



# Assignment

## System of Co-ordinates

### Basic Level

- The distance between the points  $(17, 105^\circ)$  and  $(5\sqrt{2}, 60^\circ)$  is  
(a) 13 (b) 12 (c) 11 (d) 10
- In a plane, the co-ordinates  $(r, \theta)$  of a point are equivalent  
(a)  $(r, -\theta)$  (b)  $(-r, \theta)$  (c)  $(-r, \pi + \theta)$  (d)  $(r, \pi + \theta)$
- The system of coordinates known as the cartesian system of coordinates was first introduced by  
(a) Euclid (b) Euler (c) Descarte (d) Bhasker
- Which of the following polar coordinates are associated to the same point  
I :  $(2, 30^\circ)$  II :  $(3, 150^\circ)$   
III :  $(-2, 45^\circ)$  IV :  $(-3, 330^\circ)$   
V :  $(3, -210^\circ)$  VI :  $(-3, 30^\circ)$   
(a) I, III and IV (b) II, IV and VI (c) II, IV, V and VI (d) IV and VI

## Distance Formula

### Basic Level

- If the distance between the points  $(a, 2)$  and  $(3, 4)$  be 8, then  $a =$  [MNR 1978]  
(a)  $2 + 3\sqrt{15}$  (b)  $2 - 3\sqrt{15}$  (c)  $2 \pm 3\sqrt{15}$  (d)  $3 \pm 2\sqrt{15}$
- The distance between the points  $(am_1^2, 2am_1)$  and  $(am_2^2, 2am_2)$  is  
(a)  $a(m_1 - m_2)\sqrt{(m_1 + m_2)^2 + 4}$  (b)  $(m_1 - m_2)\sqrt{(m_1 + m_2)^2 + 4}$   
(c)  $a(m_1 - m_2)\sqrt{(m_1 + m_2)^2 - 4}$  (d)  $(m_1 - m_2)\sqrt{(m_1 + m_2)^2 - 4}$

7. The distance of the point  $(b \cos \theta, b \sin \theta)$  from origin is [MP PET 1984]  
 (a)  $b \cot \theta$  (b)  $b$  (c)  $b \tan \theta$  (d)  $b\sqrt{2}$
8. The distance between the points  $(a \cos \alpha, a \sin \alpha)$  and  $(a \cos \beta, a \sin \beta)$  is  
 (a)  $a \cos \frac{\alpha - \beta}{2}$  (b)  $2a \cos \frac{\alpha - \beta}{2}$  (c)  $a \sin \frac{\alpha - \beta}{2}$  (d)  $2a \sin \frac{\alpha - \beta}{2}$
9. The point on  $y$ -axis equidistant from the points  $(3, 2)$  and  $(-1, 3)$  is  
 (a)  $(0, -3)$  (b)  $(0, -3/2)$  (c)  $(0, 3/2)$  (d)  $(0, 3)$
10. The point  $P$  is equidistant from  $A(1, 3)$ ,  $B(-3, 5)$  and  $C(5, -1)$ . Then  $PA =$  [EAMCET 2003]  
 (a) 5 (b)  $5\sqrt{5}$  (c) 25 (d)  $5\sqrt{10}$
11. The point whose abscissa is equal to its ordinate and which is equidistant from the points  $(1, 0)$  and  $(0, 3)$  is  
 (a)  $(1, 1)$  (b)  $(2, 2)$  (c)  $(3, 3)$  (d)  $(4, 4)$
12. Mid-point of the sides  $AB$  and  $AC$  of a  $\triangle ABC$  are  $(3, 5)$  and  $(-3, -3)$  respectively, then the length of the side  $BC$  is  
 (a) 10 (b) 20 (c) 15 (d) 30
13. The distance of the middle point of the line joining the points  $(a \sin \theta, 0)$  and  $(0, a \cos \theta)$  from the origin  
 (a)  $\frac{a}{2}$  (b)  $\frac{1}{2}a(\sin \theta + \cos \theta)$  (c)  $a(\sin \theta + \cos \theta)$  (d)  $a$
14. A point on the line  $y = x$  at a distance of 2 units from the origin is [MP PET 1984]  
 (a)  $(0, \sqrt{2})$  (b)  $(\sqrt{2}, 0)$  (c)  $(2, 2)$  (d)  $(\sqrt{2}, \sqrt{2})$
15. If the points  $(1, 1)$ ,  $(-1, -1)$  and  $(-\sqrt{3}, k)$  are vertices of an equilateral triangle then the value of  $k$  will be  
 (a) 1 (b) -1 (c)  $\sqrt{3}$  (d)  $-\sqrt{3}$

### Advance Level

16. If  $O$  be the origin and if the coordinates of any two points  $Q_1$  and  $Q_2$  be  $(x_1, y_1)$  and  $(x_2, y_2)$  respectively, then  $OQ_1 \cdot OQ_2 \cos \angle Q_1 O Q_2 =$  [IIT 1961]  
 (a)  $x_1 x_2 - y_1 y_2$  (b)  $x_1 y_1 - x_2 y_2$  (c)  $x_1 x_2 + y_1 y_2$  (d)  $x_1 y_1 + x_2 y_2$
17. If the line segment joining the points  $A(a, b)$  and  $B(c, d)$  subtends an angle  $\theta$  at the origin, then  $\cos \theta$  is equal to [IIT 1961]  
 (a)  $\frac{ab + cd}{\sqrt{(a^2 + b^2)(c^2 + d^2)}}$  (b)  $\frac{ac + bd}{\sqrt{(a^2 + b^2)(c^2 + d^2)}}$  (c)  $\frac{ac - bd}{\sqrt{(a^2 + b^2)(c^2 + d^2)}}$  (d) None of these
18. The vertices of a triangle  $ABC$  are  $(0, 0)$ ,  $(2, -1)$  and  $(9, 2)$  respectively, then  $\cos B =$  [AMU 1977]  
 (a)  $\frac{11}{290}$  (b)  $\frac{\sqrt{11}}{290}$  (c)  $-\frac{11}{\sqrt{290}}$  (d)  $-\sqrt{\frac{11}{290}}$
19. If  $A(2, 2)$ ,  $B(-4, -4)$ ,  $C(5, -8)$  are vertices of any triangle, then the length of median passes through  $C$  will be [Rajasthan PET 1988]  
 (a)  $\sqrt{65}$  (b)  $\sqrt{117}$  (c)  $\sqrt{85}$  (d)  $\sqrt{113}$

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20. If a vertex of an equilateral triangle is on origin and second vertex is  $(4, 0)$ , then its third vertex is  
 (a)  $(2, \pm\sqrt{3})$  (b)  $(3, \pm\sqrt{2})$  (c)  $(2, \pm 2\sqrt{3})$  (d)  $(3, \pm 2\sqrt{2})$
21. The locus of the point  $P$  equidistant from the points  $(x_1, y_1)$  and  $(x_2, y_2)$  is  $(x_1 - x_2)x + (y_1 - y_2)y + c = 0$ , then the value of  $c$  is  
 (a)  $(x_1^2 - x_2^2) + (y_1^2 - y_2^2)$  (b)  $\frac{1}{2}(x_1^2 + x_2^2 + y_1^2 + y_2^2)$  (c)  $\frac{1}{2}(x_2^2 - x_1^2 + y_2^2 - y_1^2)$  (d)  $\sqrt{x_1^2 - x_2^2 + y_1^2 - y_2^2}$
22. Let  $S_1, S_2, \dots$  be squares such that for each  $n \geq 1$ , the length of a side of  $S_n$  equals the length of a diagonal of  $S_{n+1}$ . If the length of a side of  $S_1$  is  $10 \text{ cm}$ , then for which of the following values of  $n$  is the area of  $S_n$  less than  $1 \text{ sq. cm}$ .  
 (a) 7 (b) 8 (c) 9 (d) 10

### Problems concerning to geometrical conditions

#### Basic Level

23. The three points  $(-2, 2)$ ,  $(8, -2)$  and  $(-4, -3)$  are the vertices of [Rajasthan PET 1987]  
 (a) An isosceles triangle (b) An equilateral triangle (c) A right angled triangle (d) None of these
24. The points  $A(-4, -1)$ ;  $B(-2, -4)$ ;  $C(4, 0)$  and  $D(2, 3)$  are the vertices of a  
 (a) Parallelogram (b) Rectangle (c) Rhombus (d) None of these
25. Two opposite vertices of a rectangle are  $(1, 3)$  and  $(5, 1)$ . If the other two vertices of the rectangle lie on the line  $y - x + \lambda = 0$ , then  $\lambda =$   
 (a) 1 (b) -1 (c) 2 (d) None of these
26. Three vertices of a parallelogram are  $(1, 3)$ ,  $(2, 0)$  and  $(5, 1)$ . Then its fourth vertex is [Rajasthan PET 1988, 2001]  
 (a)  $(3, 3)$  (b)  $(4, 4)$  (c)  $(4, 0)$  (d)  $(0, -4)$
27. The quadrilateral formed by the vertices  $(-1, 1)$ ,  $(0, -3)$ ,  $(5, 2)$  and  $(4, 6)$  will be [Rajasthan PET 1986]  
 (a) Square (b) Parallelogram (c) Rectangle (d) Rhombus
28. The triangle formed by the lines  $x + y = 0$ ,  $3x + y - 4 = 0$  and  $x + 3y = 4$  is [IIT 1983; MNR 1992; Rajasthan PET 1995; UPSEAT 2001]  
 (a) Equilateral (b) Isosceles (c) Right angled (d) None of these
29. The following points  $A(2a, 4a)$ ,  $B(2a, 6a)$  and  $C(2a + \sqrt{3}a, 5a)$ ,  $(a > 0)$  are the vertices of  
 (a) An acute angled triangle (b) An obtuse angled triangle (c) A right angled triangle (d) An isosceles triangle
30. The triangle joining the points  $P(2, 7)$ ,  $Q(4, -1)$ ,  $R(-2, 6)$  is [MP PET 1997]  
 (a) Equilateral triangle (b) Right-angled triangle (c) Isosceles triangle (d) Scalene triangle
31. The points  $(1, 3)$  and  $(5, 1)$  are the opposite vertices of a rectangle. The other two vertices lie on the line  $y = 2x + c$ , then the value of  $c$  will be [IIT 1981]  
 (a) 4 (b) -4 (c) 2 (d) -2
32. If the three vertices of a rectangle taken in order are the points  $(2, -2)$ ,  $(8, 4)$  and  $(5, 7)$ . The coordinates of fourth vertex are

[Kurukshetra CEE 1993]

- (a) (1, 1) (b) (1, -1) (c) (-1, 1) (d) None of these

33. If vertices of a quadrilateral are  $A(0,0)$ ,  $B(3,4)$ ,  $C(7,7)$  and  $D(4,3)$  then quadrilateral  $ABCD$  is a [Rajasthan PET 1986]

- (a) Parallelogram (b) Rectangle (c) Square (d) Rhombus

34. The coordinates of the third vertex of an equilateral triangle whose two vertices are at (3, 4) and (-2, 3) are

- (a) (1, 1) or (1, -1) (b)  $\left(\frac{1+\sqrt{3}}{2}, \frac{7-5\sqrt{3}}{2}\right)$  or  $\left(\frac{1-\sqrt{3}}{2}, \frac{7+5\sqrt{3}}{2}\right)$

- (c)  $(-\sqrt{3}, \sqrt{3})$  or  $(\sqrt{3}, -\sqrt{3})$  (d) None of these

35. The quadrilateral joining the points (1, -2); (3, 0); (1, 2) and (-1, 0) is [Rajasthan PET 1999]

- (a) Parallelogram (b) Rectangle (c) Square (d) Rhombus

36. If  $\begin{vmatrix} x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \\ x_3 & y_3 & 1 \end{vmatrix} = \begin{vmatrix} a_1 & b_1 & 1 \\ a_2 & b_2 & 1 \\ a_3 & b_3 & 1 \end{vmatrix}$ , then the two triangle with vertices  $(x_1, y_1)$ ;  $(x_2, y_2)$ ;  $(x_3, y_3)$  and  $(a_1, b_1)$ ;  $(a_2, b_2)$ ;  $(a_3, b_3)$  must be

[IIT 1985]

- (a) Similar (b) Congruent (c) Never congruent (d) None of these

37. All points lying inside the triangle formed by the points (1, 3), (5, 0) and (-1, 2) satisfy [IIT 1986; Kurukshetra CEE 1998]

- (a)  $3x + 2y \geq 0$  (b)  $2x + y - 13 \leq 0$  (c)  $2x - 3y - 12 \leq 0$  (d) All of these

38. The common property of points lying on x-axis, is [MP PET 1988]

- (a)  $x = 0$  (b)  $y = 0$  (c)  $a = 0, y = 0$  (d)  $y = 0, b = 0$

39. Vertices of a figure are (-2, 2); (-2, -1); (3, -1); (3, 2), it is a [Karnataka CET 1998]

- (a) Square (b) Rhombus (c) Rectangle (d) Parallelogram

40. If  $ABCD$  is a quadrilateral, if the mid point of consecutive sides  $AB$ ,  $BC$ ,  $CD$  and  $DA$  are combined by straight lines, then the quadrilateral  $PQRS$  is always [Orissa JEE 2002]

- (a) Square (b) Parallelogram (c) Rectangle (d) Rhombus

41. Three vertices of a parallelogram taken in order are (-1, -6), (2, -5) and (7, 2). The fourth vertex is

- (a) (1, 4) (b) (4, 1) (c) (1, 1) (d) (4, 4)

42. If  $P(1,2)$ ,  $Q(4,6)$ ,  $R(5,7)$  and  $S(a,b)$  are the vertices of a parallelogram  $PQRS$ , then [IIT 1998]

- (a)  $a = 2, b = 4$  (b)  $a = 3, b = 4$  (c)  $a = 2, b = 3$  (d)  $a = 3, b = 5$

### Advance Level

43. The sides of a triangle are  $3x + 4y$ ,  $4x + 3y$  and  $5x + 5y$  where  $x, y > 0$ , then the triangle is [AIEEE 2002]

- (a) Right angled (b) Obtuse angled (c) Equilateral (d) None of these

44. If the vertices of triangle have integral coordinates then the triangle is [IIT 1975; MP PET 1983]

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- (a) Equilateral (b) Never equilateral (c) Isosceles (d) None of these
45. The opposite angular points of a square are (3, 4) and (1, -1). Then the coordinates of other two vertices are [Roorkee 1985]  
 (a)  $D\left(\frac{1}{2}, \frac{9}{2}\right); B\left(-\frac{1}{2}, \frac{5}{2}\right)$  (b)  $D\left(-\frac{1}{2}, \frac{9}{2}\right); B\left(\frac{1}{2}, \frac{5}{2}\right)$  (c)  $D\left(\frac{9}{2}, \frac{1}{2}\right); B\left(-\frac{1}{2}, \frac{5}{2}\right)$  (d) None of these
46. The quadrilateral formed by the lines  $ax \pm by \pm c = 0$  is [Rajasthan PET 1998]  
 (a) Square (b) Rectangle (c) Rhombus (d) Parallelogram

### Section Formulae

#### Basic Level

47. Point  $\left(\frac{1}{2}, \frac{-13}{4}\right)$  divides the line joining the points (3, -5) and (-7, 2) in the ratio of  
 (a) 1 : 3 internally (b) 3 : 1 internally (c) 1 : 3 externally (d) 3 : 1 externally
48. In what ratio does the  $y$ -axis divide the join of (-3, -4) and (1, -2) [Rajasthan PET 1995]  
 (a) 1 : 3 (b) 2 : 3 (c) 3 : 1 (d) None of these
49. The points which trisect the line segment joining the points (0, 0) and (9, 12) are [Rajasthan PET 1986]  
 (a) (3, 4), (6, 8) (b) (4, 3), (6, 8) (c) (4, 3), (8, 6) (d) (3, 4), (8, 6)
50. If the point dividing internally the line segment joining the points (a, b) and (5, 7) in the ratio 2 : 1 be (4, 6) then  
 (a)  $a = 1, b = 2$  (b)  $a = 2, b = -4$  (c)  $a = 2, b = 4$  (d)  $a = -2, b = 4$
51. If A and B are the points (-3, 4) and (2, 1). Then the co-ordinates of point C on AB produced such that  $AC = 2BC$  are  
 (a) (2, 4) (b) (3, 7) (c) (7, -2) (d)  $\left(-\frac{1}{2}, \frac{5}{2}\right)$
52. The line segment joining the points (1, 2) and (-2, 1) is divided by the line  $3x + 4y = 7$  in the ratio  
 (a) 3 : 4 (b) 4 : 3 (c) 9 : 4 (d) 4 : 9

#### Advance Level

53. If the points  $P_1, P_2, P_3, \dots$  are the middle points of line segments  $AB, P_1B, P_2B, \dots$  respectively and particles of masses  $m; \frac{m}{2}, \frac{m}{2^2}, \dots$  are placed respectively on these points. If G is the mass-centre of so placed infinite particles and  $\overline{BG} = p \overline{BA}$ , then p is [MP PET 1998]  
 (a) 0 (b)  $\frac{1}{2}$  (c)  $\frac{1}{3}$  (d)  $\frac{1}{4}$
54. If coordinates of the points A and B are (2, 4) and (4, 2) respectively and point M is such that A-M-B also  $AB = 3AM$ , then the coordinates of M are

- (a)  $\left(\frac{8}{3}, \frac{10}{3}\right)$  (b)  $\left(\frac{10}{3}, \frac{14}{4}\right)$  (c)  $\left(\frac{10}{3}, \frac{6}{3}\right)$  (d)  $\left(\frac{13}{4}, \frac{10}{4}\right)$

55. The mid-points of sides of a triangle are  $(2, 1)$ ,  $(-1, -3)$  and  $(4, 5)$ . Then the coordinates of its vertices are  
 (a)  $(7, 9)$ ,  $(-3, -7)$ ,  $(1, 1)$  (b)  $(-3, -7)$ ,  $(1, 1)$ ,  $(2, 3)$  (c)  $(1, 1)$ ,  $(2, 3)$ ,  $(-5, 8)$  (d) None of these
56. The coordinates of the points  $A, B, C$  are  $(x_1, y_1)$ ,  $(x_2, y_2)$ ,  $(x_3, y_3)$  and  $D$  divides the line  $AB$  in the ratio  $l : k$ . If  $P$  divides the line  $DC$  in the ratio  $m : k + l$ , then the coordinates of  $P$  are  
 (a)  $\left(\frac{kx_1 + lx_2 + mx_3}{k + l + m}, \frac{ky_1 + ly_2 + my_3}{k + l + m}\right)$  (b)  $\left(\frac{lx_1 + mx_2 + kx_3}{l + m + k}, \frac{ly_1 + my_2 + ky_3}{l + m + k}\right)$   
 (c)  $\left(\frac{mx_1 + kx_2 + lx_3}{m + k + l}, \frac{my_1 + ky_2 + ly_3}{m + k + l}\right)$  (d) None of these

### Some points related to Triangle

#### Basic Level

57. If the coordinates of the vertices of a triangle be  $(1, a)$ ,  $(2, b)$  and  $(c^2, 3)$ , then the centroid of the triangle  
 (a) Lies at the origin (b) Cannot lie on  $x$ -axis (c) Cannot lie on  $y$ -axis (d) None of these
58. If  $A(4, -3)$ ,  $B(3, -2)$  and  $C(2, 8)$  are the vertices of a triangle, then its centroid will be [Rajasthan PET 1984, 1986]  
 (a)  $(-3, 3)$  (b)  $(3, 3)$  (c)  $(3, 1)$  (d)  $(1, 3)$
59. Two vertices of a triangle are  $(5, 4)$  and  $(-2, 4)$ . If its centroid is  $(5, 6)$  then the third vertex has the coordinates [MP PET 1993]  
 (a)  $(12, 10)$  (b)  $(10, 12)$  (c)  $(-10, 12)$  (d)  $(12, -10)$
60. The centroid of a triangle, whose vertices are  $(2, 1)$ ,  $(5, 2)$  and  $(3, 4)$  is [IIT 1964]  
 (a)  $\left(\frac{8}{3}, \frac{7}{3}\right)$  (b)  $\left(\frac{10}{3}, \frac{7}{3}\right)$  (c)  $\left(-\frac{10}{3}, \frac{7}{3}\right)$  (d)  $\left(\frac{10}{3}, -\frac{7}{3}\right)$
61. If the middle points of the sides of a triangle be  $(-2, 3)$ ,  $(4, -3)$  and  $(4, 5)$ , then the centroid of the triangle is  
 (a)  $(5/3, 2)$  (b)  $(5/6, 1)$  (c)  $(2, 5/3)$  (d)  $(1, 5/6)$
62. If  $A(x_1, y_1)$ ,  $B(x_2, y_2)$  and  $C(x_3, y_3)$  are the vertices of a triangle, then the excentre with respect to  $B$  is [Rajasthan PET 2000]  
 (a)  $\left(\frac{ax_1 - bx_2 + cx_3}{a - b + c}, \frac{ay_1 - by_2 + cy_3}{a - b + c}\right)$  (b)  $\left(\frac{ax_1 + bx_2 - cx_3}{a + b - c}, \frac{ay_1 + by_2 - cy_3}{a + b - c}\right)$   
 (c)  $\left(\frac{ax_1 - bx_2 - cx_3}{a - b - c}, \frac{ay_1 - by_2 - cy_3}{a - b - c}\right)$  (d) None of these
63. If two vertices of an equilateral triangle have integral co-ordinates then the third vertex will have  
 (a) Integral co-ordinates (b) Co-ordinates which are rational  
 (c) At least one co-ordinate irrational (d) Co-ordinates which are irrational
64. If the orthocentre and centroid of triangle are  $(-3, 5)$ ,  $(3, 3)$ , then the circumcentre is [Kurukshetra CEE 1999]  
 (a)  $(6, 2)$  (b)  $(0, 8)$  (c)  $(6, -2)$  (d)  $(0, 4)$

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65. The centroid and a vertex of an equilateral triangle are  $(1, 1)$  and  $(1, 2)$  respectively. Another vertex of the triangle can be  
 (a)  $\left(\frac{2-\sqrt{3}}{2}, \frac{1}{2}\right)$  (b)  $\left(\frac{2+3\sqrt{3}}{2}, \frac{1}{2}\right)$  (c)  $\left(\frac{2+\sqrt{3}}{2}, \frac{1}{2}\right)$  (d) None of these
66. The incentre of triangle formed by lines  $x = 0$ ,  $y = 0$  and  $3x + 4y = 12$  is [Rajasthan PET 1990]  
 (a)  $\left(\frac{1}{2}, \frac{1}{2}\right)$  (b)  $(1, 1)$  (c)  $\left(1, \frac{1}{2}\right)$  (d)  $\left(\frac{11}{2}, 1\right)$
67. Orthocentre of triangle with vertices  $(0, 0)$ ,  $(3, 4)$ ,  $(4, 0)$  is [IIT Screening 2003]  
 (a)  $\left(3, \frac{5}{4}\right)$  (b)  $(3, 12)$  (c)  $\left(3, \frac{3}{4}\right)$  (d)  $(3, 9)$
68. Orthocentre of the triangle whose vertices are  $(0, 0)$ ,  $(2, -1)$  and  $(1, 3)$  is [ISM Dhanbad 1970; IIT 1967, 1974]  
 (a)  $\left(\frac{4}{7}, \frac{1}{7}\right)$  (b)  $\left(-\frac{4}{7}, -\frac{1}{7}\right)$  (c)  $(-4, -1)$  (d)  $(4, 1)$
69. The orthocentre of the triangle formed by the lines  $4x - 7y + 10 = 0$ ,  $x + y = 5$  and  $7x + 4y = 15$  is [IIT 1969, 1976]  
 (a)  $(1, 2)$  (b)  $(1, -2)$  (c)  $(-1, -2)$  (d)  $(-1, 2)$
70. Coordinates of the orthocentre of the triangle whose sides are  $x = 3$ ,  $y = 4$  and  $3x + 4y = 6$ , will be [MNR 1989]  
 (a)  $(0, 0)$  (b)  $(3, 0)$  (c)  $(0, 4)$  (d)  $(3, 4)$
71. The orthocentre of the triangle formed by  $(0, 0)$ ,  $(8, 0)$ ,  $(4, 6)$  is [EAMCET 1991]  
 (a)  $\left(4, \frac{8}{3}\right)$  (b)  $(3, 4)$  (c)  $(4, 3)$  (d)  $(-3, 4)$
72. If the line  $3x + 4y - 24 = 0$  cuts the  $x$ -axis in  $A$  and  $y$ -axis in  $B$ , then incentre of  $\triangle OAB$  (where  $O$  is the origin) is  
 (a)  $(1, 2)$  (b)  $(2, 2)$  (c)  $(12, 12)$  (d)  $(2, 12)$
73. The distance between the orthocentre and circumcentre of the triangle with vertices  $(0, 0)$ ,  $(0, a)$  and  $(b, 0)$  is  
 (a)  $\frac{\sqrt{a^2 - b^2}}{2}$  (b)  $a + b$  (c)  $a - b$  (d)  $\frac{\sqrt{a^2 + b^2}}{2}$
74. The incentre of the triangle formed by  $(0, 0)$ ,  $(5, 12)$ ,  $(16, 12)$  is [EAMCET 1984]  
 (a)  $(9, 7)$  (b)  $(7, 9)$  (c)  $(-9, 7)$  (d)  $(-7, 9)$
75. If two vertices of a triangle are  $(6, 4)$ ,  $(2, 6)$  and its centroid is  $(4, 6)$ , then the third vertex is [Rajasthan PET 1996]  
 (a)  $(4, 8)$  (b)  $(8, 4)$  (c)  $(6, 4)$  (d) None of these
76. If the vertices of a triangle be  $(a, 1)$ ,  $(b, 3)$  and  $(4, c)$ , then the centroid of the triangle will lie on  $x$ -axis if  
 (a)  $a + c = -4$  (b)  $a + b = -4$  (c)  $c = -4$  (d)  $b + c = -4$
77. The vertices of a triangle are  $(0, 0)$ ,  $(3, 0)$  and  $(0, 4)$ . Its orthocentre is at [MNR 1982; Rajasthan PET 1997; DCE 1994]  
 (a)  $(0, 0)$  (b)  $\left(1, \frac{4}{3}\right)$  (c)  $\left(\frac{3}{2}, 2\right)$  (d) None of these

78. The equations of the sides of a triangle are  $x + y - 5 = 0$ ;  $x - y + 1 = 0$  and  $y - 1 = 0$ , then the coordinates of the circumcentre are [MP PET 1996]
- (a) (2, 1) (b) (1, 2) (c) (2, -2) (d) (1, -2)
79. The mid points of the sides of a triangle are (5, 0); (5, 12) and (0, 12). The orthocentre of this triangle is
- (a) (0, 0) (b) (10, 0) (c) (0, 24) (d)  $\left(\frac{13}{3}, 8\right)$
80. The orthocentre of the triangle with vertices  $\left(2, \frac{\sqrt{3}-1}{2}\right)$ ;  $\left(\frac{1}{2}, -\frac{1}{2}\right)$  and  $\left(2, -\frac{1}{2}\right)$  is [IIT 1993]
- (a)  $\left(\frac{3}{2}, \frac{\sqrt{3}-3}{6}\right)$  (b)  $\left(2, -\frac{1}{2}\right)$  (c)  $\left(\frac{5}{4}, \frac{\sqrt{3}-2}{5}\right)$  (d)  $\left(\frac{1}{2}, -\frac{1}{2}\right)$
81. If the coordinates of the vertices of a triangle are rational numbers then which of the following points of the triangle will always have rational coordinates
- (a) Centroid (b) Incentre (c) Circumcentre (d) Orthocentre
82. In the  $\triangle ABC$ , the coordinates of  $B$  are (0, 0),  $AB = 2$ ,  $\angle ABC = \frac{\pi}{3}$  and the middle point of  $BC$  has the coordinates (2, 0). The centroid of the triangle is
- (a)  $\left(\frac{1}{2}, \frac{\sqrt{3}}{2}\right)$  (b)  $\left(\frac{5}{\sqrt{3}}, \frac{1}{\sqrt{3}}\right)$  (c)  $\left(\frac{4+\sqrt{3}}{3}, \frac{1}{3}\right)$  (d) None of these
83. The vertices of triangle are (6, 0), (0, 6) and (6, 6). The distance between its circumcentre and centroid is
- (a)  $2\sqrt{2}$  (b) 2 (c)  $\sqrt{2}$  (d) 1
84. Two vertices of a triangle are (5, -1) and (-2, 3). If orthocentre is the origin then co-ordinates of the third vertex are
- (a) (7, 4) (b) (-4, 7) (c) (4, -7) (d) (-4, -7)
85. The orthocentre of the triangle formed by the lines  $x + y = 1$ ,  $2x + 3y = 6$  and  $4x - y + 4 = 0$  lies in quadrant [IIT 1985]
- (a) First (b) Second (c) Third (d) Fourth
86. Two vertices of a triangle are (4, -3) and (-2, 5). If the orthocentre of the triangle is at (1, 2), then the third vertex is [Roorkee 1987]
- (a) (-33, -26) (b) (33, 26) (c) (26, 33) (d) None of these
87. The equations to the sides of a triangle are  $x - 3y = 0$ ,  $4x + 3y = 5$  and  $3x + y = 0$ . The line  $3x - 4y = 0$  passes through [EAMCET 1994]
- (a) The incentre (b) The centroid (c) The circumcentre (d) The orthocentre of the triangle
88. The vertices of a triangle are  $|at_1t_2; a(t_1 + t_2)|$ ,  $|at_2t_3; a(t_2 + t_3)|$ ,  $|at_3t_1; a(t_3 + t_1)|$ , then the coordinates of its orthocentre are [IIT 1983]
- (a)  $|a, a(t_1 + t_2 + t_3 + t_1t_2t_3)|$  (b)  $[-a, a(t_1 + t_2 + t_3 + t_1t_2t_3)]$
- (c)  $[-a, (t_1 + t_2 + t_3 + t_1t_2t_3), a]$  (d) None of these
89. The equations of the three sides of a triangle are  $x = 2$ ,  $y + 1 = 0$  and  $x + 2y = 4$ . The coordinates of the circumcentre of the triangle are
- (a) (4, 0) (b) (2, -1) (c) (0, 4) (d) None of these



## Basic Level

90. The area of the triangle with vertices at  $(-4, 1)$ ,  $(1, 2)$ ,  $(4, -3)$  is [EAMCET 1980]  
 (a) 14 (b) 16 (c) 15 (d) None of these
91. If the coordinates of the points  $A, B, C$  be  $(4, 4)$ ,  $(3, -2)$  and  $(3, -16)$  respectively, then the area of the triangle  $ABC$  is [MP PET 1982]  
 (a) 27 (b) 15 (c) 18 (d) 7
92. If the vertices of a triangle are  $(5, 2)$ ,  $(2/3, 2)$  and  $(-4, 3)$ , then the area of the triangle is [Kurukshetra CEE 2002]  
 (a)  $\frac{28}{6}$  (b)  $\frac{5}{2}$  (c) 43 (d)  $\frac{13}{6}$
93. The area of a triangle whose vertices are  $(1, -1)$ ,  $(-1, 1)$  and  $(-1, -1)$  is given by [AMU 1981; Rajasthan PET 1989; MP PET 1993]  
 (a) 2 (b)  $\frac{1}{2}$  (c) 1 (d) 3
94. The vertices of a triangle  $ABC$  are  $(\lambda, 2 - 2\lambda)$ ,  $(-\lambda + 1, 2\lambda)$  and  $(-4 - \lambda, 6 - 2\lambda)$ . If its area be 70 units then number of integral values of  $\lambda$  is  
 (a) 1 (b) 2 (c) 4 (d) 0
95. The area of the pentagon whose vertices are  $(1, 2)$ ,  $(-3, 2)$ ,  $(4, 5)$ ,  $(-3, 3)$  and  $(-3, 0)$  is  
 (a)  $15/2$  unit<sup>2</sup> (b) 30 unit<sup>2</sup> (c) 45 unit<sup>2</sup> (d) None of these

## Advance Level

96. If  $A(6, 3)$ ,  $B(-3, 5)$ ,  $C(4, -2)$  and  $D(x, 3x)$  are four points. If the ratio of area of  $\triangle DBC$  and  $\triangle ABC$  is  $1 : 2$ , then the value of  $x$  will be [IIT 1959]  
 (a)  $\frac{11}{8}$  (b)  $\frac{8}{11}$  (c) 3 (d) None of these
97. The point  $A$  divides the join of the points  $(-5, 1)$  and  $(3, 5)$  in the ratio  $k : 1$  and the coordinates of the points  $B$  and  $C$  are  $(1, 5)$  and  $(7, -2)$  respectively. If the area of the triangle  $ABC$  be 2 units, then  $k =$  [IIT 1967; Kurukshetra CEE 1998]  
 (a) 6, 7 (b)  $31/9, 9$  (c)  $7, 31/9$  (d) 7, 9
98. The area of a triangle is 5. If two of its vertices are  $(2, 1)$ ,  $(3, -2)$  and the third vertex lies on the line  $y = x + 3$ , then the third vertex is [IIT 1978; UPSEAT 1999]  
 (a)  $\left(-\frac{7}{2}, -\frac{13}{2}\right)$  (b)  $\left(-\frac{7}{2}, \frac{13}{2}\right)$  (c)  $\left(\frac{7}{2}, -\frac{13}{2}\right)$  (d)  $\left(\frac{7}{2}, \frac{13}{2}\right)$
99. The area of the triangle formed by the lines  $7x - 2y + 10 = 0$ ,  $7x + 2y - 10 = 0$  and  $y + 2 = 0$  is [IIT 1977]  
 (a) 8 sq. units (b) 12 sq. units (c) 14 sq. units (d) None of these

100. Area of the triangle with vertices  $(a, b)$ ,  $(x_1, y_1)$  and  $(x_2, y_2)$  where  $a, x_1, x_2$  are in G.P. with common ratio ' $r$ ' and  $b, y_1, y_2$  are in G.P. with common ratio ' $s$ ' is
- (a)  $ab(r-1)(s-1)(s-r)$  (b)  $\frac{1}{2}ab(r+1)(s+1)(s-r)$  (c)  $\frac{1}{2}ab(r-1)(s-1)(s-r)$  (d)  $ab(r+1)(s+1)(r-s)$
101. If the area of the triangle whose vertices are  $(b, c), (c, a)$  and  $(a, b)$  is  $\Delta$ , then the area of triangle whose vertices are  $(ac-b^2, ab-c^2)$ ,  $(ba-c^2, bc-a^2)$  and  $(cb-a^2, ca-b^2)$  is
- (a)  $\Delta^2$  (b)  $(a+b+c)^2\Delta$  (c)  $a\Delta+b\Delta^2$  (d) None of these
102.  $P(2, 1), Q(4, -1), R(3, 2)$  are the vertices of a triangle and if through  $P$  and  $R$  lines parallel to opposite sides are drawn to intersect in  $S$ , then the area of  $PQRS$  is
- (a) 6 (b) 4 (c) 8 (d) 12
103. An equilateral triangle has each side equal to  $a$ . If the coordinates of its vertices are  $(x_1, y_1); (x_2, y_2); (x_3, y_3)$ , then the square of the determinant  $\begin{vmatrix} x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \\ x_3 & y_3 & 1 \end{vmatrix}$  equals
- (a)  $3a^4$  (b)  $\frac{3a^4}{4}$  (c)  $4a^4$  (d) None of these
104. Area of a  $\Delta ABC = 20$  units and its vertices  $A$  and  $B$  are  $(-5, 0)$  and  $(3, 0)$  respectively. If its vertex  $C$  lies on the line  $x - y = 2$ , then  $C$  is [IIT 1990]
- (a)  $(3, 5)$  (b)  $(-3, -5)$  (c)  $(-5, 7)$  (d) None of these
105. Point  $P$  divides the line segment joining  $A(-5, 1)$  and  $B(3, 5)$  internally in the ratio  $\lambda : 1$ . If  $Q \equiv (1, 5), R \equiv (7, 2)$  and area of  $\Delta PQR = 2$ , then  $\lambda$  equals [Kurukshetra CEE 1998]
- (a) 23 (b)  $31/9$  (c)  $29/5$  (d) None of these

Collinearity

Basic Level

106. Three points  $(p+1, 1), (2p+1, 3)$  and  $(2p+2, 2p)$  are collinear if  $p =$  [MP PET 1986]
- (a)  $-1$  (b)  $1$  (c)  $2$  (d)  $0$
107. If the points  $(a, 0), (0, b)$  and  $(1, 1)$  are collinear, then
- (a)  $\frac{1}{a^2} + \frac{1}{b^2} = 1$  (b)  $\frac{1}{a^2} - \frac{1}{b^2} = 1$  (c)  $\frac{1}{a} + \frac{1}{b} = 1$  (d)  $\frac{1}{a} - \frac{1}{b} = 1$
108. If the points  $(a, b), (a', b')$  and  $(a-a', b-b')$  are collinear, then [Rajasthan PET 1999]
- (a)  $ab' = a'b$  (b)  $ab = a'b'$  (c)  $aa' = bb'$  (d)  $a^2 + b^2 = 1$

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109. If the points  $(k, 2-2k), (1-k, 2k)$  and  $(-k-4, 6-2k)$  be collinear, then the possible values of  $k$  are [AMU 1978; Rajasthan PET 1997]
- (a)  $\frac{1}{2}, -1$  (b)  $1, -\frac{1}{2}$  (c)  $1, -2$  (d)  $2, -1$
110. If the points  $(-5, 1), (p, 5)$  and  $(10, 7)$  are collinear, then the value of  $p$  will be [MP PET 1984]
- (a) 5 (b) 3 (c) 4 (d) 7
111. If the points  $(-2, -5), (2, -2), (8, a)$  are collinear, then the value of  $a$  is [MP PET 2002]
- (a)  $-\frac{5}{2}$  (b)  $\frac{5}{2}$  (c)  $\frac{3}{2}$  (d)  $\frac{1}{2}$
112. If the points  $(5, 5), (10, K)$  and  $(-5, 1)$  are collinear, then  $K =$  [MP PET 1994, 1999; Rajasthan PET 2003]
- (a) 3 (b) 5 (c) 7 (d) 9
113. The points  $(-a, -b), (a, b), (a^2, ab)$  are
- (a) Vertices of an equilateral triangle (b) Vertices of a right angled triangle  
(c) Vertices of an isosceles triangle (d) Collinear
114. The points  $(3a, 0), (0, 3b)$  and  $(a, 2b)$  are [MP PET 1982]
- (a) Vertices of an equilateral triangle (b) Vertices of an isosceles triangle  
(c) Vertices of a right angled isosceles triangle (d) Collinear
115. The points  $(a, b), (c, d)$  and  $\left(\frac{kc+la}{k+l}, \frac{kd+lb}{k+l}\right)$  are
- (a) Vertices of an equilateral triangle (b) Vertices of an isosceles triangle  
(c) Vertices of a right angled triangle (d) Collinear

### Advance Level

116.  $A, B, C$  are the points  $(a, p), (b, q)$  and  $(c, r)$  respectively such that  $a, b, c$  are in A.P. and  $p, q, r$  in G.P. If the points are collinear, then
- (a)  $p = q = r$  (b)  $p^2 = q$  (c)  $q^2 = r$  (d)  $r^2 = p$
117.  $A, B, C$  are three collinear points such that  $AB = 2.5$  and the co-ordinates of  $A$  and  $C$  are respectively  $(3, 4)$  and  $(11, 10)$ , then the co-ordinates of the point  $B$  are
- (a)  $\left(5, \frac{11}{2}\right)$  (b)  $\left(5, \frac{5}{2}\right)$  (c)  $\left(1, \frac{11}{2}\right)$  (d)  $\left(1, \frac{5}{2}\right)$
118. The points  $(x, 2x), (2y, y)$  and  $(3, 3)$  are collinear
- (a) For all values of  $(x, y)$  (b) 2 is A.M. of  $x, y$  (c) 2 is G.M. of  $x, y$  (d) 2 is H.M. of  $x, y$
119. If  $t_1, t_2$  and  $t_3$  are distinct, the points  $(t_1, 2at_1 + at_1^3), (t_2, 2at_2 + at_2^3)$  and  $(t_3, 2at_3 + at_3^3)$  are collinear if

- (a)  $t_1 t_2 t_3 = -1$  (b)  $t_1 + t_2 + t_3 = t_1 t_2 t_3$  (c)  $t_1 + t_2 + t_3 = 0$  (d)  $t_1 + t_2 + t_3 = -1$

120. The points  $(-a, -b), (0, 0), (a, b)$  and  $(a^2, ab)$  are [IIT 1979; Kurukshetra CEE 1993; Jamia Millia Entrance Exam. 2001]

- (a) Collinear (b) Vertices of a rectangle (c) Vertices of a parallelogram (d) None of these

### Transformation of Axes

#### Basic Level

121. The new coordinates of a point  $(4, 5)$ , when the origin is shifted to the point  $(1, -2)$  are [MNR 1988; IIT 1989; UPSEAT 2000]

- (a)  $(5, 3)$  (b)  $(3, 5)$  (c)  $(3, 7)$  (d) None of these

122. The co-ordinate axes are rotated through an angle  $135^\circ$ . If the co-ordinates of a point  $P$  in the new system are known to be  $(4, -3)$ , then the co-ordinates of  $P$  in the original system are [EAMCET 2003]

- (a)  $\left(\frac{1}{\sqrt{2}}, \frac{7}{\sqrt{2}}\right)$  (b)  $\left(\frac{1}{\sqrt{2}}, \frac{-7}{\sqrt{2}}\right)$  (c)  $\left(\frac{-1}{\sqrt{2}}, \frac{-7}{\sqrt{2}}\right)$  (d)  $\left(\frac{-1}{\sqrt{2}}, \frac{7}{\sqrt{2}}\right)$

123. If the axes be rotated through an angle of  $60^\circ$  in the clockwise direction, the point  $(4, 2)$  in the new system was formally

- (a)  $(2 - \sqrt{3}, 2\sqrt{3} + 1)$  (b)  $(2 + \sqrt{3}, -2\sqrt{3} + 1)$  (c)  $(2 - \sqrt{3}, 1 - 2\sqrt{3})$  (d) None of these

#### Advance Level

124. Without changing the direction of coordinate axes origin is transferred to  $(h, k)$ , so that the linear (one degree) terms in the equation  $x^2 + y^2 - 4x + 6y - 7 = 0$  are eliminated. Then the point  $(h, k)$  is

- (a)  $(3, 2)$  (b)  $(-3, 2)$  (c)  $(2, -3)$  (d) None of these

125. The point  $(4, 1)$  undergoes the following two successive transformations

- (i) reflection about the line  $y = x$   
(ii) rotation through a distance 2 units along the positive  $x$ -axis

Then the final coordinates of the point are

- (a)  $(4, 3)$  (b)  $(3, 4)$  (c)  $(1, 4)$  (d)  $(7/2, 7/2)$

### Locus

#### Basic Level

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126. Two points  $A$  and  $B$  have coordinates  $(1, 0)$  and  $(-1, 0)$  respectively and  $Q$  is a point which satisfies the relation  $AQ - BQ = \pm 1$ . The locus of  $Q$  is [MP PET 1986]
- (a)  $12x^2 + 4y^2 = 3$  (b)  $12x^2 - 4y^2 = 3$  (c)  $12x^2 - 4y^2 + 3 = 0$  (d)  $12x^2 + 4y^2 + 3 = 0$
127. A point moves such that the sum of its distances from two fixed points  $(ae, 0)$  and  $(-ae, 0)$  is always  $2a$ . Then equation of its locus is [MNR 1981]
- (a)  $\frac{x^2}{a^2} + \frac{y^2}{a^2(1-e^2)} = 1$  (b)  $\frac{x^2}{a^2} - \frac{y^2}{a^2(1-e^2)} = 1$  (c)  $\frac{x^2}{a^2(1-e^2)} + \frac{y^2}{a^2} = 1$  (d) None of these
128. The locus of a point whose distance from the point  $(-g, -f)$  is always ' $d$ ', will be (where  $k = g^2 + f^2 - a^2$ )
- (a)  $x^2 + y^2 + 2gx + 2fy + k = 0$  (b)  $x^2 - y^2 + 2gx + 2fy + k = 0$   
(c)  $x^2 + y^2 + 2xy + 2gx + 2fy + k = 0$  (d) None of these
129. The coordinates of the points  $A$  and  $B$  are  $(a, 0)$  and  $(-a, 0)$  respectively. If a point  $P$  moves so that  $PA^2 - PB^2 = 2k^2$ , when  $k$  is a constant, then the equation to the locus of the point  $P$  is
- (a)  $2ax - k^2 = 0$  (b)  $2ax + k^2 = 0$  (c)  $2ay - k^2 = 0$  (d)  $2ay + k^2 = 0$
130. If the distance of any point  $P$  from the points  $A(a+b, a-b)$  and  $B(a-b, a+b)$  are equal, then the locus of  $P$  is [Karnataka CET 2003]
- (a)  $x - y = 0$  (b)  $ax + by = 0$  (c)  $bx - ay = 0$  (d)  $x + y = 0$
131. The locus of a point whose difference of distance from points  $(3, 0)$  and  $(-3, 0)$  is 4, is [MP PET 2002]
- (a)  $\frac{x^2}{4} - \frac{y^2}{5} = 1$  (b)  $\frac{x^2}{5} - \frac{y^2}{4} = 1$  (c)  $\frac{x^2}{2} - \frac{y^2}{3} = 1$  (d)  $\frac{x^2}{3} - \frac{y^2}{2} = 1$
132. If  $A$  and  $B$  are two fixed points in a plane and  $PA - PB = \text{constant}$ , then the locus of  $P$  is
- (a) Hyperbola (b) Circle (c) Parabola (d) Ellipse
133. If  $A$  and  $B$  are two points in a plane, so that  $PA + PB = \text{constant}$ , then the locus of  $P$  is [MNR 1991]
- (a) Hyperbola (b) Circle (c) Parabola (d) Ellipse
134. The equation of the locus of all points equidistant from the point  $(4, 2)$  and the  $x$ -axis, is [Kurukshetra CEE 1993]
- (a)  $x^2 + 8x + 4y - 20 = 0$  (b)  $x^2 - 8x - 4y + 20 = 0$  (c)  $y^2 - 4y - 8x + 20 = 0$  (d) None of these
135. The locus of a point which moves so that it is always equidistant from the points  $A(a, 0)$  and  $B(-a, 0)$  is
- (a) A circle (b) Perpendicular bisector of the line segment  $AB$   
(c) A line parallel to  $x$ -axis (d) None of these
136. The locus of a point which moves so that its distance from  $x$ -axis is double of its distance from  $y$ -axis is [AMU 1978; MP PET 1984]
- (a)  $x = 2y$  (b)  $y = 2x$  (c)  $x = 5y + 1$  (d)  $y = 2x + 3$
137.  $O$  is the origin and  $A$  is the point  $(3, 4)$ . If a point  $P$  moves so that the line segment  $OP$  is always parallel to the line segment  $OA$ , then the equation to the locus of  $P$  is

- (a)  $4x - 3y = 0$  (b)  $4x + 3y = 0$  (c)  $3x + 4y = 0$  (d)  $3x - 4y = 0$
138. If A and B are two fixed points in a plane and P is another variable point such that  $PA^2 + PB^2 = \text{constant}$ , then the locus of the point P is  
 (a) Hyperbola (b) Circle (c) Parabola (d) Ellipse
139. If sum of distances of a point from the origin and line  $x = 2$  is 4, then its locus is [Rajasthan PET 1997]  
 (a)  $x^2 - 12y = 36$  (b)  $y^2 + 12x = 36$  (c)  $y^2 - 12x = 36$  (d)  $x^2 + 12y = 36$
140. The coordinates of the points A and B are  $(ak, 0)$  and  $\left(\frac{a}{k}, 0\right)$ , ( $k = \pm 1$ ). If a point P moves so that  $PA = k PB$ , then the equation to the locus of P is  
 (a)  $k^2(x^2 + y^2) - a^2 = 0$  (b)  $x^2 + y^2 - k^2 a^2 = 0$  (c)  $x^2 + y^2 + a^2 = 0$  (d)  $x^2 + y^2 - a^2 = 0$
141. The equation of the locus of a point whose distance from  $(a, 0)$  is equal to its distance from y-axis, is  
 (a)  $y^2 - 2ax = a^2$  (b)  $y^2 - 2ax + a^2 = 0$  (c)  $y^2 + 2ax + a^2 = 0$  (d)  $y^2 + 2ax = a^2$
142. The locus of the point of intersection of lines  $x \cos \alpha + y \sin \alpha = a$  and  $x \sin \alpha - y \cos \alpha = b$  is ( $\alpha$  is a variable)  
 (a)  $2(x^2 + y^2) = a^2 + b^2$  (b)  $x^2 - y^2 = a^2 - b^2$  (c)  $x^2 + y^2 = a^2 + b^2$  (d) None of these
143. Two points A and B move on the x-axis and the y-axis respectively such that the distance between the two points is always the same. The locus of the middle point of AB is  
 (a) A straight line (b) A circle (c) A parabola (d) An ellipse

### Advance Level

144. The locus of P such that area of  $\triangle PAB = 12 \text{ sq. units}$ , where  $A(2, 3)$  and  $B(-4, 5)$  is [EAMCET 1989]  
 (a)  $(x + 3y - 1)(x + 3y - 23) = 0$  (b)  $(x + 3y + 1)(x + 3y - 23) = 0$   
 (c)  $(3x + y - 1)(3x + y - 23) = 0$  (d)  $(3x + y + 1)(3x + y + 23) = 0$
145. Locus of centroid of the triangle whose vertices are  $(a \cos t, a \sin t)$ ,  $(b \sin t, -b \cos t)$  and  $(1, 0)$ , where  $t$  is a parameter is [AIEEE 2003]  
 (a)  $(3x - 1)^2 + (3y)^2 = a^2 - b^2$  (b)  $(3x - 1)^2 + (3y)^2 = a^2 + b^2$   
 (c)  $(3x + 1)^2 + (3y)^2 = a^2 + b^2$  (d)  $(3x + 1)^2 + (3y)^2 = a^2 - b^2$
146. If A is  $(2, 5)$ , B is  $(4, -11)$  and C lies on  $9x + 7y + 4 = 0$ , then the locus of the centroid of the  $\triangle ABC$  is a straight line parallel to the straight line [MP PET 1986]  
 (a)  $7x - 9y + 4 = 0$  (b)  $9x - 7y - 4 = 0$  (c)  $9x + 7y + 4 = 0$  (d)  $7x + 9y + 4 = 0$
147. Two fixed points are  $A(a, 0)$  and  $B(-a, 0)$ . If  $\angle A - \angle B = \theta$ , then the locus of point C of triangle ABC will be [Roorkee 1982]  
 (a)  $x^2 + y^2 + 2xy \tan \theta = a^2$  (b)  $x^2 - y^2 + 2xy \tan \theta = a^2$  (c)  $x^2 + y^2 + 2xy \cot \theta = a^2$  (d)  $x^2 - y^2 + 2xy \cot \theta = a^2$
148. If  $A(-a, 0)$  and  $B(a, 0)$  are two fixed points, then the locus of the point on which the line AB subtends the right angle, is

## 28 Rectangular Cartesian Co-ordinates

- (a)  $x^2 + y^2 = 2a^2$       (b)  $x^2 - y^2 = a^2$       (c)  $x^2 + y^2 + a^2 = 0$       (d)  $x^2 + y^2 = a^2$
149. The coordinates of the points  $O$ ,  $A$  and  $B$  are  $(0, 0)$ ,  $(0, 4)$  and  $(6, 0)$  respectively. If a point  $P$  moves such that the area of  $\Delta POA$  is always twice the area of  $\Delta POB$ , then the equation to both parts of the locus of  $P$  is [IIT 1964]
- (a)  $(x - 3y)(x + 3y) = 0$       (b)  $(x - 3y)(x + y) = 0$       (c)  $(3x - y)(3x + y) = 0$       (d) None of these
150. A stick of length  $l$  rests against the floor and a wall of a room. If the stick begins to slide on the floor, then the locus of its middle point is
- (a) A straight line      (b) Circle      (c) Parabola      (d) Ellipse
151. Given the points  $A(0, 4)$  and  $B(0, -4)$ . Then the equation of the locus of the point  $P(x, y)$  such that  $|AP - BP| = 6$ , is [IIT 1983; MP PET 1994]
- (a)  $\frac{x^2}{7} + \frac{y^2}{9} = 1$       (b)  $\frac{x^2}{9} + \frac{y^2}{7} = 1$       (c)  $\frac{x^2}{7} - \frac{y^2}{9} = 1$       (d)  $\frac{y^2}{9} - \frac{x^2}{7} = 1$
152. If  $P = (1, 0)$ ,  $Q = (-1, 0)$  and  $R = (2, 0)$  are three given points, then the locus of a point  $S$  satisfying the relation  $SQ^2 + SR^2 = 2SP^2$  is [IIT 1988]
- (a) A straight line parallel to  $x$ -axis      (b) A circle through origin  
(c) A circle with centre at the origin      (d) A straight line parallel to  $y$ -axis
153. The locus of a point which moves in such a way that its distance from  $(0, 0)$  is three times its distance from the  $x$ -axis, as given by [MP PET 1993]
- (a)  $x^2 - 8y^2 = 0$       (b)  $x^2 + 8y^2 = 0$       (c)  $4x^2 - y^2 = 0$       (d)  $x^2 - 4y^2 = 0$
154.  $A(a, 0)$  and  $B(-a, 0)$  are two fixed points of triangle  $ABC$ . The vertex  $C$  moves in such a way that  $\cot A + \cot B = \lambda$ , where  $\lambda$  is a constant. Then the locus of the point  $C$  is [MP PET 1981]
- (a)  $y\lambda = 2a$       (b)  $ya = 2\lambda$       (c)  $y = \lambda a$       (d) None of these
155. A line of fixed length  $(a + b)$  moves so that its ends are always on two fixed perpendicular lines. The locus of the point which divides this line into portions of lengths  $a$  and  $b$  is
- (a) A circle      (b) An ellipse      (c) A hyperbola      (d) None of these

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# Answer Sheet

Rectangular Cartesian Co-ordinates

Assianment (Basic and Advance Level)

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
a	c	c	c	d	a	b	d	b	d	b	b	a	d	c	c	b	c	c	c
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40
c	c	c	b	a	b	b	b	a	b	b	c	d	b	c	d	d	b	c	b
41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60
b	c	b	b	c	c	a	c	a	c	c	d	c	a	a	a	c	c	a	b
61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80
c	a	c	a	a,c	b	c	b	a	d	a	b	b	b	a	c	a	a	a	b
81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100
a,c,d	b	c	d	a	b	d	b	a	a	d	d	a	a	a	a	c	d	c	c
101	102	103	104	105	106	107	108	109	110	111	112	113	114	115	116	117	118	119	120
b	b	b	b	a	c	c	a	a	a	b	c	d	d	d	a	a	d	c	a
121	122	123	124	125	126	127	128	129	130	131	132	133	134	135	136	137	138	139	140
c	d	b	c	b	b	a	a	b	a	a	a	d	b	b	b	a	b	b	d



141	142	143	144	145	146	147	148	149	150	151	152	153	154	155
b	c	b	b	b	c	d	d	a	b	d	d	a	a	b