prelim Exam. 13.11.2005)

**97.** How many positive integers less than 1000 are multiples of 11 whose square roots are whole numbers.

- (1) 2      (2) 4  
 (3) 8      (4) 11

(SSC CPO S.I. Exam. 07.09.2003)

**98.** The number, whose square is equal to the difference of the squares of 75.15 and 60.12, is

- (1) 46.09      (2) 48.09  
 (3) 45.09      (4) 47.09

(SSC CGL Prelim Exam. 08.02.2004  
 (Second Sitting))

**99.** The sum of the squares of two numbers is 386. If one of the numbers is 5, the other will be :

- (1) 18      (2) 19  
 (3) 15      (4) 20

(SSC CGL Prelim Exam. 08.02.2004  
 (Second Sitting))

**100.** The number, whose square is equal to the difference between the squares of 975 and 585, is :

- (1) 780      (2) 390  
 (3) 1560      (4) 130

(SSC CPO S.I. Exam. 26.05.2005)

**101.** If the sum and difference of two numbers are 20 and 8 respectively, then the difference of their squares is :

- (1) 12      (2) 28  
 (3) 80      (4) 160

(SSC CGL Prelim Exam. 13.11.2005  
 (First Sitting))

**102.** The sum of the squares of two positive integers is 100 and the difference of their squares is 28. The sum of the numbers is :

- (1) 12      (2) 13  
 (3) 14      (4) 15

(SSC CGL Prelim Exam. 13.11.2005  
 (First Sitting))

**103.** If  $x$  is a perfect square integer such that  $7 < (2x - 3) < 17$ , then the value of  $x$  is :

- (1) 25      (2) 16  
 (3) 9      (4) 4

(SSC CHSL DEO & LDC Exam. 27.11.2010)

**104.** If the product of four consecutive natural numbers increased by a natural number  $p$ , is a perfect square; then the value of  $p$  is

- (1) 8      (2) 4  
 (3) 2      (4) 1

(SSC CPO S.I. Exam. 03.09.2006)

**105.** Given that  $\sqrt{24}$  is approxi-

ly equal to 4.898.  $\sqrt{\frac{8}{3}}$  is nearly

equal to

- (1) 0.544      (2) 1.333  
 (3) 1.633      (4) 2.666

(SSC CGL Prelim Exam. 04.02.2007  
 (First Sitting))

**106.** There are some boys and girls in a room. The square of the number of the girls is less than the square of the number of boys by 28. If there were two more girls, the number of boys would have been the same as that of the girls. The total number of the boys and girls in the room are

- (1) 56      (2) 14  
 (3) 10      (4) 7

(SSC CPO S.I. Exam. 16.12.2007)

**107.** If the sum of the squares of three consecutive natural numbers is 110, then the smallest of these natural numbers is :

- (1) 8      (2) 6  
 (3) 7      (4) 5

(SSC CPO S.I. Exam. 16.12.2007)

- 108.** The product of two whole numbers is 37. The square root of the difference of the numbers is  
 (1) 8                    (2) 7.5  
 (3) 6                    (4) 4.5

(SSC CPO S.I. Exam. 16.12.2007)

- 109.** The number, whose square is equal to the difference of the squares of the numbers 68 and 32, is  
 (1) 36                    (2) 48  
 (3) 60                    (4) 64

(SSC CGL Prelim Exam. 27.07.2008  
 (Second Sitting)

- 110.** The sum of a positive integer and its square is 2450. The positive integer is  
 (1) 45                    (2) 48  
 (3) 49                    (4) 50

(SSC (South Zone) Investigator Exam 12.09.2010)

- 111.** The product of two numbers is 45 and their difference is 4. The sum of squares of the two numbers is  
 (1) 135                    (2) 240  
 (3) 73                    (4) 106

(SSC CGL Tier-I Exam 19.06.2011  
 (First Sitting)

- 112.** 1008 divided by which single digit number gives a perfect square?  
 (1) 9                    (2) 4  
 (3) 8                    (4) 7

(SSC CGL Exam. 27.02.2000  
 (Ist Sitting)

- 113.** The least number that must be subtracted from 63520 to make the result a perfect square is :  
 (1) 16                    (2) 20  
 (3) 24                    (4) 30

(SSC CGL Exam. 24.02.2002  
 (IIInd Sitting)

- 114.** What is the least number which should be subtracted from 0.000326, to have perfect square ?  
 (1) 0.000004            (2) 0.000002  
 (3) 0.04                    (4) 0.02

(SSC CGL Prelim Exam. 11.05.2003 (First Sitting)

- 115.** By which smallest number should 5808 be multiplied so that it becomes a perfect square?  
 (1) 2                    (2) 7  
 (3) 11                    (4) 3

(SSC CGL Exam. 04.07.1999  
 (Ist Sitting)

- 116.** By which smallest number should 20184 be multiplied so that it becomes a perfect square ?  
 (1) 2                    (2) 3  
 (3) 5                    (4) 6

(SSC CGL Prelim Exam. 24.02.2002  
 (Middle Zone)

- 117.** The least number which must be added to 1728 to make it a perfect square is \_\_\_\_\_.

(1) 36                    (2) 32  
 (3) 38                    (4) 30

(SSC CGL Tier-I

Re-Exam. (2013) 27.04.2014

- 118.** If  $a = 64$  and  $b = 289$ , then the value of

$$\left( \sqrt{\sqrt{a} + \sqrt{b}} - \sqrt{\sqrt{b} - \sqrt{a}} \right)^{\frac{1}{2}}$$

- (1)  $2^{\frac{1}{2}}$                     (2) 2  
 (3) 4                            (4) -2

(SSC CGL Tier-II Exam. 21.09.2014)

- 119.**  $\sqrt{64009}$  is equal to

- (1) 352                    (2) 523  
 (3) 253                    (4) 532

(SSC CGL Tier-II Exam. 21.09.2014)

- 120.** A tourist spends daily as many rupees as the number of days of his total tour. If his total expenses were ₹ 361, then how many days did his tour last ?

- (1) 17 days                    (2) 19 days  
 (3) 21 days                    (4) 31 days

- 121.** The value of  $\sqrt{10^{-6} \times 0.25}$  is

- (1) 0.0025                    (2) 0.0005  
 (3) 0.25                            (4) 0.50

(SSC CAPFs SI, CISF ASI & Delhi Police SI Exam. 22.06.2014)

- 122.** The simplified value of

$$\frac{3\sqrt{2}}{\sqrt{3} + \sqrt{6}} - \frac{4\sqrt{3}}{\sqrt{6} + \sqrt{2}}$$

$$+ \frac{\sqrt{6}}{\sqrt{3} + \sqrt{2}}$$

- (1)  $\sqrt{2}$                     (2)  $\frac{1}{\sqrt{2}}$

- (3)  $\sqrt{3} - \sqrt{2}$                     (4) 0

(SSC CHSL DEO & LDC Exam. 02.11.2014 (IIInd Sitting))

- 123.** The value of  $\frac{4 - \sqrt{0.04}}{4 + \sqrt{0.4}}$  is close to

- (1) 0.4                    (2) 0.8  
 (3) 1.0                    (4) 1.4

(SSC CHSL DEO & LDC Exam. 02.11.2014 (IIInd Sitting))

- 124.** If  $\sqrt{0.05 \times 0.5 \times a} = 0.5 \times 0.05$

$\times \sqrt{b}$ , then  $\frac{a}{b}$  is equal to

- (1) 0.0025                    (2) 0.025  
 (3) 0.25                            (4) 0.00025

(SSC CHSL DEO & LDC Exam. 02.11.2014 (IIInd Sitting))

- 125.** A teacher wants to arrange his students in an equal number of rows and columns. If there are 1369 students, the number of students in the last row are

- (1) 37                            (2) 33  
 (3) 63                            (4) 47

(SSC CHSL DEO & LDC Exam. 9.11.2014)

- 126.** Which of the following is true?

$$(1) \sqrt{5} + \sqrt{3} > \sqrt{6} + \sqrt{2}$$

$$(2) \sqrt{5} + \sqrt{3} < \sqrt{6} + \sqrt{2}$$

$$(3) \sqrt{5} + \sqrt{3} = \sqrt{6} + \sqrt{2}$$

$$(4) (\sqrt{5} + \sqrt{3})(\sqrt{6} + \sqrt{2}) = 1$$

(SSC CHSL DEO & LDC Exam. 9.11.2014)

- 127.** The least number by which 20184 must be multiplied so as to make the product a perfect square is

- (1) 2                            (2) 3  
 (3) 5                            (4) 6

(SSC CHSL DEO Exam. 16.11.2014)

(Ist Sitting)

- 128.** 1008 divided by which single digit number gives a perfect square ?

- (1) 9                            (2) 4  
 (3) 8                            (4) 7

(SSC Constable (GD) Exam. 04.10.2015, Ist Sitting)

- 129.** The sum of two numbers is 37 and the difference of their squares is 185, then the difference between the two numbers is :

- (1) 10                            (2) 4  
 (3) 5                            (4) 3

(SSC CHSL (10+2) LDC, DEO & PA/SA Exam. 15.11.2015 (Ist Sitting) TF No. 6636838)

**130.** A General of Army wants to form a square from 36562 armies. After arrangement, he found some armies left. How many armies were left?

- (1) 81      (2) 36  
 (3) 97      (4) 65

(SSC CGL Tier-II Exam. 12.04.2015  
 TF No. 567 TL 9)

**131.** The square root of  $\frac{2 + \sqrt{3}}{2}$  is

- (1)  $\pm \frac{1}{\sqrt{2}}(\sqrt{3} + 1)$   
 (2)  $\pm \frac{1}{2}(\sqrt{3} - 2)$   
 (3) None of these  
 (4)  $\pm \frac{1}{2}(\sqrt{3} - 1)$

(SSC CGL Tier-II Exam. 12.04.2015  
 TF No. 567 TL 9)

**132.** The value of  $(11111)^2$  is

- (1) 12344321      (2) 121212121  
 (3) 123454321      (4) 11344311  
 (SSC CGL Tier-II Exam. 12.04.2015  
 TF No. 567 TL 9)

**133.** The smallest whole number that is to be multiplied with 59535 to make a perfect square number is  $x$ . The sum of digits of  $x$  is

- (1) 9      (2) 5  
 (3) 7      (4) 6

(SSC CAPFs SI, CISF ASI & Delhi Police SI Exam, 21.06.2015  
 (Ist Sitting) TF No. 8037731)

**134.** The digit in the unit place in the square root of 66049 is

- (1) 3      (2) 7  
 (3) 8      (4) 2  
 (SSC CGL Tier-I  
 Re-Exam, 30.08.2015)

**135.** The value of  $\sqrt{0.000441}$  is equal to

- (1) 0.21      (2) 0.00021  
 (3) 0.0021      (4) 0.021

(SSC Constable (GD)  
 Exam, 04.10.2015, Ist Sitting)

**136.** The sum of the perfect squares between 120 and 300 is

- (1) 1400      (2) 1296  
 (3) 1024      (4) 1204

(SSC CHSL (10+2) LDC, DEO & PA/SA Exam, 01.11.2015, IInd Sitting)

**137.** The least number that should be subtracted from the number 32146 to make it a perfect square is :

- (1) 305      (2) 105  
 (3) 205      (4) 405

(SSC CHSL (10+2) LDC, DEO & PA/SA Exam, 06.12.2015  
 (Ist Sitting) TF No. 1375232)

**138.** If  $5416 * 6$  is a perfect square, then the digit at '\*' is :

- (1) 9      (2) 4  
 (3) 6      (4) 5

(SSC CHSL (10+2) LDC, DEO & PA/SA Exam, 06.12.2015  
 (Ist Sitting) TF No. 1375232)

**139.** A number of boys raised Rs. 12,544 for a famine fund, each boy has given as many rupees as there were boys. The number of boys was :

- (1) 102      (2) 112  
 (3) 122      (4) 132

(SSC CHSL (10+2) LDC, DEO & PA/SA Exam, 06.12.2015  
 (IInd Sitting) TF No. 3441135)

**140.** The sum of three positive numbers is 18 and their product is 162. If the sum of two numbers is equal to the third number, then the sum of squares of the numbers is

- (1) 120      (2) 126  
 (3) 132      (4) 138

(SSC CGL Tier-II Online Exam.01.12.2016)

**141.** Three numbers are such that their sum is 50, product is 3750 and the sum of their reciprocals

is  $\frac{31}{150}$ . Find the sum of the squares of the three numbers.

- (1) 2500      (2) 1250  
 (3) 950      (4) 122

(SSC CPO SI & ASI, Online Exam. 06.06.2016) (IInd Sitting)

**142.** The greatest perfect square number of 6 digits is

- (1) 999001      (2) 998001  
 (3) 998009      (4) 998101

(SSC CGL Tier-I (CBE) Exam. 27.08.2016) (Ist Sitting)

**143.** If a perfect square, not divisible by 6, be divided by 6, the remainder will be

- (1) 1, 3 or 5      (2) 1, 2 or 5  
 (3) 1, 3 or 4      (4) 1, 2 or 4

(SSC CGL Tier-I (CBE) Exam. 02.09.2016) (Ist Sitting)

**144.** Find the least number which must be subtracted from 18265 to make it a perfect square.

- (1) 30      (2) 38  
 (3) 40      (4) 45

(SSC CGL Tier-I (CBE) Exam. 07.09.2016) (Ist Sitting)

**145.** If the sum of squares of two real numbers is 41 and their sum is 9, then the sum of cubes of these two numbers is

- (1) 169      (2) 209  
 (3) 189      (4) 198

(SSC CGL Tier-II (CBE) Exam. 30.11.2016)

**146.** The product of two positive integers is 2048 and one of them is twice the other. The smaller number is

- (1) 32      (2) 64  
 (3) 16      (4) 1024

(SSC CGL Tier-I (CBE) Exam. 30.08.2016) (Ist Sitting)

**147.** A number when divided by 6 leaves remainder 3. When the square of the same number is divided by 6, the remainder is:

- (1) 0      (2) 2  
 (3) 1      (4) 3

(SSC CGL Tier-I (CBE) Exam. 02.09.2016) (IInd Sitting)

**148.** Each member of a club contributes as much rupees and as much paise as the number of members of the club. If the total contribution is Rs. 2525, then the number of members of the club is

- (1) 60      (2) 45  
 (3) 55      (4) 50

(SSC CGL Tier-II (CBE) Exam. 30.11.2016)

**149.** The sum of squares of three positive integers is 323. If the sum of squares of two numbers is twice the third, their product is

- (1) 255      (2) 260  
 (3) 265      (4) 270

(SSC CGL Tier-II (CBE) Exam. 30.11.2016)

**150.** The difference between two numbers is 9 and the difference between their squares is 207. The numbers are :

- (1) 17 and 8      (2) 16 and 7  
 (3) 15 and 6      (4) 23 and 14

(SSC CGL Tier-I (CBE) Exam. 28.08.2016 (IST Sitting))

**151.** The least number that must be subtracted from 63520 to make the result a perfect square is

- (1) 30      (2) 24  
 (3) 14      (4) 16

(SSC CGL Tier-I (CBE)

Exam. 30.08.2016 (IIIrd Sitting)

**152.** The least six digit number which is a perfect square is

- (1) 100489      (2) 100000  
 (3) 100256      (4) 100225

(SSC CGL Tier-I (CBE)

Exam. 01.09.2016 (IIIrd Sitting)

**153.** The sum of two positive integers is 80 and the difference between them is 20. What is the difference between squares of those numbers?

- (1) 1400      (2) 1600  
 (3) 1800      (4) 2000

(SSC CGL Tier-I (CBE)

Exam. 03.09.2016 (IIIrd Sitting)

**154.** Twenty one times of a positive number is less than its square by 100. The value of the positive number is

- (1) 25      (2) 26  
 (3) 42      (4) 41

(SSC CGL Tier-II (CBE)

Exam. 12.01.2017)

**155.** A General of an Army wants to create a formation of square from 36562 army men. After arrangement, he found some army men remained unused. Then the number of such army men remained unused was

- (1) 36      (2) 65  
 (3) 81      (4) 97

(SSC CGL Tier-II (CBE)

Exam. 12.01.2017)

**156.** The least number to be subtracted from 16800 to make it a perfect square is

- (1) 169      (2) 219  
 (3) 159      (4) 249

(SSC Multi-Tasking Staff Exam. 30.04.2017)

#### TYPE-IV

**1.** The sum of the cubes of the numbers 22, -15 and -7 is equal to

- (1) 6930      (2) 9630  
 (3) 3      (4) 0

(SSC CPO S.I. Exam. 05.09.2004)

**2.**  $\frac{\sqrt[3]{8}}{\sqrt{16}} \div \sqrt{\frac{100}{49}} \times \sqrt[3]{125}$  is equal to :

- (1) 7      (2)  $1\frac{3}{4}$   
 (3)  $\frac{7}{100}$       (4)  $\frac{4}{7}$

(SSC CGL Prelim Exam. 04.07.1999

(Second Sitting)

**3.**  $\sqrt[3]{\frac{72.9}{0.4096}}$  is equal to :

- (1) 0.5625      (2) 5.625  
 (3) 182      (4) 13.6

(SSC CGL Prelim Exam. 27.02.2000  
 (First Sitting)

**4.**  $(5.5)^3 - (4.5)^3$  is equal to :

- (1) 1      (2) 75  
 (3) 74.25      (4) 75.25

(SSC CGL Prelim Exam. 27.02.2000  
 (First Sitting)

**5.** The value of  $\sqrt[3]{\frac{7}{875}}$  is equal to

- (1)  $\frac{1}{3}$       (2)  $\frac{1}{15}$   
 (3)  $\frac{1}{4}$       (4)  $\frac{1}{5}$

(SSC CPO S.I. Exam. 07.09.2003)

**6.**  $\sqrt[3]{\frac{19}{513}}$  is equal to

- (1)  $\frac{1}{9}$       (2)  $\frac{1}{3}$   
 (3)  $\frac{1}{\sqrt{27}}$       (4)  $\frac{1}{\sqrt{3}}$

(SSC CPO S.I. Exam. 05.09.2004)

**7.**

$\sqrt[3]{(333)^3 + (333)^3 + (334)^3 - 3 \times 333 \times 333 \times 334}$  is equal to

- (1) 12      (2) 11  
 (3) 10      (4) 15

(SSC Section Officer (Commercial Audit) Exam. 30.09.2007  
 (Second Sitting)

**8.** If cube root of 175616 is 56, then the value of

$\sqrt[3]{175616} + \sqrt[3]{0.175616} + \sqrt[3]{0.000175616}$  is equal to :

- (1) 0.168      (2) 62.16  
 (3) 6.216      (4) 6.116

(SSC CGL Prelim Exam. 24.02.2002  
 (Second Sitting)

**9.**  $\sqrt[3]{0.000064}$  is equal to

- (1) 0.0002      (2) 0.002  
 (3) 0.02      (4) 0.2

(SSC CISF ASI Exam 29.08.2010  
 (Paper-1)

**10.**  $\sqrt[3]{15612 + \sqrt{154 + \sqrt{225}}}$  is equal

- to  
 (1) 15      (2) 25  
 (3) 75      (4) 125

(SSC (South Zone) Investigator Exam 12.09.2010)

**11.**  $\sqrt[3]{0.000125}$  is equal to

- (1) 0.5      (2) 0.15  
 (3) 0.05      (4) 0.005

(SSC (South Zone) Investigator Exam 12.09.2010)

**12.** The sum of the squares of 2 numbers is 146 and the square root of one of them is  $\sqrt{5}$ . The cube of the other number is

- (1) 1111      (2) 1221  
 (3) 1331      (4) 1441

(SSC CGL Prelim Exam. 04.02.2007  
 (Second Sitting)

**13.**  $(\sqrt[3]{1000} + \sqrt[3]{0.008} - \sqrt[3]{0.125})$  is

- equal to  
 (1) 9.7      (2) 9.97  
 (3) 9.997      (4) 9.9997

(SSC CPO S.I.  
 Exam 12.12.2010 (Paper-I))

**14.**  $\sqrt[3]{1 - \frac{127}{343}}$  is equal to

- (1)  $\frac{5}{9}$       (2)  $1 - \frac{1}{7}$   
 (3)  $\frac{4}{7}$       (4)  $1 - \frac{2}{7}$

(SSC CGL Tier-1 Exam 26.06.2011  
 (First Sitting))

**15.** If  $\sqrt[3]{3^n} = 27$ , then the value of n is :

- (1) 9      (2) 6  
 (3) 1      (4) 3

(SSC CHSL DEO & LDC Exam. 04.11.2012, 1st Sitting)

**16.** The value of  $\sqrt[3]{0.000729}$  is

- (1) 0.9      (2) 0.3  
 (3) 0.03      (4) 0.09

(SSC Multi-Tasking Staff Exam. 10.03.2013, 1st Sitting : Patna)

**17.** The value of  $\left(\sqrt{4^3 + 15^2}\right)^3$  is :

- (1) 4913      (2) 4313  
 (3) 4193      (4) 3943

(SSC Multi-Tasking Staff Exam. 10.03.2013)

**18.**  $\sqrt[3]{4 - \frac{12}{125}}$  is equal to

- (1) 1.4      (2) 1.6  
 (3) 1.8      (4) 2.4

(SSC CPO Sub Inspector Exam. 06.09.2009) & SSC CPO S.I. Exam. 12.12.2010 (Paper-I) & SSC MTS Exam. 17.03.2013 (1st Sitting)

**19.** By which smallest number 1323 must be multiplied, so that it becomes a perfect cube?

- (1) 2      (2) 3  
 (3) 5      (4) 7

(SSC CGL Prelim Exam. 04.07.1999  
 (Second Sitting))

## SIMPLIFICATION

- 20.** Sum of digits of the smallest number by which 1440 be multiplied so that it becomes a perfect cube, is  
 (1) 4      (2) 6  
 (3) 7      (4) 8  
 (SSC CGL Prelim Exam. 11.05.2003  
 (Second Sitting)
- 21.** The sum of the digits of the smallest number which, when multiplied by 1800, gives a perfect cube, is :  
 (1) 2      (2) 3  
 (3) 6      (4) 8  
 (SSC CGL Prelim Exam. 08.02.2004  
 (Second Sitting)
- 22.** Which smallest number must be added to 710 so that the sum is a perfect cube ?  
 (1) 29      (2) 19  
 (3) 11      (4) 21  
 (SSC CGL Prelim Exam. 13.11.2005  
 (Second Sitting)
- 23.** The least number, by which 1944 must be multiplied so as to make the result a perfect cube, is  
 (1) 2      (2) 3  
 (3) 6      (4) 13  
 (SSC CGL Prelim Exam. 04.02.2007  
 (Second Sitting)
- 24.** The smallest natural number, by which 3000 must be divided to make the quotient a perfect cube, is :  
 (1) 3      (2) 4  
 (3) 5      (4) 6  
 (SSC CPO S.I. Exam. 16.12.2007)
- 25.** The smallest positive integer  $n$ , for which  $864n$  is a perfect cube, is :  
 (1) 1      (2) 2  
 (3) 3      (4) 4  
 (SSC CPO S.I. Exam. 16.12.2007)
- 26.** By what least number should 675 be multiplied so as to obtain a perfect cube number ?  
 (1) 3      (2) 5  
 (3) 24      (4) 40  
 (SSC CGL Tier-I Exam. 16.05.2010  
 (First Sitting)
- 27.** The least number, that must be added to 1720 so as to obtain a perfect cube, is  
 (1) 7      (2) 8  
 (3) 11      (4) 13  
 (SSC SAS Exam 26.06.2010  
 (Paper-1))
- 28.** By what least number should 4320 be multiplied so as to obtain a number which is a perfect cube ?  
 (1) 40      (2) 50  
 (3) 60      (4) 80  
 (SSC CPO S.I. Exam. 12.12.2010  
 (Paper-I))
- 29.** Which of the following is a perfect square as well as a cube?  
 343, 125, 81, or 64  
 (1) 81      (2) 125  
 (3) 343      (4) 64  
 (SSC CGL Prelim Exam. 27.02.2000  
 (First Sitting))
- 30.** The square of a natural number subtracted from its cube is 48. The number is :  
 (1) 8      (2) 6  
 (3) 5      (4) 4  
 (SSC CGL Prelim Exam. 27.02.2000  
 (Second Sitting))
- 31.** The least possible value of  $A$  for which  $90 \times A$  is a perfect cube is  
 (1) 200      (2) 300  
 (3) 500      (4) 600  
 (SSC CPO S.I. Exam. 12.01.2003)
- 32.** If the square root of  $x$  is the cube root of  $y$ , then the relation between  $x$  and  $y$  is  
 (1)  $x^3 = y^2$       (2)  $x^2 = y^3$   
 (3)  $x = y$       (4)  $x^6 = y^5$   
 FCI Assistant Grade-III  
 Exam. 25.02.2012 (Paper-I)  
 North Zone (Ist Sitting)
- 33.** If  $x = \sqrt{3} + \sqrt{2}$  then the value of  
 $x^3 - \frac{1}{x^3}$  is  
 (1)  $10\sqrt{2}$       (2)  $14\sqrt{2}$   
 (3)  $22\sqrt{2}$       (4)  $8\sqrt{2}$   
 (SSC CGL Tier-I  
 Re-Exam. (2013) 27.04.2014)
- 34.** The value of  $(1001)^3$  is  
 (1) 1003003001  
 (2) 100303001  
 (3) 100300301  
 (4) 103003001  
 (SSC CGL Tier-I Exam. 26.10.2014)
- 35.** What is the smallest number by which 625 must be divided so that the quotient is a perfect cube ?  
 (1) 25      (2) 5  
 (3) 2      (4) 3  
 (SSC CGL Tier-II Exam. 21.09.2014)
- 36.** The sum of the cubes of two numbers is 793. The sum of the numbers is 13. Then the difference of the two numbers is  
 (1) 7      (2) 6  
 (3) 5      (4) 8  
 (SSC CGL Tier-II Exam.  
 2014 12.04.2015 (Kolkata Region)  
 TF No. 789 TH 7)
- 37.** The smallest number by which 243000 be divided so that the quotient is a perfect cube is  
 (1) 3      (2) 27  
 (3) 9      (4) 1  
 (SSC Constable (GD)  
 Exam. 04.10.2015, 1st Sitting)
- 38.** When simplified, the product  
 $\left(2 - \frac{1}{3}\right)\left(2 - \frac{3}{5}\right)\left(2 - \frac{5}{7}\right) \dots \left(2 - \frac{997}{999}\right)$   
 equals  
 (1)  $\frac{5}{999}$       (2)  $\frac{5}{3}$   
 (3)  $\frac{1001}{999}$       (4)  $\frac{1001}{3}$   
 (SSC CAPFs SI, CISF ASI & Delhi  
 Police SI Exam, 21.06.2015  
 IInd Sitting)
- 39.** If the cube root of 79507 is 43, then the value of  
 $\sqrt[3]{79507} + \sqrt[3]{0.079507} + \sqrt[3]{0.000079507}$   
 is  
 (1) 0.4773      (2) 477.3  
 (3) 47.73      (4) 4.773  
 (SSC CGL Tier-I Exam, 09.08.2015  
 (IInd Sitting) TF No. 4239378)
- 40.** Find the cube root of  $(-13824)$ .  
 or  
 Find the value of  $\sqrt[3]{-13824}$ .  
 (1) 38      (2) -38  
 (3) 24      (4) -24  
 (SSC CGL Tier-II Online  
 Exam.01.12.2016)
- 41.** The cube of 105 is  
 (1) 1157625      (2) 1175625  
 (3) 1185625      (4) 1158625  
 (SSC CGL Tier-I (CBE)  
 Exam. 09.09.2016) (Ist Sitting)
- 42.** The least number which when divides 37044, gives the result a perfect cube, is :  
 (1) 2      (2) 4  
 (3) 14      (4) 21  
 (SSC CGL Tier-I (CBE)  
 Exam. 07.09.2016 (IIInd Sitting))
- 43.** The cube of 997 is :  
 (1) 991026973      (2) 991029673  
 (3) 991029773      (4) 991097273  
 (SSC CGL Tier-I (CBE)  
 Exam. 10.09.2016 (IIInd Sitting))
- 44.** The sum of the cubes of two numbers in the ratio 3 : 4 is 5824. The sum of the numbers is :  
 (1)  $(5824)^{\frac{1}{3}}$       (2) 28  
 (3) 24      (4) 14  
 (SSC CGL Tier-I (CBE)  
 Exam. 11.09.2016 (IIInd Sitting))

## TYPE-V

- 1.** The simplified value of  

$$\frac{(0.0539 - 0.002) \times 0.4 + 0.56 \times 0.07}{0.04 \times 0.25} = ?$$

(1) 59.96      (2) 0.5996  
 (3) 5.996      (4) 599.6

(SSC CAPFs SI, CISF ASI & Delhi Police SI Exam, 21.06.2015  
 (1st Sitting) TF No. 8037731)

### **TYPE-III**

<b>1.</b> (3)	<b>2.</b> (3)	<b>3.</b> (1)	<b>4.</b> (4)
<b>5.</b> (4)	<b>6.</b> (3)	<b>7.</b> (2)	<b>8.</b> (2)
<b>9.</b> (2)	<b>10.</b> (3)	<b>11.</b> (4)	<b>12.</b> (2)
<b>13.</b> (1)	<b>14.</b> (4)	<b>15.</b> (4)	<b>16.</b> (4)
<b>17.</b> (4)	<b>18.</b> (2)	<b>19.</b> (2)	<b>20.</b> (2)
<b>21.</b> (1)	<b>22.</b> (4)	<b>23.</b> (2)	<b>24.</b> (4)
<b>25.</b> (1)	<b>26.</b> (3)	<b>27.</b> (3)	<b>28.</b> (3)
<b>29.</b> (2)	<b>30.</b> (3)	<b>31.</b> (1)	<b>32.</b> (3)
<b>33.</b> (2)	<b>34.</b> (4)	<b>35.</b> (2)	<b>36.</b> (1)
<b>37.</b> (2)	<b>38.</b> (2)	<b>39.</b> (2)	<b>40.</b> (2)
<b>41.</b> (2)	<b>42.</b> (4)	<b>43.</b> (3)	<b>44.</b> (4)
<b>45.</b> (2)	<b>46.</b> (3)	<b>47.</b> (3)	<b>48.</b> (4)
<b>49.</b> (3)	<b>50.</b> (3)	<b>51.</b> (3)	<b>52.</b> (2)
<b>53.</b> (3)	<b>54.</b> (2)	<b>55.</b> (1)	<b>56.</b> (4)
<b>57.</b> (1)	<b>58.</b> (3)	<b>59.</b> (3)	<b>60.</b> (2)
<b>61.</b> (3)	<b>62.</b> (3)	<b>63.</b> (2)	<b>64.</b> (2)
<b>65.</b> (2)	<b>66.</b> (2)	<b>67.</b> (1)	<b>68.</b> (3)
<b>69.</b> (2)	<b>70.</b> (3)	<b>71.</b> (4)	<b>72.</b> (2)
<b>73.</b> (1)	<b>74.</b> (4)	<b>75.</b> (4)	<b>76.</b> (3)
<b>77.</b> (4)	<b>78.</b> (2)	<b>79.</b> (1)	<b>80.</b> (3)
<b>81.</b> (1)	<b>82.</b> (4)	<b>83.</b> (3)	<b>84.</b> (4)
<b>85.</b> (2)	<b>86.</b> (3)	<b>87.</b> (3)	<b>88.</b> (3)
<b>89.</b> (3)	<b>90.</b> (3)	<b>91.</b> (1)	<b>92.</b> (3)
<b>93.</b> (3)	<b>94.</b> (1)	<b>95.</b> (4)	<b>96.</b> (3)
<b>97.</b> (1)	<b>98.</b> (3)	<b>99.</b> (2)	<b>100.</b> (1)
<b>101.</b> (4)	<b>102.</b> (3)	<b>103.</b> (3)	<b>104.</b> (4)
<b>105.</b> (3)	<b>106.</b> (2)	<b>107.</b> (4)	<b>108.</b> (3)
<b>109.</b> (3)	<b>110.</b> (3)	<b>111.</b> (4)	<b>112.</b> (4)
<b>113.</b> (1)	<b>114.</b> (2)	<b>115.</b> (4)	<b>116.</b> (4)
<b>117.</b> (1)	<b>118.</b> (1)	<b>119.</b> (3)	<b>120.</b> (2)
<b>121.</b> (2)	<b>122.</b> (4)	<b>123.</b> (2)	<b>124.</b> (2)
<b>125.</b> (1)	<b>126.</b> (1)	<b>127.</b> (4)	<b>128.</b> (4)
<b>129.</b> (3)	<b>130.</b> (1)	<b>131.</b> (3)	<b>132.</b> (3)
<b>133.</b> (4)	<b>134.</b> (2)	<b>135.</b> (4)	<b>136.</b> (1)
<b>137.</b> (2)	<b>138.</b> (1)	<b>139.</b> (2)	<b>140.</b> (2)
<b>141.</b> (3)	<b>142.</b> (2)	<b>143.</b> (3)	<b>144.</b> (3)
<b>145.</b> (3)	<b>146.</b> (1)	<b>147.</b> (4)	<b>148.</b> (4)
<b>149.</b> (1)	<b>150.</b> (2)	<b>151.</b> (4)	<b>152.</b> (1)
<b>153.</b> (2)	<b>154.</b> (1)	<b>155.</b> (3)	<b>156.</b> (3)

#### **TYPE-IV**

<b>1.</b> (1)	<b>2.</b> (2)	<b>3.</b> (2)	<b>4.</b> (4)
<b>5.</b> (4)	<b>6.</b> (2)	<b>7.</b> (3)	<b>8.</b> (3)
<b>9.</b> (4)	<b>10.</b> (2)	<b>11.</b> (3)	<b>12.</b> (3)
<b>13.</b> (1)	<b>14.</b> (2)	<b>15.</b> (1)	<b>16.</b> (2)
<b>17.</b> (1)	<b>18.</b> (2)	<b>19.</b> (4)	<b>20.</b> (2)
<b>21.</b> (3)	<b>22.</b> (2)	<b>23.</b> (2)	<b>24.</b> (1)
<b>25.</b> (2)	<b>26.</b> (2)	<b>27.</b> (2)	<b>28.</b> (2)
<b>29.</b> (4)	<b>30.</b> (4)	<b>31.</b> (2)	<b>32.</b> (1)
<b>33.</b> (3)	<b>34.</b> (1)	<b>35.</b> (2)	<b>36.</b> (3)
<b>37.</b> (3)	<b>38.</b> (4)	<b>39.</b> (4)	<b>40.</b> (4)
<b>41.</b> (1)	<b>42.</b> (2)	<b>43.</b> (1)	<b>44.</b> (2)

## **TYPE-V**

1. (3)			
--------	--	--	--

## **EXPLANATIONS**

## **TYPE-I**

$$\begin{aligned} \text{1. (1)} \\ ? &= 1 + \frac{1}{1 + \frac{2}{2 + \frac{3}{1 + \frac{4}{5}}}} \\ &= 1 + \frac{1}{1 + \frac{2}{2 + \frac{3 \times 5}{5 + 4}}} = 1 + \frac{1}{1 + \frac{2}{2 + \frac{15}{9}}} \\ &= 1 + \frac{1}{1 + \frac{2}{2 + \frac{5}{3}}} = 1 + \frac{1}{1 + \frac{2}{\frac{11}{3}}} = 1 + \frac{1}{\frac{13}{3}} = \frac{16}{13} \end{aligned}$$

$$\text{2. (1)} \quad ? = 1 + \frac{2}{1 + \frac{3 \times 5}{9}} = 1 + \frac{2}{1 + \frac{5}{3}}$$

$$= 1 + \frac{2 \times 3}{8} = \frac{7}{4}$$

$$3. \quad (4) \quad \frac{1}{3 + \frac{1}{2 - \frac{1}{\frac{7}{9}}}} + \frac{17}{22}$$

$$= \frac{1}{3 + \frac{1}{2 - \frac{9}{7}}} + \frac{17}{22}$$

$$= \frac{1}{3 + \frac{1}{\frac{14-9}{7}}} + \frac{17}{22}$$

$$= \frac{1}{3 + \frac{1}{5}} + \frac{17}{22} = \frac{1}{3 + \frac{7}{5}} + \frac{17}{22}$$

$$= \frac{1}{\frac{15+7}{5}} + \frac{17}{22}$$

$$= \frac{5}{22} + \frac{17}{2} = \frac{22}{22} = 1$$

$$4. (3) x = 1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{2}}}}$$

$$= 1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{3}}}} = 1 + \frac{1}{1 + \frac{1}{1 + \frac{2}{3}}}$$

$$= 1 + \frac{1}{1 + \frac{1}{5}} = 1 + \frac{1}{1 + \frac{3}{5}}$$

$$= 1 + \frac{1}{\frac{8}{5}} = 1 + \frac{5}{8} = \frac{13}{8}$$

$$\therefore 2x + \frac{7}{4} = 2 \times \frac{13}{8} + \frac{7}{4}$$

$$= \frac{13+7}{4} = \frac{20}{4} = 5$$

$$5. (1) \frac{19}{43} \div \frac{1}{2 + \frac{1}{3 + \frac{1}{1 + \frac{1}{4}}}}$$

$$= \frac{19}{43} \div \frac{1}{2 + \frac{1}{3 + \frac{4}{5}}}$$

$$= \frac{19}{43} \div \frac{1}{2 + \frac{5}{19}} = \frac{19}{43} \div \frac{19}{43}$$

$$= \frac{19}{43} \times \frac{43}{19} = 1$$

$$6. (3) \frac{5}{3 + \frac{3}{3 - 2}} = \frac{5}{3 + \frac{3}{1}} \\ \frac{5}{3 + 3 \times 3} = \frac{5}{3 + 9} = \frac{5}{12}$$

$$7. (2) 2 = x + \frac{1}{1 + \frac{1}{3 + \frac{1}{4}}}$$

$$\Rightarrow 2 = x + \frac{1}{1 + \frac{1}{\frac{12+1}{4}}}$$

$$\Rightarrow 2 = x + \frac{1}{1 + \frac{4}{13}}$$

$$\Rightarrow 2 = x + \frac{1}{\frac{13+4}{13}}$$

$$\Rightarrow 2 = x + \frac{1}{\frac{17}{13}}$$

$$\Rightarrow 2 = x + \frac{13}{17} \Rightarrow x = 2 - \frac{13}{17}$$

$$= \frac{34-13}{17} = \frac{21}{17}$$

$$8. (4) \frac{2}{1 + \frac{1}{\frac{1}{2}}} \times \frac{3}{\left(\frac{5}{6} \times \frac{3}{2}\right) \div \frac{5}{4}}$$

$$= \frac{2}{1+2} \times \frac{3}{\frac{5}{4} \div \frac{5}{4}}$$

$$= \frac{2}{3} \times \frac{3}{\frac{5}{4} \times \frac{4}{5}} = \frac{2}{3} \times 3 = 2$$

$$9. (2) 1 + \frac{4}{2 + \frac{3}{2 + \frac{10-1}{2}}} - \frac{1}{2} \times 5$$

$$= 1 + \frac{4}{2 + \frac{6}{9}} - \frac{5}{2} = 1 + \frac{4}{2 + \frac{2}{3}} - \frac{5}{2}$$

$$= 1 + \frac{4}{8} - \frac{5}{2} = 1 + \frac{4 \times 3}{8} - \frac{5}{2}$$

$$= 1 + \frac{3}{2} - \frac{5}{2} = \frac{2+3-5}{2} = 0$$

10. (3) Suppose that

$$1 + \frac{1}{10 + \frac{1}{10}} = \frac{111}{101} = a$$

$$\text{and, } 1 - \frac{1}{10 + \frac{1}{10}} = \frac{91}{101} = b.$$

$$\therefore \frac{a^2 - b^2}{(a+b)} = \frac{(a+b)(a-b)}{(a+b)}$$

$$= (a-b)$$

$$= \frac{111}{101} - \frac{91}{101} = \frac{20}{101}$$

79

$$11. (1) \frac{\frac{14}{14}}{5 + \frac{3}{3 + \frac{5}{3}}}$$

$$= \frac{\frac{79}{14}}{5 + \frac{3}{\frac{9+5}{3}}}$$

$$= \frac{\frac{79}{14}}{5 + \frac{9}{14}} = \frac{\frac{79}{14}}{\frac{70+9}{14}}$$

$$= \frac{79}{14} \times \frac{14}{79} = 1$$

$$12. (4) \frac{2}{2 + \frac{2}{3 + \frac{2}{\frac{2}{3} \times 0.39}}}$$

$$= \frac{2}{2 + \frac{2}{3 + \frac{6}{11}} \times 0.39}$$

$$= \frac{2}{2 + \frac{2}{\frac{33+6}{11}} \times 0.39}$$

$$= \frac{2}{2 + \frac{11 \times 2}{39} \times 0.39}$$

$$= \frac{2}{2 + \frac{11 \times 2}{39} \times \frac{39}{100}}$$

$$= \frac{2}{2 + \frac{11}{50}} = \frac{2}{\frac{100+11}{50}}$$

$$= \frac{100}{111}$$

13. (4) Expression =  $1 + \frac{1}{1 + \frac{1}{2}}$

$$= 1 + \frac{1}{\frac{2+1}{2}} = 1 + \frac{2}{3} = \frac{3+2}{3} = \frac{5}{3}$$

14. (4) Check through options

$$\frac{1}{3 + \frac{1}{1 + \frac{1}{2 + \frac{1}{4}}}}$$

$$= \frac{1}{3 + \frac{1}{1 + \frac{1}{8+1}}} = \frac{1}{3 + \frac{1}{1 + \frac{4}{9}}} = \frac{1}{3 + \frac{1}{\frac{9+4}{9}}}$$

$$= \frac{1}{3 + \frac{1}{\frac{9+4}{9}}} = \frac{1}{3 + \frac{9}{13}} = \frac{1}{\frac{39+9}{13}} = \frac{13}{48}$$

15. (3) Expression

$$= 1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{3+2}}}}$$

$$= 1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{3}{5}}}}$$

$$= 1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{5+3}{5}}}}$$

$$= 1 + \frac{1}{1 + \frac{1}{1 + \frac{5}{8}}}$$

$$= 1 + \frac{1}{1 + \frac{1}{\frac{8+5}{8}}}$$

$$= 1 + \frac{1}{1 + \frac{8}{13}} = 1 + \frac{1}{\frac{13+8}{13}}$$

$$= 1 + \frac{13}{21} = \frac{21+13}{21} = \frac{34}{21}$$

16. (1) Expression

$$= \frac{\frac{7}{3} - \frac{13}{11}}{3 + \frac{1}{3 + \frac{1}{3 + \frac{1}{9+1}}}} = \frac{\frac{77-39}{33}}{3 + \frac{1}{3 + \frac{3}{10}}}$$

$$= \frac{\frac{38}{33}}{3 + \frac{1}{3 + \frac{30+3}{10}}} = \frac{\frac{38}{33}}{3 + \frac{10}{33}}$$

$$= \frac{\frac{38}{33}}{\frac{99+10}{109}} = \frac{38}{33} \times \frac{33}{109} = \frac{38}{109}$$

17. (2) Expression =  $3 + \frac{3}{3 + \frac{1}{\frac{9+1}{3}}}$

$$= 3 + \frac{3}{3 + \frac{3}{10}} = 3 + \frac{3}{\frac{30+3}{10}}$$

$$= 3 + \frac{30}{33} = 3 + \frac{10}{11} = \frac{33+10}{11} = \frac{43}{11}$$

18. (1) Expression =  $1 + \frac{1}{1 + \frac{1}{5}}$

$$= 1 + \frac{1}{\frac{5+1}{5}} = 1 + \frac{5}{6} = \frac{6+5}{6} = \frac{11}{6}$$

19. (3) First part =  $\frac{\frac{30}{7} - \frac{1}{2}}{\frac{7}{2} + \frac{8}{7}}$

$$= \frac{\frac{60-7}{14}}{\frac{49+16}{14}} = \frac{53}{14} \times \frac{14}{65} = \frac{53}{65}$$

Second part =  $\frac{1}{2 + \frac{1}{2 + \frac{1}{2 + \frac{25-1}{5}}}}$

$$= \frac{1}{2 + \frac{1}{2 + \frac{5}{24}}} = \frac{1}{2 + \frac{1}{48+5}} = \frac{1}{24}$$

$$= \frac{1}{2 + \frac{24}{53}} = \frac{1}{\frac{106+24}{53}}$$

$$= \frac{53}{130}$$

∴ Expression

$$= \frac{53}{65} \div \frac{53}{130} = \frac{53}{65} \times \frac{130}{53} = 2$$

20. (3)

$$4 - \frac{5}{1 + \frac{1}{3 + \frac{1}{9}}} = 4 - \frac{5}{1 + \frac{1}{3 + \frac{4}{9}}} = 4 - \frac{5}{1 + \frac{1}{3 + \frac{4}{9}}}$$

$$= 4 - \frac{5}{1 + \frac{1}{27+4}} = 4 - \frac{5}{1 + \frac{9}{31}}$$

$$= 4 - \frac{5}{\frac{40}{31}} = 4 - \frac{5 \times 31}{40}$$

$$= 4 - \frac{31}{8} = \frac{32-31}{8} = \frac{1}{8}$$

∴ Time taken in completing

$$\frac{1}{8} \text{ part} = 10 \text{ minutes}$$

∴ Time taken in completing

$$\frac{3}{5} \text{ part}$$

$$= 10 \times 8 \times \frac{3}{5}$$

= 48 minutes

$$21. (1) \frac{4\frac{1}{7} - 2\frac{1}{4}}{3\frac{1}{2} + 1\frac{1}{7}} = \frac{\frac{29}{7} - \frac{9}{4}}{\frac{7}{2} + \frac{8}{7}}$$

$$= \frac{\frac{116 - 63}{28}}{\frac{49 + 16}{14}} = \frac{53}{28} \times \frac{14}{65} = \frac{53}{130}$$

Again,

$$\frac{1}{2 + \frac{1}{2 + \frac{1}{2 + \frac{1}{25-1}}}} = \frac{1}{2 + \frac{1}{2 + \frac{5}{24}}} = \frac{1}{2 + \frac{5}{24}}$$

$$= \frac{1}{2 + \frac{1}{2 + \frac{48+5}{48+5}}} = \frac{1}{2 + \frac{24}{53}} = \frac{1}{24}$$

$$= \frac{1}{106+24} = \frac{53}{130}$$

$$\therefore \text{Expression} = \sqrt{\frac{53}{130} \div \frac{53}{130}} = 1$$

$$22. (3) 1 + \frac{1}{1 + \frac{1}{1 + \frac{15+4}{5}}}$$

$$= 1 + \frac{1}{1 + \frac{2 \times 5}{19}} = 1 + \frac{1}{19 + 10} = \frac{1}{19}$$

$$= 1 + \frac{19}{29} = \frac{29 + 19}{29} = \frac{48}{29}$$

$$23. (4) \text{ Expression} = 1 - \frac{a}{1 - \frac{1}{1 + \frac{a}{1-a}}}$$

$$= 1 - \frac{a}{1 - \frac{1}{1-a+a}} = \frac{a}{1-a}$$

$$= 1 - \frac{a}{1 - \frac{1}{1-a}}$$

$$= 1 - \frac{a}{1-(1-a)} = 1 - \frac{a}{1-1+a} = 1 - 1 = 0$$

$$24. (3) \text{ First part} = \frac{4\frac{1}{7} - 2\frac{1}{7}}{3\frac{1}{2} + 1\frac{1}{7}}$$

$$= \frac{\frac{29}{7} - \frac{15}{7}}{\frac{7}{2} + \frac{8}{7}} = \frac{\frac{14}{7}}{\frac{49+16}{14}} = \frac{14}{49+16}$$

$$= \frac{2}{14} = \frac{2 \times 14}{65} = \frac{28}{65}$$

$$\text{Second part} = \frac{1}{2 + \frac{1}{2 + \frac{1}{2 + \frac{1}{25-1}}}} = \frac{1}{2 + \frac{1}{2 + \frac{5}{24}}}$$

$$= \frac{1}{2 + \frac{1}{2 + \frac{5}{24}}} = \frac{1}{2 + \frac{1}{48+5}} = \frac{1}{24}$$

$$= \frac{1}{2 + \frac{24}{53}} = \frac{1}{106+24} = \frac{53}{130}$$

$$\therefore \text{Expression} = \frac{28}{65} \div \frac{53}{130}$$

$$= \frac{28}{65} \times \frac{130}{53} = \frac{56}{53}$$

$$25. (*) \text{ Let, } a = 1 + \frac{1}{10 + \frac{1}{10}}$$

$$= 1 + \frac{1}{100+1} = 1 + \frac{10}{101}$$

$$= \frac{101+10}{101} = \frac{111}{101}$$

Again,

$$b = 1 - \frac{1}{10 + \frac{1}{10}} = 1 - \frac{1}{100+1} = \frac{1}{10}$$

$$= 1 - \frac{10}{101}$$

$$= \frac{101-10}{101} = \frac{91}{101}$$

∴ Expression

$$= (a^2 - b^2) \div ab$$

$$= \{(a+b)(a-b)\} \div ab$$

$$= \left( \frac{111}{101} + \frac{91}{101} \right) \left( \frac{111}{101} - \frac{91}{101} \right)$$

$$\div \left( \frac{111}{101} \times \frac{91}{101} \right)$$

$$= \frac{202}{101} \times \frac{20}{101} \times \frac{101 \times 101}{111 \times 91}$$

$$= \frac{4040}{10101}$$

26. (1) Expression

$$= 4 - \frac{5}{1 + \frac{1}{3 + \frac{1}{\frac{8+1}{4}}}}$$

$$= 4 - \frac{5}{1 + \frac{1}{3 + \frac{1}{\frac{9}{9}}}} = 4 - \frac{5}{1 + \frac{1}{27+4}} = 4 - \frac{5}{1 + \frac{1}{31}}$$

$$= 4 - \frac{5}{31} = 4 - \frac{5}{31+9} = 4 - \frac{5 \times 31}{40} = \frac{160 - 155}{40}$$

$$= \frac{5}{40} = \frac{1}{8}$$

## TYPE-II

$$1. (3) ? = \frac{9|3-5|-5|4| \div 10}{-3(5)-2 \times 4 \div 2}$$

$$= \frac{9 \times 2 - 5 \times 4 \div 10}{-15 - 8 \div 2}$$

$$= \frac{18-2}{-19} = -\frac{16}{19}$$

2. (1) Using Rule 1,

$$\begin{aligned} ? &= 5 - [4 - \{3 - (3-3-6)\}] \\ &= 5 - [4 - \{3 - (-6)\}] \\ &= 5 - [4 - \{3 + 6\}] \\ &= 5 - [4 - 9] \\ &= 5 + 5 = 10 \end{aligned}$$

3. (3) ? =  $\frac{(-2)^2 + 6 + 6}{18 - 15}$

$$= \frac{-4 + 12}{3} = \frac{8}{3}$$

4. (3) Using Rule 1,

$$\begin{aligned} & \frac{5}{3} \times \frac{7}{5} \text{ of } \frac{17}{5} - \frac{1}{3} \\ & \frac{2}{9} \times \frac{5}{7} \text{ of } \frac{28}{5} - \frac{2}{3} \end{aligned}$$

$$\begin{aligned} & = \frac{5}{3} \times \frac{7}{15} - \frac{1}{3} \\ & = \frac{2}{9} \times 4 - \frac{2}{3} \end{aligned}$$

$$= \frac{7}{8} - \frac{1}{2} = \frac{4}{9} \times \frac{9}{2} = 2$$

5. (1) Using Rule 1,

$$? = 1 - [5 - \{2 + (-1)2\}]$$

$$= 1 - [5 - \{2 - 2\}]$$

$$= 1 - [5 - 0]$$

$$= 1 - 5 = -4$$

6. (2) Using Rule 1,

$$3034 - (1002 \div 20.04)$$

$$= 3034 - \frac{1002}{20.04}$$

$$= 3034 - \frac{1002}{2004} \times 100$$

$$= 3034 - 50 = 2984$$

7. (1) Using Rule 1,

$$(100) \frac{1}{2} \times (0.001) \frac{1}{3} - (0.0016) \frac{1}{4} \times 3^0 + \left( \frac{5}{4} \right)^{-1}$$

$$= 10 \times 0.1 - 0.2 \times 1 + \frac{4}{5}$$

$$= 1 - 0.2 + 0.8 = 1.6$$

8. (1) Using Rule 1,

$$? = \left( \frac{1}{2} - \frac{1}{4} + \frac{1}{5} - \frac{1}{6} \right)$$

$$+ \left( \frac{2}{5} - \frac{5}{9} + \frac{3}{5} - \frac{7}{18} \right)$$

$$= \left( \frac{30 - 15 + 12 - 10}{60} \right)$$

$$+ \left( \frac{36 - 50 + 54 - 35}{90} \right)$$

$$= \left( \frac{17}{60} \right) \div \left( \frac{5}{90} \right) = \frac{17}{60} \times 18$$

$$= \frac{51}{10} = 5 \frac{1}{10}$$

9. (2) Using Rule 1,

$$8 \frac{1}{2} - \left[ 3 \frac{1}{4} \div \left\{ 1 \frac{1}{4} - \frac{1}{2} \left( 1 \frac{1}{2} - \frac{1}{3} - \frac{1}{6} \right) \right\} \right]$$

$$= \frac{17}{2} - \left[ \frac{13}{4} \div \left\{ \frac{5}{4} - \frac{1}{2} \left( \frac{3}{2} - \frac{1}{3} - \frac{1}{6} \right) \right\} \right]$$

$$= \frac{17}{2} - \left[ \frac{13}{4} \div \left\{ \frac{5}{4} - \frac{1}{2} \left( \frac{9 - 2 - 1}{6} \right) \right\} \right]$$

$$= \frac{17}{2} - \left[ \frac{13}{4} \div \left\{ \frac{5}{4} - \frac{1}{2} \times \frac{6}{6} \right\} \right]$$

$$= \frac{17}{2} - \left[ \frac{13}{4} \div \left\{ \frac{5}{4} - \frac{1}{2} \right\} \right]$$

$$= \frac{17}{2} - \left[ \frac{13}{4} \div \left\{ \frac{5 - 2}{4} \right\} \right]$$

$$= \frac{17}{2} - \left[ \frac{13}{4} \div \frac{3}{4} \right]$$

$$= \frac{17}{2} - \left[ \frac{13}{4} \times \frac{4}{3} \right] = \frac{17}{2} - \frac{13}{3}$$

$$= \frac{51 - 26}{6} = \frac{25}{6} = 4 \frac{1}{6}$$

10. (4) Let the value of \* be x.

$$\therefore \frac{50}{x} = \frac{x}{12 \frac{1}{2}}$$

$$\Rightarrow \frac{50}{x} = \frac{2x}{25}$$

$$\Rightarrow 2x^2 = 50 \times 25$$

$$\Rightarrow x^2 = 25 \times 25$$

$$\therefore x = 25$$

11. (2) Using Rule 1,

$$0.008 \times 0.01 \times 0.072 \div (0.12 \times 0.0004)$$

$$= 0.008 \times 0.01 \times 0.072 \div (0.000048)$$

$$= 0.008 \times 0.01 \times \frac{0.072}{0.000048}$$

$$= \frac{0.00000576}{0.000048} = 0.12$$

12. (1) Using Rule 1,

$$\frac{2}{3} \times \frac{3}{\frac{5}{6} \div \frac{2}{3} \text{ of } 1 \frac{1}{4}}$$

$$= \frac{2}{3} \times \frac{3}{\frac{5}{6} \div \frac{2}{3} \text{ of } \frac{5}{4}}$$

$$= \frac{2}{3} \times \frac{3}{\frac{5}{6} \div \frac{10}{12}}$$

$$= \frac{2}{3} \times \frac{3}{\frac{5}{6} \times \frac{12}{10}} = \frac{2}{3} \times \frac{3}{1} = 2$$

13. (1)

$$\frac{1}{9} + \frac{1}{6} + \frac{1}{12} + \frac{1}{20} + \frac{1}{30} + \frac{1}{42} + \frac{1}{56} + \frac{1}{72}$$

$$= \frac{1}{9} + \frac{1}{2 \times 3} + \frac{1}{3 \times 4} + \frac{1}{4 \times 5}$$

$$+ \frac{1}{5 \times 6} + \dots + \frac{1}{8 \times 9}$$

$$= \frac{1}{9} + \frac{1}{2} - \frac{1}{3} + \frac{1}{3} - \frac{1}{4} + \dots + \frac{1}{8} - \frac{1}{9} = \frac{1}{2}$$

**Aliter :**

Using Rule 2,

$$\frac{1}{9} + \frac{1}{6} + \frac{1}{12} + \frac{1}{20} + \frac{1}{30} + \frac{1}{42} + \frac{1}{56} + \frac{1}{72}$$

$$= \frac{1}{9} + \frac{1}{2 \times 3} + \frac{1}{3 \times 4} + \frac{1}{4 \times 5}$$

$$+ \frac{1}{5 \times 6} + \frac{1}{6 \times 7} + \frac{1}{7 \times 8} + \frac{1}{8 \times 9}$$

$$= \frac{1}{9} + \left[ \frac{1}{2} - \frac{1}{(2+7)} \right]$$

$\therefore n = 2$  and  $r = 7$

$$= \frac{1}{9} + \frac{1}{2} - \frac{1}{9} = \frac{1}{2}$$

14. (3) Using Rule 1,

Expression

$$= 25 - 5 [2 + 3 \{2 - 2(5 - 3) + 5\}$$

$$- 10] \div 4$$

$$= 25 - 5 [2 + 3 \{2 - 2 \times 2 + 5\} - 10] \div 4$$

$$= 25 - 5 [2 + 9 - 10] \div 4$$

$$= 25 - 5 \div 4 = 25 - \frac{5}{4}$$

$$= \frac{100 - 5}{4} = \frac{95}{4} = 23.75$$

**15.** (4) Using Rule 1,

We have

$$\frac{5}{3} \div \frac{2}{7} \times \frac{*}{7} = \frac{5}{4} \times \frac{2}{3} \times 6$$

$$\Rightarrow \frac{5}{3} \times \frac{7}{2} \times \frac{*}{7} = \frac{5 \times 2 \times 6}{4 \times 3}$$

$$\therefore * = \frac{5 \times 2 \times 6 \times 3 \times 2 \times 7}{5 \times 7 \times 4 \times 3} = 6$$

**16.** (1) Using Rule 1,

Expression

$$= 9 - \frac{11}{9} \text{ of } \frac{36}{11} \div \frac{36}{7} \text{ of } \frac{7}{9}$$

$$= 9 - \frac{11}{9} \times \frac{36}{11} \div \frac{36}{7} \times \frac{7}{9}$$

$$= 9 - 4 \div 4$$

$$= 9 - 4 \times \frac{1}{4} = 9 - 1 = 8$$

**17.** (1) Using Rule 1,

$$\frac{5}{\frac{15}{8} \times \frac{4}{3}} \times \frac{\frac{21}{10}}{\frac{7}{2}} \text{ of } \frac{5}{4}$$

$$= 5 \times \frac{2}{5} \times \frac{21}{10} \times \frac{2}{7} \times \frac{5}{4}$$

$$= \frac{3}{2} = 1\frac{1}{2}$$

**18.** (1) Using Rule 1,

$$\frac{9}{20} - \left[ \frac{1}{5} + \left\{ \frac{1}{4} + \left( \frac{5}{6} - \frac{1}{3} + \frac{1}{2} \right) \right\} \right]$$

$$= \frac{9}{20} - \left[ \frac{1}{5} + \left\{ \frac{1}{4} + \left( \frac{5}{6} - \frac{5}{6} \right) \right\} \right]$$

$$= \frac{9}{20} - \left[ \frac{1}{5} + \frac{1}{4} \right] = \frac{9}{20} - \frac{9}{20} = 0$$

$$\text{19. (4)} \quad \frac{0.83 \div 7.5}{2.321 - 0.098} = \frac{\frac{83}{100} \div 7.5}{2 \frac{321}{100} - \frac{98}{100}}$$

$$= \frac{\frac{75}{90} \div 7.5}{2 \frac{318}{990} - \frac{98}{990}} = \frac{\frac{75}{90} \div 7.5}{2 \frac{220}{990}}$$

$$= \frac{7.5}{90 \times 7.5} \times \frac{990}{2200} = \frac{1}{20} = 0.05$$

**20.** (3) Let '\*' be H

$$\left[ \frac{(H)}{21} \times \frac{(H)}{189} \right] = 1$$

$$\Rightarrow (H)^2 = 21 \times 189$$

$$\Rightarrow H = \sqrt{21 \times 189} = 63$$

$$\text{21. (3)} \quad 80 \times \sqrt{P} = 1120$$

$$\Rightarrow \sqrt{P} = \frac{1120}{80} = 14$$

$$\Rightarrow P = (14)^2 = 196$$

**22.** (3) Using Rule 1,

$$\frac{\frac{13}{4} - \frac{5}{6} \times \frac{4}{5}}{\frac{13}{3} \div \frac{1}{5} - \left( \frac{3}{10} + \frac{106}{5} \right)} - \left( \frac{3}{2} \times \frac{5}{3} \right)$$

$$= \frac{\frac{13}{4} - \frac{2}{3}}{\frac{13 \times 5}{3} - \left( \frac{3+212}{10} \right)} - \frac{5}{2}$$

$$= \frac{\frac{39-8}{12}}{\frac{65-215}{30}} - \frac{5}{2} = \frac{\frac{31}{12}}{\frac{650-645}{30}} - \frac{5}{2}$$

$$= \frac{31}{12} \times \frac{30}{5} - \frac{5}{2}$$

$$= \frac{31}{2} - \frac{5}{2} = \frac{31-5}{2} = \frac{26}{2} = 13$$

**23.** (2) Using Rule 1,

$$\left[ \frac{13}{4} \div \left\{ \frac{5}{4} - \frac{1}{2} \left( \frac{5}{2} - \frac{3-2}{12} \right) \right\} \right] \div \frac{13}{6}$$

$$= \left[ \frac{13}{4} \div \left\{ \frac{5}{4} - \frac{1}{2} \left( \frac{5}{2} - \frac{1}{12} \right) \right\} \right] \div \frac{13}{6}$$

$$= \left[ \frac{13}{4} \div \left\{ \frac{5}{4} - \frac{1}{2} \left( \frac{30-1}{12} \right) \right\} \right] \div \frac{13}{6}$$

$$= \left[ \frac{13}{4} \div \left\{ \frac{5}{4} - \frac{1}{2} \times \frac{29}{12} \right\} \right] \div \frac{13}{6}$$

$$= \left[ \frac{13}{4} \div \left\{ \frac{30-29}{24} \right\} \right] \div \frac{13}{6}$$

$$= \left[ \frac{13}{4} \div \frac{1}{24} \right] \div \frac{13}{6}$$

$$= \left[ \frac{13}{4} \times 24 \right] \div \frac{13}{6}$$

$$= 13 \times 6 \times \frac{6}{13} = 36$$

**24.** (2) Using (x) of Basic Formulae

Let 0.1 = a, 0.2 = b and 0.3 = c  
Then, we have,

$$\frac{a \times a \times a + b \times b \times b + c \times c \times c - 3abc}{a \times a + b \times b + c \times c - ab - bc - ac}$$

$$= \frac{a^3 + b^3 + c^3 - 3abc}{a^2 + b^2 + c^2 - ab - bc - ac}$$

$$= a + b + c$$

$$= 0.1 + 0.2 + 0.3 = 0.6$$

**25.** (4) Using Rule 2,

$$\frac{\frac{1}{5 \times 6} + \frac{1}{6 \times 7} + \frac{1}{7 \times 8} + \frac{1}{8 \times 9} + \frac{1}{9 \times 10} + \frac{1}{10 \times 11}}{\frac{1}{5} - \frac{1}{6} + \frac{1}{6} - \frac{1}{7} + \frac{1}{7} - \frac{1}{8} + \frac{1}{8} - \frac{1}{9} + \frac{1}{9} - \frac{1}{10} + \frac{1}{10} - \frac{1}{11}}$$

$$= \frac{1}{5} - \frac{1}{11} = \frac{11-5}{55} = \frac{6}{55}$$

**26.** (2) Using Rule 1,

$$\text{I.} = \frac{3}{4} \times \frac{6}{5} = \frac{9}{10}$$

$$\text{II.} = 3 \div \left[ \frac{4}{5} \times \frac{1}{6} \right] = 3 \div \frac{2}{15} = \frac{45}{2}$$

$$\text{III.} = \left[ 3 \div \frac{4}{5} \right] \div 6 = \frac{15}{4} \div 6 = \frac{5}{8}$$

$$\text{IV.} = 3 \div 4 \times \frac{5}{6} = 3 \div \frac{10}{3} = \frac{9}{10}$$

Obviously, (I) and (IV) are equal

**27.** (2) Using Rule 1,

$$= 1 \div \left[ 1 + 1 \div \left\{ 1 + 1 \div \left( 1 + 1 \div 2 \right) \right\} \right]$$

$$= 1 \div \left[ 1 + 1 \div \left\{ 1 + 1 \div \left( 1 + \frac{1}{2} \right) \right\} \right]$$

$$= 1 \div \left[ 1 + 1 \div \left\{ 1 + 1 \div \frac{3}{2} \right\} \right]$$

$$= 1 \div \left[ 1 + 1 \div \left\{ 1 + \frac{2}{3} \right\} \right] = 1 \div \left[ 1 + 1 \div \frac{5}{3} \right]$$

$$= 1 \div \left[ 1 + \frac{3}{5} \right] = 1 \div \frac{8}{5} = \frac{5}{8}$$

**28.** (1) Using Rule 1,  
The given expression

$$= \frac{\frac{1}{3} \times 3 \times \frac{1}{3}}{\frac{1}{3} \div \left( \frac{1}{3} \times \frac{1}{3} \right)} - \frac{1}{9}$$

$$= \frac{\frac{1}{3}}{\frac{1}{3} \div \frac{1}{9}} - \frac{1}{9} = \frac{\frac{1}{3}}{\frac{1}{3} \times 9} - \frac{1}{9}$$

$$= \frac{\frac{1}{3}}{\frac{3}{9}} - \frac{1}{9} = \frac{1}{9} - \frac{1}{9} = 0$$

**29.** (4) Using Rule 1,

The given expression

$$= \frac{11}{\frac{4}{11} \div \frac{7}{8} \left( \frac{4+3}{12} \right) + \frac{5}{7} \div \frac{3}{4} \text{ of } \frac{3}{7}}$$

$$= \left( \frac{11}{4} \times \frac{6}{11} \right) \div \frac{7}{8} \times \frac{7}{12} + \frac{5}{7} \div \left( \frac{3}{4} \times \frac{3}{7} \right)$$

$$= \frac{3}{2} \div \frac{7}{8} \times \frac{7}{12} + \frac{5}{7} \div \frac{9}{28}$$

$$= \frac{3}{2} \times \frac{8}{7} \times \frac{7}{12} + \frac{5}{7} \times \frac{28}{9}$$

$$= 1 + \frac{20}{9} = \frac{9+20}{9} = \frac{29}{9} = 3 \frac{2}{9}$$

**30.** (4)  $3.\overline{36} - 2.\overline{05} + 1.\overline{33}$

$$= 3 \frac{36}{99} - 2 \frac{05}{99} + 1 \frac{33}{99}$$

$$= 3 + \frac{36}{99} - 2 - \frac{5}{99} + 1 + \frac{33}{99}$$

$$= (3-2+1) + \left( \frac{36}{99} - \frac{5}{99} + \frac{33}{99} \right)$$

$$= 2 + \left( \frac{36-5+33}{99} \right)$$

$$= 2 + \frac{64}{99} = 2 \frac{64}{99} = 2.\overline{64}$$

**31.** (1) Using (x) of Basic Formulae

Let  $0.9 = x$ ,  $0.2 = y$  and  $0.3 = z$   
Then, the given expression

$$= \frac{x \times x \times x + y \times y \times y + z \times z \times z - 3 \times x \times y \times z}{x \times x + y \times y + z \times z - x \times y - y \times z - z \times x}$$

$$= \frac{x^3 + y^3 + z^3 - 3xyz}{x^2 + y^2 + z^2 - xy - yz - zx}$$

$$= \frac{(x+y+z)(x^2+y^2+z^2-xy-yz-zx)}{x^2+y^2+z^2-xy-yz-zx}$$

$$= x + y + z$$

$$= 0.9 + 0.2 + 0.3 = 1.4$$

**32.** (2) Using Rule 1,

$$\left( \frac{1}{9} \right)^2 \left\{ 1 - 9 \left( \frac{16-1}{90} \right)^2 \right\}$$

$$= \frac{1}{81} \left\{ 1 - \frac{9 \times 15 \times 15}{90 \times 90} \right\}$$

$$= \frac{1}{81} \times \left\{ 1 - \frac{1}{4} \right\}$$

$$= \frac{1}{81} \times \frac{3}{4} = \frac{1}{108}$$

**33.** (3) Using Rule 1,

$$\frac{\frac{3}{2}}{\frac{1}{2} \div \frac{4}{7} \left( \frac{4+3}{10} \right) \text{ of } \frac{\frac{3+2}{6}}{\frac{3-2}{6}}}$$

$$= 3 \div \frac{4}{7} \left( \frac{7}{10} \right) \text{ of } \left( \frac{5}{6} \times 6 \right)$$

$$= 3 \div \left( \frac{4}{7} \times \frac{7}{10} \times 5 \right) = 3 \div 2 = \frac{3}{2}$$

**34.** (3) Using Rule 1,

$$[0.9 - \{2.3 - 3.2 - (7.1 - 8.9)\}]$$

$$= [0.9 - \{2.3 - 3.2 + 1.8\}]$$

$$= [0.9 - 0.9] = 0$$

**35.** (2) Using (x) of Basic Formulae

Let,  $32 = a$

$79 = b$ ,  $-111 = c$

When  $(a+b+c) = 0$

$$\text{then } a^3 + b^3 + c^3 - 3abc = 0$$

$$\text{Here, } a+b+c = 32+79-111 = 0$$

$$\therefore (32)^3 + (79)^3 - (111)^3 + 3 \times 32 \times 79 \times 111 = 0$$

**36.** (2) Using Rule 1,

$$\left( \frac{5}{2} + \frac{3}{2} \right) \left( \frac{25}{4} - \frac{15}{4} + \frac{9}{4} \right)$$

$$= 4 \times \frac{19}{4} = 19$$

$$\text{37. (1) Expression} = \frac{(0.04 + 0.01)}{(0.01 + 0.02)}$$

$$= \frac{0.05}{0.03} = \frac{5}{3}$$

**38.** (3) Using Rule 1,

Expression

$$= \frac{1}{2} + \left\{ \frac{19}{4} - \left( \frac{19}{6} - \frac{7}{3} \right) \right\}$$

$$= \frac{1}{2} + \left\{ \frac{19}{4} - \left( \frac{19-14}{6} \right) \right\}$$

$$= \frac{1}{2} + \left\{ \frac{19}{4} - \frac{5}{6} \right\}$$

$$= \frac{1}{2} + \frac{19}{4} - \frac{5}{6}$$

$$= \frac{6+57-10}{12} = \frac{53}{12} = 4 \frac{5}{12}$$

$$\text{39. (1) Expression} = 0.125 + 0.015625 + 0.001953125 + 0.00024414 + 0.000030517 \\ = 0.1428 \approx 0.143$$

$$\text{40. (3) Using Rule 1, Expression} \\ = 8.7 - [7.6 - \{6.5 - (5.4 - \frac{4.3-2}{2})\}] \\ = 8.7 - [7.6 - \{6.5 - (5.4 - 2.3)\}] \\ = 8.7 - [7.6 - \{6.5 - 3.1\}] \\ = 8.7 - [7.6 - 3.4] \\ = 8.7 - 4.2 = 4.5$$

$$\text{41. (2) Using (x) of Basic Formulae} \\ \text{If } a + b + c = 0, \text{ then } a^3 + b^3 + c^3 = 3abc \\ \text{Here, } 0.111 + 0.222 + (-0.333) = 0 \\ \therefore (0.111)^3 + (0.222)^3 + (-0.333)^3$$

$$= -3 \times 0.111 \times 0.222 \times 0.333 \\ = - (0.333)^2 \times 0.222$$

$$\therefore \text{Expression} \\ = [- (0.333)^2 \times 0.222 + (0.333)^2 \times 0.222]^3 = 0$$

**42.** (4) Using Rule 1,  
Expression

$$= \frac{\frac{5}{4} \div \frac{3}{2}}{\left( \frac{2+30-27}{30} \right)}$$

$$= \frac{\frac{5}{4} \times \frac{2}{3}}{\frac{5}{30}} = \frac{5}{6} \times \frac{30}{5} = 5$$

**43.** (2) Using Rule 1,  
Expression

$$\begin{aligned} & -30 - 40 + 48 - 20 + 12 + 45 \\ & = \frac{60}{30 + 40 - 80 + 20 - 12 - 48} \\ & = \frac{60}{-105} \end{aligned}$$

$$= \frac{105-90}{90-140} = -\frac{15}{50} = -\frac{3}{10}$$

**44.** (2) Expression

$$\begin{aligned} & = 0.\overline{63} + 0.\overline{37} + 0.\overline{80} \\ & = \frac{63}{99} + \frac{37}{99} + \frac{80}{99} \\ & = \frac{63+37+80}{99} = \frac{180}{99} \\ & = 1\frac{81}{99} = 1.\overline{81} \end{aligned}$$

$$\text{45. (4) Let } (4.53 - 3.07) = a \\ (3.07 - 2.15) = b \text{ and } (2.15 - 4.53) = c \therefore a + b + c = 0 \\ \therefore \text{Expression}$$

- 52.** (3) Expression  

$$= \frac{a^2}{bc} + \frac{b^2}{ac} + \frac{c^2}{ab}$$

$$= \frac{a^3 + b^3 + c^3}{abc} = \frac{3abc}{abc} = 3$$
 [If  $a + b + c = 0$ ,  $a^3 + b^3 + c^3 = 3abc$ ]
- 46.** (2) Using Rule 1,  
 Expression  

$$= \frac{17}{15} \times \frac{17}{15} + \frac{2}{15} \times \frac{2}{15} - 2 \times \frac{17}{15} \times \frac{2}{15}$$

$$= \left( \frac{17}{15} - \frac{2}{15} \right)^2$$

$$= \left( \frac{17-2}{15} \right)^2 = \left( \frac{15}{15} \right)^2 = 1$$
- 47.** (4) Using (v) of Basic Formulae  
 Let  $4\frac{11}{15} = a$  and  $\frac{15}{71} = b$ .  
 $\therefore$  Expression  

$$= (a+b)^2 - (a-b)^2$$

$$= (a^2 + b^2 + 2ab) - (a^2 + b^2 - 2ab) = 4ab$$

$$= 4 \times 4\frac{11}{15} \times \frac{15}{71} = 4 \times \frac{71}{15} \times \frac{15}{71} = 4$$
- 48.** (2) Let  $0.1 = a \Rightarrow 0.2 = 2a$   
 and  $0.02 = b \Rightarrow 0.04 = 2b$   
 $\therefore$  Expression  

$$= \frac{a^3 + b^3}{8a^3 + 8b^3}$$

$$= \frac{a^3 + b^3}{8(a^3 + b^3)} = \frac{1}{8} = 0.125$$
- 49.** (1)  $5\frac{3}{*} \times \frac{7}{2} = 19$   
 $\Rightarrow 5\frac{3}{*} = \frac{19 \times 2}{7}$ 
 $\Rightarrow 5\frac{3}{*} = \frac{38}{7} = 5\frac{3}{7}$ 
 $\Rightarrow * = 7$
- 50.** (3) Using Rule 7,  

$$\left( \sqrt{2} + \frac{1}{\sqrt{2}} \right)^2$$

$$= 2 + \frac{1}{2} + 2 \times \sqrt{2} \times \frac{1}{\sqrt{2}} = 4\frac{1}{2}$$
- 51.** (4) Expression  

$$= (0.98)^3 + (0.02)^3 + 3 \times 0.98 \times 0.02 - 1$$

$$= (0.98)^3 + (0.02)^3 + 3 \times 0.98 \times 0.02 (0.98+0.02) - 1$$

$$= (0.98 + 0.02)^3 - 1 = 1 - 1 = 0$$
- 52.** (3) Expression  

$$= 71 \times 29 + 27 \times 15 + 8 \times 4$$

$$= 2059 + 405 + 32 = 2496$$
- 53.** (2) Expression  

$$= 0.05 \times 5 - 0.005 \times 5$$

$$= 0.25 - 0.025 = 0.225$$
- 54.** (1) Let  $0.2 = a$  and  $0.04 = b$   
 $\Rightarrow 0.4 = 2a$  and  $0.08 = 2b$   
 $\therefore$  Expression  

$$= 3 \sqrt[3]{\frac{a \times a \times a + b \times b \times b}{2a \times 2a \times 2a + 2b \times 2b \times 2b}}$$

$$= 3 \sqrt[3]{\frac{a^3 + b^3}{8(a^3 + b^3)}} = 3 \sqrt[3]{\frac{1}{8}} = \frac{1}{2} = 0.5$$
- 55.** (1) Expression  

$$= (256)^{0.16} \times (16)^{0.18}$$

$$= (2^8)^{0.16} \times (2^4)^{0.18}$$

$$= (2)^{8 \times 0.16} \times (2)^{4 \times 0.18}$$

$$= (2)^{1.28} \times (2)^{0.72} = (2)^{1.28+0.72}$$

$$= (2)^2 = 4$$
- 56.** (4) Expression  

$$\begin{aligned} & \left( \frac{1}{3.5} + \frac{1}{5.7} + \frac{1}{7.9} + \frac{1}{9.11} \right. \\ & \quad \left. + \frac{1}{11.13} + \frac{1}{13.15} \right) \\ & = \frac{1}{2} \left( \frac{2}{3.5} + \frac{2}{5.7} + \frac{2}{7.9} + \frac{2}{9.11} + \frac{2}{11.13} + \frac{2}{13.15} \right) \\ & = \frac{1}{2} \left( \frac{1}{3} - \frac{1}{5} + \frac{1}{5} - \frac{1}{7} + \frac{1}{7} - \frac{1}{9} + \frac{1}{9} - \frac{1}{11} + \frac{1}{11} - \frac{1}{13} + \frac{1}{13} - \frac{1}{15} \right) \\ & = \frac{1}{2} \left( \frac{1}{3} - \frac{1}{15} \right) = \frac{1}{2} \left( \frac{5-1}{15} \right) \\ & = \frac{1}{2} \times \frac{4}{15} = \frac{2}{15} \end{aligned}$$
- Aliter :**  
 Using Rule 3,  

$$\frac{1}{3.5} + \frac{1}{5.7} + \frac{1}{7.9} + \frac{1}{9.11} + \frac{1}{11.13} + \frac{1}{13.15}$$
 Here,  $n = 3$  and  $r = 6$
- $$\Rightarrow \frac{1}{2} \left( \frac{1}{n} - \frac{1}{n+2r} \right)$$

$$= \frac{1}{2} \left( \frac{1}{3} - \frac{1}{3+2 \times 6} \right)$$

$$= \frac{1}{2} \left( \frac{1}{3} - \frac{1}{15} \right)$$

$$= \frac{1}{2} \left( \frac{5-1}{15} \right) = \frac{2}{15}$$
- 57.** (3) Expression  

$$= (53 \times 87 + 159 \times 21 + 106 \times 25)$$

$$= 53 (87 + 3 \times 21 + 2 \times 25)$$

$$= 53 (87 + 63 + 50)$$

$$= 53 \times 200 = 10600$$
- 58.** (4) Using Rule 4,  
 Expression  

$$= \frac{(0.5)^3 + (0.3)^3}{(0.5)^2 - 0.5 \times 0.3 + (0.3)^2}$$
 Let  $0.5 = a$ , and  $0.3 = b$   
 $\therefore$  Expression  $= \frac{a^3 + b^3}{a^2 - ab + b^2}$ 

$$= \frac{(a+b)(a^2 - ab + b^2)}{a^2 - ab + b^2}$$

$$= a + b = 0.5 + 0.3 = 0.8$$
- 59.** (4) Using Rule 4,  

$$\text{Expression} = \frac{8(3.75)^3 + 1}{(7.5)^2 - 6.5}$$

$$= \frac{(2 \times 3.75)^3 + 1}{(7.5)^2 - 7.5 \times 1 + 1^2}$$

$$= \frac{(7.5)^3 + 1}{(7.5)^2 - 7.5 \times 1 + 1^2}$$

$$\left[ a^3 + b^3 = (a+b)(a^2 - ab + b^2) \right]$$

$$= 7.5 + 1 = 8.5$$
- 60.** (2) Using Rule 6,  
 Let  $2.697 = a$  and  $0.498 = b$   
 $\therefore$  Expression  

$$= \frac{(a-b)^2 + (a+b)^2}{a^2 + b^2}$$

$$= \frac{2(a^2 + b^2)}{a^2 + b^2} = 2$$
- 61.** (1) Using Rule 1,  
 Expression  

$$\begin{aligned} & \frac{13}{4} - \frac{4}{5} \times \frac{5}{6} \\ & = \frac{13}{3} \times 5 - \left( \frac{3}{10} + \frac{106}{5} \right) \\ & = \frac{13}{3} - \frac{2}{4} - \frac{106}{30} \\ & = \frac{39-8}{12} \\ & = \frac{650-9-636}{30} \\ & = \frac{31}{12} \times \frac{30}{5} = \frac{31}{2} = 15\frac{1}{2} \\ & \therefore \text{Required answer} \\ & = 15\frac{1}{2} - 15 = \frac{1}{2} \end{aligned}$$

## SIMPLIFICATION

**62.** (2)  $\sqrt[2]{0.014 \times 0.14x}$

$$= 0.014 \times 0.14 \sqrt[2]{y}$$

On squaring both sides,

$$0.014 \times 0.14x$$

$$= (0.014)^2 \times (0.14)^2 xy$$

$$\therefore \frac{x}{y} = 0.014 \times 0.14 = 0.00196$$

**63.** (1)

$$\frac{4.41 \times 0.16}{2.1 \times 1.6 \times 0.21} = \frac{441 \times 16}{21 \times 16 \times 21} = 1$$

**64.** (4)  $0.1 \times 0.01 \times 0.001 \times 10^7$

$$= 10^{-6} \times 10^7 = 10$$

**65.** (4) Expression

$$= \frac{3.20(3.25 - 3.05)}{0.064}$$

$$= \frac{3.20 \times 0.20}{0.064} = 10$$

**66.** (4)  $\frac{0.01 - 0.0001}{0.0001} + 1 = \frac{0.0099}{0.0001} + 1$

$$= 99 + 1 = 100$$

**67.** (1) Expression

$$= 0.5(5 + 0.25 + 4 + 0.75) \\ = 0.5 \times 10 = 5$$

**68.** (4) Using Rule 1,

Expression

$$= \frac{20 \div 5}{9 + 3 \div 3} = \frac{4}{10} = \frac{2}{5}$$

**69.** (3) Expression

$$(100 - 1)(100 - 2)(100 - 3) \dots$$

$$= \frac{(100 - 100) \dots (100 - 200)}{100 \times 99 \times 98 \times \dots \times 3 \times 2 \times 1}$$

$$= 0 [\because 100 - 100 = 0]$$

**70.** (1)  $(0.9)^3 + (0.1)^3$

$$= 0.729 + 0.001 = 0.73$$

**71.** (4) Using Rule 4,

Let  $0.0347 = a$

and,  $0.9653 = b$

$$\therefore \text{Expression} = \frac{a^3 + b^3}{a^2 - ab + b^2}$$

$$= \frac{(a+b)(a^2 - ab + b^2)}{a^2 - ab + b^2} = a + b$$

$$= 0.0347 + 0.9653 = 1$$

**72.** (4) Using Rule 5,

Expression

$$= \frac{(3.2)^3 - (0.2)^3}{(3.2)^2 + 3.2 \times 0.2 + (0.2)^2}$$

Let  $3.2 = a$  and  $0.2 = b$

$$\therefore \text{Expression} = \frac{a^3 - b^3}{a^2 + ab + b^2}$$

$$= \frac{(a-b)(a^2 + ab + b^2)}{a^2 + ab + b^2} = a - b \\ = 3.2 - 0.2 = 3$$

**73.** (1) Using Rule 1,

$$\text{Expression} = \frac{\frac{1}{3} + \frac{1}{4} \left[ \frac{4-5}{10} \right]}{\frac{3}{4} \times \frac{5}{3} - \frac{4}{5} \times \frac{3}{4}}$$

$$= \frac{\frac{1}{3} - \frac{1}{4} \times \frac{1}{10}}{\frac{5}{4} - \frac{3}{5}} = \frac{\frac{1}{3} - \frac{1}{40}}{\frac{1}{4} - \frac{3}{5}}$$

$$= \frac{\frac{40-3}{120}}{\frac{25-12}{120}} = \frac{37}{120} \times \frac{20}{13} = \frac{37}{78}$$

**74.** (2) Using Rule 1,  
Expression

$$= \frac{0.04}{0.03} \times \frac{\left( \frac{10}{3} - \frac{5}{2} \right) \div \frac{5}{4} \times \frac{1}{2}}{\frac{1}{3} + \frac{1}{9} \times \frac{1}{5}}$$

$$= \frac{4}{3} \times \frac{\left( \frac{20-15}{6} \right) \div \frac{5}{8}}{\frac{1}{3} + \frac{1}{45}}$$

$$= \frac{4}{3} \times \frac{\frac{5}{6} \times \frac{8}{5}}{\frac{15+1}{45}} = \frac{4}{3} \times \frac{45}{16} \times \frac{4}{3} = 5$$

**75.** (3) Expression

$$= \frac{0.3555 \times 0.5555 \times 2.025}{0.2225 \times 1.7775 \times 0.2222}$$

$$= \frac{3555 \times 5555 \times 2025}{225 \times 17775 \times 2222} = 4.5$$

**76.** (2) Using Rule 1,

$$100 \times 10 - 100 + 2000 \div 100$$

$$= 100 \times 10 - 100 + 20$$

$$= 100(10 - 1) + 20$$

$$= 100 \times 9 + 20$$

$$= 900 + 20 = 920$$

**77.** (4)  $\frac{547.527}{0.0082} = x$

$$\Rightarrow \frac{5475270}{82} = x$$

$$\Rightarrow \frac{547527}{82} = \frac{x}{10}$$

**78.** (3)  $\frac{1}{1+2^{a-b}} + \frac{1}{1+2^{b-a}}$

$$= \frac{1}{1+\frac{2^a}{2^b}} + \frac{1}{1+\frac{2^b}{2^a}}$$

$$= \frac{2^b}{2^b+2^a} + \frac{2^a}{2^a+2^b} = \frac{2^b+2^a}{2^b+2^a} = 1$$

**79.** (1) Using Rule 1,  
Expression

$$= \frac{7}{2} - \left[ \frac{9}{4} \div \left\{ \frac{5}{4} - \frac{1}{2} \left( \frac{3}{2} - \frac{1}{3} - \frac{1}{6} \right) \right\} \right]$$

$$= \frac{7}{2} - \left[ \frac{9}{4} \div \left\{ \frac{5}{4} - \frac{1}{2} \left( \frac{9-2-1}{6} \right) \right\} \right]$$

$$= \frac{7}{2} - \left[ \frac{9}{4} \div \left\{ \frac{5}{4} - \frac{1}{2} \right\} \right]$$

$$= \frac{7}{2} - \left[ \frac{9}{4} \div \left\{ \frac{5-2}{4} \right\} \right]$$

$$= \frac{7}{2} - \left[ \frac{9}{4} \div \frac{3}{4} \right]$$

$$= \frac{7}{2} - \frac{9}{4} \times \frac{4}{3}$$

$$= \frac{7}{2} - 3 = \frac{7-6}{2} = \frac{1}{2}$$

**80.** (2) Using Rule 7,

Let  $3\frac{3}{5} = a$  and  $\frac{2}{5} = b$ , then

$$\text{Expression} = a^2 + 2ab + b^2$$

$$= (a+b)^2$$

$$= \left( 3\frac{3}{5} + \frac{2}{5} \right)^2 = (4)^2 = 16$$

**81.** (2)

$$\left( 1 - \frac{1}{n+1} \right) + \left( 1 - \frac{2}{n+1} \right) + \left( 1 - \frac{3}{n+1} \right)$$

$$+ \dots \dots \left( 1 - \frac{n}{n+1} \right)$$

$$= n - \left( \frac{1}{n+1} + \frac{2}{n+1} + \frac{3}{n+1} + \dots + \frac{n}{n+1} \right)$$

$$= n - \frac{1+2+3+\dots+n}{n+1}$$

$$= n - \frac{n(n+1)}{2(n+1)} = n - \frac{n}{2} = \frac{n}{2} = \frac{1}{2}n$$

**82.** (1) Using Rule 1,

Expression

$$= \frac{16}{3} \div \frac{11}{9} \times \frac{1}{4} \left( 10 + \frac{3}{\frac{5-1}{5}} \right)$$

$$= \frac{16}{3} \times \frac{9}{11} \times \frac{1}{4} \left( 10 + \frac{15}{4} \right)$$

$$= \frac{16}{3} \times \frac{9}{11} \times \frac{1}{4} \left( \frac{40+15}{4} \right)$$

$$= \frac{16}{3} \times \frac{9}{11} \times \frac{1}{4} \times \frac{55}{4} = 15$$

**83.** (2) Using Rule 1,

$$x[-2(-4(-a))] + 5[-2(-2(-a))]$$

$$\} = 4a$$

$$\Rightarrow x \times (-8a) + 5 \times (-4a) = 4a$$

$$\Rightarrow x \times (-2) + 5 \times (-1) = 1$$

$$\Rightarrow 2x + 5 = -1$$

$$\Rightarrow 2x = -5 - 1 = -6$$

$$\Rightarrow x = \frac{-6}{2} = -3$$

**84.** (\*) Using Rule 1,

Expression

$$= 3 \div \left[ (8-5) \div \left\{ (4-2) + \left( 2 + \frac{8}{13} \right) \right\} \right]$$

$$= 3 \div \left[ 3 \div \left\{ 2 + \frac{26+8}{13} \right\} \right]$$

$$= 3 \div \left[ 3 \div \left\{ 2 + \frac{34}{13} \right\} \right]$$

$$= 3 \div \left[ 3 \div \left\{ \frac{26+34}{13} \right\} \right]$$

$$= 3 \div \left[ 3 \div \frac{60}{13} \right]$$

$$= 3 \div \left[ \frac{3 \times 13}{60} \right]$$

$$= 3 \div \frac{13}{20} = 3 \times \frac{20}{13} = \frac{60}{13}$$

**85.** (4) Using Rule 1,

$$? = 9 + 3 \div 4 - 8 \times 2$$

After respective substitutions,

$$? = 9 \div 3 \times 4 + 8 - 2$$

$$= \frac{9}{3} \times 4 + 8 - 2$$

$$= 20 - 2 = 18$$

**86.** (1) Using Rule 1,

Expression

$$= \frac{4}{15} \text{ of } \frac{5}{8} \times 6 + 15 - 10$$

$$= 1 + 15 - 10 = 16 - 10 = 6$$

**87.** (4) Expression

$$= \frac{0.2 \times 0.02 \times 0.002 \times 32}{0.4 \times 0.04 \times 0.004 \times 16}$$

$$= \frac{32}{2 \times 2 \times 2 \times 16} = \frac{1}{4} = 0.25$$

**88.** (4)  $a^2 + b^2 + c^2 - ab - bc - ac$

$$= \frac{1}{2} (2a^2 + 2b^2 + 2c^2 - 2ab - 2bc - 2ac)$$

$$= \frac{1}{2} [(a-b)^2 + (b-c)^2 + (c-a)^2]$$

$$= \frac{1}{2} [(113 - 115)^2 + (115 - 117)^2 + (117 - 113)^2]$$

$$\text{Where, } a = 113, b = 115, c = 117.$$

$$= \frac{1}{2} [(-2)^2 + (-2)^2 + 4^2]$$

$$= \frac{1}{2} (4 + 4 + 16)$$

$$= \frac{1}{2} \times 24 = 12$$

### TYPE-III

**1.** (3)  $\sqrt{1.3} + \sqrt{1300} + \sqrt{0.013}$

$$= \sqrt{\frac{130}{100}} + 10\sqrt{13} + \sqrt{\frac{130}{10000}}$$

$$= \frac{1}{10}\sqrt{130} + 10\sqrt{13} + \frac{1}{100}\sqrt{130}$$

$$= \frac{11.40}{10} + 3.605 \times 10 + \frac{11.40}{100}$$

$$= 1.140 + 36.05 + 0.1140$$

$$= 37.304$$

**2.** (3)  $? = \frac{(2.644)^2 - (2.356)^2}{0.288}$

$$= \frac{(2.644 - 2.356)(2.644 + 2.356)}{0.288}$$

$$= \frac{0.288 \times 5}{0.288} = 5$$

**Aliter :**

Using Rule 8,

$$\frac{(2.644)^2 - (2.356)^2}{0.288}$$

$$= \frac{(2.644)^2 - (2.356)^2}{(2.644 - 2.356)}$$

$$= (2.644 + 2.356) = 5$$

**3.** (1)

$$? = \frac{(3.4567 + 3.4533)(3.4567 - 3.4533)}{0.0034}$$

$$= \frac{6.9100 \times 0.0034}{0.0034} = 6.91$$

**Aliter :**

Using Rule 8,

$$\frac{(3.4567 + 3.4533)(3.4567 - 3.4533)}{0.0034}$$

$$= \frac{3.4567^2 - 3.4533^2}{(3.4567 - 3.4533)}$$

$$= 3.4567 + 3.4533 = 6.91$$

$$4. (4) \frac{(0.03)^2 - (0.01)^2}{0.03 - 0.01}$$

[Using  $a^2 - b^2 = (a+b)(a-b)$ ]

$$= \frac{(0.03 + 0.01)(0.03 - 0.01)}{0.03 - 0.01}$$

$$= 0.03 + 0.01 = 0.04$$

**Aliter :**

Using Rule 8,

$$\frac{(0.03)^2 - (0.01)^2}{0.03 - 0.01}$$

$$= (0.03 + 0.01) = 0.04$$

$$5. (4) (\sqrt{72} - \sqrt{18}) \div \sqrt{12}$$

$$= \frac{\sqrt{72} - \sqrt{18}}{\sqrt{12}}$$

$$= \frac{6\sqrt{2} - 3\sqrt{2}}{2\sqrt{3}} = \frac{3\sqrt{2}}{2\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} = \frac{\sqrt{6}}{2}$$

$$6. (3) \frac{\sqrt{80} - \sqrt{112}}{\sqrt{45} - \sqrt{63}}$$

$$= \frac{\sqrt{16 \times 5} - \sqrt{16 \times 7}}{\sqrt{9 \times 5} - \sqrt{9 \times 7}}$$

$$= \frac{4\sqrt{5} - 4\sqrt{7}}{3\sqrt{5} - 3\sqrt{7}} = \frac{4(\sqrt{5} - \sqrt{7})}{3(\sqrt{5} - \sqrt{7})}$$

$$= \frac{4}{3} = 1\frac{1}{3}$$

**7. (2)**

$$\sqrt{\frac{(0.1)^2 + (0.01)^2 + (0.009)^2}{(0.01)^2 + (0.001)^2 + (0.0009)^2}}$$

$$= \sqrt{\frac{0.01 + 0.0001 + 0.000081}{0.0001 + 0.000001 + 0.00000081}}$$

$$= \sqrt{\frac{0.010181}{0.00010181}} = \sqrt{100} = 10$$

**8. (2)** Let  $0.03 = x \Rightarrow 0.003 = \frac{x}{10}$

$$0.21 = y \Rightarrow 0.021 = \frac{y}{10}$$

$$\text{and } 0.065 = z \Rightarrow 0.0065 = \frac{z}{10}$$

∴ Expression

$$= \sqrt{\frac{x^2 + y^2 + z^2}{\left(\frac{x}{10}\right)^2 + \left(\frac{y}{10}\right)^2 + \left(\frac{z}{10}\right)^2}}$$

$$= \sqrt{100 \frac{(x^2 + y^2 + z^2)}{(x^2 + y^2 + z^2)}} = \sqrt{100} = 10$$

**9. (2)**

$$\sqrt{0.01} + \sqrt{0.81} + \sqrt{1.21} + \sqrt{0.0009}$$

$$= 0.1 + 0.9 + 1.1 + 0.03$$

$$= 2.13$$

$$\text{10. (3)} \quad \sqrt{\frac{(6.1)^2 + (61.1)^2 + (611.1)^2}{(0.61)^2 + (6.11)^2 + (61.11)^2}}$$

$$= \sqrt{\frac{(10 \times 0.61)^2 + (10 \times 6.11)^2 + (10 \times 61.11)^2}{(0.61)^2 + (6.11)^2 + (61.11)^2}} = \sqrt{100} = 10$$

$$= \sqrt{100} = 10$$

$$\text{11. (4)} \quad \sqrt{\frac{20.2 \times 4}{0.25 \times 20.2}} = \sqrt{\frac{4}{0.25}}$$

$$= \sqrt{\frac{400}{25}} = \sqrt{16} = 4$$

**12. (2)** Using Rule 4,

$$\text{Let } 0.051 = x \text{ and } 0.041 = y$$

∴ The given expression

$$= \frac{x^3 + y^3}{x^2 - xy + y^2}$$

$$\begin{aligned} &= \frac{(x+y)(x^2 - xy + y^2)}{x^2 - xy + y^2} \\ &= x + y = 0.051 + 0.041 \\ &= 0.092 \end{aligned}$$

$$\text{13. (1)} \quad \sqrt{5 + \sqrt{11 + \sqrt{19 + \sqrt{29 + 7}}}}$$

$$= \sqrt{5 + \sqrt{11 + \sqrt{19 + 6}}}$$

$$= \sqrt{5 + \sqrt{11 + \sqrt{25}}}$$

$$= \sqrt{5 + \sqrt{11 + 5}} = \sqrt{5 + 4}$$

$$= \sqrt{9} = 3$$

$$\text{14. (4)} \quad \frac{(75.8)^2 - (55.8)^2}{20}$$

$$= \frac{(75.8 - 55.8)(75.8 + 55.8)}{20}$$

$$= \frac{20 \times 131.6}{20} = 131.6$$

**Aliter :**

Using Rule 8.

$$\frac{(75.8)^2 - (55.8)^2}{(75.8 - 55.8)}$$

$$= 75.8 + 55.8 = 131.6$$

**15. (4) Expression**

$$= \sqrt{\frac{(0.25 \times 0.09)}{0.0009 \times 0.36}}$$

$$= \sqrt{\frac{\frac{25}{100} \times \frac{9}{100}}{\frac{9}{10000} \times \frac{36}{100}}}$$

$$= \sqrt{\frac{25 \times 9 \times 1000000}{9 \times 36 \times 10000}}$$

$$= \frac{5 \times 10}{6} = \frac{25}{3} = 8 \frac{1}{3}$$

**16. (4) Using Rule 8,**

Let  $3.63 = a$  and  $2.37 = b$

$$\therefore \text{Expression} = \frac{a^2 - b^2}{a + b}$$

$$= \frac{(a - b)(a + b)}{a + b}$$

$$= a - b = 3.63 - 2.37 = 1.26$$

**17. (4) Expression**

$$= \sqrt{\frac{0.081 \times 0.484}{0.0064 \times 6.25}}$$

$$= \sqrt{\frac{81 \times 484}{64 \times 625}} = \frac{9 \times 22}{8 \times 25} = 0.99$$

**18. (2) Expression**

$$= \sqrt{900} + \sqrt{0.09} - \sqrt{0.000009}$$

$$= 30 + 0.3 - 0.003$$

$$= 30.297$$

**19. (2) Expression**

$$= \sqrt{\frac{0.009 \times 0.036 \times 0.016 \times 0.08}{0.002 \times 0.0008 \times 0.0002}}$$

$$= \sqrt{\frac{9 \times 36 \times 16 \times 8}{2 \times 8 \times 2}} = 3 \times 2 \times 3 \times 2 = 36$$

**20. (2) Expression**

$$= \sqrt{\frac{5}{4} \times \frac{64}{125} \times 1.44}$$

$$= \sqrt{\frac{16}{25} \times \frac{144}{100}} = \frac{4}{5} \times \frac{12}{10} = \frac{24}{25}$$

**21. (1) Expression**

$$= 2\sqrt{54} - 6\sqrt{\frac{2}{3}} - \sqrt{96}$$

$$= 2\sqrt{9 \times 6} - \sqrt{\frac{2 \times 6 \times 6}{3}} - \sqrt{16 \times 6}$$

$$= 2 \times 3\sqrt{6} - 2\sqrt{6} - 4\sqrt{6} = 0$$

$$\text{22. (4)} \quad \frac{\sqrt{24} + \sqrt{216}}{\sqrt{96}} = \frac{2\sqrt{6} + 6\sqrt{6}}{4\sqrt{6}}$$

$$= \frac{8\sqrt{6}}{4\sqrt{6}} = 2$$

$$\text{23. (2)} \quad \frac{4 - \sqrt{0.04}}{4 + \sqrt{0.4}} = \frac{4 - 0.2}{4 + \sqrt{0.4}}$$

$$= \frac{3.8}{4 + 0.632} = \frac{3.8}{4.632} = 0.8$$

$$= (a + b) = 0.08 + 0.02 = 0.1$$

$$\text{24. (4)} \quad \frac{1}{3 - \sqrt{8}} = \frac{3 + \sqrt{8}}{(3 - \sqrt{8})(3 + \sqrt{8})}$$

(Rationalising the denominator)

$$= \frac{3 + \sqrt{8}}{9 - 8} = 3 + \sqrt{8}$$

∴ Expression

$$= 3 + \sqrt{8} + 3 + \sqrt{8} - 6 - 4\sqrt{2}$$

$$= 6 + 2\sqrt{8} - 6 - 4\sqrt{2} = 2\sqrt{8} - 4\sqrt{2}$$

$$= 2 \times 2\sqrt{2} - 4\sqrt{2} = 0$$

25. (1)  $\sqrt{0.09} = \sqrt{0.3 \times 0.3} = 0.3$

26. (3) Expression

$$= \frac{(0.75)^3 + (1 - 0.75)((0.75)^2 + 0.75 \times 1 + 1^2)}{1 - 0.075}$$

$$= \frac{(0.75)^3 + 1^3 - (0.75)^3}{0.25}$$

$$= \frac{1}{0.25} = \frac{100}{25} = 4$$

∴ Required square root

$$= \sqrt{4} = 2$$

27. (3) ? =  $\sqrt{(272^2 - 128^2)}$

$$= \sqrt{(272 + 128)(272 - 128)}$$

$$= \sqrt{400 \times 144} = 20 \times 12 = 240$$

28. (3)  $\sqrt{0.000441}$

$$= \sqrt{0.021 \times 0.021}$$

$$= 0.021$$

29. (2) Expression =  $\frac{\sqrt{0.441}}{\sqrt{0.625}}$

$$= \sqrt{\frac{0.441}{0.625}} = \sqrt{\frac{441}{625}}$$

$$= \frac{21}{25} = 0.84$$

30. (3)  $\sqrt{\frac{0.342 \times 0.684}{0.000342 \times 0.000171}}$

$$= \sqrt{\frac{342 \times 684 \times 10^6}{342 \times 171}}$$

$$= \sqrt{4 \times 10^6} = 2 \times 10^3 = 2000$$

31. (1)  $\sqrt{0.00060516} = 0.0246$

32. (3)  $\sqrt{\frac{9.5 \times 0.085}{0.017 \times 0.019}} = \sqrt{2500}$   
= 50

33. (2)  $\sqrt{248 + \sqrt{52 + \sqrt{144}}}$

$$= \sqrt{248 + \sqrt{52 + 12}}$$

$$= \sqrt{248 + \sqrt{64}} = \sqrt{248 + 8}$$

$$\sqrt{256} = \pm 16$$

34. (4) ∵  $(102)^2 = 10404$

$$\Rightarrow \sqrt{10404} = 102$$

$$\sqrt{104.04} + \sqrt{1.0404} + \sqrt{0.010404}$$

$$= 10.2 + 1.02 + 0.102$$

$$= 11.322$$

35. (2)  $\sqrt{0.00004761} = \sqrt{\frac{4761}{10^8}}$

$$= \sqrt{\frac{3 \times 3 \times 23 \times 23}{10^4 \times 10^4}}$$

$$= \frac{69}{10^4} = 0.0069$$

36. (1)  $\sqrt{2} = 1.414$  (Given)

Now,

$$\frac{\sqrt{2} - 1}{\sqrt{2} + 1} = \frac{(\sqrt{2} - 1)(\sqrt{2} - 1)}{(\sqrt{2} + 1)(\sqrt{2} - 1)}$$

$$= \frac{(\sqrt{2} - 1)^2}{2 - 1} = (\sqrt{2} - 1)^2$$

$$= 2 + 1 - 2\sqrt{2}$$

$$= 3 - 2\sqrt{2}$$

$$= 3 - 2 \times 1.44$$

$$= 3 - 2.828$$

$$= 0.172$$

37. (2)  $\sqrt{\frac{0.00001225}{0.00005329}}$

$$= \sqrt{\frac{1225}{\frac{10^8}{5329}}} = \sqrt{\frac{1225}{5329}} = \frac{35}{73}$$

38. (2)  $0.\overline{4} = \frac{4}{9}$

$$\therefore \sqrt{\frac{4}{9}} = \frac{2}{3} = \frac{2 \times 3}{3 \times 3} = \frac{6}{9} = 0.\overline{6}$$

39. (2) Given expression

$$= \frac{\left(3\frac{1}{4}\right)^4 - \left(4\frac{1}{3}\right)^4}{\left(3\frac{1}{4}\right)^2 - \left(4\frac{1}{3}\right)^2}$$

$$= \frac{\left[\left(3\frac{1}{4}\right)^2 + \left(4\frac{1}{3}\right)^2\right] \left[\left(3\frac{1}{4}\right)^2 - \left(4\frac{1}{3}\right)^2\right]}{\left(3\frac{1}{4}\right)^2 - \left(4\frac{1}{3}\right)^2}$$

[∵  $a^2 - b^2 = (a + b)(a - b)$ ]

$$= \left(3\frac{1}{4}\right)^2 + \left(4\frac{1}{3}\right)^2 = \left(\frac{13}{4}\right)^2 + \left(\frac{13}{3}\right)^2$$

$$= \frac{169}{16} + \frac{169}{9} = 169\left(\frac{1}{16} + \frac{1}{9}\right)$$

$$= 169\left(\frac{9+16}{144}\right) = \frac{169 \times 25}{144}$$

∴ Required answer

$$= \sqrt{\frac{169 \times 25}{144}} = \frac{13 \times 5}{12} = \frac{65}{12} = 5\frac{5}{12}$$

40. (2) Expression =  $0.6 \times 0.6 \times 0.6 + 0.4 \times 0.4 \times 0.4 + 3 \times 0.6 \times 0.4$   
 $(0.6 + 0.4) = (0.6+0.4)^3 = 1$

∴ Required square root = 1

41. (2)  $\sqrt{\frac{0.49}{0.25}} + \sqrt{\frac{0.81}{0.36}}$

$$= \frac{0.7}{0.5} + \frac{0.9}{0.6} = \frac{42+45}{30} = \frac{87}{30}$$

$$= \frac{29}{10} = 2\frac{9}{10}$$

42. (4)  $\sqrt{x} \div \sqrt{441} = 0.02$

$$\Rightarrow \sqrt{x} = 0.02 \times 21$$

$$\Rightarrow x = 0.1764$$

43. (3) ? =  $\sqrt{4 + \sqrt{44 + 100}}$

$$= \sqrt{4 + \sqrt{144}} = \sqrt{4 + 12} = 4$$

44. (4)  $\sqrt{0.00005746} = \sqrt{5746 \times 10^{-8}}$   
=  $75.8 \times 10^{-4} = 0.00758$

45. (2)

$$\sqrt{(0.798)^2 + 0.404 \times 0.798 + (0.202)^2} + 1$$

$$= \sqrt{(0.798)^2 + 2 \times 0.798 \times 0.202 + (0.202)^2} + 1$$

$$= \sqrt{(0.798 + 0.202)^2} + 1$$

$$= \sqrt{(1.000)^2} + 1 = 1 + 1 = 2$$

46. (3)  $\sqrt{11.981 + 7\sqrt{1.2996}}$

$$= \sqrt{11.981 + 7 \times 1.14}$$

$$= \sqrt{11.981 + 7.98}$$

$$= \sqrt{19.961}$$

$$= 4.467 \approx 4.5$$

47. (3) Expression

$$= 4\sqrt{2} - 8\sqrt{2} + 5\sqrt{2}$$

$$= \sqrt{2}(4 - 8 + 5) = \sqrt{2}$$

$$= 1.414$$

48. (4)

$$(7 + 3\sqrt{5})(7 - 3\sqrt{5}) = (7)^2 - (3\sqrt{5})^2$$

$$= 49 - 45 = 4$$

∴ Required square root

$$= \sqrt{4} = 2$$

**49.** (3) Expression

$$\begin{aligned} &= \sqrt{400} + \sqrt{0.0400} + \sqrt{0.000004} \\ &= 20 + 0.2 + 0.002 \\ &= 20.202 \end{aligned}$$

**50.** (3) Expression

$$\begin{aligned} &= \sqrt{192} - \frac{1}{2}\sqrt{48} - \sqrt{75} \\ &= \sqrt{64 \times 3} - \frac{1}{2}\sqrt{16 \times 3} - \sqrt{25 \times 3} \end{aligned}$$

$$= 8\sqrt{3} - \frac{1}{2} \times 4\sqrt{3} - 5\sqrt{3}$$

$$= 8\sqrt{3} - 2\sqrt{3} - 5\sqrt{3}$$

$$= \sqrt{3} = 1.7321$$

$$51. (3) \sqrt{\frac{48.4}{0.289}} = \sqrt{\frac{484}{2.89}}$$

$$= \frac{22}{1.7} = \frac{220}{17} = 12\frac{16}{17}$$

$$52. (2) 10^2 + 11^2 + 12^2 \\ = 100 + 121 + 144 = 365 \\ \therefore \text{Required sum} = 10+11+12 = 33$$

**53.** (3)  $\sqrt{4096} = 64$

$$\therefore \sqrt{40.96} = 6.4 \text{ and}$$

$$\sqrt{0.4096} = 0.64 \text{ etc.}$$

$$\therefore \text{Expression} \\ = 6.4 + 0.64 + 0.064 + 0.0064 \\ = 7.1104$$

**54.** (2)  $\sqrt{13} = 3.6$  and  $\sqrt{130} = 11.4$

$$\therefore \sqrt{13} + \sqrt{1300} + \sqrt{0.013}$$

$$= \sqrt{\frac{130}{100}} + \sqrt{13 \times 100} + \sqrt{\frac{130}{10000}}$$

$$= \frac{11.4}{10} + 3.6 \times 10 + \frac{11.4}{100}$$

$$= 1.14 + 36 + 0.114$$

$$= 37.254$$

**55.** (1) Expression

$$= \sqrt{5 + \sqrt{11 + \sqrt{19 + \sqrt{29 + 7}}}}$$

$$= \sqrt{5 + \sqrt{11 + \sqrt{19 + 6}}}$$

$$= \sqrt{5 + \sqrt{11 + 5}}$$

$$= \sqrt{5 + 4} = \sqrt{9} = 3$$

$$56. (4) \sqrt{110\frac{1}{4}} = \sqrt{\frac{441}{4}} = \sqrt{\frac{21 \times 21}{2 \times 2}}$$

$$= \frac{21}{2} = 10\frac{1}{2} = 10.5$$

**57.** (1) Expression

$$= \sqrt{8 + \sqrt{57 + \sqrt{38 + \sqrt{108 + \sqrt{169}}}}}$$

$$= \sqrt{8 + \sqrt{57 + \sqrt{38 + \sqrt{108 + 13}}}}$$

$$= \sqrt{8 + \sqrt{57 + \sqrt{38 + \sqrt{121}}}}$$

$$= \sqrt{8 + \sqrt{57 + \sqrt{38 + 11}}}$$

$$= \sqrt{8 + \sqrt{57 + \sqrt{49}}}$$

$$= \sqrt{8 + \sqrt{57 + 7}} = \sqrt{8 + \sqrt{64}}$$

$$= \sqrt{8 + 8} = \sqrt{16} = 4$$

**58.** (3)  $(10.15)^2 = 103.0225$

$$\Rightarrow (1.015)^2 = 1.030225 \\ \text{and } (101.5)^2 = 10302.25$$

$$\therefore \sqrt{1.030225} + \sqrt{10302.25}$$

$$= \sqrt{(1.015)^2} + \sqrt{(101.5)^2}$$

$$= 1.015 + 101.5$$

$$= 102.515$$

**59.** (3) The number of digits in  $625686734489$  is 12.

$\therefore$  Number of digits in its square root = 6

$$\text{i.e., } \sqrt{625686734489} = 791003.625$$

**60.** (2)  $\sqrt{841} = 29$

$$\frac{\sqrt{841}}{10000} = \frac{29}{10000}$$

$$\Rightarrow \frac{\sqrt{841}}{100000000} = \frac{29}{10000}$$

$$\therefore \sqrt{0.00000841} = 0.0029$$

**61.** (3) Expression

$$= \sqrt{\frac{0.324 \times 0.081 \times 4.624}{1.5625 \times 0.0289 \times 72.9 \times 64}}$$

$$= \sqrt{\frac{324 \times 81 \times 4624}{15625 \times 289 \times 729 \times 64}}$$

$$= \frac{18 \times 9 \times 68}{125 \times 17 \times 27 \times 8} = 0.024$$

**62.** (3)  $\sqrt{0.25 \times 2.25} = 0.5 \times 1.5$

$$= 0.75$$

**63.** (2)  $\sqrt{64} - \sqrt{36} = 8 - 6 = 2$

**64.** (2)  $\sqrt{18225} = 135$

$$\therefore \sqrt{182.25} = 13.5;$$

$$\sqrt{1.8225} = 1.35;$$

$$\sqrt{0.018225} = 0.135$$

$$\therefore \text{Expression} = 135 + 13.5 + 1.35 + 0.135$$

$$= 149.985$$

$$65. (2) 21\frac{51}{169} = \frac{21 \times 169 + 51}{169}$$

$$= \frac{3600}{169}$$

$$\therefore \sqrt{21\frac{51}{169}} = \sqrt{\frac{3600}{169}} = \frac{60}{13} = 4\frac{8}{13}$$

**66.** (2)  $(1101)^2 = 1212201$

$$\Rightarrow 1101 = \sqrt{1212201}$$

$$= \sqrt{1212201}$$

$$= \sqrt{\frac{1212201}{10000}} = \frac{1101}{100} = 11.01$$

**67.** (1) Expression

$$= \sqrt{\frac{0.064 \times 0.256 \times 15.625}{0.025 \times 0.625 \times 4.096}}$$

$$= \sqrt{\frac{64 \times 256 \times 15625}{25 \times 625 \times 4096}}$$

$$= \frac{8 \times 16 \times 125}{5 \times 25 \times 64} = 2$$

**68.** (3)

$$\sqrt{19.36} + \sqrt{0.1936} + \sqrt{0.001936}$$

$$+ \sqrt{0.00001936}$$

$$= 4.4 + 0.44 + 0.044 + 0.0044$$

$$= 4.8884$$

**69.** (2) Let the numbers be  $x$  and  $y$  where  $x > y$

$$\therefore x^2 - y^2 = 45$$

$$\Rightarrow (x+y)(x-y) = 45$$

$$\text{Now, } 45 = 5 \times 9$$

$$= 15 \times 3 = 45 \times 1$$

$$\therefore \text{Number of pairs} = 3$$

**70.** (3) Expression =  $\frac{\sqrt{24} + \sqrt{216}}{\sqrt{96}}$

$$= \frac{2\sqrt{6} + 6\sqrt{6}}{4\sqrt{6}} = \frac{8\sqrt{6}}{4\sqrt{6}} = 2$$

**71.** (4) Expression

$$\begin{aligned}
 &= \sqrt{3 \frac{33}{64}} \div \sqrt{9 \frac{1}{7}} \times 2 \sqrt{3 \frac{1}{9}} \\
 &= \sqrt{\frac{225}{64}} \div \sqrt{\frac{64}{7}} \times 2 \sqrt{\frac{28}{9}} \\
 &= \sqrt{\frac{225}{64} \times \frac{7}{64} \times \frac{28}{9}} \times 2 \\
 &= \frac{5 \times 7}{8 \times 4} \times 2 = \frac{35}{16} = 2 \frac{3}{16}
 \end{aligned}$$

**72.** (2) Expression

$$\begin{aligned}
 &= \frac{\sqrt{32} + \sqrt{48}}{\sqrt{8} + \sqrt{12}} \\
 &= \frac{4\sqrt{2} + 4\sqrt{3}}{2\sqrt{2} + 2\sqrt{3}} = \frac{4(\sqrt{2} + \sqrt{3})}{2(\sqrt{2} + \sqrt{3})} = 2
 \end{aligned}$$

**73.** (1) Number of digits in

$$62478078 = 8$$

∴ Number of digits in its square root = 4

$$\Rightarrow \sqrt{62478078} \approx 7904$$

$$\Rightarrow \sqrt{62473216} = 7904$$

**74.** (4) For  $n^r - tn + \frac{1}{4}$  to be a perfect square,  
 $r = 2$  and  $t = \pm 1$

$$\begin{aligned}
 \left[ n^2 - n + \frac{1}{4} \right] &= n^2 - 2.n \cdot \frac{1}{2} + \frac{1}{4} \\
 &= \left( n - \frac{1}{2} \right)^2
 \end{aligned}$$

$$\begin{aligned}
 n^2 + n + \frac{1}{4} &= n^2 + 2.n \cdot \frac{1}{2} + \frac{1}{4} \\
 &= \left( n + \frac{1}{2} \right)^2
 \end{aligned}$$

**75.** (4)  $33 - 4 \sqrt{35}$

$$= 33 - 2 \times 2 \sqrt{5 \times 7}$$

$$= 33 - 2 \times 2 \sqrt{7} \times \sqrt{5}$$

$$= 28 + 5 - 2 \times 2 \sqrt{7} \times \sqrt{5}$$

$$\begin{aligned}
 &= (2\sqrt{7})^2 + (\sqrt{5})^2 - 2 \times 2\sqrt{7} \times \sqrt{5} \\
 &= (2\sqrt{7} - \sqrt{5})^2
 \end{aligned}$$

$$\therefore \sqrt{33 - 4\sqrt{35}}$$

$$= \sqrt{(2\sqrt{7} - \sqrt{5})^2}$$

$$= \pm(2\sqrt{7} - \sqrt{5})$$

**76.** (3) Expression

$$\begin{aligned}
 &= \sqrt{156.25} + \sqrt{0.0081} - \sqrt{0.0361} \\
 &= 12.5 + 0.09 - 0.19 = 12.4
 \end{aligned}$$

**77.** (4)  $\sqrt{24010000} = 4900$

$$\text{Again, } \sqrt{4900} = 70$$

$$\therefore \sqrt[4]{24010000} = 70$$

**78.** (2)  $\sqrt{15876} = 126$

The digit at the unit's place is 6.

$$\begin{array}{r|rr|l}
 1 & 1 & \overline{58} & 76 \mid 126 \\
 1 & 1 & & \\
 \hline
 22 & 58 & & \\
 2 & 44 & & \\
 \hline
 246 & 1476 & & \\
 6 & 1476 & & \\
 \hline
 252 & & & \times
 \end{array}$$

**79.** (1) Unit's digit in  $(1570)^2 = 0$

Unit's digit in  $(1571)^2 = 1$

Unit's digit in  $(1572)^2 = 4$

Unit's digit in  $(1573)^2 = 9$

∴ Required unit's digit

= Unit's digit in  $(0+1+4+9) = 4$

**80.** (3) The smallest 4-digit number = 1000

The smallest 4 digit perfect square number =  $2^{10} = 1024$

**81.** (1)  $\begin{array}{r|rr|l} 8 & 68 & 06 & 21 \mid 824 \\ 8 & 64 & & \\ \hline 162 & 406 & & \\ 2 & 324 & & \\ \hline 1644 & 8221 & & \\ & 6576 & & \\ & 1645 & & \end{array}$

$\therefore (824)^2 < 680621 < (825)^2$

∴ Required number

$$= [(825)^2 - 680621] = 4$$

**82.** (4)  $392 = 2 \times 2 \times 2 \times 7 \times 7 = 2^2 \times 7^2 \times 2$

Clearly, when 392 is multiplied by 2, the product is a perfect square.

**83.** (3)  $47 \times 47 = 2209$

Clearly, 6 should be added to 2203 to get a perfect square.

**84.** (4) Perfect square numbers between 50 and 1000 start from 64 to 961 i.e.,  $(8)^2$  to  $(31)^2$   
 $\therefore$  The required number  
 $= (31 - 8) + 1 = 24$

**85.** (2)  $\begin{array}{r|rr|l} 9 & 89 & 58 \mid 94 \\ 9 & 81 & & \\ \hline 184 & \times 858 & & \\ 4 & 736 & & \\ \hline 188 & 122 & & \end{array}$

$$\text{Now, } 95 \times 95 = 9025$$

$$\therefore \text{Required number} = 9025 - 8958 = 67$$

**86.** (3) Largest 5-digit number = 99999

Now,

$$\begin{array}{r|rr|l}
 3 & 9 & 9 & 9 & 9 \mid 316 \\
 3 & 9 & & & \\
 \hline
 61 & \times 99 & & & \\
 1 & 62 & & & \\
 \hline
 626 & 3799 & & & \\
 6 & 3756 & & & \\
 \hline
 632 & & & \times 43 &
 \end{array}$$

$$\therefore \text{Required number} = 99999 - 43 = 99856$$

**87.** (3)  $11^2 = 121, 12^2 = 144, 13^2 = 169, 14^2 = 196, 15^2 = 225, 16^2 = 256, 17^2 = 289$

So, total perfect squares = 7

**88.** (3)  $31^2 = 961$

$$32^2 = 1024$$

$$\therefore \text{Required number} = 1000 - 961 = 39$$

**89.** (3)  $(31)^2 < 1000 < 32^2$

$$32 \times 32 = 1024$$

$$\therefore \text{Required number} = 1024 - 1000 = 24$$

**90.** (3)  $99 \times 99 = 9801$

**91.** (1)  $a^2 - 2ab + b^2 = (a - b)^2$   
 $\therefore 16a^2 - 12a$

$$= (4a)^2 - 2 \times 4a \times \frac{3}{2}$$

Hence, on adding  $\left(\frac{3}{2}\right)^2 = \frac{9}{4}$ , expression will be a perfect square.

**92.** (3)  $p = q + 5$

$$\Rightarrow p - q = 5$$

$$p^2 + q^2 = 55$$

$$\therefore (p - q)^2 + 2pq = 55$$

$$\Rightarrow 25 + 2pq = 55$$

$$\Rightarrow 2pq = 30$$

$$\Rightarrow pq = 15$$

**93.** (3) Since the numbers between – 10 and 10 will be single digit and the numbers below 100 will be either one digit or two digit. We know that the square root of one or two digit number is always single digit number. Therefore, required answer is option (3).

**94.** (1) Let the two numbers be A and B. Then,  $A + B = 22$  and  $A^2 + B^2 = 404$ . We know that  $(A + B)^2 = A^2 + B^2 + 2AB$  or  $(22)^2 = 404 + 2AB$  or  $484 = 404 + 2AB$  or  $2AB = 80$  or  $AB = 40$ .

∴ The product of the two numbers = 40

**95.** (4) According to question,

$$\frac{1}{3} \times \sqrt{x} = 0.001 \\ \Rightarrow \sqrt{x} = 0.003 \Rightarrow x = 0.000009$$

**96.** (3) Let the number be x. According to the question

$$\frac{3}{5} \text{ of } x^2 = 126.15 \\ \Rightarrow x^2 = \frac{126.15 \times 5}{3} \\ \Rightarrow x^2 = 210.25 \\ \therefore x = \sqrt{210.25} = 14.5$$

**97.** (1) Multiples of 11 whose square root are whole number

$$\text{First} = 11 \times 11 = 121$$

$$\text{Second} = 11 \times 11 \times 4 = 484$$

**98.** (3) Let the number be x. Then,  $x^2 = (75.15)^2 - (60.12)^2$

$$= (75.15 + 60.12)(75.15 - 60.12) \\ = 135.27 \times 15.03$$

$$= 2033.1081$$

$$\Rightarrow x = \sqrt{2033.1081} \\ = 45.09$$

**99.** (2) Let the required number be x. Then,

$$x^2 + 5^2 = 386$$

$$\Rightarrow x^2 = 386 - 25$$

$$\Rightarrow x^2 = 361$$

$$\Rightarrow x = \sqrt{361} = 19$$

**100.** (1) Let the required number be x. As per given information,

$$x^2 = (975)^2 - (585)^2$$

$$\Rightarrow x^2 = (975 + 585)(975 - 585)$$

$$\Rightarrow x^2 = 1560 \times 390$$

$$\Rightarrow x = \sqrt{1560 \times 390}$$

$$= \sqrt{13 \times 12 \times 3 \times 13 \times 10 \times 10}$$

$$= 780$$

**101.** (4) Let  $x + y = 20$  and

$$x - y = 8$$

$$\therefore (x + y)(x - y) = 20 \times 8$$

$$\Rightarrow x^2 - y^2 = 160$$

**102.** (3) Let the numbers be x and y.

Then,

$$x^2 + y^2 = 100 \quad \dots(i)$$

$$x^2 - y^2 = 28 \quad \dots(ii)$$

On adding,

$$2x^2 = 128$$

$$\Rightarrow x^2 = 64 \Rightarrow x = 8$$

From equation (i),

$$64 + y^2 = 100$$

$$\Rightarrow y^2 = 36 \Rightarrow y = 6$$

∴ Required sum

$$= 8 + 6 = 14$$

**103.** (3) Check through options

When  $x = 9$ ,

$$2x - 3 = 2 \times 9 - 3 = 15 < 17$$

**104.** (4)  $1 \times 2 \times 3 \times 4 = 24$

$$\Rightarrow 24 + 1 = 25 = 5^2;$$

$$2 \times 3 \times 4 \times 5 = 120$$

$$\Rightarrow 120 + 1 = 121 = 11^2$$

$$\therefore P = 1$$

**105.** (3) Expression

$$= \sqrt{\frac{8}{3}} = \sqrt{\frac{8 \times 3}{3 \times 3}} = \frac{\sqrt{24}}{3} \\ = \frac{4.898}{3} = 1.6326 \approx 1.633$$

**106.** (2) Let the number of boys and girls in the room be x and y respectively.

According to the question,

$$x^2 = y^2 + 28$$

$$\Rightarrow x^2 - y^2 = 28 \quad \dots(i)$$

and  $x = y + 2$

$$\Rightarrow x - y = 2 \quad \dots(ii)$$

On dividing equation (i) by equation (ii), we have

$$\frac{x^2 - y^2}{x - y} = \frac{28}{2}$$

$$\Rightarrow \frac{(x+y)(x-y)}{x-y} = 14$$

$$\Rightarrow x + y = 14$$

∴ Total number of boys and girls = 14

**107.** (4) From the given alternatives,

$$5^2 + 6^2 + 7^2 = 110$$

∴ The smallest number = 5

**108.** (3) 37 is a prime number.

$$\therefore 37 = 1 \times 37$$

∴ Required answer

$$= \sqrt{37 - 1} = \sqrt{36} = 6$$

**109.** (3) According to the question,  $= 68^2 - 32^2 = (68 + 32)(68 - 32)$

$$= 100 \times 36$$

$$= 3600 = (60)^2$$

**110.** (3)  $x^2 + x = 2450$

$$\Rightarrow x(x+1) = 2450 = 49 \times 50$$

$$\therefore x = 49$$

**111.** (4) Let the numbers be x and y and  $x > y$ .

$$\therefore xy = 45$$

$$\text{and } x - y = 4$$

$$\therefore x^2 + y^2 = (x - y)^2 + 2xy \\ = (4)^2 + 2 \times 45 = 16 + 90$$

$$= 106$$

**112.** (4)  $1008 = 4 \times 4 \times 3 \times 3 \times 7$

$$\therefore \frac{1008}{7} = (4 \times 3)^2 = (12)^2$$

**113.** (1) Obviously, 16 must be subtracted to make the result a perfect square.

$$\text{i.e. } 63520 - 16 = \sqrt{63504} = 252$$

**114.** (2) The given number has 6 decimal places.

Now,	1	326	18
	1	226	
	28	224	
	8	2	

i.e.  $326 - 2 = 324$  Which is a perfect square of 18.

Therefore, 0.000002 should be subtracted from 0.000326 to make it a perfect square of 0.018.

**115.** (4)  $5808 = 2 \times 2 \times 2 \times 2 \times 3 \times 11 \times 11 = 2^2 \times 2^2 \times 11^2 \times 3$

Therefore, when 5808 is multiplied by 3, then it will be perfect square number.

116.	2	20184
	2	10092
	2	5046
	3	2523
	29	841
		29

$$\therefore 20184 = 2 \times 2 \times 2 \times 3 \times 29 \times 29 = 2^2 \times 29^2 \times 2 \times 3.$$

∴ Required number  
=  $2 \times 3 = 6$

**117.** (1)  $41 \times 41 = 1681$

$42 \times 42 = 1764$

$\therefore$  Required answer  
 $= 1764 - 1728 = 36$

**118.** (1)  $a = 64$  and  $b = 289$

$\therefore \sqrt{a} = \sqrt{64} = 8$  and

$\sqrt{b} = \sqrt{289} = 17$

$$\therefore \left( \sqrt{\sqrt{a} + \sqrt{b}} - \sqrt{\sqrt{b} - \sqrt{a}} \right)^2$$

$$= (\sqrt{8+17} - \sqrt{17-8})^{\frac{1}{2}}$$

$$= (\sqrt{25} - \sqrt{9})^{\frac{1}{2}}$$

$$= (5-3)^{\frac{1}{2}} = (2)^{\frac{1}{2}}$$

**119.** (3)

2	6	4	0	0	9	253
2	4					
45	240					
5	225					
503	1509					
3	1509					
506	x					

$\therefore \sqrt{64009} = 253$

**120.** (2) Let the number of days of tour be  $x$ .

$\therefore$  Total expenditure  $= x^2$

$\therefore x^2 = 361 \Rightarrow x = \sqrt{361} = 19$

**121.** (2) Expression  $= \sqrt{10^{-6} \times 0.25}$

$$= \sqrt{\frac{0.25}{10^6}} = \sqrt{\frac{25}{10^6 \times 10^2}}$$

$$= \sqrt{\frac{25}{10^8}} = \frac{5}{10^4} = 0.0005$$

**122.** (4)  $\frac{3\sqrt{2}}{\sqrt{6} + \sqrt{3}}$

$$= \frac{3\sqrt{2}(\sqrt{6} - \sqrt{3})}{(\sqrt{6} + \sqrt{3})(\sqrt{6} - \sqrt{3})}$$

$$= \frac{3\sqrt{2}(\sqrt{6} - \sqrt{3})}{6 - 3}$$

$$= \sqrt{2} (\sqrt{6} - \sqrt{3}) = \sqrt{12} - \sqrt{6}$$

$$= 2 \sqrt{3} - \sqrt{6}$$

$$\frac{4\sqrt{3}}{\sqrt{6} + \sqrt{2}}$$

$$= \frac{4\sqrt{3}(\sqrt{6} - \sqrt{2})}{(\sqrt{6} + \sqrt{2})(\sqrt{6} - \sqrt{2})}$$

$$= \frac{4\sqrt{3}(\sqrt{6} - \sqrt{2})}{6 - 2}$$

$$= \sqrt{3} (\sqrt{6} - \sqrt{2}) = \sqrt{18} - \sqrt{6}$$

$$= 3\sqrt{2} - \sqrt{6}$$

$$\frac{\sqrt{6}}{\sqrt{3} + \sqrt{2}}$$

$$= \frac{\sqrt{6}(\sqrt{3} - \sqrt{2})}{(\sqrt{3} + \sqrt{2})(\sqrt{3} - \sqrt{2})}$$

$$= \frac{\sqrt{18} - \sqrt{12}}{3 - 2}$$

$$= 3\sqrt{2} - 2\sqrt{3}$$

$\therefore$  Expression

$$= 2\sqrt{3} - \sqrt{6} - (3\sqrt{2} - \sqrt{6}) + 3\sqrt{2} - 2\sqrt{3}$$

$$= 2\sqrt{3} - \sqrt{6} - 3\sqrt{2} + \sqrt{6} + 3\sqrt{2} - 2\sqrt{3} = 0$$

**123.** (2) Expression  $= \frac{4 - \sqrt{0.04}}{4 + \sqrt{0.4}}$

$$= \frac{4 - 0.2}{4 + 0.6}$$

$$= \frac{3.8}{4.6} = \frac{38}{46} = \frac{19}{23}$$

$$\approx 0.83 \approx 0.8$$

**124.** (2)  $\sqrt{0.05 \times 0.5 \times a}$

$$= 0.5 \times 0.05 \times \sqrt{b}$$

On squaring both sides,

$$0.05 \times 0.5 \times a = 0.5 \times 0.5 \times 0.05 \times 0.05 \times b$$

$$\Rightarrow a = 0.5 \times 0.05b$$

$$\Rightarrow \frac{a}{b} = 0.5 \times 0.05 = 0.025$$

**125.** (1) Number of students in the last

$$\text{row} = \sqrt{1369} = 37$$

**Illustration :**

3	1	3	6	9	37
3		9			
67		469			
7		469			
74	x				

**126.** (1)  $\sqrt{5} = 2.24$

$$\sqrt{3} = 1.73$$

$$\sqrt{6} = 2.45$$

$$\sqrt{2} = 1.41$$

$$\therefore \sqrt{5} + \sqrt{3} = 2.24 + 1.73$$

$$= 3.97$$

$$\sqrt{6} + \sqrt{2} = 2.45 + 1.41 = 3.86$$

Clearly,  $3.97 > 3.86$

**127.** (4)

2	20184
2	10092
2	5046
3	2523
29	841
	29

$$\therefore 20184 = 2 \times 2 \times 2 \times 3 \times 29 \times 29 = 2^2 \times 29^2 \times 2 \times 3$$

$\therefore$  For making it a perfect square, 20184 should be multiplied by 2  $\times 3 = 6$

$$20184 \times 6 = 121104;$$

$$\sqrt{121104} = 348$$

**128.** (4)

2	1008
2	504
2	252
2	126
3	63
3	21
	7

$$\therefore 1008$$

$$= 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 7$$

$$= 2^2 \times 2^2 \times 3^2 \times 7$$

$\therefore$  Required answer = 7

- 129.** (3) Let the numbers be  $x$  and  $y$  where  $x > y$ .

According to the question,

$$x + y = 37$$

and

$$x^2 - y^2 = 185$$

$$\Rightarrow (x+y)(x-y) = 185$$

$$\Rightarrow 37(x-y) = 185$$

$$\Rightarrow x-y = \frac{185}{37} = 5$$

**130.** (1)  $\begin{array}{r|rr} 1 & 36\overline{5}\overline{6}2 & |191 \\ \hline 1 & 265 & \\ 29 & 261 & \\ \hline 9 & 462 & \\ 381 & 381 & \\ \hline 1 & 81 & \end{array}$

∴ Number of armies left = 81

**131.** (3)  $\frac{2+\sqrt{3}}{2} = \frac{2(2+\sqrt{3})}{4}$

$$= \frac{4+2\sqrt{3}}{4} = \frac{3+1+2\sqrt{3}}{4}$$

$$= \frac{(\sqrt{3})^2 + (1)^2 + 2 \times \sqrt{3} \times 1}{4}$$

$$= \left( \frac{\sqrt{3}+1}{2} \right)^2$$

$$\therefore \sqrt{\frac{2+\sqrt{3}}{2}} = \pm \frac{\sqrt{3}+1}{2}$$

**132.** (3)  $11^2 = 121$

$$111^2 = 12321$$

$$1111^2 = 1234321$$

$$11111^2 = 123454321$$

**133.** (4)  $\begin{array}{r|rr} 5 & 59535 \\ \hline 3 & 11907 \\ 3 & 3969 \\ 3 & 1323 \\ 3 & 441 \\ 3 & 147 \\ 7 & 49 \\ \hline & 7 \end{array}$

$$\therefore 59535 = 3 \times 3 \times 3 \times 3 \times 7^2 \times 3 \times 5$$

$$= 3^2 \times 3^2 \times 7^2 \times 3 \times 5$$

∴ According to the question,

$$x = 3 \times 5 = 15$$

$$\therefore \text{Sum of digits} = 1 + 5 = 6$$

**134.** (2)  $\begin{array}{r|rrr} 2 & 6 & 60 & 49 & |257 \\ \hline 2 & 4 & & & \\ 45 & 260 & & & \\ 5 & 225 & & & \\ \hline 507 & 3549 & & & \\ 7 & 3549 & & & \\ \hline 514 & & x & & \end{array}$

$$\therefore \sqrt{66049} = 257$$

∴ Unit place digit = 7

**135.** (4)  $\sqrt{0.000441} = \sqrt{\frac{441}{1000000}}$

$$= \frac{21}{1000} = 0.021$$

**136.** (1) Required sum =  $121 + 144 + 169 + 196 + 225 + 256 + 289 = 1400$

**137.** (2)  $\sqrt{32146} > 179$

$$179 \times 179 = 32041$$

$$\therefore \text{Required answer} = 32146 - 32041 = 105$$

**138.** (1)  $\begin{array}{r|rrr} 7 & 54\overline{16} & *6 & |736 \\ \hline 7 & 49 & & \\ 143 & 516 & & \\ 3 & 429 & & \\ \hline 1466 & 87*6 & & \end{array}$

$$\therefore 1466 \times 6 = 8796$$

$$\therefore * = 9$$

**139.** (2) Number of boys =  $\sqrt{12544} = 112$

Illustration :

$$\begin{array}{r|rr} 1 & 1\overline{25}\overline{44} & |112 \\ \hline 1 & 1 & \\ 21 & \times 25 & \\ \hline 222 & 444 & \\ 2 & 444 & \\ \hline 224 & & x \end{array}$$

- 140.** (2) Let three positive integers be  $x, y$  and  $z$ .

According to the question,

$$x + y + z = 18 \quad \dots \dots \text{(i)}$$

$$xyz = 162 \quad \dots \dots \text{(ii)}$$

$$\text{and } x + y = z \quad \dots \dots \text{(iii)}$$

From equation (i),

$$z + z = 18 \Rightarrow 2z = 18 \Rightarrow z = 9$$

$$\therefore xyz = 162$$

$$\Rightarrow xy \times 9 = 162$$

$$\Rightarrow xy = \frac{162}{9} = 18 \quad \dots \dots \text{(iv)}$$

$$\therefore (x-y)^2 = (x+y)^2 - 4xy$$

$$= (9)^2 - 4 \times 18$$

$$= 81 - 72 = 9$$

$$\therefore x - y = 3$$

$$\therefore x + y + x - y = 9 + 3$$

$$\Rightarrow 2x = 12 \Rightarrow x = 6$$

$$\therefore x + y + z = 18$$

$$\Rightarrow 6 + y + 9 = 18$$

$$\Rightarrow y = 18 - 15 = 3$$

$$\therefore x^2 + y^2 + z^2$$

$$= (6)^2 + (3)^2 + (9)^2$$

$$= 36 + 9 + 81 = 126$$

- 141.** (3)  $x + y + z = 50 ; xyz = 3750$

$$\therefore \frac{1}{x} + \frac{1}{y} + \frac{1}{z} = \frac{yz + zx + xy}{xyz}$$

$$= \frac{31}{150}$$

$$\Rightarrow xy + yz + zx = \frac{31}{150} xyz$$

$$= \frac{31}{150} \times 3750 = 775$$

$$\therefore (x+y+z)^2 = x^2 + y^2 + z^2 + 2(xy + yz + zx)$$

$$\Rightarrow (50)^2 = x^2 + y^2 + z^2 + 2 \times 775$$

$$\Rightarrow 2500 = x^2 + y^2 + z^2 + 1550$$

$$\Rightarrow x^2 + y^2 + z^2 = 2500 - 1550$$

$$= 950$$

- 142.** (2) Largest 6-digit number = 999999

$$\begin{array}{r|rr} 9 & 9\overline{99999} & |999 \\ 9 & 81 & \\ \hline 189 & 1899 & \\ 9 & 1701 & \\ \hline 1989 & 19899 & \\ 9 & 17901 & \\ \hline 1998 & 17901 & \\ & 1998 & \end{array}$$

∴ Required perfect square number = 999999 - 1998

$$= 998001$$

- 143.** (3) Remainder on dividing  $3^2 = 9$  by 6 = 3

Remainder on dividing  $4^2 = 16$  by 6 = 4

Remainder on dividing  $5^2 = 25$  by 6 = 1

## SIMPLIFICATION

**144.** (3)

1	18265	135
1	1	
23	$\times 82$	
3	69	
265	1365	
5	1325	
		40

$\therefore$  Required answer = 40

- 145.** (3) Let the two real numbers be  $x$  and  $y$ .

According to the question,

$$x^2 + y^2 = 41$$

$$x + y = 9$$

$$\therefore (x + y)^2 = x^2 + y^2 + 2xy$$

$$\Rightarrow 81 = 41 + 2xy$$

$$\Rightarrow 2xy = 81 - 41 = 40$$

$$\Rightarrow xy = \frac{40}{2} = 20$$

$$\therefore x^3 + y^3 = (x + y)^3 - 3xy(x + y) \\ = (9)^3 - 3 \times 20(9) \\ = 729 - 540 = 189$$

- 146.** (1) Let the smaller number be  $x$ .

$$\therefore$$
 Larger number =  $2x$

According to the question,

$$2x^2 = 2048$$

$$\Rightarrow x^2 = \frac{2048}{2} = 1024$$

$$\therefore x = \sqrt{1024} = 32$$

- 147.** (4) Let the number ( $n$ ) be  $6m + 3$  where  $m$  = quotient.

On squaring both sides,

$$n^2 = (6m + 3)^2$$

$$= 36m^2 + 36m + 3^2$$

$$\therefore$$
 Required remainder =  $3^2$

$$\therefore$$
 Remainder on dividing 9 by 6 = 3

- 148.** (4) Number of members in the club =  $x$  (let)

According to the question,

$$x^2 + \frac{x^2}{100} = 2525$$

$$\Rightarrow \frac{100x^2 + x^2}{100} = 2525$$

$$\Rightarrow 101x^2 = 252500$$

$$\Rightarrow x^2 = \frac{252500}{101} = 2500$$

$$\Rightarrow x = \sqrt{2500} = 50$$

- 149.** (1) Let the positive numbers be  $x$ ,  $y$  and  $z$  (respectively).

$$\therefore x^2 + y^2 + z^2 = 323 \quad \dots \text{(i)}$$

$$\text{and, } x^2 + y^2 = 2z \quad \dots \text{(ii)}$$

$$\therefore z^2 + 2z = 323$$

$$\Rightarrow z^2 + 2z - 323 = 0$$

$$\Rightarrow z^2 + 19z - 17z - 323 = 0$$

$$\Rightarrow z(z + 19) - 17(z + 19) = 0$$

$$\Rightarrow (z - 17)(z + 19) = 0$$

$$\Rightarrow z = 17 \text{ because } z \neq -19$$

$$\therefore x^2 + y^2 = 2 \times 17 = 34$$

$$= 3^2 + 5^2$$

$$\therefore xyz = 3 \times 5 \times 17 = 255$$

- 150.** (2) Let the numbers be  $a$  and  $b$  where  $a > b$ .

According to the question,

$$a - b = 9 \dots \text{(i)}$$

$$\text{and } a^2 - b^2 = 207$$

$$\Rightarrow (a + b)(a - b) = 207$$

$$\Rightarrow 9(a + b) = 207$$

$$\Rightarrow a + b = \frac{207}{9} = 23 \dots \text{(ii)}$$

On adding equations (i) and (ii),

$$a + b + a - b = 23 + 9$$

$$\Rightarrow 2a = 32 \Rightarrow a = 16$$

$$\therefore a - b = 9$$

$$\Rightarrow 16 - b = 9$$

$$\Rightarrow b = 16 - 9 = 7$$

- 151.** (4)

2	63520	252
2	4	
45	235	
5	225	
502	1020	
2	1004	
504	16	

Now,  $63520 - 16 = 63504$

$$\text{and } \sqrt{63504} = 252$$

$\therefore$  Required number = 16

- 152.** (1) The smallest 6-digit number = 100000

3	100000	316
3	9	
61	100	
1	61	
626	3900	
6	3756	
632	144	

Clearly,

$$316 < \sqrt{100000} < 317$$

$$317 \times 317 = 100489$$

$\therefore$  Required number = 100489

- 153.** (2) Let the numbers be  $x$  and  $y$  where  $x > y$ .

$$\therefore x + y = 80$$

$$x - y = 20$$

$$\therefore (x + y)(x - y) = 80 \times 20$$

$$\Rightarrow x^2 - y^2 = 1600$$

- 154.** (1) Suppose, the positive number be  $x$ .

According to the question,

$$x^2 - 21x = 100$$

$$\Rightarrow x^2 - 21x - 100 = 0$$

$$\Rightarrow x^2 - 25x + 4x - 100 = 0$$

$$\Rightarrow x(x - 25) + 4(x - 25) = 0$$

$$\Rightarrow (x - 25)(x + 4) = 0$$

$$\Rightarrow x = 25 \text{ because } x \neq -4$$

- 155.** (3) Let's find the square root of 36562.

1	3 65 62	191
1	1	
29	265	
9	261	
381	462	
1	381	
382	81	

Clearly, the remaining army men = 81

- 156.** (3)

1	1 68 00	129
1	1	
22	x68	
2	44	
249	2400	
9	2241	
258	159	⇒ Remainder

$\therefore$  Required number = 159

$$16800 - 159 = 16641$$

$$\text{and } \sqrt{16641} = 129$$

### TYPE-IV

- 1.** (1) Here,  $22 - 15 - 7 = 0$

We know that

$$a^2 + b^3 + c^3 = 3abc,$$

$$\text{if } a + b + c = 0$$

$$\therefore (22)^3 + (-15)^3 + (-7)^3$$

$$= 3 \times 22 \times (-15) (-7) = 6930$$

- 2.** (2) On simplification,

$$\text{Expression} = \frac{2}{4} \times \frac{7}{10} \times 5$$

$$= \frac{7}{4} = 1\frac{3}{4}$$

$$3. (2) \sqrt[3]{\frac{72.9}{0.4096}} = \sqrt[3]{\frac{72900}{4096}}$$

$$= \sqrt[3]{\frac{(90)^3}{(16)^3}} = \frac{90}{16} = \frac{45}{8} = 5.625$$

- 4.** (4)  $(5.5)^3 - (4.5)^3$

$$= (5.5 - 4.5)^3 + 3 \times 5.5 \times 4.5 (5.5 - 4.5)$$

$$= (1)^3 + 74.25 (1)$$

$$= 1 + 74.25 = 75.25$$

$$5. (4) \sqrt[3]{\frac{7}{875}} = \left(\frac{7}{875}\right)^{\frac{1}{3}}$$

$$= \left(\frac{1}{125}\right)^{\frac{1}{3}} = \frac{1}{5}$$

6. (2)  $\sqrt[3]{\frac{19}{513}} = \sqrt[3]{\frac{1}{27}} = \frac{1}{3}$

7. (3) We know that

$$a^3 + b^3 + c^3 - 3abc = (a+b+c)(a^2+b^2+c^2-ab-bc-ca)$$

$$= \frac{1}{2}(a+b+c)[(a-b)^2 + (b-c)^2 + (c-a)^2]$$

$$\therefore \sqrt[3]{\frac{(333)^3 + (333)^3 + (334)^3}{-3 \times 333 \times 333 \times 334}}$$

$$= \sqrt[3]{\frac{1}{2}(333+333+334)[(333-333)^2 + (333-334)^2 + (334-333)^2]} \\ = \sqrt[3]{\frac{1}{2} \times 1000 \times 2} = \sqrt[3]{1000}$$

$$= \sqrt[3]{10 \times 10 \times 10} = 10$$

8. (3) Here,  $\sqrt[3]{175616} = 56$

$$\therefore \sqrt[3]{175.616} = 5.6$$

$$\sqrt[3]{0.175616} = 0.56$$

$$\text{and } \sqrt[3]{0.000175616} = 0.056$$

$\therefore$  Required sum

$$= 56. + 0.56 + 0.056 = 6.216$$

9. (4)  $\sqrt[3]{\sqrt{0.000064}} = \sqrt[3]{0.008}$

$$= \sqrt[3]{0.2 \times 0.2 \times 0.2}$$

$$= 0.2$$

10. (2) Expression

$$= \sqrt[3]{15612 + \sqrt{154 + \sqrt{225}}}$$

$$= \sqrt[3]{15612 + \sqrt{154 + 15}}$$

$$= \sqrt[3]{15612 + 13}$$

$$= \sqrt[3]{15625} = 25$$

11. (3)

$$\sqrt[3]{0.000125} = \sqrt[3]{0.05 \times 0.05 \times 0.05}$$

$$= 0.05$$

12. (3) First number  $= (\sqrt{5})^2 = 5$

Let the second number be  $x$ .

$$\therefore x^2 + 5^2 = 146$$

$$\Rightarrow x^2 = 146 - 25 = 121$$

$$\Rightarrow x = \sqrt{121} = 11$$

$$\therefore \text{Cube of } 11 = 1331$$

13. (1)  $\sqrt[3]{1000} + \sqrt[3]{0.008} - \sqrt[3]{0.125}$   
 $= 10 + 0.2 - 0.5 = 9.7$

14. (2) Expression

$$= \sqrt[3]{1 - \frac{127}{343}} = \sqrt[3]{\frac{343 - 127}{343}}$$

$$= \sqrt[3]{\frac{216}{343}} = \sqrt[3]{\frac{(6)^3}{(7)^3}} = \frac{6}{7} = 1 - \frac{1}{7}$$

15. (1)  $\sqrt[3]{3^n} = 27$

$$\Rightarrow (3)^{\frac{n}{3}} = 3^3$$

$$\Rightarrow \frac{n}{3} = 3 \Rightarrow n = 3 \times 3 = 9$$

16. (2) Expression

$$= \sqrt[3]{0.000729}$$

$$= \sqrt[3]{0.09 \times 0.09 \times 0.09}$$

$$= \sqrt[3]{0.09} = \sqrt{0.3 \times 0.3}$$

$$= 0.3$$

17. (1) Expression  $= \left(\sqrt{4^3 + 15^2}\right)^3$

$$= \left(\sqrt{64 + 225}\right)^3 = \left(\sqrt{289}\right)^3$$

$$= (17)^3 = 4913$$

18. (2) Expression  $= \sqrt[3]{4 \frac{12}{125}}$

$$= \sqrt[3]{\frac{512}{125}} = \sqrt[3]{\frac{8 \times 8 \times 8}{5 \times 5 \times 5}} = \frac{8}{5} = 1.6$$

19. (4)  $1323 = 3 \times 3 \times 3 \times 7 \times 7$

$\therefore$  It must be multiplied by 7.

20. (2)  $1440 = 2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 5 = 2^3 \times 2^2 \times 3^2 \times 5$

To make 1440 a perfect cube, it must be multiplied by  $2 \times 3 \times 5 \times 5 = 150$ .

$\therefore$  The required sum  $= 1+5+0 = 6$

21. (3)  $1800 = 2 \times 2 \times 2 \times 3 \times 3 \times 5 \times 5 = 2^3 \times 3^2 \times 5^2$

To make 1800 a perfect cube, it must be multiplied by 15 (least number).

$$\therefore \text{Required sum} = 1 + 5 = 6$$

22. (2) Clearly,  $\sqrt[3]{729} = 9$

$\therefore 19$  should be added to 710 to get a perfect cube.

2	1944
2	972
2	486
3	243
3	81
3	27
3	9
	3

$$\therefore 1944 = 2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 3 \\ = 2^3 \times 3^3 \times 3^2$$

Clearly, 1944 should be multiplied by 3 to make the result a perfect cube.

24. (1)  $3000 = 3 \times 1000 = 3 \times 10^3$

Clearly, when we divide 3000 by natural number 3, the quotient is 1000 which is a perfect cube.

2	864
2	432
2	216
2	108
2	54
3	27
3	9
	3

$$\therefore 864 = 2^3 \times 3^3 \times 2^2$$

For  $864n$  to be a perfect cube,  $n = 2$

26. (2)  $675 = 5 \times 5 \times 3 \times 3 \times 3$

$\therefore$  Required number  $= 5$

27. (2)  $12 \times 12 \times 12 = 1728$

$\therefore$  Required number

$$= 1728 - 1720 = 8$$

28. (2)  $4320 = 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 5$

$$= 2^3 \times 3^3 \times 2^2 \times 5$$

$\therefore$  Required number  $= 2 \times 5 \times 5 = 50$

29. (4)  $343 = 7 \times 7 \times 7$

$$125 = 5 \times 5 \times 5$$

$$81 = 3 \times 3 \times 3 \times 3$$

$$64 = 8 \times 8 = 4 \times 4 \times 4$$

We see that 343 and 125 are only perfect cubes of 7 and 5 respectively. 81 is only a perfect square of 9.

64 is a perfect square of 8 as well as a perfect cube of 4.

30. (4) Let number be  $x$

$\therefore$  According to question,

$$x^3 - x^2 = 48 \quad \therefore x = 4$$

## SIMPLIFICATION

**31.** (2) The number =  $90 \times A$

$$= 3 \times 3 \times 2 \times 5 \times A$$

The least value of A for which the given number is a perfect cube  
 $= 3 \times 2^2 \times 5^2$   
 $= 3 \times 4 \times 25 = 300$

**32.** (1)  $\sqrt{x} = \sqrt[3]{y}$

$$\Rightarrow x^{\frac{1}{2}} = y^{\frac{1}{3}}$$

$$\Rightarrow (\frac{1}{x})^6 = (\frac{1}{y^3})^6$$

$$\Rightarrow x^3 = y^2$$

**33.** (3)  $x = \sqrt{3} + \sqrt{2}$

$$\therefore \frac{1}{x} = \frac{1}{\sqrt{3} + \sqrt{2}} = \frac{\sqrt{3} - \sqrt{2}}{(\sqrt{3} + \sqrt{2})(\sqrt{3} - \sqrt{2})}$$

$$= \frac{\sqrt{3} - \sqrt{2}}{3 - 2} = \sqrt{3} - \sqrt{2}$$

$$\therefore x - \frac{1}{x} = \sqrt{3} + \sqrt{2} - \sqrt{3} + \sqrt{2}$$

$$= 2\sqrt{2}$$

$$\therefore x^3 - \frac{1}{x^3} = \left(x - \frac{1}{x}\right)^3 + 3\left(x - \frac{1}{x}\right)$$

$$= (2\sqrt{2})^3 + 3 \times 2\sqrt{2}$$

$$= 16\sqrt{2} + 6\sqrt{2} = 22\sqrt{2}$$

**34.** (1) Look at the pattern :

$$1001 \times 1001 = 1002001$$

$$1001 \times 1001 \times 1001 = 1003003001$$

**35.** (2) 

5	625
5	125
5	25
	5

$$\therefore 625 = 5 \times 5 \times 5 \times 5 = 5^3 \times 5$$

For the smallest cube number, 625 should be divided by 5,

$$625 \div 5 = 125 = 5^3$$

**36.** (3) Let the numbers be  $a$  and  $b$  where  $a > b$ .

According to the question,

$$a^3 + b^3 = 793$$

$$\text{and } a + b = 13$$

$$\therefore (a + b)^3 = a^3 + b^3 + 3ab(a + b)$$

$$\Rightarrow (13)^3 = 793 + 3ab \times 13$$

$$\Rightarrow 2197 = 793 + 39ab$$

$$\Rightarrow 39ab = 2197 - 793 = 1404$$

$$\Rightarrow ab = \frac{1404}{39} = 36$$

$$\therefore (a + b)^2 = (a + b)^2 - 4ab \\ = (13)^2 - 4 \times 36 \\ = 169 - 144 = 25$$

$$\Rightarrow a - b = \sqrt{25} = 5$$

$$\begin{aligned} \text{37. (3)} \quad 243000 &= 243 \times 1000 \\ &= 3 \times 3 \times 3 \times 3 \times 10 \times 10 \times 10 \\ &= 3^3 \times 3^2 \times 10^3 \end{aligned}$$

$$\therefore \text{Required number} = 3^2 = 9$$

**38.** (4) Expression

$$\begin{aligned} &= \left(2 - \frac{1}{3}\right) \left(2 - \frac{3}{5}\right) \left(2 - \frac{5}{7}\right) \dots \left(2 - \frac{997}{999}\right) \\ &= \left(\frac{6-1}{3}\right) \left(\frac{10-3}{5}\right) \\ &\quad \left(\frac{14-5}{7}\right) \dots \left(\frac{1998-997}{999}\right) \\ &= \frac{5}{3} \times \frac{7}{5} \times \frac{9}{7} \times \dots \times \frac{1001}{999} \\ &= \frac{1001}{3} \end{aligned}$$

**39.** (4)  $\sqrt[3]{79507} = 43$

$$\begin{aligned} &\therefore \sqrt[3]{79.507} + \sqrt[3]{0.079507} + \\ &\sqrt[3]{0.000079507} \\ &= 4.3 + 0.43 + 0.043 \\ &= 4.773 \end{aligned}$$

**40.** (4) 

2	13824
2	6912
2	3456
2	1728
2	864
2	432
2	216
2	108
2	54
3	27
3	9
	3

$$\therefore 13824 = 2^3 \times 2^3 \times 2^3 \times 3^3$$

$$\therefore \sqrt[3]{-13824}$$

$$\begin{aligned} &= \sqrt[3]{(-1)^3 2^3 \times 2^3 \times 2^3 \times 3^3} \\ &= (-1) 2 \times 2 \times 2 \times 3 = -24 \end{aligned}$$

**41.** (1)  $(105)^3 = (100 + 5)^3$

$$\begin{aligned} &= (100)^3 + (5)^3 + 3 \times 100 \times 5 (100 \\ &+ 5) \\ &[\because (a + b)^3 = a^3 + b^3 + 3ab(a + b)] \\ &= 1000000 + 125 + 1500 \times 105 \\ &= 1000000 + 125 + 157500 \\ &= 1157625 \end{aligned}$$

**42.** (2) 

2	37044
2	18522
3	9261
3	3087
3	1029
7	343
7	49
	7

$$\begin{aligned} &\therefore 37044 = 3 \times 3 \times 3 \times 7 \times 7 \times \\ &7 \times 2 \times 2 \\ &= 3^3 \times 7^3 \times 2^2 \\ &\therefore \text{Required number} = 2 \times 2 \\ &= 4 \end{aligned}$$

**43.** (1)  $(997)^3 = (1000 - 3)^3$

$$\begin{aligned} &= (1000)^3 - (3)^3 - 3 \times 1000 \times 3 (1000 - 3) \\ &= 1000000000 - 27 - 9000 \times 997 \\ &= 1000000000 - 27 - 8973000 \\ &= 991026973 \end{aligned}$$

**44.** (2) Let the numbers be  $3x$  and  $4x$ .

According to the question,

$$(3x)^3 + (4x)^3 = 5824$$

$$\Rightarrow 27x^3 + 64x^3 = 5824$$

$$\Rightarrow 91x^3 = 5824$$

$$\Rightarrow x^3 = \frac{5824}{91} = 64$$

$$\Rightarrow x = \sqrt[3]{64} = 4$$

∴ Sum of numbers

$$= 3x + 4x = 7x$$

$$= 7 \times 4 = 28$$

### TYPE-V

**1.** (3) ? =

$$\frac{(0.0539 - 0.002) \times 0.4 + 0.56 \times 0.07}{0.04 \times 0.25}$$

$$= \frac{0.0519 \times 0.4 + 0.0392}{0.01}$$

$$= \frac{0.02076 + 0.0392}{0.01}$$

$$= \frac{0.05996}{0.01} = 5.996$$

# TEST YOURSELF

**1.** Simplify :

$$\frac{3.5 \times 1.5}{0.025 \div 0.125 \times 7.5} \times \frac{1}{3 + \frac{1}{1 + \frac{1}{2}}}$$

- (1) 0.9      (2) 0.95  
 (3) 0.095      (4) 0.082

**2.** Simplify :

$$\frac{3}{4 + \frac{5}{6 + \frac{7}{8}}} - \frac{3}{5} \div \frac{1}{2} \text{ of } 1\frac{1}{5} + 1\frac{3}{26}$$

- (1)  $\frac{3}{4}$       (2)  $\frac{1}{2}$   
 (3)  $\frac{3}{5}$       (4)  $\frac{3}{7}$

**3.** Simplify :

$$999\frac{998}{999} \times 999 + 999$$

- (1) 999997      (2) 999998  
 (3) 99998      (4) 999994

**4.** Simplify

$$2 \div \frac{3}{17} \text{ of } \left( 2\frac{3}{4} + 3\frac{5}{8} \right) + \frac{2}{5} \div 2\frac{1}{5} + \frac{2}{9}$$

- (1)  $\frac{9}{17}$       (2)  $\frac{7}{11}$   
 (3)  $\frac{13}{11}$       (4)  $\frac{24}{11}$

**5.** Simplify :

$$120 + 3 \text{ of } 5 \div$$

$$\left[ 7 \times 2 \left\{ 10 \div 5 \left( 24 - 10 \times 2 + \overline{7+3 \times 10+5} \right) \right\} \right]$$

- (1) 120.03      (2) 116.04  
 (3) 118      (4) 125

$$6. \frac{2.5 \times 3 + 7.5 \div 2.5 - 0.5 \text{ of } 3}{47 + 12 \div 1.5 - 6 \text{ of } 2 \times 3} = ?$$

- (1)  $\frac{3}{17}$       (2)  $\frac{9}{19}$   
 (3)  $\frac{4}{11}$       (4)  $\frac{3}{11}$

**7.** Simplify :

$$\frac{17}{7 + \frac{3}{4 - 2\frac{3}{4}}} \times \frac{2021}{2193} \div \left( 1\frac{37}{48} - \frac{15}{16} \right)$$

$$+\frac{3}{4} \text{ of } \frac{3\frac{1}{2}}{2\frac{1}{2}}$$

- (1)  $2\frac{1}{8}$       (2)  $4\frac{1}{8}$   
 (3)  $3\frac{1}{8}$       (4)  $3\frac{1}{7}$

$$8. \frac{\frac{1}{9} \text{ of } \frac{27}{64}}{\frac{11}{12} \times 9\frac{9}{11}} \div \frac{\frac{4}{7} \text{ of } \frac{21}{160}}{2\frac{5}{6} \div 2\frac{2}{15}} = ?$$

- (1)  $\frac{425}{2344}$       (2)  $\frac{425}{2434}$   
 (3)  $\frac{421}{2443}$       (4)  $\frac{425}{2304}$

**9.** Simplify :

$$\frac{8\frac{3}{5} + 7\frac{3}{4} + 5\frac{2}{3} - 4\frac{1}{2}}{13 - 11\frac{9}{10} + 10\frac{7}{9} - 9\frac{17}{20}}$$

of  $\frac{2}{11}$  of 365

- (1)  $573\frac{3}{11}$       (2)  $571\frac{7}{11}$   
 (3)  $572\frac{3}{11}$       (4)  $575\frac{4}{11}$

**10.** Simplify :

$$\frac{1}{8} \text{ of } \left( \frac{1}{10} - \frac{1}{11} \right) \div$$

$$\frac{\frac{1}{7} - \frac{1}{9} \div \left( \frac{4}{9} + \frac{4}{11} \right)}{\frac{1}{7} + \frac{1}{9} \div \left( \frac{4}{9} - \frac{4}{11} \right)}$$

$$\times \frac{\frac{1}{3} + \frac{1}{7} \div \left( \frac{1}{7} - \frac{1}{9} \right)}{\left( \frac{1}{3} + \frac{1}{7} \right) \div \frac{1}{7} - \frac{1}{9}}$$

- (1)  $\frac{85}{176}$       (2)  $\frac{83}{176}$   
 (3) 83      (4) 86

**11.** Simplify

$$\begin{aligned} & 2\frac{4}{9} \div 3\frac{2}{3} \text{ of } \frac{2}{5} \times \frac{3}{5} + 1\frac{1}{9} - \frac{5\frac{1}{2} - \frac{3}{4}}{1\frac{1}{9} \times \frac{3}{4} \text{ of } 1\frac{2}{5} \div \frac{21}{38} - 3\frac{1}{3}} \\ & - \frac{2\frac{1}{5} \times 1\frac{9}{11}}{2\frac{1}{5} \times 1\frac{9}{11}} \end{aligned}$$

- (1) 1      (2) 0  
 (3) 2      (4) 3

**12.** Simplify :

$$\begin{aligned} & \frac{\frac{5}{6} + \frac{7}{8} \text{ of } \frac{4}{5} \div \frac{3}{4} \text{ of } \frac{9}{10}}{\frac{8}{3} - \left( \frac{4}{1 - \frac{7}{8}} \text{ of } 2\frac{1}{4} \right) \div \frac{7}{9} \text{ of } 12} \\ & \text{of } 6\frac{1}{2} + 5\frac{1}{9} \end{aligned}$$

- (1)  $24\frac{1}{4}$       (2)  $24\frac{3}{4}$   
 (3)  $22\frac{1}{2}$       (4)  $23\frac{1}{3}$

**13.** Simplify :

$$\begin{aligned} & \frac{\frac{2}{3} \div \frac{3}{4} \text{ of } \frac{5}{6} + 2 + 2 \times 2}{\frac{2}{3} \div \frac{3}{4} \times \frac{5}{6} + 2 \div 2 \times 2} \div \frac{\frac{1}{2} \div \frac{1}{2} \text{ of } \frac{1}{2}}{\frac{1}{2} + \frac{1}{2} \text{ of } \frac{1}{2}} \\ & (1) 2 \quad (2) 2.5 \\ & (3) 4 \quad (4) 4.5 \end{aligned}$$

**14.** Simplify :

$$\begin{aligned} & \frac{\frac{5+5 \times 5}{5 \times 5+5} \times \frac{1}{5} \div \frac{1}{5} \text{ of } \frac{1}{5}}{\frac{1}{5} \text{ of } \frac{1}{5} \div \frac{1}{5}} \times \left( 5 - \frac{1}{5} \right) \times \\ & \frac{1}{\frac{46}{5} - \frac{3}{1 - \frac{2}{3}}} \end{aligned}$$

- (1) 400      (2) 500  
 (3) 600      (4) 300

$$15. \text{ Simplify } 1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{9}}}$$

- (1)  $1\frac{9}{19}$       (2)  $1\frac{10}{19}$   
 (3)  $2\frac{9}{19}$       (4)  $3\frac{9}{19}$

**16.** Compute the following :

$$7 + \frac{2}{5 + \frac{3}{4 + \frac{2}{3 + \frac{1}{4}}}}$$

- (1)  $3\frac{40}{113}$       (2)  $6\frac{40}{113}$   
 (3)  $7\frac{40}{113}$       (4)  $5\frac{40}{113}$

**17. Simplify :**

$$7\frac{1}{2} - \left[ 2\frac{1}{4} \div \left\{ 1\frac{1}{4} - \frac{1}{2} \left( 1\frac{1}{2} - \frac{1}{3} - \frac{1}{6} \right) \right\} \right]$$

- (1)  $4\frac{1}{2}$       (2)  $3\frac{1}{2}$

- (3)  $4\frac{1}{3}$       (4)  $\frac{1}{3}$

**18. Simplify :**

$$3 \div \left[ (8-5) \div \left\{ (4-2) \div \left( 2 + \frac{8}{13} \right) \right\} \right] = ?$$

- (1)  $\frac{17}{13}$       (2)  $\frac{13}{17}$

- (3)  $\frac{15}{17}$       (4)  $\frac{17}{15}$

**19. Simplify**

$$5\frac{1}{2} - \left[ 2\frac{1}{3} \div \left\{ \frac{3}{4} - \frac{1}{2} \left( \frac{2}{3} - \frac{1}{6} - \frac{1}{8} \right) \right\} \right]$$

- (1)  $\frac{1}{2}$       (2)  $\frac{1}{4}$

- (3)  $\frac{1}{6}$       (4)  $\frac{2}{3}$

### ■ SHORT ANSWERS ■

<b>1.</b> (2)	<b>2.</b> (1)	<b>3.</b> (2)	<b>4.</b> (4)
<b>5.</b> (1)	<b>6.</b> (2)	<b>7.</b> (3)	<b>8.</b> (4)
<b>9.</b> (1)	<b>10.</b> (1)	<b>11.</b> (2)	<b>12.</b> (2)
<b>13.</b> (2)	<b>14.</b> (3)	<b>15.</b> (2)	<b>16.</b> (3)
<b>17.</b> (1)	<b>18.</b> (2)	<b>19.</b> (3)	

### ■ EXPLANATIONS ■

**1. (2) Expression =**

$$\frac{3.5 \times 1.5}{0.025 \times \frac{1}{0.125} \times 7.5} \times \frac{1}{3 + \frac{1}{1 + \frac{1}{2}}}$$

$$= \frac{3.5 \times 1.5 \times 125}{25 \times 7.5} \times \frac{1}{3 + \frac{1}{\frac{3}{2}}}$$

$$= 3.5 \times \frac{1}{3 + \frac{2}{3}} = 3.5 \times \frac{1}{\frac{9+2}{3}}$$

$$= \frac{3.5 \times 3}{11} = \frac{10.5}{11} = 0.95$$

$$2. (1) \frac{3}{4 + \frac{5}{6 + \frac{7}{8}}} = \frac{3}{4 + \frac{5}{\frac{48+7}{8}}} = \frac{3}{4 + \frac{5 \times 8}{55}}$$

$$= \frac{3}{4 + \frac{40}{55}} = \frac{3}{4 + \frac{8}{11}}$$

$$= \frac{3}{\frac{44+8}{11}} = \frac{3 \times 11}{52} = \frac{33}{52}$$

$$\therefore \text{Expression} = \frac{33}{52} - \frac{3}{5} \div \frac{1}{2}$$

$$\text{of } 1\frac{1}{5} + 1\frac{3}{26}$$

$$= \frac{33}{52} - \frac{3}{5} \div \frac{1}{2} \times \frac{6}{5} + \frac{29}{26}$$

$$= \frac{33}{52} - \frac{3}{5} \times \frac{5}{3} + \frac{29}{26}$$

$$= \frac{33}{52} - 1 + \frac{29}{26}$$

$$= \frac{33 - 52 + 58}{52} = \frac{39}{52} = \frac{3}{4}$$

$$3. (2) \left( 999 + \frac{998}{999} \right) 999 + 999$$

$$= (999)^2 + 998 + 999$$

$$= (1000 - 1)^2 + 998 + 999$$

$$= 1000000 + 1 - 2000 + 998 + 999$$

$$= 999998$$

**4. (4) The given expression**

$$= 2 \div \frac{3}{17} \text{ of } \left( \frac{11}{4} + \frac{29}{8} \right) + \frac{2}{5} \div \frac{11}{5} + \frac{2}{9}$$

$$= 2 \div \frac{3}{17} \text{ of } \left( \frac{22+29}{8} \right) + \frac{2}{5} \div \frac{11}{5} + \frac{2}{9}$$

$$= 2 \div \frac{3}{17} \text{ of } \frac{51}{8} + \frac{2}{5} \div \frac{11}{5} + \frac{2}{9}$$

$$= 2 \div \frac{3}{17} \times \frac{51}{8} + \frac{2}{5} \div \frac{11}{5} + \frac{2}{9}$$

$$= 2 \div \frac{9}{8} + \frac{2}{5} \div \frac{11}{5} + \frac{2}{9}$$

$$= 2 \times \frac{8}{9} + \frac{2}{5} \times \frac{5}{11} + \frac{2}{9}$$

$$= \frac{16}{9} + \frac{2}{11} + \frac{2}{9} = \frac{176+18+22}{99}$$

$$= \frac{216}{99} = \frac{24}{11}$$

**5. (1) The given expression**

$$120 + 3 \text{ of } 5 \div$$

$$\left[ 7 \times 2 \left\{ 10 \div 5 (24 - 10 \times 2 + 7 + 3 \times 10 \div 5) \right\} \right]$$

$$= 120 + 3 \text{ of } 5 \div$$

$$\left[ 7 \times 2 \left\{ 10 \div 5 (24 - 10 \times 2 + 7 + 3 \times 2) \right\} \right]$$

$$= 120 + 3 \text{ of } 5 \div$$

$$\left[ 7 \times 2 \left\{ 10 \div 5 (24 - 10 \times 2 + 7 + 6) \right\} \right]$$

$$= 120 + 3 \text{ of } 5 \div$$

$$\left[ 7 \times 2 \left\{ 10 \div 5 (24 - 10 \times 2 + 13) \right\} \right]$$

$$= 120 + 3 \text{ of } 5 \div \left[ 7 \times 2 \left\{ 10 \div 5 \times 17 \right\} \right]$$

$$= 120 + 3 \text{ of } 5 \div \left[ 7 \times 2 \left\{ 10 \times \frac{1}{5} \times 17 \right\} \right]$$

$$= 120 + 3 \text{ of } 5 \div \left[ 7 \times 2 \left\{ 2 \times 17 \right\} \right]$$

$$= 120 + 3 \text{ of } 5 \div [7 \times 2 \times 34]$$

$$= 120 + 3 \times 5 \div 476 = 120 + 15 \div 476$$

$$= 120 + \frac{15}{476} = 120 \frac{15}{476}$$

$$= 120.03$$

**6. (2) The given expression**

$$= \frac{2.5 \times 3 + 7.5 \div 2.5 - 0.5 \text{ of } 3}{47 + 12 \div 1.5 - 6 \text{ of } 2 \times 3}$$

$$= \frac{2.5 \times 3 + 7.5 \times \frac{1}{2.5} - 0.5 \times 3}{47 + 12 \times \frac{1}{1.5} - 6 \times 2 \times 3}$$

$$= \frac{7.5 + 3 - 1.5}{47 + 8 - 36} = \frac{9}{19}$$

**7. (3)**

$$\frac{17}{7 + \frac{3}{4 - \frac{11}{4}}} \times \frac{2021}{2193} \div \left( \frac{85}{48} - \frac{15}{16} \right) + \frac{3}{4} \text{ of } \frac{\frac{3}{2}}{\frac{5}{2}}$$

$$= \frac{17}{7 + \frac{3}{\frac{16-11}{4}}} \times \frac{47}{51} \div \left( \frac{85}{48} - \frac{15}{16} \right) + \frac{3}{4} \text{ of } \frac{\frac{3}{4}}{\frac{5}{2}}$$

$$= \frac{17}{7 + \frac{12}{5}} \times \frac{47}{51} \div \left( \frac{85}{48} - \frac{15}{48} \right)$$

$$+ \frac{3}{4} \times \frac{15}{4} \times \frac{2}{5}$$

$$\begin{aligned}
 &= \frac{17}{\frac{35+12}{5}} \times \frac{47}{51} \div \frac{40}{48} + \frac{9}{8} \\
 &= \frac{17 \times 5}{47} \times \frac{47}{51} \times \frac{48}{40} + \frac{9}{8} \\
 &= 2 + 1 \frac{1}{8} = 3 \frac{1}{8}
 \end{aligned}$$

$$\begin{aligned}
 8. (4) \quad &\frac{16}{9} \text{ of } \frac{27}{64} \div \frac{32}{7} \text{ of } \frac{21}{160} \\
 &\frac{11}{12} \times \frac{108}{11} \div \frac{17}{6} \div \frac{32}{15} \\
 &= \frac{16}{9} \times \frac{27}{64} \div \frac{32}{7} \times \frac{21}{160} \\
 &= \frac{11}{12} \times \frac{108}{11} \div \frac{17}{6} \times \frac{15}{32} \\
 &= \frac{3}{4} \div \frac{5}{17 \times 5} \\
 &= \frac{9}{1} \times \frac{3}{32 \times 2} \\
 &= \frac{3}{4} \times \frac{1}{9} \div \frac{3 \times 2 \times 32}{17 \times 5 \times 5} \\
 &= \frac{1}{4} \times \frac{1}{3} \times \frac{17 \times 5 \times 5}{3 \times 2 \times 32} = \frac{425}{2304}
 \end{aligned}$$

$$\begin{aligned}
 9. (1) \quad &\frac{43}{5} + \frac{31}{4} + \frac{17}{3} - \frac{9}{2} \\
 &\frac{119}{13} - \frac{97}{10} + \frac{197}{9} - \frac{19}{20} \text{ of } \frac{2}{11} \text{ of } 365 \\
 &= \frac{516 + 465 + 340 - 270}{60} \\
 &= \frac{2340 - 2142 + 1940 - 1773}{180} \\
 &\text{of } \frac{2}{11} \times 365
 \end{aligned}$$

$$\begin{aligned}
 &= \frac{1321 - 270}{60} \\
 &= \frac{4280 - 3915}{180} \text{ of } \frac{2 \times 365}{11} \\
 &= \frac{1051}{60} \text{ of } \frac{2 \times 365}{11} \\
 &= \frac{1051}{365} \times \frac{180}{180} \times \frac{2 \times 365}{11} \\
 &= \frac{1051 \times 3 \times 2}{11} \\
 &= \frac{6306}{11} = 573 \frac{3}{11}
 \end{aligned}$$

$$\begin{aligned}
 10. (1) \quad &\frac{1}{8} \text{ of } \left( \frac{11-10}{110} \right) \\
 &+ \frac{\frac{1}{7} - \frac{1}{9} \div \left( \frac{44+36}{99} \right)}{\frac{1}{7} + \frac{1}{9} \div \left( \frac{44-36}{99} \right)} \\
 &\times \frac{\frac{1}{3} + \frac{1}{7} \div \left( \frac{9-7}{63} \right)}{\left( \frac{7+3}{21} \right) \div \frac{1}{7} - \frac{1}{9}} \\
 &= \frac{1}{8} \text{ of } \frac{1}{110} \div \frac{\frac{1}{7} - \frac{1}{9} \times \frac{99}{80}}{\frac{1}{7} + \frac{1}{9} \times \frac{99}{8}} \times \frac{\frac{1}{3} + \frac{1}{7} \times \frac{63}{2}}{\frac{10}{21} \times \frac{7}{1} - \frac{1}{9}} \\
 &= \frac{1}{8} \text{ of } \frac{1}{110} \div \frac{\frac{1}{7} - \frac{11}{80}}{\frac{1}{7} + \frac{11}{8}} \times \frac{\frac{1}{3} + \frac{9}{2}}{\frac{10}{3} - \frac{1}{9}} \\
 &= \frac{1}{8} \times \frac{1}{110} \div \frac{\frac{80-77}{560}}{\frac{8177}{56}} \times \frac{\frac{2127}{9}}{\frac{30-1}{9}} \\
 &= \frac{1}{8} \times \frac{1}{110} \times \frac{850}{3} \times \frac{9}{6} = \frac{85}{176}
 \end{aligned}$$

$$\begin{aligned}
 11. (2) \quad &2 \frac{4}{9} \div 3 \frac{2}{3} \text{ of } \frac{2}{5} \times \frac{3}{5} + 1 \frac{1}{9} - \frac{5 \frac{1}{2} - \frac{3}{4}}{2 \frac{1}{5} \times 1 \frac{9}{11}} \\
 &1 \frac{1}{9} \times \frac{3}{4} \text{ of } 1 \frac{2}{5} \div \frac{21}{38} - \frac{1}{3} - 2 \frac{1}{5} \times 1 \frac{9}{11} \\
 &= \frac{22}{9} \div \frac{11}{3} \text{ of } \frac{2}{5} \times \frac{3}{5} + \frac{10}{9} - \frac{\frac{11}{2} - \frac{3}{4}}{\frac{11}{5} \times \frac{20}{11}} \\
 &= \frac{22}{9} \times \frac{3}{4} \text{ of } \frac{7}{5} \div \frac{21}{38} - \frac{1}{3} - \frac{\frac{11}{2} \times \frac{20}{11}}{\frac{11}{5} \times \frac{20}{11}} \\
 &= \frac{22}{9} \div \frac{22}{15} \times \frac{3}{5} + \frac{10}{9} - \frac{22-3}{4} \\
 &= \frac{10}{9} \times \frac{21}{20} \div \frac{21}{38} - \frac{1}{3} - \frac{4}{4} \\
 &= \frac{\left( \frac{22}{9} \times \frac{15}{22} \right) \times \frac{3}{5} + \frac{10}{9}}{\frac{10}{9} \times \left( \frac{21}{20} \times \frac{38}{21} \right)} - \frac{1}{3} - \frac{4}{4} \\
 &= \frac{\frac{5}{3} \times \frac{3}{5} + \frac{10}{9}}{\frac{10}{9} \times \frac{19}{10} - \frac{1}{3}} - \frac{19}{4} \times \frac{1}{4} \\
 &= \frac{1 + \frac{10}{9}}{\frac{19}{9} - \frac{1}{3}} - \frac{19}{16} = \frac{\frac{9+10}{9}}{\frac{19-3}{9}} - \frac{19}{16}
 \end{aligned}$$

$$\begin{aligned}
 &= \frac{\frac{19}{9}}{\frac{16}{9}} - \frac{19}{16} = \frac{19}{16} - \frac{19}{16} = 0 \\
 12. (2) \quad &\frac{\frac{5}{6} + \left( \frac{7}{8} \times \frac{4}{5} \right) \div \left( \frac{3}{4} \times \frac{9}{10} \right)}{\frac{25}{3} - \left( \frac{\frac{4}{8-7} \text{ of } \frac{9}{4}}{8} \right) \div \left( \frac{7}{9} \times 12 \right)} \\
 &\text{of } \frac{13}{2} + \frac{46}{9} \\
 &= \frac{\frac{5}{6} + \frac{7}{10} \div \frac{27}{40}}{\frac{25}{3} - 32 \times \frac{9}{4} \div \frac{28}{3}} \text{ of } \frac{13}{2} + \frac{46}{9} \\
 &= \frac{\frac{5}{6} + \frac{7}{10} \times \frac{40}{27}}{\frac{25}{3} - 32 \times \frac{9}{4} \times \frac{3}{28}} \text{ of } \frac{13}{2} + \frac{46}{9} \\
 &= \frac{\frac{5}{6} + \frac{28}{27}}{\frac{25}{3} - \frac{54}{7}} \text{ of } \frac{13}{2} + \frac{46}{9} \\
 &= \frac{\frac{45+56}{54}}{\frac{175-162}{21}} \text{ of } \frac{13}{2} + \frac{46}{9} \\
 &= \frac{101}{54} \times \frac{21}{13} \times \frac{13}{2} + \frac{46}{9} \\
 &= \frac{707}{36} + \frac{46}{9} = \frac{707+184}{36} \\
 &8 \frac{91}{36} = 24 \frac{27}{36} = 24 \frac{3}{4}
 \end{aligned}$$

$$\begin{aligned}
 13. (2) \quad &\text{The given expression} \\
 &\frac{2}{3} \div \frac{3}{4} \text{ of } \frac{5}{6} + 2 + 2 \times 2 \div \frac{1}{2} \div \frac{1}{2} \text{ of } \frac{1}{2} \\
 &\frac{2}{3} \div \frac{3}{4} \times \frac{5}{6} + 2 \div 2 \times 2 \div \frac{1}{2} + \frac{1}{2} \text{ of } \frac{1}{2} \\
 &= \frac{\frac{2}{3} \div \left( \frac{3}{4} \times \frac{5}{6} \right)}{\left( \frac{2}{3} \times \frac{4}{3} \right) \times \frac{5}{6}} + \frac{2+4}{\left( 2 \times \frac{1}{2} \right) \times 2} \div \frac{1}{2} + \frac{1}{2} \times \frac{1}{2} \\
 &= \frac{\frac{2}{3} \div \frac{15}{8}}{\frac{8}{9} \times \frac{5}{6}} + \frac{6}{2} \div \frac{1}{2} \div \frac{1}{4} \\
 &= \frac{\frac{2}{3} \times \frac{8}{15}}{\frac{8}{9} \times \frac{5}{6}} + 3 \div \frac{2}{2+1} \\
 &= \frac{\frac{16}{45}}{\frac{40}{27}} + 3 \div \frac{2}{3} \\
 &= \frac{2}{27} + 3 \div \frac{2}{3} = \frac{2}{27} + \frac{9}{2} = \frac{45}{27} = \frac{5}{3}
 \end{aligned}$$

$$\begin{aligned}
 &= \frac{16}{15} \times \frac{27}{20} + 3 \div \frac{2}{\frac{3}{4}} \\
 &= \frac{36}{25} + 3 \div \left( 2 \times \frac{4}{3} \right) \\
 &= \frac{36}{25} + 3 \div \frac{8}{3} = \frac{36}{25} + 3 \times \frac{3}{8} \\
 &= \frac{288+225}{200} = \frac{513}{200} = 2 \frac{113}{200} = 2.5
 \end{aligned}$$

**14.** (3) The given expression

$$\begin{aligned}
 &= \frac{5+25}{25+5} \times \frac{\frac{1}{5} \div \left( \frac{1}{5} \times \frac{1}{5} \right)}{\left( \frac{1}{5} \times \frac{1}{5} \right) \div \frac{1}{5}} \\
 &\quad \times \left( \frac{25-1}{5} \right) \times \frac{1}{\frac{46}{5} - \frac{3}{\frac{3-2}{3}}} \\
 &\quad \times \left( \frac{25-1}{5} \right) \times \frac{1}{\frac{46}{5} - \frac{3}{\frac{3-2}{3}}}
 \end{aligned}$$

$$\begin{aligned}
 &= \frac{30}{30} \times \frac{\frac{1}{5} \div \frac{1}{25}}{\frac{1}{25} \div \frac{1}{5}} \times \frac{24}{5} \times \frac{1}{\frac{46}{5} - \frac{1}{\frac{3}{3}}} \\
 &= \frac{1}{25} \times \frac{24}{5} \times \frac{1}{\frac{46}{5} - 9}
 \end{aligned}$$

$$\begin{aligned}
 &= \frac{5}{1} \times \frac{24}{5} \times \frac{1}{\frac{46}{5} - 45} \\
 &= 5 \times 5 \times \frac{24}{5} \times \frac{5}{1} = 600
 \end{aligned}$$

**15.** (2) It is a continued fraction. In such problems, we should start from the bottom and work upwards.

The given expression

$$\begin{aligned}
 &= 1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{9}}} = 1 + \frac{1}{1 + \frac{1}{9+1}}
 \end{aligned}$$

$$\begin{aligned}
 &= 1 + \frac{1}{1 + \frac{1}{10}} = 1 + \frac{1}{1 + 1 \times \frac{9}{10}} \\
 &= 1 + \frac{1}{1 + \frac{9}{10}} = 1 + \frac{1}{\frac{10+9}{10}}
 \end{aligned}$$

$$= 1 + \frac{10}{19} = \frac{19+10}{19} = \frac{29}{19} = 1 \frac{10}{19}$$

$$\begin{aligned}
 &16. (3) 7 + \frac{2}{5 + \frac{3}{4 + \frac{2}{3 + \frac{1}{4}}}} \\
 &= 7 + \frac{2}{5 + \frac{3}{4 + \frac{2}{12+1}}}
 \end{aligned}$$

$$\begin{aligned}
 &= 7 + \frac{2}{5 + \frac{3}{4 + \frac{2 \times 4}{13}}} \\
 &= 7 + \frac{2}{5 + \frac{3}{4 + \frac{8}{13}}}
 \end{aligned}$$

$$\begin{aligned}
 &= 7 + \frac{2}{5 + \frac{3}{52+8}} \\
 &= 7 + \frac{2}{5 + 3 \times \frac{13}{60}} \\
 &= 7 + \frac{2}{5 + \frac{13}{20}} = 7 + \frac{2}{\frac{100+13}{20}}
 \end{aligned}$$

$$\begin{aligned}
 &= 7 + \frac{2 \times 20}{113} \\
 &= 7 + \frac{40}{113} = 7 \frac{40}{113}
 \end{aligned}$$

**17. (1)** The given expression

$$\begin{aligned}
 &= 7 \frac{1}{2} - \left[ 2 \frac{1}{4} \div \left\{ 1 \frac{1}{4} - \frac{1}{2} \left( 1 \frac{1}{2} - \frac{1}{3} - \frac{1}{6} \right) \right\} \right] \\
 &= \frac{15}{2} - \left[ \frac{9}{4} \div \left\{ \frac{5}{4} - \frac{1}{2} \left( \frac{3}{2} - \frac{1}{3} - \frac{1}{6} \right) \right\} \right] \\
 &= \frac{15}{2} - \left[ \frac{9}{4} \div \left\{ \frac{5}{4} - \frac{1}{2} \left( \frac{9-2-1}{6} \right) \right\} \right] \\
 &= \frac{15}{2} - \left[ \frac{9}{4} \div \left\{ \frac{5}{4} - \frac{1}{2} \times 1 \right\} \right] \\
 &= \frac{15}{2} - \left[ \frac{9}{4} \div \left\{ \frac{5-2}{4} \right\} \right] \\
 &= \frac{15}{2} - \left[ \frac{9}{4} \div \frac{3}{4} \right]
 \end{aligned}$$

$$\begin{aligned}
 &= \frac{15}{2} - \left[ \frac{9}{4} \times \frac{4}{3} \right] \\
 &= \frac{15}{2} - 3 = \frac{15-6}{2} = \frac{9}{2} = 4 \frac{1}{2}
 \end{aligned}$$

**18. (2)** The given expression

$$= 3 \div \left[ (8-5) \div \left\{ (4-2) \div \left( 2 + \frac{8}{13} \right) \right\} \right]$$

$$\begin{aligned}
 &= 3 \div \left[ 3 \div \left\{ 2 \div \left( \frac{26+8}{13} \right) \right\} \right] \\
 &= 3 \div \left[ 3 \div \left\{ 2 \div \frac{34}{13} \right\} \right] \\
 &= 3 \div \left[ 3 \div \left\{ 2 \times \frac{13}{34} \right\} \right] \\
 &= 3 \div \left[ \frac{3 \times 34}{26} \right] = \frac{3 \times 26}{3 \times 34} = \frac{13}{17}
 \end{aligned}$$

**19. (3)** The given expression

$$= 5 \frac{1}{2} - \left[ 2 \frac{1}{3} \div \left\{ \frac{3}{4} - \frac{1}{2} \left( \frac{2}{3} - \frac{1}{6} - \frac{1}{8} \right) \right\} \right]$$

$$= \frac{11}{2} - \left[ \frac{7}{3} \div \left\{ \frac{3}{4} - \frac{1}{2} \left( \frac{2}{3} - \frac{1}{6} - \frac{1}{8} \right) \right\} \right]$$

$$= \frac{11}{2} - \left[ \frac{7}{3} \div \left\{ \frac{3}{4} - \frac{1}{2} \left( \frac{2}{3} - \frac{4-3}{24} \right) \right\} \right]$$

$$= \frac{11}{2} - \left[ \frac{7}{3} \div \left\{ \frac{3}{4} - \frac{1}{2} \left( \frac{2}{3} - \frac{1}{24} \right) \right\} \right]$$

$$= \frac{11}{2} - \left[ \frac{7}{3} \div \left\{ \frac{3}{4} - \frac{1}{2} \left( \frac{16-1}{24} \right) \right\} \right]$$

$$= \frac{11}{2} - \left[ \frac{7}{3} \div \left\{ \frac{3}{4} - \frac{1}{2} \times \frac{15}{24} \right\} \right]$$

$$= \frac{11}{2} - \left[ \frac{7}{3} \div \left\{ \frac{3}{4} - \frac{15}{48} \right\} \right]$$

$$= \frac{11}{2} - \left[ \frac{7}{3} \div \left\{ \frac{36-15}{48} \right\} \right]$$

$$= \frac{11}{2} - \left[ \frac{7}{3} \div \frac{21}{48} \right]$$

$$= \frac{11}{2} - \left[ \frac{7}{3} \times \frac{48}{21} \right]$$

$$= \frac{11}{2} - \frac{16}{3} = \frac{33-32}{6} = \frac{1}{6}$$

□□□