## Number System and its Operations

## QUESTIONS

OLYMPIAD XCELLENCE MATHEMATICS

1.	Which is the smallest d	igit?				
	(a) 1	(b) –1	(c) 0	(d) 10		
2.	Which is the smallest n	umber of one digit.				
	(a) 9	(b) 2	(c) 1	(d) 10		
3.	The difference between	the place value and the f	ace value of 8 in 658742	is		
	(a) 0	(b) 7992	(c) 6800	(d) 5930		
4.	How many times does the digit 9 occur between 1 to 100?					
	(a) 11	(b) 15	(c) 18	(d) 20		
5.	One billion equals					
	(a) 1 Crore	(b) 10 Crore	(c) 100 Crore	(d) 1000 Crore		
6.	How many lakhs are there in one million?					
	(a) 100	(b) 10	(c) 1000	(d) None of these		
7.	The additive inverse of	17 is				
	(a) 17	(b) -17	(c) $\frac{1}{17}$	$(d) - \frac{1}{17}$		
8.	Evaluate: $7 \times  -15  -  -15 $	-9 ×8				
	(a) 22	(b) 33	(c) 11	(d) –120		
9.	The integer 8 more tha	n –12 is				
	(a) 4	(b) –4	(c) –20	(d) 20		
10.	Which of the following	pairs of integer does repre	esent 5 as a difference?			
	(a) 10, 5	(b) –10, –5	(c) 5,-20	(d) both (a) & (b)		
11.	Which of the following	is not meaningful?				
	(a) XIV	(b) XXXV	(c) XXV	(d) VX		
12.	The smallest number w	hen rounded off to the ne	arest hundred as 600, is			
	(a) 550	(b) 595	(c) 604	(d) 599		
13.	Expanded form of $M$ +	DC + LXX + IX = ?				
	(a) 1015	(b) 1679	(c) 1999	(d) 2000		
14.	Express CDXLVI in Hir	ndu-Arabic numerical.				
	(a) 446	(b) 228	(c) 165	(d) 500		
15.	The largest three digit r	number formed by the dig	its 8, 5, 9, is			
	(a) 985	(b) 859	(c) 958	(d) 589		
16.	The total number of 4 o	ligit numbers is				
	(a) 8999	(b) 9000	(c) 8000	(d) 9999		
17.	$244 + (8 \times 4) - 300 \div 6$	=?				
	(a) 226	(b) 220	(c) 223	(d) 224		

10	I					
18.		ce value-system, we write				
10	(a) 1 lakh $(12)$ is as	(b) 10 lakh	(c) 100 lakh	(d) 1 Crore		
19.	(-16) + 14 - (-13) is equivalent of (-16) and (-13) is equivalent of (-13) is equivalent		( ) 11			
	(a) -11	(b) 12	(c) 11	(d) –15		
20.	_	ers is $-22$ and one of the				
	(a) -12	(b) 12	(c) –36	(d) 40		
21.	-	-	-	d denominator to the nearest hundreds.		
	(a) 28	(b) 20	(c) 24	(d) 26		
22.		digit number with unique	-			
	(a) 102	(b) 103	(c) 101	(d) 104		
23.			o the nearest hundred, I	am 500. Rounding off to the nearest 10		
	makes me 530. What a		( ) 221			
	(a) 543	(b) 534	(c) 831	(d) 426		
24.			ha School. If the annual f	fee per student is Rs. 62,606. What is the		
	total fee collected annu					
	(a) Rs. 4,00,000	(b) Rs. 49,145,710	(c) Rs. 7,96,42,000	(d) Rs. 4,66,72,000		
25.		- digit number having fou	-			
	(a) 1000023	(b) 1000027	(c) 1000026	(d) 700426		
26.	Find $1 - 2 + 3 - 4 + 5 - 6$	6+				
	+17 - 18 + 19 - 20 = ?					
	(a) 10	(b) -10	(c) 100	(d) 200		
27.	If $x = (-23) + 22 + (-23)$	+22+ (up to 40	terms) $y = 12 + (-11) + 12$	$2 + (-11) + \dots$ (up to 20 terms), then find		
	y - x = ?					
	(a) 30	(b) -30	(c) 40	(d) -40		
28.	The number 170916A	B (A, B, are digits) is divisi	ble by 66. Then the value	e of A can be		
	(a) 9	(b) 3	(c) 7	(d) 5		
29.	Rohit started a game of	Rohit started a game of monopoly with Rs. 70. He had to pay Rs. 25 as tax and he received Rs. 10 as rent of one of				
	his sites. He won Rs. 2	s sites. He won Rs. 20 by way of lottery and was then fined Rs. 50 for overspending. How much money was left				
	with him at the end of	the game?				
	(a) 25	(b) 30	(c) 36	(d) 100		
30.	If $x$ and $y$ are two int	egers such that x is the pr	edecessor of y, the $x - y$ i	s equal to		
	(a) 1	(b) 0	(c) 2	(d) –1		
31.	What is the minimum r	number of four digits form	ed by using the digits 3, 4	, 0, 8?		
	(a) 3048	(b) 3348	(c) 3408	(d) 3480		
32.	Find the unit's digit in (	261) <sup>43</sup> + (426) <sup>73</sup>				
	(a) 8	(b) 7	(c) 4	(d) 5		

33.	How many zeros will be	e there at the end of 1000 :	×25×8×32×125×3	
	(a) 9	(b) 6	(c) 7	(d) 8
34.	Rohit had forgotten his	6 - digit bank account nun	nber but only remembered	d that it was of the form A515A0 and was
	divisible by 36. What is	the value of A?		
	(a) 4	(b) 7	(c) 8	(d) 9
35.	How many number betw	ween 1 and 250 can be re	epresented for $a^b$ , where $b$	b > a > 1 ?
	(a) 6	(b) 7	(c) 8	(d) 9
36.	I have 76 sweets and I	want to distribute them e	qually among 23 students	s after each of the student got maximum
	integral sweets. How ma	any sweets are left with m	e?	
	(a) 1	(b) 8	(c) 6	(d) 5
37.	Which of the following n	numbers is the greatest nur	nber dividing a family of n	number $(N^3 - N)$ , Where N is any natural
	number?			
	(a) 0	(b) 2	(c) 7	(d) 6
38.	$N^2 = 12345678910111$	.0987654321.		
	Find N			
	(a) 11111111111	(b) 10000001	(c) 12345111	(d) 12312111
39.	In Patna, all the number	rs are expressed with the l	help of three alphabets x,	y, and z.
	15 is written as xyz.			
	6 is written as yz.			
	60 is written as yzyz.			
	How to many ways doe	es write 17 in Patna?		
	(a) хуу	(b) yxy	(c) yxx	(d) xyx
40.	Let x, y and z be digits s	such that $(100x + 10y + z)$	(x + y + z) = 2005. What i	s the value of x?
	(a) 4	(b) 2	(c) 3	(d) 6

ANSWER - KEY					
<b>1</b> . C	<b>2</b> . C	<b>3.</b> B	<b>4.</b> D	<b>5.</b> C	
<b>6.</b> B	<b>7.</b> B	<b>8.</b> B	<b>9.</b> B	<b>10.</b> A	
<b>11</b> . C	<b>12</b> . A	<b>13.</b> B	14. A	<b>15.</b> A	
<b>16.</b> B	<b>17</b> . A	<b>18.</b> B	<b>19.</b> C	<b>20.</b> C	
<b>21</b> . A	<b>22</b> . A	<b>23.</b> B	<b>24.</b> B	<b>25</b> . A	
<b>26.</b> B	<b>27</b> . A	<b>28.</b> A	<b>29.</b> A	<b>30.</b> D	
<b>31</b> . A	<b>32.</b> B	<b>33.</b> A	<b>34.</b> C	<b>35.</b> B	
<b>36</b> . A	<b>37</b> . D	<b>38.</b> A	<b>39.</b> A	<b>40.</b> A	

## **SOLUTIONS**

 $\therefore 0 = \text{Smallest}$ 0, 1, 2, 3, 4, 5, 6, 7, 8, 9 2.  $\therefore$  1 = Smallest number of one digit. 658742 3. Place Value =  $8 \times 1000 = 8000$ Face value = 8Difference = 8000 - 8 = 79929,19,29,39,49,59,69,79,89,90,91,92,93,94,95,96,97,98,99 4.  $\therefore$  Total no. of 9 occurs = 20 One billion = 1000 millions 5. =100Crores One million = 1000 thousands = 10 lakhs 6. 7. 17 + x = 0x = -17*.*.  $7 \times |-15| - |-9| \times 8$  (|-15| = 15 and |-9| = 9) 8.  $\therefore$  7 × 15 - 9 × 8 = 105 - 72 = 33 Let no. be x9. Then; x = -12 + 8 = -4∴ No. is -4 10. 10 - 5 = 511. XXV (it does not mean anything) 12. 550 (smallest no. rounded near hundreds is 600) 13. M + DC + LXX + IX=1000+600+70+9=1679CDXLVI = 400 + 40 + 6 = 44614. 15. 985 16. (999 - 1000 + 1) = (8999 + 1) = 9000 $244 + (8 \times 4) - 300 \div 6$ 17. = 244 + 32 - 50 = 276 - 50 = 22618. One million = 1000 thousands = 10 lakhs 19. (-16) + 14 - (-13)=(-16)+14+13=27-16=11

0, 1, 2, 3, 4, 5, 6, 7, 8, 9

1.

x = -22 - 14 = -36 $\frac{2828}{125} \Rightarrow \frac{2800}{100}$ 2828 (after rounding) 21. = 28 22. 100, 101, 102 (102 is unique digits because its all digit are different) 23. The number is between 525 & 534 and its digit sum is 12 5 + 3 + 4 - 12So, 534 is the number. Total fee =  $785 \times 62606 = \text{Rs.} 49,145,710$ 24. 25. 1000023 unique digits (4 only)  $1\!-\!2\!+\!3\!-\!4\!+\!5\!-\!6\!+\!\ldots\!+\!19\!-\!20$ 26.  $(-1) + (-1) + (-1) + \dots + (-1) \rightarrow 10$  times = -1027. x = (-1) + (-1) + (-1).... (20 terms) = -20 y = 1 + 1 + 1 c..... (10 terms) = 10 y - x = 10 - (-20) = 10 + 20 = 30**28**. 170916AB = -(1+0+1+A) + (7+9+6+B) $= 22 + B - 2 - A = 20 + B - A = 11 \rightarrow A - B = 9$ And 1+7+0+9+1+6+A+B=24+A+BcA = 9 and B = 029. Initially he had Rs. +70 Paid as tax Rs. -25 Received rent of site Rs. 10 Won lottery money Rs. 20 Fined for over speeding Rs. -50At the end of the game she was left with RS. = [70 + (-25) + 10 + 20 + (-50)]  $= \left[ (70 + 10 + 20) + \{(-25) + (-50)\} \right]$ = [100 + (-75)] = Rs.25**30**. y - x = 1 $\therefore x - y = -1$ 31. Required Number = 3048Required units digit = Units digit in  $(1)^{43} + (6)^{73}$ 32.

Let the integer be x, then 14 + x = -22

20.

Now  $(1)^{43} = 1$  and  $(6)^{73} = 6$ 

Hence Units digit in  $(216)^{43} + (426)^{73} =$  unit digit

In 
$$(1+6) = 7$$

- **33.** No of zero  $= 1000 \times 25 \times 8 \times 32 \times 125 \times 3 = 9$
- **34.** Divisibility rule of 9 is that the sum of all digits should be divisible by 9. Therefore

$$\frac{A+5+1+5+A+O}{9} = \frac{11+2A}{9}$$

From here, A should be 8.

Therefore, the number is 851, 580, which is also divisible by 4.

- **35.** For a = 3 there are five number present form  $2^3$  to  $2^7$ , for x = 3, there are two number present form  $3^4$  and  $3^5$ .
- **36.** The question is asking about the remainder When we divide  $7^6$  by  $2^3$ . Remainder is 1.
- **37.** Substitute the value of N(1,2,3...) find value of  $N^3 N$ , which is always divisible by 6.
- **38.**  $(1111111111)^2 = 12345678910111098765432$
- **39.** The key is the fact that in Patna, only three symbols are used to write numbers. Therefore,  $6 = (20)_3 = (yz)_3$ , y = 2, z = 0 and  $x = 1, 17 = (122)_3 = xyy$
- **40.** Clearly, the two quantities are both integers, and therefore, we check the prim factorization of  $2005 = 5 \times 401$ . It can be seen that (x, y, z) = (4, 0, 1)

Satisfies the relation. Hence, option (a) is the answer.