BITSAT : SOLVED PAPER 2013 (memory based)

INSTRUCTIONS

• This question paper contains total 150 questions divided into four parts:

Part I: Physics Q. No. 1 to 40

Part II : Chemistry Q. No. 41 to 80

Part III : Mathematics Q. No. 81 to 125

Part IV: (A) English Proficiency Q. No. 126 to 140

(B) Logical Reasoning Q. No. 141 to 150

- All questions are multiple choice questions with four options, only one of them is correct.
- Each correct answer awarded 3 marks and -1 for each incorrect answer.
- Duration of paper 3 Hours

PART - I : PHYSICS

1. The velocity and acceleration vectors of a particle undergoing circular motion are $\vec{v} = 2\hat{i} m/s$ and $\vec{a} = 2\hat{i} + 4\hat{j} m/s^2$ respectively at an instant of time. The radius of the circle is –

(a) 1m (b) 2m (c) 3m (d) 4m

- 2. A man runs at a speed of 4 m/s to overtake a standing bus. When he is 6 m behind the door at t = 0, the bus moves forward and continuous with a constant acceleration of 1.2 m/s². The man reaches the door in time t. Then,
 - (a) $4t = 6 + 0.6t^2$ (b) $1.2t^2 = 4t$
 - (c) $4t^2 = 1.2t$ (d) $6+4t = 0.2t^2$
- 3. Wave pulse can travel along a tense string like a violin spring. A series of experiments showed that the wave velocity V of a pulse depends on the following quantities, the tension T of the string, the cross-section area A of the string and then as per unit volume ρ of the string. Obtain an expression for V in terms of the T, A and ρ using dimensional analysis.

(a)
$$V = k \sqrt{\frac{T}{A\rho}}$$
 (b) $V = k \sqrt{\frac{T}{A}}$
(c) $V = k \sqrt{\frac{A\rho}{T}}$ (d) None of these

4. A body is projected, making an acute angle with the horizontal. If angle between velocity \vec{v} and acceleration \vec{g} is θ , then

(a)
$$\theta = 90^{\circ}$$
 (b) $\theta = 0^{\circ}$
(c) $\theta = 0^{\circ}$ (d) $\theta = 0^{\circ}$

(c)
$$90^{\circ} < \theta < 0^{\circ}$$
 (d) $0^{\circ} < \theta < 180^{\circ}$
The minimum value its (in ms⁻¹) with which

- 5. The minimum velocity (in ms⁻¹) with which a car driver must traverse a flat curve of radius 150 m and coefficient of friction 0.6 to avoid skidding is (a) 60 (b) 30 (c) 15 (d) 25
- 6. A bob is hanging over a pulley inside a car through, a string. The second end of the string is in the hand of a person standing in the car. The car is



1000

moving with constant acceleration 'a' directed horizontally as shown in figure. Other end of the string is pulled with constant acceleration 'a' vertically. The tension in the string is equal to –

(a)
$$m\sqrt{g^2 + a^2}$$
 (b) $m\sqrt{g^2 + a^2} - ma$

(c)
$$m\sqrt{g^2 + a^2} + ma$$
 (d) $m(g+a)$

7. A block of mass m is placed on a smooth inclined wedge ABC of inclination θ as shown in the figure. The wedge is given an acceleration 'a' towards the right. The relation between a and θ for the block to remain stationary on the wedge is



- 8. A 3.628 kg freight car moving along a horizontal rail road spur track at 7.2 km/hour strikes a bumper whose coil springs experiences a maximum compression of 30 cm in stopping the car. The elastic potential energy of the springs at the instant when they are compressed 15 cm is
 - (a) $12.1 \times 10^4 \text{ J}$ (b) $121 \times 10^4 \text{ J}$ (c) $1.21 \times 10^4 \text{ J}$ (d) $1.21 \times 10^6 \text{ J}$
- 9. A light inextensible string that goes over a smooth fixed pulley as shown in the figure connects two blocks of masses 0.36 kg and 0.72 kg. Taking $g = 10 \text{ m/s}^2$, find the work done (in **joules**) by the string on the block of mass 0.36 kg during the first second after the system is released from rest.

(a)



10. Two rings of radius R and nR made of same material have the ratio of moment of inertia about an axis passing through centre is 1:8. The value of n is

(a) 2 (b)
$$2\sqrt{2}$$
 (c) 4 (d) $1/2$

11. A particle of mass 'm' is projected with a velocity v making an angle of 30° with the horizontal. The magnitude of angular momentum of the projectile about the point of projection when the particle is at its maximum height 'h' is

(a)
$$\frac{\sqrt{3}}{2} \frac{mv^2}{g}$$
 (b) zero (c) $\frac{mv^3}{\sqrt{2g}}$ (d) $\frac{\sqrt{3}}{16} \frac{mv^3}{g}$

- **12.** A disc is performing pure rolling on a smooth stationary surface with constant angular velocity as shown in figure. At any instant, for the lower most point of the disc v/R
 - (a) velocity is v, acceleration is zero (b) velocity is zero,
 - acceleration is zero
 - (c) velocity is v, acceleration is v^2/R
 - (d) velocity is zero, acceleration is v^2/R

13. There is a shell of mass M and density of the shell is uniform. The work done to take a point mass from point A to B is [AB = r]



14. A cube is subjected to a uniform volume compression. If the side of the cube decreases by 2% the bulk strain is

(a) 0.02 (b) 0.03 (c) 0.04 (d) 0.06

- A ball whose density is 0.4×10^3 kg/m³ falls into 15. water from a height of 9 cm. To what depth does the ball sink?
- (a) $2 \,\mathrm{cm}$ (b) $6 \,\mathrm{cm}$ (c) 4.5 cm (d) 2.25 cm **16.** Figure shows a copper rod joined to a steel rod. The rods have equal length and equal crosssectional area. The free end of the copper rod is kept at 0°C and that of steel rod is kept at 100°C. Find the temperature of the junction of the rod. Conductivity of copper = $390 \text{ W/m}^{\circ}\text{C}$. Conductivity of steel = $46 \text{ W/m} \circ \text{C}$

(a) 18.01°C (b) 26°C (c) 10.6°C (d) 20°C 17. If the radius of a star is *R* and it acts as a black body, what would be the temperature of the star, in which the rate of energy production is Q?

(a)
$$Q/4\pi R^2 \sigma$$
 (b) $(Q/4\pi R^2 \sigma)^{-1/2}$

- (c) $(4\pi R^2 Q/\sigma)^{1/4}$ (d) $(Q/4\pi R^2\sigma)^{1/4}$
- 18. A thermodynamical system is changed from state (P_1, V_1) to (P_2, V_2) by two different process, the quantity which will remain same will be (a) ΔQ (b) ΔW

(c)
$$\Delta Q + \Delta W$$
 (d) $\Delta Q - \Delta W$

- **19.** A Carnot's heat engine works between the temperatures 427°C and 27°C. What amount of heat should it consume per second to deliver mechanical work at the rate of 1.0 kW?
 - (b) 4.17 kcal/s (a) 0.417 kcal/s
 - (c) 41.7 kcal/s(d) 0.212 kcal/s
- A vessel containing 1 more of O₂ gas (molar mass 20. 32) at temperature T. The pressure of the gas is p. An identical vessel containing one mole of he gas (molar mass 4) at temperature 2T has a pressure of
 - (a) p/8 (c) 2 p (d) 8p (b) p

21. The temperature of an ideal gas is increased from 27° C to 127° C, then percentage increase in v_{rms} is

(a) 37% (b) 11% (c) 33% (d) 15.5%

22. Two gases occupy two containers A and B the gas in A, of volume $0.10m^3$, exerts a pressure of 1.40 MPa and that in B of volume $0.15m^3$ exerts a pressure 0.7 MPa. The two containers are united by a tube of negligible volume and the gases are allowed to intermingle. Then if the temperature remains constant, the final pressure in the container will be (in MPa)

(a) 0.70 (b) 0.98 (c) 1.40 (d) 210

- 23. An instantaneous displacement of a simple harmonic oscillator is $x = A \cos (\omega t + \pi/4)$. Its speed will be maximum at time
 - (a) $\pi/4 \omega$ (b) $\pi/2 \omega$ (c) π/ω (d) $2 \pi/\omega$
- 24. Two waves of wavelengths 99 cm and 100 cm both travelling with velocity 396 m/s are made to interfere. The number of beats produced by them per second is

(a) 1 (b) 2 (c) 4 (d) 8

25. If equation of transverse wave is $y = x_0 \cos 2\pi \left(nt - \frac{x}{\lambda} \right)$. Maximum velocity of particle is

twice of wave velocity, if λ is-

(a) $\pi/2x_0$ (b) $2\pi x_0$ (c) πx (d) πx_0

26. Three equal charges (q) are placed at corners of an equilateral triangle of side a. The force on any charge is

(a) zero
(b)
$$\sqrt{3} \frac{Kq^2}{a^2}$$

(c) $\frac{Kq^2}{\sqrt{3}a^2}$
(d) $3\sqrt{3} \frac{Kq^2}{a^2}$

27. Two identical capacitors, have the same capacitance C. One of them is charged to potential V_1 and the other to V_2 . The negative ends of the capacitors are connected together. When the positive ends are also connected, the decrease in energy of the combined system is –

(a)
$$\frac{1}{4}C(V_1^2 - V_2^2)$$
 (b) $\frac{1}{4}C(V_1^2 + V_2^2)$
(c) $\frac{1}{4}C(V_1 - V_2)^2$ (d) $\frac{1}{4}C(V_1 + V_2)^2$

- 28. What should be the characteristic of fuse wire?(a) High melting point, high specific resistance.
 - (b) Low melting point, low specific resistance.
 - (c) High melting point, low specific resistance.
 - (d) Low melting point, high specific resistance.

29. In the circuit shown in figure potential difference between points A and B is 16 V. the current passing through 2Ω resistance will be

(a) 2.5A (b) 3.5A (c) 4.0A (d) zero
30. Two parallel conductors carry current in opposite directions as shown in figure. One conductor carries a current of 10.0 A. Point C is a distance

 $\frac{d}{2}$ to the right of the 10.0 A current. If d = 18 cm

and I is adjusted so that the magnetic field at C is zero, the value of the current I is

 $I \downarrow \uparrow 10.0 A$

- (a) 10.0A
- (b) 30.0 A
- (c) 8.0A
- (d) 18.0A
- **31.** A uniform electric field and uniform magnetic field are acting along the same direction in a certain region. If an electron is projected in the region such that its velocity is pointed along the direction of fields, then the electron
 - (a) will turn towards right of direction of motion
 - (b) speed will decrease
 - (c) speed will increase
 - (d) will turn towards left direction of motion
- **32.** Eddy currents are produced when
 - (a) a metal is kept in varying magnetic field
 - (b) a metal is kept in steady magnetic field
 - (c) a circular coil is placed in a magnetic field
 - (d) through a circular coil, current is passed
- **33.** Two coaxial solenoids are made by winding thin insulated wire over a pipe of cross-sectional area $A = 10 \text{ cm}^2$ and length = 20 cm. If one of the solenoid has 300 turns and the other 400 turns, their mutual inductance is

 $(\mu_0 = 4\pi \times 10^{-7} \,\mathrm{Tm}\,\mathrm{A}^{-1})$

(a)
$$2.4\pi \times 10^{-5}$$
 H (b) $4.8\pi \times 10^{-4}$ H

(c) $4.8\pi \times 10^{-5}$ H (d) $2.4\pi \times 10^{-4}$ H

34. The ratio of secondary and primary turns of step-up transformer is 4 : 1. If a current of 4 A is applied to the primary, the induced current in secondary will be

(a) 8A (b) 2A (c) 1A (d) 0.5A

- **35.** Which of the following electromagnetic radiations has the smallest wavelength?
 - (a) Ultraviolet rays (b) X-rays
 - (c) γ-rays (d) Microwaves
- **36.** When light is refracted, which of the following does not change ?
 - (a) Wavelength (b) Frequency
 - (c) Velocity (d) Amplitude
- **37.** The given lens is broken into four parts and rearranged as shown. If the initial focal length is f then after rearrangement the equivalent focal length is
- **38.** In Young's double slit experiment 10th order maximum is obtained at the point of observation in the interference pattern for $\lambda = 7000$ Å. If the source is replaced by another one of wavelength 5000 Å then the order of maximum at the same point will be
 - (a) 12 th (b) 14 th (c) 16 th (d) 18 th
- **39.** Transfer characteristics [output voltage (V_0) vs input voltage (V_1)] for a base biased transistor in CE configuration is as shown in the figure. For using transistor as a switch, it is used
 - (a) in region (III)
 (b) both in region (I)
 (c) in region (II)
 (d) in region (I)
- **40.** The circuit is equivalent to



PART - II : CHEMISTRY

- **41.** How many grams of concentrated nitric acid solution should be used to prepare 250 mL of 2.0M HNO₃? The concentrated acid is 70% HNO₃.
 - (a) 90.0 g conc. HNO_3
 - (b) $70.0 \text{ g conc. HNO}_3$
 - (c) $54.0 \text{ g conc. HNO}_3$
 - (d) $45.0 \text{ g conc. HNO}_3$

42. The Bohr orbit radius for the hydrogen atom (n = 1) is approximately 0.530 Å. The radius for the first excited state (n = 2) orbit is (in Å)

(a) 0.13 (b) 1.06 (c) 4.77 (d) 2.12

- **43.** The screening effect of *d*-electrons is
 - (a) Equal to *p*-electrons
 - (b) Much more than *p*-electrons
 - (c) Same as *f*-electrons
 - (d) Less than *p*-electrons.
- **44.** When the first ionisation energies are plotted against atomic number, the peaks are occupied by
 - (a) Alkali metals
 - (b) Rare gases
 - (c) Halogens
 - (d) Transition elements
- **45.** The ions O²⁻, F⁻, Na⁺, Mg²⁺ and Al³⁺ are isoelectronic. Their ionic radii show :
 - (a) A decrease from O^{2-} to F^- and then increase from Na^+ to Al^{3+}
 - (b) A significant increase from O²⁻ to Al³⁺
 - (c) A significant decrease from O^{2-} to Al^{3+}
 - (d) An increase from O^{2-} to F^- and then decrease from Na^+ to Al^{3+}
- **46.** Using MOT, which of the following pairs denote paramagnetic species?
 - (a) B_2 and C_2 (b) B_2 and O_2
 - (c) N_2 and C_2 (d) O_2 and O_2^{2-1}
- 47. Increasing order of rms velocities of H_2 , O_2 , N_2 and HBr is
 - (a) $H_2 > O_2 > N_2 > HBr$
 - (b) $HBr < O_2 < N_2 < H_2$
 - (c) $H_2 > N_2 < O_2 > HBr$
 - (d) $HBr > N_2 < O_2 < H_2$
- **48.** For the dissociation reaction, $H_2(g) \rightarrow 2H(g) \qquad \Delta H = 162$ Kcal, heat of atomisation of H is (a) 81 Kcal (b) 162 Kcal
 - (c) 208 Kcal (d) 218 Kcal
- **49.** The enthalpy of combustion of 2 moles of benzene at 27°C differs from the value determined in bomb calorimeter by
 - (a) -2.494 kJ (b) 2.494 kJ (c) -7.483 kJ (d) 7.483 kJ

- **50.** If 1.0 mole of I₂ is introduced into 1.0 litre flask at 1000 K, at equilibrium ($K_c = 10^{-6}$), which one is correct?
 - (a) $[I_2(g)] > [I^-(g)]$
 - (b) $[I_2(g)] < [I^-(g)]$
 - (c) $[I_2(g)] = [I^-(g)]$
 - (d) $[I_2(g)] = \frac{1}{2}[I^-(g)]$
- 51. For the reaction $CO(g) + (1/2)O_2(g) \longrightarrow CO_2(g), K_p/K_c$ is (a) RT (b) $(RT)^{-1}$
 - (c) $(RT)^{-1/2}$ (d) $(RT)^{1/2}$
- **52.** The oxidation state of sulphur in $Na_2S_4O_6$ is

(a) +6 (b)
$$\frac{+3}{2}$$

(c) $\frac{+5}{2}$ (d) -2

53. When same amount of zinc is treated separately with excess of sulphuric acid and excess of sodium hydroxide solution, the ratio of volumes of hydrogen evolved is:

(a) 1:1 (b) 1:2 (c) 2:1 (d) 9:4

- **54.** The alkali metals form salt-like hydrides by the direct synthesis at elevated temperature. The thermal stability of these hydrides decreases in which of the following orders ?
 - (a) CsH > RbH > KH > NaH > LiH
 - (b) KH > NaH > LiH > CsH > RbH
 - (c) NaH > LiH > KH > RbH > CsH
 - (d) LiH > NaH > KH > RbH > CsH
- **55.** The most stable carbanion among the following is :



56. Among the following four structures I to IV,

$$C_{2}H_{5} - CH - C_{3}H_{7}, CH_{3} - C - CH - C_{2}H_{5}$$

$$C_{2}H_{5} - CH - C_{3}H_{7}, CH_{3} - C - CH - C_{2}H_{5}$$

$$(I) \qquad (II)$$

$$H - C + C_{2}H_{5} - CH - C_{2}H_{5}$$

$$H - C + C_{2}H_{5} - CH - C_{2}H_{5}$$

$$(III) \qquad (IV)$$

it is true that

- (a) only I and II are chiral compounds.
- (b) only III is a chiral compound.
- (c) only II and IV are chiral compounds.
- (d) all four are chiral compounds.
- **57.** The number of enantiomers of the compound CH₃CHBrCHBrCOOH is
- (a) 0 (b) 1 (c) 3 (d) 4
 58. Which one of the following reactions is expected to readily give a hydrocarbon product in good yields ?
 - (a) RCOOK $\xrightarrow{\text{Electrolytic}}$ oxidation
 - (b) RCOO⁻Ag⁺ $\xrightarrow{\text{Br}_2}$ \rightarrow
 - (c) $CH_3CH_3 \xrightarrow{Cl_2}_{hv}$
 - (d) $(CH_3)_3CCl \xrightarrow{C_2H_5OH}$
- **59.** What will be the main product when acetylene reacts with hypochlorous acid?
 - (a) Trichloroacetaldehyde
 - (b) Acetaldehyde
 - (c) Dichloroacetaldehyde
 - (d) Chloro acetaldehyde
- **60.** The greenhouse effect is because of the
 - (a) presence of gases, which in general are strong infrared absorbers, in the atmosphere.
 - (b) presence of CO_2 only in the atmosphere.
 - (c) presence of O_3 and CH_4 in the atmosphere.
 - (d) N_2O and chlorofluorohydrocarbons in the atmosphere.
- 61. Due to Frenkel defect, the density of ionic solids
 - (a) decreases (b) increases
 - (c) does not change (d) changes

- **62.** Equal weights of NaCl and KCl are dissolved separately in equal volumes of solutions. Molarity of the two solutions will be :
 - (a) Equal
 - (b) That of NaCl will be less than that of KCl
 - (c) That of NaCl will be more than that of KCl solution
 - (d) That of NaCl will be about half of that of KCl solution
- 63. A current of 2.0 A passed for 5 hours through a molten metal salt deposits 22.2 g of metal (At wt. = 177). The oxidation state of the metal in the metal salt is

(a)
$$+1$$
 (b) $+2$ (c) $+3$ (d) $+4$

- 64. The electrolytic cells, one containing acidified ferrous chloride and another acidified ferric chloride are connected in series. The ratio of iron deposited at cathodes in the two cells when electricity is passed through the cells will be
 (a) 3:1 (b) 2:1 (c) 1:1 (d) 3:2
- **65.** Velocity constant of a reaction at 290 K was found to be 3.2×10^{-3} . At 300 K it will be
 - (a) 1.28×10^{-2} (b) 9.6×10^{-3}
 - (c) 6.4×10^{-3} (d) 3.2×10^{-4}
- **66.** At high pressure, the entire surface gets covered by a monomolecular layer of the gas follows
 - (a) three-halved order (b) second-order
 - (c) first-order (d) zero-order
- **67.** Which of the following is incorrect with respect to property indicated ?
 - (a) E.N:F>Cl>Br
 - (b) E.A: Cl > F > Br
 - (c) Oxidising power: $F_2 > Cl_2 > Br_2$
 - (d) Bond energy: $F_2 > \tilde{C}l_2 > \tilde{B}r_2$
- 68. Strong reducing behaviour of H₃PO₂ is due to
 (a) presence of one -OH group and two P-H
 - bonds
 - (b) high electron gain enthalpy of phosphorus
 - (c) high oxidation state of phosphorus
 - (d) presence of two –OH groups and one P–H bond
- **69.** The pair in which both species have same magnetic moment (spin only value) is :
 - (a) $[Cr(H_2O)_6]^{2+}, [CoCI_4]^{2-}$
 - (b) $[Cr(H_2O_6)^{2+}, [Fe(H_2O_6)^{3+}]^{3+}$
 - (c) $[Mn(H_2O)_6)^{2+}, [Cr(H_2O)_6]^{2+}$
 - (d) $[CoCl_4)^{2-}, [Fe(H_2O)_6]^{2+}$

- **70.** Which of the following is less acidic among the given halogen compounds?
 - (a) CHF_3 (b) CHI_3
 - (c) CHCl₃ (d) CHBr₃
- 71. In a S_N^2 substitution reaction of the type $R - Br + Cl^- \xrightarrow{DMF} R - Cl + Br^$ which one of the following has the highest relative rate ?

(a)
$$CH_3 - CH_2 - CH_2Br$$

(b)
$$CH_3 - CH - CH_2Br$$

 $|$
 CH_3
 CH_3
(c) $CH_3 - C - CH_2Br$
 $|$
 CH_3

(d)
$$CH_3CH_2Br$$

Which of the following is not the product of

72.





73. What will be the correct structural formula of product for the following reaction?



- 74. Nucleophilic addition reaction will be most favoured in
 - (a) $(CH_3)_2C = O$
 - (b) CH_3CH_2CHO

- (d) $CH_3 CH_2 CH_2 \overset{\|}{C} CH_3$
- 75. Identify the prdouct C in the series

$$CH_{3}CN \xrightarrow{Na/C_{2}H_{5}OH} A$$

$$\xrightarrow{HNO_{2}} B \xrightarrow{Cu/573K} C$$
(a) CH_{3}COOH
(b) CH_{3}CH_{2}NHOH
(c) CH_{3}CONH_{2}
(d) CH_{3}CHO
When NH is passed over bested metal A its

0

- 76. When NH₃ is passed over heated metal A, its amide is formed. The metal is
 (a) Mg
 (b) K
 (c) Al
 (d) Pb
- 77. Insulin production and its action in human body are responsible for the level of diabetes. This compound belongs to which of the following categories ?
 - (a) An enzyme (b) A hormone
 - (c) A co-enzyme (d) An antibiotic
- **78.** Which statement is incorrect about peptide bond?
 - (a) C–N bond length in proteins is longer than usual C–N bond length.
 - (b) Spectroscopic analysis shows planar structure of -C-NH- bond.
 II
 O
 - (c) C-N bond length in proteins is smaller than usual C-N bond length.
 - (d) None of these
- **79.** A mixture of chlorides of copper, cadmium, chromium, iron and aluminium was dissolved in water acidified with HCl and hydrogen sulphide gas was passed for sufficient time. It was filtered, boiled and a few drops of nitric acid were added while boiling. To this solution ammonium chloride and sodium hydroxide were added and filtered. The filterate shall give test for.
 - (a) Sodium and iron
 - (b) Sodium and aluminium
 - (c) Aluminium and iron
 - (d) Sodium, iron, cadmium and Al
- **80.** Volume of 3% solution of sodium carbonate necessary to neutralise a litre of 0.1 N sulphuric acid

(a)	176.66 ml	(b)	156.6 ml	
(c)	116.0 ml	(d)	196.1 ml	

PART - III : MATHEMATICS

81. A class has 175 students. The following data shows the number of students obtaining one or more subjects. Mathematics 100, Physics 70, Chemistry 40; Mathematics and Physics 30, Mathematics and Chemistry 28, Physics and Chemistry 23; Mathematics, Physics and Chemistry 18. How many students have offered Mathematics alone?

(a) 35 (b) 48 (c) 60 (d) 22
82. If
$$x \sin^3 \theta + y \cos^3 \theta = \sin \theta \cos \theta$$
 and $x \sin \theta = y \cos \theta$, then $x^2 + y^2 =$

- (a) 1 (b) 2
- (c) 0 (d) None of these
- 83. If $\cos 7\theta = \cos \theta \sin 4\theta$, then the general value of θ is

(a)
$$\frac{n\pi}{6}, \frac{n\pi}{3} + (-1)^n \frac{\pi}{18}$$

(b)
$$\frac{n\pi}{3}, \frac{n\pi}{3} + (-1)^n \frac{\pi}{18}$$

(c)
$$\frac{n\pi}{4}, \frac{n\pi}{3} \pm \frac{\pi}{18}$$

(d)
$$\frac{n\pi}{4}, \frac{n\pi}{3} + (-1)^n \frac{\pi}{18}$$

- 84. If the real part of $\frac{\overline{z}+2}{\overline{z}-1}$ is 4, $z \neq 1$, then the locus of the point representing z in the complex plane is
 - (a) a straight line parallel to x-axis
 - (b) a straight line equally inclined to axes
 - (c) a circle with radius 2
 - (d) a circle with radius $\frac{1}{2}$

85. If α and β are the roots of $x^2 - x + 1 = 0$, then the equation whose roots are α^{100} and β^{100} are

(a)
$$x^2 - x + 1 = 0$$
 (b) $x^2 + x - 1 = 0$

(c)
$$x^2 - x - 1 = 0$$
 (d) $x^2 + x + 1 = 0$

86. The set of all real x satisfying the inequality

$$\frac{3-|x|}{4-|x|} \ge 0, \text{ is}$$
(a) $[-3,3] \cup (-\infty,-4) \cup (4,\infty)$
(b) $(-\infty,-4) \cup (4,\infty)$
(c) $(-\infty,-3) \cup (4,\infty)$

(d) $(-\infty, -3) \cup (3, \infty)$

87. If x satisfies $|3x-2|+|3x-4|+|3x-6| \ge 12$, then

(a)
$$0 \le x \ge \frac{8}{3}$$
 (b) $x \ge \frac{8}{3}$ or $\frac{-4}{3}$
(c) $x \le 0$ or $x \ge \frac{8}{3}$ (d) $x \ge 2$ only

88. In how many ways can 5 boys and 5 girls be seated at a round table so that no two girls may be together ?

(a) 4! (b) 5! (c) 4! + 5! (d) $4! \times 5!$

- 89. A box contains two white balls, three black balls and four red balls. In how many ways can three balls be drawn from the box if at least one black ball is to be included in the draw?(a) 64 (b) 129
 - (c) 84 (d) None of these
- 90. The coefficient of the middle term in the expansion of $(2+3x)^4$ is:

(a) 6 (b) 5! (c) 8! (d) 216

- **91.** If C_0 , C_1 , C_2 , ..., C_n denote the binomial coefficients in the expansion of $(1 + x)^n$, then the value of
 - $\begin{array}{l} C_0 + (C_0 + C_1) + (C_0 + C_1 + C_2) + \dots \\ + (C_0 + C_1 + \dots + C_{n-1}) \\ (a) \quad n.2^{n-1} \qquad (b) \quad n.2^n \\ (c) \quad (n-1).2^{n-1} \qquad (d) \quad (n-1).2^n \end{array}$
- **92.** The sum of the series $1+2.2+3.2^2+4.2^3+....+100.2^{99}$ is (a) $100.2^{100}+1$ (b) $99.2^{100}+1$ (c) $99.2^{100}-1$ (d) $100.2^{100}+1$
- 93. The quadratic equation whose roots are the x and y intercepts of the line passing through (1, 1) and making a triangle of area A with the co-ordinate axes is
 - (a) $x^2 + Ax + 2A = 0$
 - (b) $x^2 2Ax + 2A = 0$
 - $(c) \quad x^2 Ax + 2A = 0$
 - (d) None of these
- 94. If $4a^2 + b^2 + 2c^2 + 4ab 6ac 3bc = 0$, the family of lines ax + by + c = 0 is concurrent at one or the other of the two points-

(a)
$$\left(-1, -\frac{1}{2}\right), (-2, -1)$$

(b) $(-1, -1), \left(-2, -\frac{1}{2}\right)$

(c)
$$(-1, 2), \left(\frac{1}{2}, -1\right)$$

(d) $(1, 2), \left(\frac{1}{2}, -1\right)$

- **95.** A pair of tangents are drawn from the origin to the circle $x^2 + y^2 + 20(x + y) + 20 = 0$, then the equation of the pair of tangent are
 - (a) $x^{2} + y^{2} 5xy = 0$ (b) $x^{2} + y^{2} + 2x + y = 0$ (c) $x^{2} + y^{2} - xy + 7 = 0$ (d) $x^{2} - 2x^{2} - 5xy = 0$
 - (d) $2x^2 + 2y^2 + 5xy = 0$
- **96.** An ellipse has OB as semi minor axis, F and F' its focii and the angle FBF' is a right angle. Then the eccentricity of the ellipse is

(a)
$$\frac{1}{\sqrt{2}}$$
 (b) $\frac{1}{2}$ (c) $\frac{1}{4}$ (d) $\frac{1}{\sqrt{3}}$

- 97. If the line 2x 3y = k touches the parabola $y^2 = 6x$, then find the value of k. (a) -15/4 (b) -27/4 (c) -1/4 (d) -3/4
- 98. S and T are the foci of an ellipse and B is an end of the minor axis. If STB is an equilateral triangle, then the eccentricity of the ellipse is

(a)
$$\frac{1}{4}$$
 (b) $\frac{1}{3}$ (c) $\frac{1}{2}$ (d) $\frac{2}{3}$

99. Let $f(x) = (x^5 - 1)(x^3 + 1)$, $g(x) = (x^2 - 1)(x^2 - x + 1)$ and let h(x) be such that f(x) = g(x)h(x). Then $\lim h(x)$ is

 $\lim_{x \to 1} h(x)$ is

(a) 0 (b) 1 (c) 3 (d) 5

- **100.** In the truth table for the statement $(p \land q) \rightarrow (q \lor \sim p)$, the last column has the truth value in the following order is
 - (a) TTFF (b) FTTT
 - (c) TFTT (d) TTTT
- 101. If the value of mode and mean is 60 and 66 respectively, then the value of median is(a) 70 (b) 64 (c) 90 (d) 50
- 102. Find the variance of the data given below

Size of item	3.5	4.5	5.5	6.5	7.5	8.5	9.5
Frequency	3	7	22	60	85	32	8
(a) 1.2		(b) 2.19					
(c) 1.3	2			(d) N	Jone of	of thes	se

- **103.** Let *R* be the relation on the set *R* of all real numbers, defined by aRb If $|a-b| \le 1$. Then, *R* is
 - (a) reflexive and symmetric only
 - (b) reflexive and transitive only
 - (c) equivalence
 - (d) None of the above
- **104.** The greatest and least values of $(\sin^{-1} x)^2 + (\cos^{-1} x)^2$ are respectively
 - (a) $\frac{\pi^2}{4}$ and 0 (b) $\frac{\pi}{2}$ and $\frac{-\pi}{2}$ (c) $\frac{5\pi^2}{4}$ and $\frac{\pi^2}{8}$ (d) $\frac{\pi^2}{4}$ and $\frac{-\pi^2}{4}$
- 105. The value of

$$\cos\left[\frac{1}{2}\cos^{-1}\left(\cos\left(\sin^{-1}\frac{\sqrt{63}}{8}\right)\right)\right] \text{ is } -$$
(a) 3/16 (b) 3/8 (c) 3/4 (d) 3/2
106. The determinant
$$\begin{vmatrix}1 & (x-3) & (x-3)^2\\ 1 & (x-4) & (x-4)^2\\ 1 & (x-5) & (x-5)^2\end{vmatrix}$$

vanishes for

- (a) 3 values of x (b) 2 values of x
- (c) 1 values of x (d) No value of x 107. If the lines $\ell x + my + n = 0$, $mx + ny + \ell = 0$ and $nx + \ell y + m = 0$ are concurrent then
 - (a) $\ell + m + n = 0$ (b) $\ell m n = 0$ (c) $\ell + m - n = 0$ (d) $m + n - \ell = 0$
- **108.** If $y=1+x+\frac{x^2}{2!}+\frac{x^3}{3!}+...\infty$, then $\frac{dy}{dx}$ is equal to (a) x (b) 1
 - (c) y (d) None of these

109. If
$$f(x) = \begin{cases} \frac{x^2 + 3x - 10}{x^2 + 2x - 15}, & \text{when } x \neq -5 \\ a, & \text{when } x = -5 \end{cases}$$

is continuous at x = -5, then the value of 'a' will be (a) 3/2 (b) 7/8 (c) 8/7 (d) 2/3

110. The equation of all lines having slope 2 which are tangent to the curve $y = \frac{1}{x-3}, x \neq 3$, is (a) y=2 (b) y=2x(c) y=2x+3 (d) None of these

- 111. The function $f(x) = (x(x-2))^2$ is increasing in the set
 - (a) $(-\infty, 0) \cup (2, \infty)$ (b) $(-\infty, 1)$
- (c) $(0, 1) \cup (2, \infty)$ (d) (1, 2)112. If $a^2 x^4 + b^2 y^4 = c^4$, then the maximum value of xv is

(a)
$$\frac{c}{\sqrt{ab}}$$
 (b) $\frac{c^2}{2\sqrt{ab}}$ (c) $\frac{c}{2\sqrt{ab}}$ (d) $\frac{c^2}{\sqrt{2ab}}$

113.
$$\int \frac{(x^2 - 1)}{(x^2 + 1)\sqrt{x^4 + 1}} dx \text{ is equal to}$$

(a) $\sec^{-1}\left(\frac{x^2 + 1}{\sqrt{2}x}\right) + c$
(b) $\frac{1}{\sqrt{2}}\sec^{-1}\left(\frac{x^2 + 1}{\sqrt{2}x}\right) + c$
(c) $\frac{1}{\sqrt{2}}\sec^{-1}\left(\frac{x^2 + 1}{\sqrt{2}}\right) + c$

114. Evaluate
$$\int_{0}^{\pi/2} \frac{\sin x}{1 + \cos^2 x} dx$$

(a)
$$\pi/2$$
 (b) $\pi/4$ (c) $\pi/3$ (d) π
115. Area intercepted by the curves $y = \cos x$, $x \in [0, \pi]$ and $y = \cos 2x$, $x \in [0, \pi]$, is

(a)
$$\frac{3\pi}{2}$$
 (b) $\frac{3\sqrt{3}}{2}$ (c) $\frac{3\pi}{4}$ (d) $\frac{3\sqrt{3}}{4}$

- **116.** The general solution of the differential equation
 - $\frac{dy}{dx} + \sin(x+y) = \sin(x-y) \text{ is}$ (a) $\log \tan y + \sin x = C$ (b) $\log \tan \frac{y}{2} + 2\sin x = C$

(c)
$$\tan\frac{y}{2} + \log\sin x = C$$

- (d) None of these
- 117. The solution to the differential equation

$$\frac{dy}{dx} = \frac{yf'(x) - y^2}{f(x)} \text{ where } f(x) \text{ is a given function}$$

is
(a) $f(x) = y(x+c)$ (b) $f(x) = cxy$
(c) $f(x) = c(x+y)$ (d) $yf(x) = cx$

118. If $\vec{a}, \vec{b}, \vec{c}$ are three unit vectors such that $\vec{a} + \vec{b} + \vec{c} = \vec{0}$, where $\vec{0}$ is null vector, then $\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a}$ is .

(a)
$$-3$$
 (b) -2 (c) $-\frac{3}{2}$ (d) 0

119. If vectors 2i - j + k, i + 2j - 3k and 3i + aj + 5k are coplanar, then the value of a is (a)

a) 2 (b)
$$-2$$
 (c) -1 (d) -4

120. The coordinates of the point where the line through the points A(3, 4, 1) and B(5, 1, 6) crosses the XY-plane are

(a)
$$\left(\frac{13}{5}, \frac{23}{5}, 0\right)$$
 (b) $\left(-\frac{13}{5}, \frac{23}{5}, 0\right)$
(c) $\left(\frac{13}{5}, -\frac{23}{5}, 0\right)$ (d) $\left(-\frac{13}{5}, \frac{-23}{5}, 0\right)$

- 121. Find the angle between the two planes 2x+y-2z=5and 3x - 6y - 2z = 7.
- (a) $\cos^{-1}(4/21)$ (b) $\cos^{-1}(2/21)$ (c) $\cos^{-1}(1/21)$ (d) $\cos^{-1}(5/21)$ **122.** For k = 1, 2, 3 the box B_k contains k red balls and

(k+1) white balls. Let $P(B_1) = \frac{1}{2}$, $P(B_2) = \frac{1}{3}$ and $P(B_3) = \frac{1}{6}$. A box is selected at random and a ball

is drawn from it. If a red ball is drawn, then the probability that it has come from box B₂, is

(a)
$$\frac{35}{78}$$
 (b) $\frac{14}{39}$ (c) $\frac{10}{13}$ (d) $\frac{12}{13}$

123. The probability of India winning a test match against West Indies is 1/2. Assuming independence from match to match, the probability that in a 5 match series India's second win occurs at the third test, is -

- 124. An object is obseved from the points A, B and C lying in a horizontal straight line which passes directly underneath the object. The angular elevation at B is twice that at A and at C three times that at A. It AB = a, BC = b, then the height of the object is
 - (a) $\frac{b}{2a}\sqrt{(a+b)(3b-a)}$ (b) $\frac{a}{b}\sqrt{(a+b)(3b-a)}$

(c)
$$\frac{a}{2b}\sqrt{(a+b)(3b-a)}$$
 (d) $\frac{2a}{b}\sqrt{(a+b)(3b-a)}$

- **125.** A shopkeeper wants to purchase two articles A and B of cost price `4 and `3 respectively. He thought that he may earn 30 paise by selling article A and 10 paise by selling article B. He has not to purchase total articles worth more than `24. If he purchases the number of articles of A and B, x and y respectively, then linear constraints are
 - (a) $x \ge 0, y \ge 0, 4x + 3y \le 24$
 - (b) $x \ge 0, y \ge 0, 30x + 10y \le 24$
 - (c) $x \ge 0, y \ge 0, 4x + 3y \ge 24$
 - (d) $x \ge 0, y \ge 0, 30x + 40y \ge 24$

PART - IV : ENGLISH

DIRECTIONS (Qs. 126 - 128): Out of the four alternatives, choose the one which express the correct meaning of the word.

126.	SAC	GACIOUS		
	(a)	Shameless	(b)	Wise
	(c)	Powerless	(d)	Foolish
127.	REN	/IEDIAL		
	(a)	Corrective	(d)	Proficient
	(c)	Damaging	(d)	Optional
128.	RET	ICENT		
	(a)	Confident	(d)	Sad
	(c)	Truthful	(d)	Secretive

DIRECTIONS (Os. 129 - 131): Choose the word opposite is meaning to the given word.

129.	FID	ELITY		
	(a)	Faith	(b)	Devotedness
	(c)	Allegiance	(d)	Treachery
130.	INF	RANGIBLE		
	(a)	Complecated	(d)	Breakable
	(c)	Weird	(d)	Software
131.	PRO	GENY		
	(a)	Kid	(b)	Parent
	(c)	Friend	(d)	Enemy

DIRECTIONS (Qs. 132 - 134): A part of sentence is underlined. Below are given alternatives to the underlined part (a), (b), (c) and (d) which may improve the sentence. Choose the correct alternative.

- 132. It was not possible to drag any conclusion so he left the case. (a) Fetch (b) Find
 - (d) No improvement (c) Draw

133.	I am looking after my pen which is missing.						
	(a)	Looking for	(b)	Looking in			
	(c)	Looking back	(d)	No improvement			
134.	"Mi	nd your language !	" he	shouted.			
	(a)	change	(b)	inspect			
	(c)	hold	(d)	No improvement			
DIRI	ECT	IONS (Qs. 135 - 137): Fil	l in the blanks.			
135.	I	. to go there when I	was	student.			
	(a)	liked	(b)	used			
	(c)	prefer	(d)	denied			
136.	She	was angry me.					
	(a)	at	(d)	about			
	(c)	with	(d)	in			
137.	• You should not laugh the poor.						
	(a)	on	(b)	at			
	(c)	with	(d)	over			

DIRECTIONS (Qs. 138 - 140): In the questions below, each passage consists of six sentences. The first and sixth sentence are given in the beginning. The middle four sentences in each have been removed and jumbled up. These are labeled as P, Q, R and S. Find out people order for the four sentences.

138. 1. He is a famous doctor.

- P. Once I had to consult with him.
- Q. I never believed him.
- R. He suggested me a proper remedy.
- S. I become completely fine.
- 6. Now I also admit this fact.
- (a) PORS (b) OPSR
- (c) QPRS (d) RQSP
- **139.** 1. We don't know the plan of Ram.
 - P. He cares for his friends.
 - Q. He is a complete person.
 - R. We want some help and advice.
 - S. As we are in a trouble.
 - 6. We hope he will do his best for us.
 - (a) PRSQ (b) QPRS
 - (c) PQRS (d) PSRQ
- **140.** 1. It is not my problem.
 - P. All residents of this society are careless.
 - Q. I am unable to convince anyone.
 - R. They don't want to do some good.
 - S. Every one seems to be unwise here.
 - 6. We all have to suffer one day.
 - (a) PRSQ (b) PRQS
 - $(c) PQRS \qquad (d) PSRQ$

- 141. In a certain code language 'DOME' is written as '8943' and 'MEAL' is written as '4321'. What group of letters can be formed for the code '38249'?
 - (a) EOADM (b) MEDOA
 - (c) EMDAO (d) EDAMO
- **142.** Find the missing number from the given response.



143. Which of the following correctly represents the relationship among illiterates, poor people and unemployed?



- 144. Sushma walks 20m towards north. Then she turns right and walks 30m. Now, she turns right and walks 35m. Now turning left, she walks 15m. Again, she turns left and moves 15m. Finally, she turns left and walks 15m. In which direction and how far is she from her original position.
 - (a) 15m East
 - (c) 15m West (d) 45 m West
- **145.** In a classroom, there are 5 rows and 5 children A, B, C, D and E are seated one behind the other in 5 separate rows as follows.
 - A is sitting behind C but in front of B.
 - C is sitting behind E and D is sitting in front of E.

(b) $30 \,\mathrm{m \, East}$

- The order in which they are sitting from the first row to the last is
- (a) DECAB (b) BACED
- (c) ACBDE (d) ABEDC
- **146.** Which of the following will fill the series? 2, 9, 28, ?, 126
 - (a) 64 (b) 65 (c) 72 (d) 56

147. Two signs in the equations have been interchanged, find out the two signs to make equation correct.

$$3 \div 5 \times 8 + 2 - 10 = 13$$

- (a) + and (b) \times and \div
- (c) \div and (d) \div and +
- 148. Assertion: [A] India is a democratic country.Reason: [R] India has a constitution of its own.Choose the correct alternative from the given options.
 - (a) Both (A) and (R) are true and (R) is correct explanation of (A).
 - (b) Both (A) and (R) are true but (R) is not the correct explanation of (A).
 - (c) (A) is true (R) is false.
 - (d) (A) is false (R) is true.
- **149.** Which one of the following figures completes the original figure?



150. How many squares are there in the following figure?



SUU

PART-I: PHYSICS

1. It can be observed that component of **(a)** acceleration perpendicular to velocity is $a = 4 \text{ m/s}^2$

r. radius =
$$\frac{v^2}{a_c} = \frac{(2)^2}{4} = 1$$
 metre

2. (a) Let us draw the figure for given situation,

$$4t = 6 + \frac{1}{2} \times 1.2 \times t^{2}$$

$$\Rightarrow$$
 4t = 6 + 0.6t²

(a) Let $V = kT^a A^b \rho^c$, 3.

.

 \Rightarrow

k = dimensional constant Writing dimension on both we side $[LT^{-1}] = [MLT^{-2}]^a [L^2]^b [ML^{-3}]^c$ $= [M^{a+c}L^{a+2b-3c}T^{-2a}]$

Comparing power on both sides we have a + c = 0, a + 2b - 3c = 1, -2a = -1

$$\therefore$$
 $a = \frac{1}{2}, c = -\frac{1}{2} \Longrightarrow b = -\frac{1}{2} \therefore V = k \sqrt{\frac{T}{A\rho}}$

- 4. (d) Here velocity is acting upwards when projectile is going upwards and acceleration is downwards. The angle θ between \vec{v} and \vec{a} is more than 0° and less than 180°.
- 5. (b) The condition to avoid skidding,

$$v = \sqrt{\mu rg} = \sqrt{0.6 \times 150 \times 10} = 30 \text{ m/s.}$$
(c) Applying Newton's law along string

ma

$$\Rightarrow T - m\sqrt{g^2 + a^2} = ma$$
or $T = m_2\sqrt{g^2 + a^2} + ma$

6.

$$T = m\sqrt{g^2 + a^2}$$

7. (c) Let the mass of block is m. It will remains stationary if forces acting on it are in equilibrium. i.e., ma $\cos \theta = \text{mg} \sin \theta$ \Rightarrow a = g tan θ

+ma



Here ma = Pseudo force on block, mg = weight.

(c)

8.

9.

10.

(c) Given m = 0.36 kg, M = 0.72 kg.The figure shows the forces on m and M. When the system is released, let the acceleration be *a*. Then <u>.....</u> T - mg = ma

$$Mg - T = Ma$$

$$a = \frac{(M - m)g}{M + m} = g / 3$$
and $T = 4 mg/3$
For block m:
$$u = 0, a = g/3, t = 1, s = ?$$

$$mg$$

$$M \downarrow a$$

$$s = ut + \frac{1}{2} at^2 = 0 + \frac{1}{2} \times \frac{g}{3} \times 1^2 = g/6$$

$$\therefore$$
 Work done by the string on *m* is

$$\vec{T}.\vec{s} = Ts = 4\frac{mg}{3} \times \frac{g}{6} = \frac{4 \times 0.36 \times 10 \times 10}{3 \times 6} = 8J$$

$$\Rightarrow \quad \frac{I_1}{I_2} = \frac{1}{n^3} = \frac{1}{8} \quad (given)$$

$$\therefore \quad n^3 = 8 \Rightarrow n = 2$$

11. (d) Angular momentum $L_0 = pr_{\perp}$

(:: linear momentum
$$p = mv \cos \theta$$
 and $r_{\perp} = H$)

$$\Rightarrow L_0 = mv \cos \theta H$$

= $mv \frac{\sqrt{3}}{2} \cdot \frac{v^2 \sin^2 30^\circ}{2g}$
= $\frac{\sqrt{3} mv^3}{16g}$

12. (d) As the disc is in combined rotation and translation, each point has a tangential velocity and a linear velocity in the forward direction. From figure 1

$$v_{net} \text{ (for lowest point)} = v - R\omega = v - v = 0$$

and acceleration
$$= \frac{v^2}{v} + 0 = \frac{v^2}{v}$$

and acceleration

$$\frac{v^2}{R} + 0 = \frac{v^2}{R}$$

(since linear speed is constant)

13. (d) Gravitaional field inside the shell is zero, so no work required.

16. (c) Heat current in first rod (copper)

$$\frac{390 \times A(0-\theta)}{\ell}$$

Here θ is temperature of the junction and A & ℓ are area and length of copper rod. Heat current in second rod (steel)

 $=\frac{46\times A(\theta-100)}{\ell}$

In series combination, heat current remains same. So,

$$\frac{390 \times A(0-\theta)}{\ell} = \frac{46 \times A(\theta-100)}{\ell}$$
$$-390 \theta = = 46 \theta - 4600$$
$$436 \theta = 4600 \Rightarrow \theta = 10.6^{\circ}C$$

17. (d) Stefan's law for black body radiation $Q = \sigma e A T^4$

$$T = \left[\frac{Q}{\sigma(4\pi R^2)}\right]^{1/4}$$

Here $e = 1$
 $A = 4\pi R^2$

- 18. (d) For all process $\Delta U = \Delta Q - \Delta W$ does not change as it depends on initial final states.
- 19. (a) The efficiency of the heat engine is

$$\eta = 1 - \frac{T_2}{T_1} = 1 - \left(\frac{273 + 27K}{273 + 427K}\right) = \frac{4}{7}$$

But $\eta = \frac{W}{Q_1}$
 $\therefore Q_1 = \frac{W}{\eta} = \frac{1.0kW}{4/7} = 1.75kW = 0.417 \text{ kcal/s}$

Thus, the engine would require 417 cal of heat per second, to deliver the requisite amount of work.

20. (c) Applying gas equation, pV = nRTWe can write, $p_1V = n_1RT_1$ and $p_2V = n_2RT_2$

$$\Rightarrow \quad \frac{p_2}{p_1} = \frac{n_2}{n_1} \times \frac{T_2}{T_1} = \frac{1}{1} \times \frac{2T}{T} = 2$$
$$\Rightarrow \quad p_2 = 2p$$

21. (d) We know,
$$V_{\text{rms}} = \sqrt{\frac{3\text{RT}}{M}}$$

$$\Rightarrow \% \text{ increase in}$$

$$V_{\text{rms}} = \frac{\sqrt{\frac{3RT_2}{M}} - \sqrt{\frac{3RT_1}{M}}}{\sqrt{\frac{3RT_1}{M}}} \times 100$$

$$= \frac{\sqrt{T_2} - \sqrt{T_1}}{\sqrt{T_1}} \times 100$$

$$= \frac{\sqrt{400} - \sqrt{300}}{\sqrt{300}} \times 100$$

$$= \frac{20 - 17.32}{\sqrt{300}} \times 100 = 15.50$$

 $= \frac{17.32}{17.32} \times 100 = 15.5\%$ 22. (b) We know that $P_A V_A = n_A RT, P_B V_B = n_B RT$ and $P_f (V_A + V_B) = (n_A + n_B) RT$ $P_f (V_A + V_B) = P_A V_A + P_B V_B$ $\therefore P_f = \left(\frac{P_A V_A + P_B V_B}{V_A + V_B}\right)$ $= \frac{1.4 \times 0.1 + 0.7 \times 0.15}{0.1 + 0.15} MPa = 0.98 MPa$

23. (a) Velocity,
$$v = \frac{dx}{dt} = -A \omega \sin (\omega t + \pi / 4)$$

Velocity will be maximum, when
 $\omega t + \pi / 4 = \pi / 2$ or $\omega t = \pi / 2 - \pi / 4 = \pi / 4$
or $t = \pi / 4 \omega$

24. (c) Velocity of wave
$$v = n\lambda$$

where $n =$ frequency of wave $\Rightarrow n = \frac{v}{\lambda}$
 $n_2 = \frac{v_2}{\lambda_2} = \frac{396}{100 \times 10^{-2}} = 396 \text{ Hz}$
no. of beats $= n_1 - n_2 = 4$

25. (d)
$$y = x_0 \cos 2\pi \left(nt - \frac{x}{\lambda} \right)$$

 $y = x_0 \cos \frac{2\pi}{\lambda} (vt - x) \quad [\because v = n\lambda]$
 $\left(\frac{dy}{dt} \right)_{max} = x_0 \times \frac{2\pi}{\lambda} v = 2v(given) \therefore \lambda = \pi x_0$

(b) $F_{\text{net}} = \sqrt{F^2 + F^2 + 2F^2 \cos 60^\circ} = \sqrt{3}F$ 26. 27. (a) Initial energy of combined system

$$U_1 = \frac{1}{2}CV_1^2 + \frac{1}{2}CV_2^2$$

Final common potential, $V = \frac{V_1 + V_2}{2}$, Final energy of system,

$$U_2 = 2 \times \frac{1}{2} C \left(\frac{V_1 + V_2}{2} \right)^2$$

Hence loss of energy = $U_1 - U_2$

$$=\frac{1}{4}C\left(V_{1}-V_{2}\right)^{2}$$

- (d) Fuse wire should be such that it melts 28. immediatley when strong current flows through the circuit. The same is possible if its melting point is low and resistivity is high.
- 29. $\therefore 4i_1 + 2(i_1 + i_2) - 3 + 4i_1 = 16V$...(i) **(b)** Using Kirchhoff's second law in the closed loop we have $9 - i_2 - 2(i_1 + i_2) = 0$...(ii) Solving equations (i) and (ii), we get $i_1 = 1.5 A \text{ and } i_2 = 2 A$

 \therefore current through 2W resistor = 2 + 1.5 = 3.5 A. **30.** (b) The magnetic field at C due to first conductor

is $B_1 = \frac{\mu_0}{2\pi} \frac{I}{3d/2}$ (since, point C is separated by $d + \frac{d}{2} = \frac{3d}{2}$ from 1st conductor). The direction of field is perpendicular to the plane of paper and directed outwards. The magnetic field at C due to second conductor is $\mathbf{B} = \frac{\mu_0}{\mu_0} \frac{10}{\mu_0}$ (since point C

is separated by
$$\frac{d}{2}$$
 from 2nd conductor)

The direction of field is perpendicular to the plane of paper and directed inwards. Since, direction of B₁ and B₂ at point C is in

opposite direction and the magnetic field at C is zero, therefore, $\mathbf{R} = \mathbf{F}$

$$\frac{\mu_0}{2\pi} \frac{I}{3d/2} = \frac{\mu_0}{2\pi} \frac{10}{d/2}$$

On solving I = 30.0 A

31. (b) \vec{v} and \vec{B} are in same direction so that magnetic force on electron becomes zero, only electric force acts. But force on electron due to electric field is opposite to the direction of velocity.

33. (d)
$$M = \frac{\mu_0 N_1 N_2 A}{\ell}$$
$$= \frac{4\pi \times 10^{-7} \times 300 \times 400 \times 100 \times 10^{-4}}{100}$$

$$= 2.4\pi \times 10^{-4} \text{ H}$$
(c)
$$\frac{\text{I}_{\text{S}}}{\text{I}_{\text{S}}} = \frac{\text{N}_{\text{P}}}{\text{I}_{\text{S}}} = \frac{1}{\text{I}} \Rightarrow \text{I}_{\text{S}} = \frac{1}{\text{I}} \times 4 = \frac{1}{\text{I}}$$

NT NT 4

34. (c)
$$\frac{I_S}{I_P} = \frac{I_V P}{N_S} = \frac{I}{4} \Rightarrow I_S = \frac{I}{4} \times 4 = 1 \text{ A}$$

35. (c)

36. (b) Frequency does not change on refraction.

0.2

37. (b) Cutting a lens in transverse direction
doubles their focal length i.e. 2*f*.
Using the formula of equivalent focal length,
$$\frac{1}{f} = \frac{1}{f_1} + \frac{1}{f_2} + \frac{1}{f_3} + \frac{1}{f_4}$$
We get equivalent focal length as *f*/2.
38. (b) $n_1 \lambda_1 = n_2 \lambda_2$

- $n_1 \lambda_1 = n_2 \lambda_2$ 10 × 7000 = $n_2 \times 5000 \Longrightarrow n_2 = 14$
- **39.** (b) $I \rightarrow ON$ $II \rightarrow OFF$ In IInd state it is used as a amplifier it is active region.

40. (b)
$$Y = A + (\overline{A}.B) = (A + \overline{A}).(A + B)$$

= $A + B$
 $\Rightarrow OR$ gate

PART - II : CHEMISTRY

- Molarity (M) = $\frac{1}{\text{mol. wt.} \times \text{vol (mL)}}$ wt×1000 41. (d) $2 = \frac{\text{wt.}}{63} \times \frac{1000}{250}$ wt. = $\frac{63}{2}$ g wt. of 70% acid = $\frac{100}{70} \times 31.5 = 45$ g
- Radius of hydrogen atom = 0.530 Å, Number 42. (d) of excited state (n) = 2 and atomic number of hydrogen atom (Z) = 1. We know that the Bohr radius.

$$(r) = \frac{n^2}{Z} \times \text{Radius of atom} = \frac{(2)^2}{1} \times 0.530$$

= 4 × 0.530 = 2.12 Å

43. (d) The screening effect of inner electron of the nucleus causes the decrease in ionization potential, therefore the order of the screening effect is

f < d < p < s

Hence, the screening effect of *d*-electron is less than *p*-electron.

- **44.** (b) Rare gases; as the e⁻ is to be removed from stable configuration.
- 45. (c) Amongst isoelectronic species, ionic radii of anion is more than that of cations. Further size of anion increase with increase in -ve charge and size of cation decrease with increase in + ve charge. Hence ionic radii decreases from O⁻ to Al³⁺.
- **46.** (b) B_2 and O_2 are paramagnetic due to presence of unpaired electron. MO electronic configuration of B_2 is :

$$\sigma ls^2 \sigma^* ls^2 \sigma 2s^2 \sigma^* 2s^2 \pi 2p_x^1 = \pi 2p_y^1$$

MO electorn i.e. configuration of O₂ is :
$$\sigma ls^2 \sigma^* ls^2 \sigma 2s^2 \sigma^* 2s^2 \sigma 2p_z^2 \pi 2p_x^2$$
$$= \pi 2p_y^2 \pi^* 2p_x^1 = \pi^* 2p_y^1$$

 (b) RMS velocity of molecules depends on mass. If mol. wt. increases, rms velocity of melocules decreases.

$$\label{eq:ms_constraint} \begin{split} & \mathrm{rms} \propto \frac{1}{\sqrt{\mathrm{m.wt}}} \\ & \mathrm{The \ order \ of \ increasing \ m. \ wt. \ is} \\ & \mathrm{H}_2 < \mathrm{N}_2 < \mathrm{O}_2 < \mathrm{HBr} \\ & \mathrm{Order \ of \ V_{rms} \ of \ molecules.} \\ & \mathrm{HBr} < \mathrm{O}_2 < \mathrm{N}_2 < \mathrm{H}_2 \ . \end{split}$$

48. (a) $\Delta H = \Delta H_{(\text{product})} - \Delta H_{(\text{reactant})}$ $162 = 2 \times \Delta H_{\text{H}} - \Delta H_{\text{H}_2}$ $\Delta H_{\text{H}} = \frac{162}{2} \quad (\because \Delta H_{\text{H}_2} = 0)$

$$\Delta H_{\rm H} = 81 \, \text{Kcal}$$

49. (c) By bomb calorimeter we get ΔE .

$$2C_{6}H_{6}(l) + 15O_{2}(g) \longrightarrow$$

$$12CO_{2}(g) + 6H_{2}O(l)$$

$$\Delta H - \Delta E = \Delta nRT$$

$$= (12 - 15) \times 8.314 \times 300 = -7.483 \text{ kJ}$$
50. (b) I₂ \longrightarrow 2I⁻

$$1 - x \longrightarrow 2x$$

$$K_{c} = \frac{(2x)^{2}}{(1-x)} = 10^{-6}$$

It shows that $(1-x) < 2x$
51. (c) $K_{p} = K_{c}(RT)^{\Delta n}$;
 $\Delta n = 1 - \left(1 + \frac{1}{2}\right) = 1 - \frac{3}{2} = -\frac{1}{2}$
 $\therefore \frac{K_{p}}{K_{c}} = (RT)^{-1/2}$

52. (c)
$$\operatorname{Na}_{2}S_{4}O_{6}$$

 $2+4x-12=0$
 $4x-10=0$
 $x = \frac{10}{4} = \frac{+5}{2}$
Oxidation state of S is $= \frac{+5}{2}$
53. (a) $\operatorname{Zn} + \operatorname{H}_{2}SO_{4} \to \operatorname{Zn}SO_{4} + \operatorname{H}_{2}$

(a)
$$\operatorname{Zn} + \operatorname{H}_2 \operatorname{SO}_4 \to \operatorname{Zn} \operatorname{SO}_4 + \operatorname{H}_2$$

 $\operatorname{Zn} + 2\operatorname{NaOH} \to \operatorname{Na}_2 \operatorname{ZnO}_2 + \operatorname{H}_2$
 Ratio of volumes of H₂ evolved is 1 :

54. (d) The stability of alkali metal hydrides decreases from Li to Cs. It is due to the fact that M-H bonds becomes weaker with increase in size of alkali metals as we move down the group from Li to Cs. Thus the order of stability of hydrides is LiH>NaH>KH>RbH>CsH

1

- **55.** (d) -NO₂ group, being strong electron withdrawing, disperses the -ve charge, hence stabilizes the concerned carbanion.
- **56.** (a) A chiral object or structure has four different groups attached to the carbon.
- 57. (d) The structure $CH_3 \stackrel{*}{C}HBr \stackrel{*}{C}HBr COOH$ has two different chiral carbon atoms, hence number of enantiomers (optically active forms) is $2^n = 2^2 = 4$
- **58.** (a) Electrolysis of a concentrated aqueous solution of either sodium or potassium salts of saturated carboxylic acids yields higher alkane at anode.

$$2\text{RCOOK} \xrightarrow{\text{Electrolytic}} 2\text{RCOO}^{-} + 2\text{K}^{+}$$
Anode
$$2\text{RCOO}^{-} \rightarrow 2\text{RCOO} + 2e^{-} \longrightarrow$$

$$R \longrightarrow R + 2\text{CO}_{2}$$
At Cathode
$$2\text{K}^{+} + 2e^{-} \rightarrow 2\text{K}$$

$$2\text{K} + \text{H}_{2}\text{O} \rightarrow 2\text{KOH} + \text{H}_{2} \uparrow$$
(Kolbe's Method)

59. (c)
$$CH \equiv CH + HO^{-} - CI^{+} \rightarrow | \begin{matrix} OH & CI \\ | \\ CH = CH \end{matrix}$$





- 60. (a) Green house gases such as CO_2 , ozone, methane, the chlorofluoro carbon compounds and water vapour form a thick cover around the earth which prevents the IR rays emitted by the earth to escape. It gradually leads to increase in temperature of atmosphere.
- 61. (c) No change in density.
- 62. (c) When equal weights of different solutes are present in equal volumes of solution the molarity is inversely related to molecular mass of the solute. Mol. mass of NaCl is less than KCl. Hence, molarity of NaCl solution will be more.

63. (c)
$$m = \frac{E.wt \times Q}{96500}$$
;
∴ E.wt = $\frac{m \times 96500}{Q}$
 $= \frac{22.2 \times 96500}{2 \times 5 \times 60 \times 60} = 60.3$
Oxidation state = $\frac{At wt.}{Eq. wt.} = \frac{177}{60.3} = 3$

64. (d) At cathodes :
$$Fe^+ + 2e^- \longrightarrow Fe_+$$

2 .

$$Fe^{3+} + 3e^{-} \longrightarrow Fe$$

$$(E_{Fe})_1 = \frac{At. wt.}{2}; \quad (E_{Fe})_2 = \frac{At. wt.}{3}$$
Hence, $\frac{(E_{Fe})_1}{(E_{Fe})_2} = \frac{3}{2}$

65. (c) The velocity constant doubles for every 10°C rise in temperature.

- **66.** (d) At high pressure the extent of adsorption follows zero order kinetics.
- 67. (d) F_2 is expected to have highest bond energy but the correct decreasing order is $Cl_2 > Br_2 > F_2$ because of fluorine atom has very small size due to which there is a high inter electronic repulsion between two fluorine atoms so the bond between two fluorine gets weaker and need less energy.
- 68. (a) The acids which contain P–H bond have strong reducing properties. Thus H₃PO₂ acid is good reducing agent as it contains two P–H bonds. For example, it reduces AgNO₃ to metallic silver.

 $4 \text{ AgNO}_3 + 2 \text{H}_2\text{O} + \text{H}_3\text{PO}_2 \longrightarrow$

$$4Ag + 4HNO_3 + H_3PO_4$$

69. (b) $[Cr(H_2O)_6]^{2+}$ Cr is in Cr²⁺ form



In $[Fe(H_2O)]^{2+} Fe^{2+}$ form. Both will have 4 unpaired electrons.

 (a) Due to stronger–I-effect of F than that of Cl, CHF₃ should be more acidic than CHCl₂. But actually reverse is true.

This is due to : CCl_3^- left after the removal of a proton from $CHCl_3$ is stabilised due to presence of *d*-orbitals in

Cl than: CF_3^- left after the removal of a

proton from CHF_3 which is not stabilised due to the absence of *d*-orbitals on F.

71. (d) S_N^2 mechanism is followed in case of primary and secondary halides i.e., S_N^2 reaction is favoured by small groups on the carbon atom attached to halogens so

$$CH_{3} CH_{2} Br > CH_{3} CH_{2} CH_{2} Br > CH_{3} CH_{3} CH_{3} - CH_{3} CH_{3} - CH_{3} CH_{3} - CH_{3} CH_{3} - CH_{3} CH_$$



74. (c) Aldehydes are more reactive than ketones due to +I effect of $-CH_3$ group. There are two $-CH_3$ group in acetone which reduces

+ve charge density on carbon atom of carbonyl group. More hindered carbonyl group becomes less reactive. So in the given case CH_3CHO is the right choice.

75. (d)
$$CH_3CN \xrightarrow{Na/C_2H_5OH} CH_3CH_2NH_2$$

 $\xrightarrow{HNO_2} CH_3CH_2OH \xrightarrow{Cu} CH_3CH_3CHO$
(B) $\xrightarrow{(A)}$
(C) $\xrightarrow{(C)}$

76. (b) When Potassium is treated with ammonia, then potassium amide is obtained.

$$K + NH_3 \longrightarrow KNH_2 + \frac{1}{2}H_2$$

Pot. amide

- 77. (b) Insulin is a biochemically active peptide harmone secreted by pancreas.
- 78. (a) Due to resonance,

 $\begin{array}{c} \mathbf{\zeta}_{\parallel}^{O} & \mathbf{\zeta}_{\cdot}^{-} \\ -\mathbf{C} - \mathbf{N}\mathbf{H} - \mathbf{\zeta} \\ \mathbf{N}\mathbf{H} - \mathbf{\zeta} \\ \mathbf{N}\mathbf{H} - \mathbf{\zeta} \\ \mathbf{N}\mathbf{H} - \mathbf{C} = \mathbf{N}\mathbf{H} - \mathbf{K} \\ \mathbf{N}\mathbf{H} - \mathbf{K} \\ \mathbf{N}\mathbf{H} \\ \mathbf$

79. (b) CuS and CdS are precipitated by H₂S. Hydroxide of Al will pass into the solution in the form of NaAlO₂ being amphoteric in nature. Hence filtrate will give test for sodium and aluminium.

80. (a) Normality of 3% Na₂CO₃.
N =
$$\frac{3 \times 1000}{53 \times 100}$$
 = 0.566 N

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For
$$H_2SO_4$$
 sol. $N_1 = 0.1$, $V_1 = 100$ mL

For
$$Na_2CO_3$$
 sol. $N_2 = 0.566$.
Now apply $N_1V_1 = N_2V_2$

ow apply
$$N_1 V_1 = N_2 V_2$$

$$V_2 = \frac{N_1 V_1}{N_2} = \frac{0.1 \times 1000 \text{ mL}}{0.566} = 176.66 \text{mL}$$

PART - III : MATHEMATICS

81. (c)
$$n (M \text{ alone})$$

= $n(M) - n(M \cap C) - n(M \cap P) + n(M \cap C \cap P)$
= $100 - 28 - 30 + 18 = 60$



82. (a) $x \sin^3 \theta + y \cos^3 \theta = \sin \theta \cos \theta$ (i)

and
$$x \sin \theta = y \cos \theta$$
 ...(ii)
Equation (i) may be written as
 $x \sin \theta .\sin^2 \theta + y \cos^3 \theta = \sin \theta \cos \theta$
 $\Rightarrow y \cos \theta \sin^2 \theta + y \cos^3 \theta = \sin \theta \cos \theta$
 $\Rightarrow y \cos \theta (\sin^2 \theta + \cos^2 \theta) = \sin \theta \cos \theta$
 $\Rightarrow y \cos \theta = \sin \theta \cos \theta \therefore y = \sin \theta$...(iii)
Putting the value of y from (iii) in (ii), we get
 $x \sin \theta = \sin \theta .\cos \theta \Rightarrow x = \cos \theta$...(iv)
Squaring (iii) and (iv) and adding, we get
 $x^2 + y^2 = \cos^2 \theta + \sin^2 \theta = 1$

83. (d) $\cos 7\theta = \cos \theta - \sin 4\theta$

$$\Rightarrow \sin 4\theta = \cos \theta - \cos 7\theta$$

$$\Rightarrow \sin 4\theta = 2\sin 4\theta \sin 3\theta$$

$$\Rightarrow \sin 4\theta (1 - 2\sin 3\theta) = 0$$

$$\therefore \sin 4\theta = 0 \text{ or } \sin 3\theta = \frac{1}{2}$$

$$\Rightarrow 4\theta = n\pi \text{ or } 3\theta = n\pi + (-1)^n \frac{\pi}{6}$$

$$\Rightarrow \theta = \frac{n\pi}{4} \text{ or } \frac{n\pi}{3} + (-1)^n \frac{\pi}{18}$$

84. (d) Real part of $\frac{\overline{z}+2}{\overline{z}-1}$ is given by $\frac{1}{2} \left[\frac{\overline{z}+2}{\overline{z}-1} + \left(\frac{\overline{z}+2}{\overline{z}-1} \right) \right] = 4$ $\Rightarrow \frac{\overline{z}+2}{\overline{z}-1} + \frac{z+2}{z-1} = 8$ $\Rightarrow z\overline{z} - \overline{z} + 2z - 2 + z\overline{z} + 2\overline{z} - z - 2 = 8(z\overline{z} - \overline{z} - z + 1)$ $\Rightarrow z\overline{z} - \frac{3}{2}z - \frac{3}{2}\overline{z} + 2 = 0 \qquad \dots (i)$ Comparing with the equation $\overline{z} + \overline{z} + z = \overline{z} + b = 0 \text{ substants} = \frac{3}{2} = 0$

$$z\overline{z} + \overline{a} z + a\overline{z} + b = 0$$
, we get $a = -\frac{3}{2}$ and $b = 2$. Thus, the locus of z given by the equation
(i) is a circle with centre $\frac{3}{2}$ and radius $=\frac{1}{2}$

85. (d) We have $x^3 + 1 \equiv (x + 1) (x^2 - x + 1)$. Therefore, α and β are the complex cube roots of -1 so that we may take $\alpha = -\omega$ and

 $\beta = -\omega^2$, where $\omega \neq 1$ is a cube root of unity. Thus $\alpha^{100} = (-\omega)^{100} = \omega$ and $\beta^{100} = (-\omega^2)^{100} = \omega^2$, so that the required equation is $x^2 + x + 1 = 0$. 86. (a) Given, $\frac{3-|x|}{4-|x|} \ge 0$ \Rightarrow 3-|x| \leq 0 and 4-|x|<0 or $3 - |x| \ge 0$ and 4 - |x| < 0 $\Rightarrow |x| \ge 3$ and |x| > 4or $|x| \leq 3$ and |x| < 4 $\Rightarrow |x| > 4$ or $|x| \le 3$ $\Rightarrow x \in (-\infty, -4) \cup [-3, 3] \cup (4, \infty)$ 87. (c) Dividing R at $\frac{2}{3}$, $\frac{4}{3}$ and 2, analyse 4 cases. When $x \le \frac{2}{3}$, the inequality becomes $2 - 3x + 4 - 3x + 6 - 3x \ge 12$. implying $-9x \ge 0 \Longrightarrow x \le 0$. when $x \ge 2$ the ineqality becomes $3x-2+3x-4+3x-6 \ge 12$, Implying $9x \ge 24 \implies x \ge 8/3$ The inequality in invalid in the other two sections. either $x \le 0$ or $x \ge 8/3$ *.*..

- 88. (d) Leaving one seat vacant between two boys, 5 boys may be seated in 4! ways. Then at remaining 5 seats, 5 girls any sit in 5! ways. Hence the required number = 4! × 5!
- **89.** (a) Atleast one black ball can be drawn in the following ways
 - (i) one black and two other colour balls = ${}^{3}C_{1} \times {}^{6}C_{2} = 3 \times 15 = 45$
 - (ii) two black and one other colour balls = ${}^{3}C_{2} \times {}^{6}C_{1} = 3 \times 6 = 18$ (iii) All the three are black = ${}^{3}C_{3} \times {}^{6}C_{0} = 1$

: Req. no. of ways =
$$45 + 18 + 1 = 64$$

90. (d) When exponent is n then total number of terms are n + 1. So, total number of terms in $(2+3x)^4=5$ Middle term is 3rd. $\Rightarrow T_3 = {}^4C_2(2)^2 . (3x)^2$

$$=\frac{4\times3\times2\times1}{2\times1\times2}\times4\times9x^{2}=216x^{2}$$

91. (a)
$$C_0 + (C_0 + C_1) + (C_0 + C_1 + C_2) + \dots + (C_0 + C_1 + \dots + C_{n-1})$$

= $nC_0 + (n-1)C_1 + (n-2)C_2 + \dots + C_{n-1}$

$$= C_1 + 2C_2 + 3C_3 + 4C_4....nC_n = n.2^{n-1}$$

92. (b) Let $S=1+2.2+3.2^2+4.2^2+...+100.2^{99}$ (i) It is an arithmetico - geometric series. On multiplying Eq. (i) by 2 and then subtracting it from Eq. (i), we get

 $S = 1 + 2.2 + 3.2^2 + 4.2^3 + ... + 100.2^{99}$ $2S = 1.2 \pm 2.2^2 \pm 3.2^3 \pm \dots \pm 99.2^{99} \pm 100.2^{100}$

$$\frac{-S = 1 + 2 + 2^{2} + 2^{3} \dots + 2^{99} - 100.2^{100}}{\Rightarrow -S = \frac{1(2^{100} - 1)}{2 - 1} - 100.2^{100}}$$
$$\Rightarrow -S = 2^{100} - 1 - 100.2^{100}$$
$$\Rightarrow -S = -1 - 99.2^{100}$$
$$\Rightarrow S = 99.2^{100} + 1$$

93. (b) Equation of the line making intercepts a and

b on the axes is $\frac{x}{a} + \frac{y}{b} = 1$. Since, it passes through (1, 1)

$$\Rightarrow \frac{1}{a} + \frac{1}{b} = 1 \qquad \dots (i)$$

Also the area of the triangle formed by the line and the axes is A.

$$\therefore \frac{1}{2}ab = A \implies ab = 2A \qquad \dots (ii)$$

From eqs. (i) and (ii), we get, a + b = 2AHence, a and b are the roots of the eq.

 $x^{2} - (a+b)x + ab = 0 \Longrightarrow x^{2} - 2Ax + 2A = 0$ 94. (a) $4a^2 + b^2 + 2c^2 + 4ab - 6ac - 3bc$ $=(2a+b)^2-3(2a+b)c+2c^2=0$ \Rightarrow (2a+b-2c) (2a+b-c) = 0 \Rightarrow c = 2a+b or $c = a + \frac{1}{2}b$

The equation of the family of lines is

$$a(x+2)+b(y+1)=0 \text{ or } a(x+1)+b\left(y+\frac{1}{2}\right)=0$$

giving the point of concurrence (-2, -1) or
$$\left(-1, -\frac{1}{2}\right).$$

95. (d) Equation of pair of tangents is given by

$$SS_1 = T^2$$
,
or $S = x^2 + y^2 + 20 (x + y) + 20$, $S_1 = 20$,
 $T = 10 (x + y) + 20 = 0$
∴ $SS_1 = T^2$
 $\Rightarrow 20 (x^2 + y^2 + 20 (x + y) + 20) = 10^2$
 $(x + y + 2)^2$
 $\Rightarrow 4x^2 + 4y^2 + 10xy = 0 \Rightarrow 2x^2 + 2y^2 + 5xy = 0$

96. (a)
$$\because \angle FBF' = 90^{\circ} \Rightarrow FB^{2} + F'B^{2} = FF'^{2}$$

 $\therefore \left(\sqrt{a^{2}e^{2} + b^{2}}\right)^{2} + \left(\sqrt{a^{2}e^{2} + b^{2}}\right)^{2} = (2ae)^{2}$
 $\Rightarrow 2(a^{2}e^{2} + b^{2}) = 4a^{2}e^{2} \Rightarrow e^{2} = \frac{b^{2}}{a^{2}} ...(i)$
 $F(-ae, 0) \qquad F(ae, 0)$

Also, $e^2 = 1 - b^2 / a^2 = 1 - e^2$ (By using equation (i)) $\Rightarrow 2e^2 = 1 \Rightarrow e = \frac{1}{\sqrt{2}}$ Given $x = \frac{3y + k}{\sqrt{2}}$

97. (b) Given
$$x = \frac{3y + k}{2}$$
(1)
and $y^2 = 6x$ (2)

$$\Rightarrow y^{2} = 6\left(\frac{3y+k}{2}\right)$$

$$\Rightarrow y^{2} = 3\left(3y+k\right) \Rightarrow y^{2} - 9y - 3k = 0 \dots (3)$$

If line (1) touches parabola (2) then roots of

If line (1) touches parabola (2) then roots of quadratic equation (3) is equal $\therefore (-9)^2 = 4 \times 1 \times (-3k) \Longrightarrow k = -27/4$

98. (c) Let eq. of ellipse be
$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$
,
S is (-ae, 0), T is (ae, 0) and B is (0, b)

$$S$$
 is (-ae, 0), T is (ae, 0) and B is (0, b).



Also
$$SB^2 = ST^2 \implies 4a^2e^2 = a^2e^2 + b^2$$

$$\Rightarrow 3a^{2}e^{2} = a^{2}(1-e^{2}) = a^{2}-a^{2}e^{2}$$
$$\Rightarrow 4a^{2}e^{2} = a^{2} \Rightarrow e^{2} = \frac{1}{4} \Rightarrow e = \frac{1}{2}$$
99. (d) Given $f(x) = g(x) h(x)$
$$\Rightarrow h(x) = \frac{f(x)}{g(x)}$$
$$\Rightarrow \lim_{x \to 1} h(x) = \lim_{x \to 1} \frac{f(x)}{g(x)}$$

$$\Rightarrow \lim_{x \to 1} \frac{(x^5 - 1)(x^3 + 1)}{(x^2 - 1)(x^2 - x + 1)}$$
$$= \lim_{x \to 1} \frac{x^5 - 1^5}{x - 1} = 5 \times 1^4 = 5$$
(d) TTTT

100. (d)

101. (b) Mode =
$$3$$
 Median $- 2$ Mean

:. Median =
$$\frac{1}{3}$$
 (mode + 2 mean) = $\frac{1}{3}$ (60+2×66)=64

(c)	Occurance (x_i)	Frequency (f _i)	$\operatorname{Freq}^*(x_i)$	(<i>x</i> _{<i>i</i>} -mean)	$(x_i$ -mean) ²	$f_i(x_i-\text{mean})^2$
	3.5	3	10.5	-3.59	12.887	38.661
	4.5	7	31.5	-2.59	6.707	46.952
	5.5	22	121	121	2.528	55.609
	6.5	60	390	-0.59	0.348	20.876
	7.5	85	637.5	0.41	0.168	14.298
	8.5	32	272	1.41	1.988	63.632
	9.5	8	76	2.41	5.809	46.47
	Total	217	1538.5	-	-	286.498

Variance $\sigma^2 = \frac{\Sigma f_i (x_i - \overline{x})^2}{\Sigma f_i} = \frac{286.49}{217}$ = 1.32

103. (a) Since, $|a-a|=0 \le 1$, so $aRa, \forall a \in R$ \therefore *R* is reflexive. Now, $aRb \Rightarrow |a-b| \le 1 \Rightarrow |b-a| \le 1 \Rightarrow bRa$

> \therefore *R* is symmetric. But *R* is not transitive as

1R2. 2R3 but 1 K 3

$$[::|1-3|=2>1]$$

104. (c) $\begin{bmatrix} ||1-3| = 2 > 1 \end{bmatrix}$ We have, $(\sin^{-1} x)^2 + (\cos^{-1} x)^2$ = $(\sin^{-1} x + \cos^{-1} x)^2 - 2 \sin^{-1} x . \cos^{-1} x$ $=\frac{\pi^2}{4} - 2\sin^{-1}x\left(\frac{\pi}{2} - \sin^{-1}x\right)$ $=\frac{\pi^2}{4} - \pi \sin^{-1} x + 2(\sin^{-1} x)^2$ $=2\left[(\sin^{-1}x)^2 - \frac{\pi}{2}\sin^{-1}x + \frac{\pi^2}{8}\right]$ $=2\left[\left(\sin^{-1}x - \frac{\pi}{4}\right)^2 + \frac{\pi^2}{16}\right]$

Thus, the least value is $2\left(\frac{\pi^2}{16}\right)$ i.e. $\frac{\pi^2}{8}$

and the greatest value is

$$2\left[\left(\frac{-\pi}{2} - \frac{\pi}{4}\right)^2 + \frac{\pi^2}{16}\right] \text{ i.e. } \frac{5\pi^2}{4}$$

105. (c) The given trigonometric ratio

$$= \cos\left[\frac{1}{2}\left(\cos\left(\cos^{-1}\frac{1}{8}\right)\right)\right]$$
$$= \cos\left(\frac{1}{2}\cos^{-1}\frac{1}{8}\right)$$
$$= \sqrt{\frac{1+\cos\left(\cos^{-1}\frac{1}{8}\right)}{2}} = \frac{3}{4}$$
The singular determinent equation

106. (d) The given determinant vanishes, i.e., 1

$$\begin{vmatrix} 1 & x-3 & (x-3)^2 \\ 1 & x-4 & (x-4)^2 \\ 1 & x-5 & (x-5)^2 \end{vmatrix} = 0$$

Expanding along C₁, we get
$$(r-4)(r-5)^2 - (r-5)(r-4)^2 - f(r-3)(r-5)^2$$

$$(x-4)(x-5)^{2} - (x-5)(x-4)^{2} - \{(x-3)(x-5)^{2} - (x-5)(x-3)^{2}\} + (x-3)(x-4)^{2} - (x-4)(x-3)^{2} = 0$$

$$\Rightarrow (x-4)(x-5)(x-5-x+4) - (x-3)(x-5)(x-5-x+3) + (x-3)(x-4)(x-4-x+3) = 0$$

$$\Rightarrow -(x-4)(x-5) + 2(x-3)(x-5) - (x-3)$$

$$(x-4) = 0$$

$$\Rightarrow -x^2 + 9x - 20 + 2x^2 - 16x + 30 - x^2 + 7x - 12 = 0$$

$$\Rightarrow -32 + 30 = 0 \Rightarrow -2 = 0$$
Which is not possible, hence no value of x satisfies the given condition.
Since the lines are concurrent, so

$$\begin{vmatrix} \ell & m & n \\ m & n & \ell \\ n & \ell & m \end{vmatrix} = 0 \Longrightarrow 3\ell m n - \ell^3 - m^3 - n^3 = 0$$
$$\Rightarrow \quad (\ell + m + n)(\ell^2 + m^2 + n^2 - \ell m - mn - n\ell) = 0$$
$$\Rightarrow \quad \ell + m + n = 0[\because \ell^2 + m^2 + n^2 > \ell m + mn + n]$$

108. (c)
$$y = e^x \Rightarrow \frac{dy}{dx} = e^x = y$$

109. (b) $\lim_{x \to -5} f(x) = \frac{(x-2)(x+5)}{(x+5)(x-3)} = \frac{-7}{-8} = \frac{7}{8}$

110. (d) The equation of the given curve is

$$y = \frac{1}{x - 3}, x \neq 3.$$

The slope of the tangent to the given curve

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at any point (x, y) is given by
$$\frac{dy}{dx} = \frac{-1}{(x-3)^2}$$

For tangent having slope 2, we must have
 $2 = \frac{-1}{(x-3)^2}$
 $\Rightarrow 2(x-3)^2 = -1 \Rightarrow (x-3)^2 = -\frac{1}{2}$

which is not possible as square of a real number cannot be negative. Hence, there is no tangent to the given curve

having slope 2. **111.** (c) Here, $f(x) = (x(x-2))^2$ \Rightarrow f'(x)=4x (x-2)(x-1) For f(x) as increasing, f'(x) > 0So, $4x(x-1)(x-2) > 0 \Rightarrow x(x-1)(x-2) > 0$



From the above figure required interval is, $(0,1)\cup(2,\infty)$

- 112. (d) If the sum of two positive quantities is a constant, then their product is maximum, when they are equal.
 - $\therefore a^2 x^4$. $b^2 y^2$ is maximum when

$$a^{2}x^{4} = b^{2}y^{4} = \frac{1}{2}(a^{2}x^{4} = \frac{1}{2}(a^{2}x^{4} + b^{2}y^{4}) = \frac{c^{4}}{2}$$

$$\therefore \text{ maximum value of} a^{2} x^{4} \cdot b^{2} y^{4} = \frac{c^{4}}{2} \cdot \frac{c^{4}}{2} = \frac{c^{8}}{4} Maximum value of xy = \left(\frac{c^{8}}{4a^{2}b^{2}}\right)^{1/4} = \frac{c^{2}}{\sqrt{2ab}} 113. (b) I = \int \frac{x^{2} \left(1 - \frac{1}{x^{2}}\right) dx}{x^{2} \left(x + \frac{1}{x}\right) \left(x^{2} + \frac{1}{x^{2}}\right)^{1/2}} Let $x + \frac{1}{x} = p \Rightarrow \left(1 - \frac{1}{x^{2}}\right) dx = dp I = \int \frac{dp}{p\sqrt{p^{2} - 2}} = \frac{1}{\sqrt{2}} \sec^{-1} \frac{p}{\sqrt{2}} = \frac{1}{\sqrt{2}} \sec^{-1} \left(\frac{x^{2} + 1}{\sqrt{2x}}\right) + c 114. (b) Let I = \int_{0}^{\pi/2} \frac{\sin x}{1 + \cos^{2} x} dx Let \cos x = t and - \sin x dx = dt. Now, $x = 0 \Rightarrow t = \cos 0 = 1 and x = \frac{\pi}{2} \Rightarrow t = \cos \frac{\pi}{2} = 0 \int_{0}^{0} \sin x \left(-dt\right) = \int_{0}^{0} dt$$$$

$$I = \int_{1}^{0} \frac{\sin x}{1+t^{2}} \left(\frac{-dt}{\sin x}\right) = -\int_{1}^{0} \frac{dt}{1+t^{2}}$$
$$= \left[\tan^{-1} t\right]_{1}^{0} = -\left[0 - \frac{\pi}{4}\right] = \frac{\pi}{4}$$

115. (d)



116. (b) The equation is,

0

$$\frac{dy}{dx} = \sin(x - y) - \sin(x + y) = 2\cos x \sin(-y)$$

$$\Rightarrow \frac{dy}{\sin y} + 2\cos x dx = 0$$

$$\Rightarrow \int \cos ec \ y \ dy + 2\int \cos x \ dx = C$$

$$\Rightarrow \log \tan \frac{y}{2} + 2\sin x = C$$

117. (a) We have $\frac{dy}{dx} = \frac{f'(x)}{f(x)}y - \frac{y^2}{f(x)}$

$$\Rightarrow \frac{dy}{dx} - \frac{f'(x)}{f(x)}y = -\frac{y^2}{f(x)}$$

Divide by y^2 : $y^{-2} \frac{dy}{dx} - y^{-1} \frac{f'(x)}{f(x)} = -\frac{1}{f(x)}$
Put $y^{-1} = z \Rightarrow -y^{-2} \frac{dy}{dx} = \frac{dz}{dx}$
 $-\frac{dz}{dx} - \frac{f'(x)}{f(x)}(z) = -\frac{1}{f(x)}$

$$\Rightarrow \frac{dz}{dx} + \frac{f'(x)}{f(x)}z = \frac{1}{f(x)}$$

I.F. $= e^{\int \frac{f'(x)}{f(x)}dx} = e^{\log f(x)} = f(x)$
 \therefore The solution is
 $z(f(x)) = \int \frac{1}{f(x)}(f(x))dx + c$
 $\Rightarrow y^{-1}(f(x)) = x + c \Rightarrow f(x) = y(x + c)$
118. (c) We have $\vec{a} + \vec{b} + \vec{c} = \vec{0}$
 $\therefore |\vec{a} + \vec{b} + \vec{c}| = 0 \Rightarrow |\vec{a} + \vec{b} + \vec{c}|^2 = 0$
 $\Rightarrow |\vec{a}|^2 + |\vec{b}|^2 + |\vec{c}|^2$
 $+2(\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a}) = 0$
 $\Rightarrow 1 + 1 + 1 + 2(\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a}) = 0$
 $\Rightarrow \vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a} = -\frac{3}{2}$

119. (d) If given vectors are coplanar, then there exists two scalar quantities x and y such that

$$2\hat{i} - \hat{j} + \hat{k} = x(\hat{i} + 2\hat{j} - 3\hat{k}) + y(3\hat{i} + a\hat{j} + 5\hat{k}) \dots (1)$$

Comparing coefficient of \hat{i}, \hat{j} and \hat{k} on both sides of (1) we get x + 3y = 2, 2x + ay = -1, -3x + 5y = 1...(2)

Solving first and third equations, we get x = 1/2, y = 1/2

Since the vectors are coplanar, therefore these values of x and y will satisfy the equation 2x + ay = -1

$$\therefore 2(1/2) + a(1/2) = -1 \Longrightarrow a = -4$$

120. (a) Equation of the line through the given

points is
$$\frac{x-3}{5-3} = \frac{y-4}{1-4} = \frac{z-1}{6-1}$$

 $\Rightarrow \frac{x-3}{2} = \frac{y-4}{-3} = \frac{z-1}{5}$

Any point on this line can be taken as $(3 + 2\lambda, 4 - 3\lambda, 1 + 5\lambda)$

If this point lies on XY-plane then the z-coordinate is zero

$$\Rightarrow 1+5\lambda=0 \Rightarrow \lambda=-\frac{1}{5}$$

Thus the required coordinates of the point are

$$\left(3 - \frac{2}{5}, 4 - 3\left(-\frac{1}{5}\right), 0\right) \equiv \left(\frac{13}{5}, \frac{23}{5}, 0\right)$$

121. (a) The angle between two planes is the angle between their normals. From the equation of the planes, the normal vectors are $\vec{N}_1 = 2\hat{i} + \hat{j} - 2\hat{k}$ and $\vec{N}_2 = 3\hat{i} - 6\hat{j} - 2\hat{k}$

$$\vec{N}_{1} = 2\hat{i} + \hat{j} - 2\hat{k} \text{ and } \vec{N}_{2} = 3\hat{i} - 6\hat{j} - 2\hat{k}$$
Therefore, $\cos \theta = \left| \frac{\vec{N}_{1} \cdot \vec{N}_{2}}{||\vec{N}_{1}||||\vec{N}_{2}||} \right|$

$$= \left| \frac{(2\hat{i} + \hat{j} - 2\hat{k}) \cdot (3\hat{i} - 6\hat{j} - 2\hat{k})}{\sqrt{4 + 1 + 4} \sqrt{9 + 36 + 4}} \right| = \left(\frac{4}{21}\right)$$

Hence,
$$\theta = \cos^{-1}\left(\frac{4}{21}\right)$$

122. (b) In a box,
$$B_1 = 1R$$
, $2W$; $B_2 = 2R$, $3W$ and $B_3 = 3R$, $4W$

Also, given that,
$$P(B_1) = \frac{1}{2}, P(B_2) = \frac{1}{3}$$

and
$$P(B_3) = \frac{1}{6}$$

$$\therefore P\left(\frac{B_2}{R}\right) = \frac{P(B_2)P\left(\frac{R}{B_2}\right)}{P(B_1)P\left(\frac{R}{B_1}\right) + P(B_2)P\left(\frac{R}{B_2}\right) + P(B_3)P\left(\frac{R}{B_3}\right)}$$
$$= \frac{\frac{1}{3} \times \frac{2}{5}}{\frac{1}{2} \times \frac{1}{3} + \frac{1}{3} \times \frac{2}{5} + \frac{1}{6} \times \frac{3}{7}} = \frac{\frac{2}{15}}{\frac{1}{6} + \frac{2}{15} + \frac{1}{14}} = \frac{14}{39}$$

123. (c) The sample space is [LWW, WLW]

$$\therefore P(LWW) + P(WLW)$$

= Probability that in 5 match series, it is
India's second win
= P(L) P(W) P(W) + P(W) P(L) P(W)
= $\frac{1}{8} + \frac{1}{8} = \frac{2}{8} = \frac{1}{4}$

Е h 3α 2α D С B k -*b*-٭ Let ED = h, $\angle EAB = \alpha$ $\therefore \angle EBD = 2\alpha, \angle ECD = 3\alpha$ Now, $\angle DBE = \angle EAB + \angle BEA$ $\Rightarrow 2\alpha = \alpha + \angle BEA$ $\Rightarrow \angle BEA = \alpha = \angle EAB$ \Rightarrow AB = EB = a Similarly, $\angle EBC = \alpha$ In $\triangle EBC$, $\frac{BC}{\sin \alpha} = \frac{EB}{\sin(180^\circ - 3\alpha)}$ $\Rightarrow \quad \frac{b}{\sin \alpha} = \frac{a}{\sin 3\alpha} \quad \Rightarrow \frac{a}{b} = \frac{\sin 3\alpha}{\sin 3\alpha}$ $\Rightarrow \quad \frac{a}{b} = \frac{3\sin\alpha - 4\sin^3\alpha}{\sin\alpha} = 3 - 4\sin^2\alpha$ $\Rightarrow 4\sin^2\alpha = 3 - \frac{a}{b} = \frac{3b-a}{b}$ $\Rightarrow \sin \alpha = \sqrt{\frac{3b-a}{4b}}$ In $\triangle EBD$, sin $2\alpha = \frac{ED}{EB}$ $\Rightarrow ED = a \cdot 2\sin \alpha \cdot \cos \alpha$ $\Rightarrow h = 2a \sqrt{\frac{3b-a}{4b}}, \sqrt{1 - \frac{3b-a}{4b}}$ $=2a\sqrt{\frac{3b-a}{4b}}\sqrt{\frac{b-a}{4b}}$ $=\frac{a}{2b}\sqrt{(a+b)(3b-a)}$ **125.** (a) $x, y \ge 0$ and $4x + 3y \le 24$.

PART - IV: ENGLISH

- Sagacious means 'judicious', so 'wise' is 126. (b) correct answer.
- 127. (a) Remedial means 'reformative', so 'corrective' is correct answer.
- 128. (d) Reticent means 'quiet' so 'secretive' is correct answer.
- 129. (d) Fidelity means 'faithfulness in relations', so 'treachery' is correct antonym.

- **130.** (b) Infrangible means 'strong', so 'breakable' is correct antonym.
- **131.** (b) Progeny means 'child', so 'parent' is correct antonym.
- 132. (c) Use of 'draw' is more suitable for using before word 'conclusion', so option (c) is correct.
- 133. (a) Use of 'looking for' is proper because look for means 'to search for something' which suits here.
- 134. (d) 'Mind your language' is proper to use here because it gives proper sense of sentence.
- 'Use to' is used when any habit is to be 135. (b) shown, so use of option (b) is proper.
- 'Angry' agrees with preposition 'with', so 136. (c) use of option (c) is correct here.
- **137.** (b) Laugh agrees with preposition 'at', so use of option (b) is correct here.
- 138. (c) 139. (b) 140. (a) 141. (d)
- 142. (d) From fig. 1, 93 - (27 + 63) = 93 - 90 = 3From fig. 2, 79 - (38 + 37) = 79 - 75 = 4From fig. 3, 67 - (16 + 42) = 67 - 58 = 9Hence, option (d) is correct.
- 143. (b) Illiterate -- Poor people Unemployed

Hence, option (b) is correct.

144. (b)

145. (a) From the information given in the question the arrangement of students is 1st D

$$2nd \longrightarrow E$$

- $3rd \longrightarrow C$
- $4th \longrightarrow A$ $5th \longrightarrow B$
- 146. (b) The given series follows the pattern $1^3 + 1 = 2$ $2^3 + 1 = 8 + 1 = 9$ 23 + 1 - 27 + 1 - 20

$$3^{3} + 1 = 27 + 1 = 28$$

 $4^{3} + 1 = 64 + 1 = 65$

$$5^3 + 1 = 125 + 1 = 126$$

147. (d) Interchanging symbols \div and + as given in option (d), we get $3 + 5 \times 8 \div 2 - 10$

$$= 3 + 5 \times \frac{8}{2} - 10 = 3 + 20 - 10 = 13$$

148. (b) Both Assertion and Reason are correct but India is a democratic country because the government is elected by its citizens and not because India has its own constitution. 149. (b) 150. (c)

124. (c)