

Topics : Solution of Triangle, Circle

Type of Questions		M.M., Min.
Single choice Objective (no negative marking) Q.1,2,3,4	(3 marks, 3 min.)	[12, 12]
Subjective Questions (no negative marking) Q.5,6	(4 marks, 5 min.)	[8, 10]
Match the Following (no negative marking) Q.7	(8 marks, 8 min.)	[8, 8]

- If in a $\triangle ABC$, $\frac{r}{r_1} = \frac{1}{2}$, then the value of $\tan \frac{A}{2} \left(\tan \frac{B}{2} + \tan \frac{C}{2} \right)$ is equal to :
 (A) 2 (B) $\frac{1}{2}$ (C) 1 (D) None of these
- A triangle is inscribed in a circle. The vertices of the triangle divide the circle into three arcs of length 3, 4 and 5 units. Then area of the triangle is equal to:
 (A) $\frac{9\sqrt{3}(1+\sqrt{3})}{\pi^2}$ (B) $\frac{9\sqrt{3}(\sqrt{3}-1)}{\pi^2}$ (C) $\frac{9\sqrt{3}(1+\sqrt{3})}{2\pi^2}$ (D) $\frac{9\sqrt{3}(\sqrt{3}-1)}{2\pi^2}$
- Let PQR be a triangle of area Δ with $a = 2$, $b = \frac{7}{2}$ and $c = \frac{5}{2}$, where a, b and c are the lengths of the sides of the triangle opposite to the angles at P, Q and R respectively. Then $\frac{2\sin P - \sin 2P}{2\sin P + \sin 2P}$ equals
 (A) $\frac{3}{4\Delta}$ (B) $\frac{45}{4\Delta}$ (C) $\left(\frac{3}{4\Delta}\right)^2$ (D) $\left(\frac{45}{4\Delta}\right)^2$
- Orthocentre of an acute triangle ABC is at the origin and its circumcentre has the co-ordinates $\left(\frac{1}{2}, -\frac{1}{2}\right)$.
 If the base BC has the equation $4x - 2y = 5$, then the radius of the circle circumscribing the triangle ABC, is
 (A) $\sqrt{5/2}$ (B) $\sqrt{3}$ (C) $\frac{3}{\sqrt{2}}$ (D) $\sqrt{6}$
- In a triangle ABC, prove that the area of the incircle is to the area of triangle itself is,
 $\pi : \cot \left(\frac{A}{2}\right) \cdot \cot \left(\frac{B}{2}\right) \cdot \cot \left(\frac{C}{2}\right)$.

6. In a triangle PQR, PL & QM are the medians. If $PL = 6$ cm, $\angle QPL = \pi/6$ and $\angle PQM = \pi/3$, then the area of triangle PQR is _____.

7. **Column – I**

Column – II

- | | |
|---|--------|
| (A) In a $\triangle ABC$, $a = 4$, $b = 3$ and the medians AA_1 and BB_1 are mutually perpendicular, then square of area of the $\triangle ABC$ is equal to | (p) 3 |
| (B) If in an acute angled $\triangle ABC$, line joining the circumcentre and orthocentre is parallel to side AC, then value of $\tan A \cdot \tan C$ is equal to | (q) 7 |
| (C) In a $\triangle ABC$, $a = 5$, $b = 4$ and $\tan \frac{C}{2} = \sqrt{\frac{7}{9}}$, then side 'c' is equal to | (r) 6 |
| (D) In a $\triangle ABC$, $2a^2 + 4b^2 + c^2 = 4ab + 2ac$, then value of $(8 \cos B)$ is equal to | (s) 11 |

Answers Key

1. (B) 2. (A) 3. (C) 4. (A)

6. $8\sqrt{3}$ sq. unit

7. (A) \rightarrow (s), (B) \rightarrow (p), (C) \rightarrow (r), (D) \rightarrow (q)