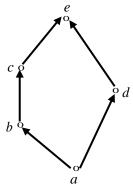
COMPUTER SCIENCE ENGINEERING

Q. No. 1 – 25 Carry One Mark Each

1. Consider the set $X = \{a, b, c, d, e\}$ under the partial ordering

$$R = \{(a,a),(a,b),(a,c),(a,d),(a,e),(b,b),(b,c),(b,e),(c,c),(c,e),(d,d),(d,e),(e,e)\}.$$

The Hasse diagram of the partial order (X, R) is shown below.



The minimum number of ordered pairs that need to be added to R to make (X, R) a lattice is _____.

Answer: (0)

- **2.** Which of the following statements about parser is/are CORRECT?
 - I. Canonical LR is more powerful than SLR.
 - II. SLR is more powerful than LALR
 - III. SLR is more powerful than Canonical LR.
 - (A) I only
- (B) II only
- (C) III only
- (D) II and III only

Answer: (A)

3. Match the following:

P.	static char var;	i.	Sequence of memory locations to store addresses
Q.	m= malloc (10); m = NULL;	ii.	A variable located in data section of memory
R.	char * ptr [10]	iii.	Request to allocate a CPU register to store data
S.	register int var1;	iv.	A lost memory which cannot be freed

(A) P-(ii), Q-(iv), R-(i), S-(iii)

(B) P-(ii), Q-(i), R-(iv), S-(iii)

- (C) P-(ii), Q-(iv), R-(iii), S-(i)
- (D) P-(iii), Q-(iv), R-(i), S-(ii)

Answer: (A)

- **4.** Let L_1, L_2 be any two context free languages and R be any regular language. Then which of the following is/are CORRECT?
 - **I.** $L_1 \cup L_2$ is context free

II. $\overline{L_1}$ is context – free

III. $L_1 - R$ is context - free

IV. $L_1 \cap L_2$ is context – free

(A) I, II and IV only

(B) I and III only

(C) II and IV only

(D) I only

Answer: (B)

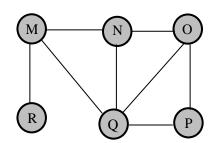
5. G is undirected graph with *n* vertices and 25 edges such that each vertex of G has degree at least 3. Then the maximum possible value of *n* is ______.

Answer: (16)

- **6.** Let p, q, r denote the statements "It is raining," It is cold", and "It is pleasant," respectively. Then the statement "It is not raining and it is pleasant, and it is not pleasant only if it is raining and it is cold" is represented by
 - (A) $(\neg p \land r) \land (\neg r \rightarrow (p \land q))$
- $(B) \quad (\neg p \land r) \land ((p \land q) \rightarrow \neg r)$
- (C) $(\neg p \land r) \lor ((p \land q) \rightarrow \neg r)$
- (D) $(\neg p \land r) \lor (r \rightarrow (p \land q))$

Answer: (A)

7. The Breadth First Search (BFS) algorithm has been implemented using the queue data structure. Which one of the following is a possible order of visiting the nodes in the graph below?



- (A) MNOPQR
- (B) NQMPOR
- (C) QMNROP
- (D) POQNMR

Answer: (D)

8. Let $P = \begin{bmatrix} 1 & 1 & -1 \\ 2 & -3 & 4 \\ 3 & -2 & 3 \end{bmatrix}$ and $Q = \begin{bmatrix} -1 & -2 & -1 \\ 6 & 12 & 6 \\ 5 & 10 & 5 \end{bmatrix}$ be two matrices.

Then the rank of P +Q is _____.

Answer: (2)

- 9. Consider socket API on a Linux machine that supports connected UDP sockets. A connected UDP socket is a UDP socket on which **connect** function has already been called. Which of the following statements is/are CORRECT?
 - I. A connected UDP socket can be used to communicate with multiple peers simultaneously.
 - **II.** A process can successfully call **connect** function again for an already connected UDP socket.
 - (A) I only
- (B) II only
- (C) Both I and II
- (D) Neither I nor IIs

Answer: (B)

10. The minimum possible number of states of a deterministic automaton that accepts the regular language $L = \{w_1 a w_2 | w_1, w_2 \in \{a, b\}^*, |w_1| = 2, |w_2| \ge 3\} \text{ is } \underline{\hspace{1cm}}.$

Answer: (8)

11. Consider the following tables T1 and T2.

P	Q
2	2
3	8
7	3
5	8
6	9
8	5
9	8

R	S
2	2
8	3
3	2
9	7
5	7
7	2

In table T1, **P** is the primary key and **Q** is the foreign key referencing **R** in table T2 with on-delete cascade and on-update cascade. In table T2, **R** is the primary key and **S** is the foreign key referencing **P** in table T1 on-delete set NULL and on-update cascade. In order to delete record $\langle 3,8 \rangle$ from table T1, the number of additional records that need to be deleted from table T1 is _______.

Answer: (0)

12. Which of the following is/are shared by all the threads in a process?

I. Program counter

II. Stack

III. Address space

IV. Registers

(A) I and II only

(B) III only (C) IV only

(D) III and IV only

Answer: (B)

- 13. A circular queue has been implemented using a single linked list where each node consists of a value and a single pointer pointing to the next node. We maintain exactly two external pointers **FRONT** and **REAR** pointing to the front node and the rear node of the queue, respectively. Which of the following statements is/are **CORRECT** for such a circular queue, so that insertion and deletion operation can be performed in O (1) time?
 - **I.** Next pointer of front node points to the rear node.
 - **II.** Next pointer of rear node points to the front node.

- (A) I only
- (B) II only
- (C) Both I and II
- (D) Neither I nor II

Answer: (B)

14. Given the following binary number in 32-bit (single precision) IEEE-754 format:

The decimal value closest to this floating- point number is

- (A) 1.45×10^{1}
- (B) 1.45×10^{-1}
- (C) 2.27×10^{-1}
- (D) 2.27×10^{1}

Answer: (C)

- 15. An ER model of a database consists of entity types A and B. These are connected by a relationship R which does not have its own attribute. Under which one of the following conditions, can the relational table for R be merged with that of A?
 - (A) Relationship R is one-to-many and the participation of A in R is total
 - (B) Relationship R is one-to-many and the participation of A in R is partial
 - (C) Relationship R is many-to one and the participation of A in R is total
 - (D) Relationship R is many-to one and the participation of A in R is partial

Answer: (C)

16. Match the algorithms with their time complexities:

Algorithm		Time complexity	
P.	Towers of Hanoi with <i>n</i> disks	i.	$\theta(n^2)$
Q.	Binary search given <i>n</i> sorted numbers	ii.	$\theta(n\log n)$
R.	Heap sort given n numbers at the worst case	iii.	$\theta(2^n)$
S.	Addition of two $n \times n$ matrices	iv.	$\theta(\log n)$

(A) P-(iii), Q-(iv), R-(i), S-(ii)

(B) P-(iv),Q-(iii), R-(i), S-(ii)

(C) P-(iii), Q-(iv), R-(ii), S-(i)

(D) P-(iv),Q-(iii), R-(ii), S-(i)

Answer: (C)

17. Match the following according to input (from the left column) to the complier phase (in the right column) that processes it.

Column-1		Column-2	
P.	Syntax tree	i.	Code generator
Q.	Character stream	ii.	Syntax analyzer
R.	Intermediate representation	iii.	Semantic analyzer
S.	Token stream	iv.	Lexical analyzer

(A) P-(ii), Q-(iii), R-(iv), S-(i)

P-(ii), Q-(i), R-(iii), S-(iv)

P-(iii), Q-(iv), R-(i), S-(ii)

(D) P-(i), Q-(iv), R-(ii), S-(iii)

Answer: (C)

- Consider the following statements about the routing protocols, Routing Information Protocol (RIP) and **18.** Open Shortest Path First (OSPF) in an IPv4 network.
 - I. RIP uses distance vector routing
 - II. RIP packets are sent using UDP
 - III. OSPF packets are sent using TCP
 - IV. OSPF operation is based on link-state routing

Which of the statements above are CORRECT?

(A) I and IV only

(B) I, II and III only

I, II and IV only (C)

II, III and IV only (D)

Answer: (C)

- 19. If $f(x) = R \sin\left(\frac{\pi x}{2}\right) + S$, $f'\left(\frac{1}{2}\right) = \sqrt{2}$ and $\int_0^1 f(x) dx = \frac{2R}{\pi}$, then the constants R and S are, respectively

- (A) $\frac{2}{\pi}$ and $\frac{16}{\pi}$ (B) $\frac{2}{\pi}$ and 0 (C) $\frac{4}{\pi}$ and 0 (D) $\frac{4}{\pi}$ and $\frac{16}{\pi}$

Answer: (C)

- **20.** In a file allocation system, which of the following allocation schemes(s) can be used if no external fragmentation is allowed?
 - I. Contiguous
- II. Linked
- III. Indexed

- (A) I and III only
- (B) II only
- (C) III only
- (D) II and III only

Answer: (D)

21. Consider a quadratic equation $x^2 - 13x + 36 = 0$ with coefficients in a base b. The solutions of this equation in the same base b are x = 5 and x = 6. Then b =______.

Answer: (8)

22. Identify the language generated by the following grammar, where S is start variable.

 $S \rightarrow XY$

 $X \rightarrow aX|a$

 $Y \rightarrow a Yb \in$

(A) $\{a^mb^n | m \ge n, n > 0\}$

(B) $\left\{a^mb^n \mid m \geq n, n \geq 0\right\}$

 $(C) \qquad \left\{a^mb^n \middle| m > n, n \ge 0\right\}$

(D) $\left\{a^{m}b^{n}\middle|m>n,n>0\right\}$

Answer: (C)

- **23.** The representation of the value of a 16-bit unsigned integer X in hexadecimal number system is BCA9. The representation of the value of X in octal number system is
 - (A) 571244
- (B) 736251
- (C) 571247
- (D) 136251

Answer: (D)

24. Consider the following function implemented in C:

void print xy (int x, int y) {

int *ptr;

x = 0;

ptr = &x;

```
y = * ptr;
* ptr = 1;
printf ("%d, %d," x,y);
}
```

The output of invoking print xy (l, l) is

- (A) 0,0
- (B) 0.1
- (C) 1,0
- (D) 1,1

Answer: (C)

25. The maximum number of IPv4 router addresses that can be listed in the record route (RR) option field of an IPv4 header is ______.

Answer: (9)

Q. No. 26 – 55 Carry Two Marks Each

26. Consider a binary code that consists of only four valid code words as given below:

00000,01011,10101,11110

Let the minimum Hamming distance of the code be p and the maximum number of erroneous bits that can be corrected by the code be q. Then the values of p and q are

(A) p = 3 and q = 1

(B) p = 3 and q = 2

(C) p = 4 and q = 1

(D) p = 4 and q = 2

Answer: (A)

27. A system shares 9 tape drives. The current allocation and maximum requirement of tape drives for three processes are shown below:

Process	Current Allocation	Maximum Requirement	
P1	3	7	
P2	1	6	
Р3	3	5	

Which of the following best describes current state of the system?

(A) Safe, Deadlocked

(B) Safe, Not Deadlocked

(C) Not Safe, Deadlocked

(D) Not Safe, Not deadlocked

Answer: (B)

28. Two transactions T_1 and T_2 are given as:

$$T_1: r_1(X)w_1(X)r_1(Y)w_1(Y)$$

 $T_2: r_2(Y)w_2(Y)r_2(Z)w_2(Z)$

where $r_i(V)$ denotes a read operation by transaction T_i on a variable V and $w_i(V)$ denotes a write operations by transaction T_i on a variable V. The total number of conflict serializable schedules that can be formed by T_1 and T_2 is ______.

Answer: (54)

29. If w, x, y, z are Boolean variables, then which one of the following is INCORRECT?

```
(A) wx+w(x+y)+x(x+y)=x+wy
```

(B)
$$\overline{wx(y+z)} + \overline{wx} = \overline{w} + x + \overline{yz}$$

(C)
$$(\overline{wx}(y+x\overline{z})+\overline{wx})y=x\overline{y}$$

(D)
$$(w+y)(wxy+wyz) = wxy+wyz$$

Answer: (C)

30. Consider the following C Program.

```
# include <stdio.h>
#include<string.h>
#int main (){
    char* c = "GATECSIT2017";
    char* p = c;
printf("%d", (int) strlen (c+2[p]-6[p]-1));
return 0;
}
```

The output of the program is ______

Answer: (2)

- 31. P and Q are considering to apply for a job. The probability that P applies for the job is $\frac{1}{4}$. The probability that P applies for the job given that Q applies for the job is $\frac{1}{2}$, and the probability that Q applies for the job given that P applies for the job $\frac{1}{3}$. Then the probability that P does not apply for the job given that Q does not apply for the job is
 - (A) $\frac{4}{5}$
- (B) $\frac{5}{6}$
- (C) $\frac{7}{8}$
- (D) $\frac{11}{12}$

Answer: (A)

32. If the characteristics polynomial of 3×3 matrix M over R (the set of real numbers) is $\lambda^3 - 4\lambda^2 + a\lambda + 30$, $a \in \mathbb{R}$, and one eigen value of M is 2, then the largest among the absolute values of the eigen values of M is _____.

Answer: (5)

33. Consider the following expression grammar G:

$$E \rightarrow E - T \mid T$$

$$T \rightarrow T + F | F$$

$$F \rightarrow (E) | id$$

Which of the following grammars is not left recursive, but is equivalent to G?

(A) $E \rightarrow E - T \mid T$

$$T \rightarrow T + F | F$$

$$F \rightarrow (E) | id$$

(B) $E \rightarrow TE'$

$$E' \rightarrow -TE' \in$$

$$T \rightarrow T + F \mid F$$

$$F \rightarrow (E) | id$$

(C) $E \rightarrow TX$

$$X \rightarrow -TX \in$$

$$T \rightarrow FY$$

$$Y \rightarrow +FY \in$$

$$F \rightarrow (E) | id$$

Answer: (C)

(D) $E \to TX | (TX)$

$$X \rightarrow -TX \mid +TX \mid \in$$

$$T \rightarrow id$$

- **34.** In a two-level cache system, the access times of L_1 and L_2 caches are 1 and 8 clock cycles, respectively. The miss penalty from L2 cache to main memory is 18 clock cycles. The miss rate of L1 cache is twice that of L₂. The average memory access time (AMAT) of this cache system is 2 cycles. This miss rates of L_1 and L_2 respectively are :
 - (A) 0.111 and 0.056

0.056 and 0.111 (B)

0.0892 and 0.1784

(D) 0.1784 and 0.0892

Answer: (A)

- Consider two hosts X and Y, connected by a single direct link of rate 10⁶ bits/sec. The distance between **35.** the two hosts is 10,000km and the propagation speed along the link is 2×10^8 m/sec. Host X sends a file of 50,000 bytes as one large message to host Y continuously. Let the transmission and propagation delays be p milliseconds and q milliseconds, respectively. Then the values of p and q are
 - (A) p = 50 and q = 100

(B) p = 50 and q = 400

p = 100 and q = 50(C)

(D) p = 400 and q = 50

Answer: (D)

Consider the recurrence function **36.**

$$T(n) = \begin{cases} 2T(\sqrt{n}) + 1, & n > 2 \\ 2, & 0 < n \le 2 \end{cases}$$

Then T(n) in terms of θ notation is

- $\theta(\log\log n)$ (A)
- (B)
- $\theta(\log n)$ (C) $\theta(\sqrt{n})$
- (D) $\theta(n)$

Answer: (B)

37. If a random variable X has a Poisson distribution with mean 5, then the expectation

$$E[(X+2)^2]$$
 equals ______.

Answer: (54) **38.** Consider the following C function

```
int fun (int n) {
     int i, j;
     for (i = 1; i < = n; i++) {
                for (j = 1 ; j < n ; j+=i)
    printf ("%d %d ,i, j );
                 }
    }
       }
```

Time complexity of fun in terms of θ notation is

- (A) $\theta(n\sqrt{n})$ (B) $\theta(n^2)$ (C) $\theta(n\log n)$ (D) $\theta(n^2\log n)$

Answer: (C)

- **39.** The pre-order transversal of a binary search tree is given by 12, 8, 6, 2, 7, 9, 10, 16, 15, 19, 17, 20. Then the post-order traversal of this tree is:
 - (A) 2,6,7,8,9,10,12,15,16,17,19,20
 - (B) 2,7,6,10,9,8,15,17,20,19,16,12
 - (C) 7,2,6,8,9,10,20,17,19,15,16,12
 - (D) 7,6,2,10,9,8,15,16,17,20,19,12

Answer: (B)

40. Consider the C program fragment below which is meant to divide x by y using repeated subtractions. The variables x, y, q and r are all unsigned int.

```
while (r >= y)
               {
r = r - y;
q = q +1;
```

Which of the following conditions on the variables x, y, q and r before the execution of the fragment will ensure that the loop terminates in a state satisfying the condition x = (y*q+r)?

(A)
$$(q = r) && (r = 0)$$

(B)
$$(x > 0) \&\& (r = =x) \&\& (y > 0)$$

(C)
$$(q = 0) \&\& (r = x) \&\& (y > 0)$$

(D)
$$(q = 0) & (y > 0)$$

Answer: (C)

41. A message is made up entirely of characters from the set $X = \{P,Q,R,S,T\}$. The table of probabilities for each of the characters is shown below:

Character	Probability	
P	0.22	
Q	0.34	
R	0.17	
S	0.19	
Т	0.08	
Total	1.00	

If a message of 100 characters over X is encoded using Huffman coding, then the expected length of the encoded message in bits is_____

Answer: (225)

42. The next state table of a 2-bit saturating up-counter is given below.

$$Q_1^{} Q_0^{} Q_1^{^+} Q_0^{^+}$$

$$0 \ 0 \ 0 \ 1$$

The counter is built as a synchronous sequential circuit using T flip-flops. The expression for T_1 and T_0 are

$$(A) \qquad T_1 = Q_1 Q_0, \qquad T_0 = \overline{Q}_1 \overline{Q}_0$$

(B)
$$T_1 = \overline{Q}_1 Q_0$$
, $T_0 = \overline{Q}_1 + \overline{Q}_0$

(C)
$$T_1 = Q_1 + Q_0$$
, $T_0 = \overline{Q}_1 + \overline{Q}_0$

(D)
$$T_1 = Q_1 Q_0$$
, $T_0 = \overline{Q}_1 + \overline{Q}_0$

Answer: (B)

43. Consider the set of processes with arrival time (in milliseconds). CPU burst time (in milliseconds), and priority (0 is the highest priority) shown below. None of the processes have I/O burst time.

Process Arriva Time		Burst Time	Priority
P ₁	P ₁ 0		2
\mathbf{P}_2	5	28	0
P ₃	12	2	3
P ₄	2	10	1
P ₅	9	16	4

The average waiting time (in milliseconds) of all the processes using preemptive priority scheduling algorithm is _____

Answer: (29)

44. For any discrete random variable X, with probability mass function

$$P\!\left(X=j\right) = p_{_j}, p_{_j} \geq 0, j \in \!\left\{0,.....N\right\} \text{ and } \sum_{_{j=0}^{N}}^{_{N}} p_{_j} = 1, \text{ define the polynomial function}$$

 $g_x(z) = \sum_{j=0}^N p_j z^j$ For a certain discrete random variable Y, there exists a scalar $\beta \in [0,1]$ such that $g_Y(z) = (1-\beta+\beta z)^N$. The expectation of Y is

- (A) $N\beta(1-\beta)$
- (B) Nβ
- (C) $N(1-\beta)$
- (D) Not expressible in terms of N and β alone

Answer: (B)

45. The read access times and the hit ratios for different caches in a memory hierarchy are as given below.

Cache	Read access time (in nanoseconds)	Hit ratio
I-cache	2	0.8
D-cache	2	0.9
L2-cache	8	0.9

The read access time of main memory is 90 nanoseconds. Assume that the caches use the referred word-first read policy and the write back policy. Assume that all the caches are direct mapped caches. Assume that the dirty bit is always 0 for all the blocks in the caches. In execution of a program, 60% of memory reads are for instruction fetch and 40% are for memory operand fetch. The average read access time in nanoseconds (up to 2 decimal places) is _______.

Answer: (4.72)

46. If the ordinary generating function of a sequence $\{a_n\}_{n=0}^{\infty}$ is $\frac{1+z}{(1-z)^3}$, then a_3-a_0 is equal to _____.

Answer: (15)

47. Consider the following snippet of a C program. Assume that swap (&x, &y) exchanges the contents of x and y.

```
int main ( )
int array[]={3,5,1,4,6,2};
```

```
int done =0;
inti;
while (done = = 0) {
    done = 1;
    for (i = 0; i <= 4; i ++) {
    if (array [i] < array [i +1])
    swap (& array [i], &array [i+1]);
        done = 0;
    }
}
for (i = 5; i > =1; i --) {
if (array [i] >array [ i-1]) {
swap ( & array [i] , &array [i-1]);
done = 0;
}
    }
printf( " %d " , array [3] );
The output of the program is ______.
```

Answer: (3)

48. Consider the following C program.

```
# include <stdio.h>
int main () {
    int m = 10;
    int n, n1;
    n = ++m;
    n1 = m++;
n--;
    --n1;
    n -=n1;
printf ("%d", n);
    return 0;
```

}

The output of the program is ______.

Answer: (0)

49. Consider the following database table named *top _scorer*.

top _scorer.

Player	Country	Goals
Klose	Germany	16
Ronald	Brazil	15
G Muller	Germany	14
Fontaine	France	13
Pele	Brazil	12
Klinsmann	Germany	11
Kocsis	Hungary	11
Batistuta	Argentina	10
Cubillas	Peru	10
Lato	Poland	10
Lineker	England	10
T Miller	Germany	10
Rahn	Germany	10

Consider the following SQL query:

SELECTta.playerFROM top _scorer AS ta
WHERE ta.goals> ALL (SELECT tb. goals

The number of tuples returned by the above SQL query is ______.

Answer: (7)

- 50. Given f (w,x,y,z) = \sum_{m} (0,1,2,3,7,8,10) + \sum_{d} (5,6,11,15), where *d* represents the don't care condition in Karnaugh maps. Which of the following is a minimum product-of-sums (POS) form of f(w,x,y,z)?
 - (A) $f = (\overline{w} + \overline{z})(\overline{x} + z)$

(B) $f = (\overline{w} + z)(x + z)$

(C) $f = (w+z)(\bar{x}+z)$

(D) $f = (w + \overline{z})(\overline{x} + z)$

Answer: (A)

51. In a B⁺ tree, if the search –key value is 8 bytes long, the block size is 512bytes and the block pointer size is 2 bytes, then maximum order of the B⁺ tree is ______.

Answer: (52)

- **52.** Let L(R) be the language represented by regular expression R. Let L(G) be the language generated by a context free grammar G. Let L (M) be the language accepted by a Turning machine M. Which of the following decision problems are undecidable?
 - **I.** Given a regular expression R and a string w, is $w \in L(R)$?
 - **II.** Given a context-free grammar G, $L(G)=\emptyset$?
 - **III.** Given a context-free grammar G, is $L(G) = \sum^*$ for some alphabet $\sum ?$
 - **IV.** Given a Turning machine M and a string w, is $w \in L(M)$?
 - (A) I and IV only (B) II and III only (C) II, III and IV only (D) III and IV only

Answer: (D)

53. Consider a machine with a byte addressable main memory of 2³²bytes divided into blocks of size 32 bytes. Assume that a direct mapped cache having 512 cache lines is used with this machine. The size of the tag field in bits is _____.

Answer: (18)

54. Let δ denote that transition function and $\hat{\delta}$ denote the extended transition function of the \in -NFA whose transition table is given below:

δ	€	a	b
\rightarrow q ₀	$\{q_2\}$	$\{q_1\}$	$\{q_0\}$
q_1	$\{q_2\}$	$\{q_2\}$	{q ₃ }
q_2	$\{q_0\}$	Ø	Ø
q_3	Ø	Ø	$\{q_2\}$

Then $\hat{\delta}(q_2,aba)$ is

- (A) \varnothing
- (B) $\{q_0, q_1, q_3\}$
- (C) $\{q_0, q_1, q_2\}$
- (D) $\{q_0, q_2, q_3\}$

Answer: (C)

55. Consider the following languages.

$$L_1 = \{a^p | p \text{ is a prime number}\}$$

$$L_2 = \{ a^n b^m c^{2m} | n \ge 0, m \ge 0 \}$$

$$L_3 = \{a^n b^n c^{2n} \ge 0\}$$

$$L_4 = \{ a^n b^n \mid n \ge 1 \}$$

Which of the following are CORRECT?

- I. L_1 is context-free but not regular.
- II. L_2 is not context-free.
- III. L_3 is not context-free but recursive.
- IV. L_4 is deterministic context-free.
- (A) I, II and IV only (B) II and III only (C) I and IV only (D) III and IV only

Answer: (D)