

Topics : Sequence & Series, Application of Derivatives

Type of Questions

M.M., Min.

Comprehension (no negative marking) Q.1 to Q.3

(3 marks, 3 min.)

[9, 9]

Single choice Objective (no negative marking) Q. 4,5

(3 marks, 3 min.)

[6, 6]

Fill in the Blanks (no negative marking) Q.6

(4 marks, 4 min.)

[4, 4]

Subjective Questions (no negative marking) Q.7,8

(4 marks, 5 min.)

[8, 10]

COMPREHENSION (Q. NO. 1 TO 3)

Consider $S_n = \frac{8}{5} + \frac{16}{65} + \dots + \frac{8r}{4r^4 + 1}$

1. Sum of infinite terms of above series will be

(A) 0 (B) $\frac{1}{2}$ (C) 2 (D) None of these

2. The value of S_{16} must be

(A) $\frac{80}{41}$ (B) $\frac{1088}{545}$ (C) $\frac{107}{245}$ (D) None of these

3. If $S_n = \frac{an^2 + bn}{cn^3 + dn^2 + en + 1}$, where a, b, c, d, e are independent of 'n', then

(A) a = 4, e = 2 (B) c = 0, d = 4 (C) b = 4, e = 4 (D) None of these

4. Tangent and normal to the curve $y = 2 \sin x + \sin 2x$ are drawn at $p \left(x = \frac{\pi}{3} \right)$. The area of the quadrilateral formed by the tangent, the normal and coordinate axes is.

(A) $\frac{\pi\sqrt{3}}{2}$ (B) $\frac{\pi}{2}$ (C) $\frac{\sqrt{3}}{2}$ (D) None of these

5. The point(s) of minimum of the function, $f(x) = 4x^3 - x|x - 2|$, $x \in [0, 3]$ is :

(A) x = 0 (B) x = $\frac{1}{3}$ (C) x = $\frac{1}{2}$ (D) x = 2

6. The value of a for which the function $f(x) = (4a - 3)(x + \log 5) + 2(a - 7) \cot \frac{x}{2} \sin^2 \frac{x}{2}$ does not posses critical points is _____.

7. Find the difference between the greatest and least values of the function,

$f(x) = \cos x + \frac{1}{2} \cos 2x - \frac{1}{3} \cos 3x$.

8. Find values of a and b such that $f(x) = \frac{a}{x} + bx$ has a minimum at point (1, 6).

Answers Key

1. (C) 2. (B) 3. (A) 4. (A)
5. (B) 6. $(-\infty, -4/3) \cup (2, \infty)$
7. $9/4$ 8. $a = b = 3$